

Linear dependence; a set of vectors $\mathbf{x}^1, \dots, \mathbf{x}^n$ is linearly dependent

- if there exists a vector \mathbf{x}^j that can be expressed as a linear combination of the other vectors, i.e.
- if the only solution to $\sum_{i=1}^n \alpha_i \mathbf{x}^i = 0$ is for all $\alpha_i = 0$.

Intuition for what the determinant $|A|$ is;

- Volume of the transformation of the matrix A up to a sign change.
- if $\det = 0$, volume = 0. At least one dim collapsed, lost information.

$\det(AB) = \det(A)\det(B)$

$\det(A^T) = \det(A)$.

$\det(A^{-1}) = 1/\det(A)$.

Pseudo inverse;

- $A^\dagger = A^T(AA^T)^{-1}$
- for a non-square matrix A such that AA^T is invertible.
- Satisfies $AA^\dagger = 1$, so also called right-inverse.