

# Low Power *In Situ* AI Calibration of a Three-Axial Magnetic Sensor

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Magnetic surveys are conventionally performed by scanning a domain with a portable scalar magnetic sensor. Unfortunately, scalar magnetometers are expensive, power consuming, and bulky. In many applications, calibrated vector magnetometers can be used to perform magnetic surveys. In recent years, algorithms based on artificial intelligence (AI) achieve state-of-the-art results in many modern applications. In this paper, we investigate an AI algorithm for the classical scalar calibration of magnetometers. A simple, low-cost method for performing a magnetic survey is presented. The method utilizes a low-power consumption sensor with an AI calibration procedure that improves the common calibration methods and suggests an alternative to the conventional technology and algorithms. The setup of the survey system is optimized for quick deployment *in situ* right before performing the magnetic survey. We present a calibration method based on a procedure of rotating the sensor in the natural earth magnetic field for an optimal time period. This technique can deal with a constant field offset and non-orthogonality issues and does not require any external reference. The calibration is done by finding an estimator that yields the calibration parameters and produces the best geometric fit to the sensor readings. A comprehensive model considering the physical, algorithmic, and hardware properties of the magnetometer of the survey system is presented. The geometric ellipsoid fitting approach is parametrically tested. The calibration procedure reduced the root-mean-square noise from the order of  $10^4$  nT to less than 10 nT with variance lower than 1 nT in a complete  $360^\circ$  rotation in the natural earth magnetic field. In a realistic survey scheme, the obtained calibration noise is suited to the environmental survey clutter. Implementing this scheme with a modern low-power analog-to-digital convertor and micro-controller results in power consumption lower than 15 mW and calibration duration of few minutes.

**Index Terms**—Three axis, algorithm, artificial intelligence (AI), calibration, fluxgate, *in situ*, scalar.

## I. INTRODUCTION

MAGNETOMETERS are used in surveys to map anomalies in the natural earth magnetic field [1]. Magnetic anomalies are caused by gradients in the magnetic permeability made by objects containing ferromagnetic mass [1], [2]. They may be used to map archaeological sites [3], prehistoric sites [4], underground pipes [5], and even wrecks [3]. The location of the anomaly caused by ferromagnetic objects such as unexploded ordnance can be estimated by employing magnetic anomaly detection and localization schemes [3].

Magnetic surveys are conventionally performed by scanning a domain with a portable scalar magnetic magnetometer. The scalar sensor measures the amplitude of the magnetic field and is not sensitive to the field bearing. Unfortunately, conventional scalar magnetometers are expensive, power consuming, and bulky. Furthermore, most sensitive scalar magnetometers have “dead zones” orientation that renders them impractical in some applications.

A practical approach to overcome the shortcomings of scalar magnetometers is to use vector magnetometers. A three-axis fluxgate magnetometer [1], [4], [5] is a low-cost, low-power, and high-resolution vector sensor [6] and is, therefore, a straight forward candidate for this application.

Unfortunately, due to mechanical and sensitivity inaccuracies between the axes, the three sensors’ axes are not precisely orthogonal [7], [8]. These imperfections lead to very significant magnitude errors when the sensor spins in  $360^\circ$ . Typical values of non-orthogonality are less than  $1^\circ$ , offset error of less than 10 nT, and scaling error of less than 0.5%. Therefore, it is impossible to use the fluxgate sensor for our purposes, without calibration.

Theoretically, the offset of the sensor may be measurable inside a perfectly shielded environment. However, since the residual field inside a practical shield is directional and non-uniform, it interferes with the offset of each axis. In order to compensate for the residual field, a calibration must be performed within the shield itself.

Calibration procedures are commonly used. They can be classified into two main approaches: the scalar approach sensor in which the reference is a scalar precise magnetometer [7], and the vector approach sensor in which the reference values come from a pre-corrected or ideal vector magnetometer [9].

Mathematical solutions were proposed by Marklund *et al.* [10] for the calibration of satellites magnetometers during magnetic mapping missions. The proposed solutions assume that the intensity of the magnetic field where the magnetometer rotated is precisely known. Other solutions, aimed for spacecraft equipped with a fluxgate sensor, use a scalar reference or a known constant field [14] to enable real-time calibration during typical spacecraft mission mode operations [11]. Merayo *et al.* [7] report a peak-to-peak (PTP) of 0.5 nT and a variance of about 0.1 nT, while Gavazzi *et al.* [12] achieved a 0.3 nT standard deviation in a different environment. However, those methods use an

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expensive scalar magnetometer while compelling the user to use an additional external device. Furthermore, the power consumption of the suggested solutions is relatively high.

Other methods suggest a calibration, which is based on a procedure of moving the sensor inside a constant (unknown) magnetic field. A comprehensive model which generalizes the problem has been suggested, and verified that the determination of all calibration parameters from a motion inside a constant magnetic field is possible [13].

The geometric approach calibration is a scalar calibration technique that was presented in several articles. This technique is capable of calibrating with a constant field offset. The calibration is done by finding an estimator which yields the calibration parameters that produce the best geometric fit to the sensor readings. This technique does not require any external reference [14]. Some calibration algorithms based on a geometric approach have been published [15], and some were even demonstrated recently in some applications like calibrating a compass mechanism of underwater gliders [16].

In this paper, we present a low-power, low-noise, and low-cost magnetometer optimized to allow both the conventional vector measurements and the calibrated scalar measurements. We experimentally compare between two approaches: a classical geometric one and a more advanced computational algorithm based on an artificial intelligence (AI) scheme. Both of them allow *in situ* calibration of the vector magnetometer.

Thus, a low-cost, low-power consumption and small size fluxgate three-axial magnetometer in magnetic surveys can be achieved. A comprehensive model considering the physical, algorithmic, and hardware properties of the magnetometer of the survey system is presented. The geometric ellipsoid fitting approach [17]–[19] is parametrically tested. An experimental system was built and tested using the suggested *in situ* low-power calibration algorithm.

## II. MAGNETIC CALIBRATION

### A. Calibration Goal

Our goal is to present a low-power *in situ* calibration process and to compare two different calibration concepts: a standard deterministic calculation and one AI approach, namely, a neural network (NN) scheme. We do this by optimizing a low-power sensor, sampling rate, and a calibration algorithm to enable a calibration process *in situ*. We use two parameters to model an error in a measurement. The first is the difference between the highest to the lowest magnetic magnitude, maximum PTP error. The second parameter is the norm of the magnetic field variance. Both parameters are calculated from the measured data during a given measurement scenario.

The low-power and *in situ* optimizations are important for highly portable magnetic survey applications. In order to perform a magnetic survey, the measurement system signal-to-noise ratio should be greater than 1 [1]. The most dominant sources of noise in land surveys are clutter in the ground and inhomogeneity of the ground ferrous composition giving rise to PTP clutter of 1–4 nT. This clutter is a source of noise as the survey is not aimed to find metal ferromagnetic scrap. Our goal is to reach a PTP calibration error of the same magnitude as of

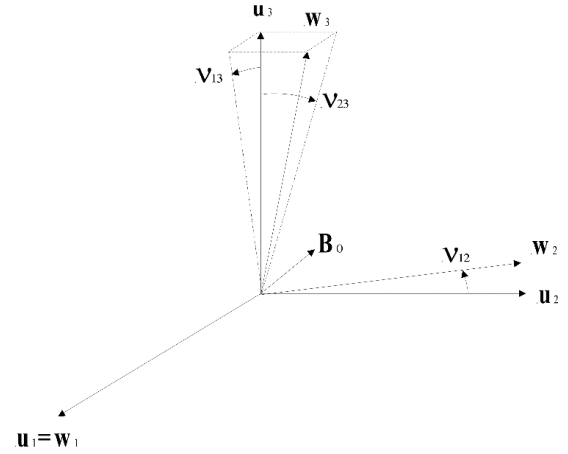


Fig. 1. Different coordinate systems of a fluxgate magnetometer. The orthogonal system is defined by the axes  $u_1$ ,  $u_2$ , and  $u_3$ , while the non-orthogonal system is defined by the axes  $W_1$ ,  $W_2$ , and  $W_3$ . The orthogonality errors are modeled by the angles  $v_{12}$ ,  $v_{23}$ , and  $v_{13}$ .

the clutter noise where the portable magnetometer is carried manually across the domain as stable as may be expected. In addition, in order to allow quick deployment, the calibration procedure should consume less than 5 min, and the power consumption should be lower than 15 mW.

### B. Magnetometer

In this paper, we focus on the simplest possible scanning configuration, in which the scanning process is done manually by walking over an area. The sensor is being held by hand during all the mapping process. Hence, while mapping an area, the sensor changes its orientation.

The simplest way to conduct a magnetic mapping is by using scalar magnetic sensors, such as Geometrics' G-823A cesium magnetometer. These types of sensors have a PTP of roughly 0.3 nT over 360° rotation and 0.2 nT during a stationary measurement, which renders them “over-spec” for magnetic mapping purposes. However, scalar sensors have “dead zones” in some sensor orientations, and an expensive tag price in the range of 10 000–40 000\$ as well as a relatively high-power consumption of about 12 W. Another alternative is using a fluxgate sensor. This is a low-priced (200–500\$) vector sensor, in which its output consists of the magnetic field components.

As illustrated in Fig. 1, the coordinate system defined by the axes  $W_1$ ,  $W_2$ , and  $W_3$  is not orthogonal. The non-orthogonality errors between the axes can be modeled by the angles  $v_{12}$ ,  $v_{23}$ , and  $v_{13}$ .

## III. CALIBRATION APPROACHES

In this paper, we present two different algorithms to perform the calibration and compare their performances. We apply the calibration procedures on the same measured data set. Moreover, we have also generated a synthetic, augmented dataset using a simulation setup, which allows a deeper analysis of the AI algorithm performance.

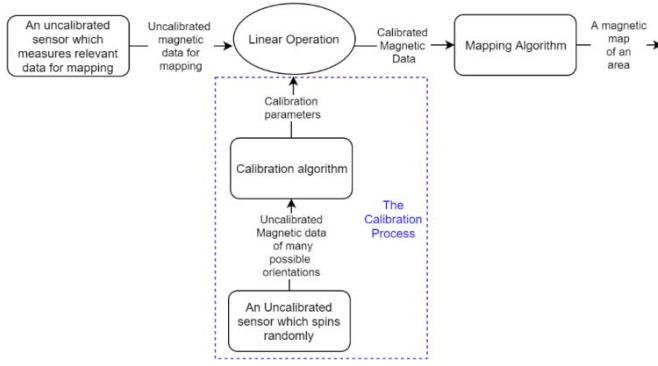


Fig. 2. Calibration data flow.

### A. Geometrical Approach

This solution is based on a linear transformation, which is applied on the sensors' raw data. This transformation solves the problem of the non-orthogonal axes by converting each vector components of the magnetic field at a given time  $(B_x(t), B_y(t), B_z(t))$  into a new corrected data. Fig. 2 shows a block diagram which demonstrates the data flow in our solution. A scalar magnetometer, which measures a constant magnetic field, would show a constant magnitude  $|B|$ , irrespective of the magnetometer's orientation. Thus, each measurement value has the same distance from the origin

$$|B| = \sqrt{B_x(t)^2 + B_y(t)^2 + B_z(t)^2}, \quad \forall t \in \mathbb{R}. \quad (1)$$

Hence, when plotting the magnetic data of different sensor orientations, a perfect sphere should be formed. However, a realistic fluxgate magnetometer has some non-orthogonality between its axes. Readings of a non-ideal magnetometer are always on an ellipsoid manifold [20]. Therefore, by using a linear transformation, it is possible to cast the calibration problem to a unified transformation parameterized by rotation ( $R$ ), scaling ( $S$ ), and offset ( $b$ ). This approach produces a linear problem that may be solved by using conventional linear methods. The rotation and scaling are due to the non-orthogonality between the axes and temperature changes, while the offset (the ellipsoid's displacement from the origin) is caused due to constant ferromagnetic variations formed by the magnetometer core itself.

The solution consists of an algorithm that performs a linear transformation of the magnetometer readings. The algorithm fits all the points into an ellipsoid manifold centered on the origin. After applying the transformation, all the data measurement points lie at the same distance from the origin. Since this distance is defined by  $|B|$ , the result is a constant magnetic magnitude, irrespective of the sensors' orientation [21], [22]. There are several approaches concerning how to transform an ellipsoid into a sphere while minimizing the fitting error. One method is the "Ellipsoid fit" presented in [22]. This algorithm describes the ellipsoid using nine parameters: semi-axis ( $a$ ,  $b$ , and  $c$ ), Euler angles ( $\varphi$ ,  $\theta$ , and  $\Psi$ ) (repressing the successive axis rotations), and coordinates of the center ( $X_0$ ,  $Y_0$ , and  $Z_0$ ). The fitting is done by performing a linear convex optimization on the raw data  $h_r$  to minimize

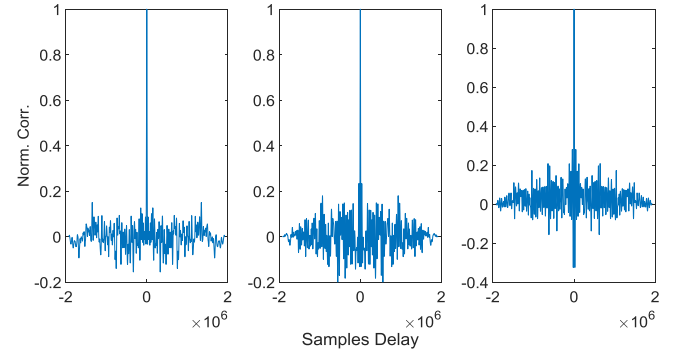


Fig. 3. Normalized cross correlation between the measurements of each three-axial component of  $L_e$  and  $L_s$ . From left to right:  $x$ -component (RMSE = 100 nT),  $y$ -component (RMSE = 77 nT), and  $z$ -component (RMSE = 89 nT).

the error of the fit, by minimizing the sum of squared algebraic error distances root mean square (rms).

According to the algorithm output, the correction matrix ( $M$ ) and the offset vector ( $b$ ), which best transform the ellipsoid into an origin-centered sphere, are calculated.  $M$  is calculated by using  $R'$  (de-rotation) and  $S^{-1}$  (de-scaling). The corrected data ( $h_c$ ) are then given by

$$h_c = M(h_r - b), \quad \text{s.t. } M = S^{-1}R'. \quad (2)$$

A constant magnetic field must be used during all time of calibration. For this purpose, we take the median value of all the earth's magnetic field measurements (about 2 million data points), which can be considered as a quite stable and precise estimation of the "true" ideal value.

### B. Artificial Intelligence Approach

In this section, we present an additional calibration algorithm. In contrast to the algorithm presented in Section III-A, this method will map each 3-D experimental data point on a 3-D ideal components that lie on a sphere, the radius of which is the median value of the measured norms of the field. Let us notate the set of noisy un-calibrated measurements as  $L_e$  and the set of their perfectly calibrated counterparts as  $L_s$ . Although each three-axial component in  $L_e$  lays on an ellipsoid, each component in  $L_s$  lays on a sphere that is centered at the origin with radius that is equal to the earth's magnetic field  $B$ . Therefore, we perform a pre-processing step to find the magnetic measurements that comprise this sphere, i.e., to generate the set  $L_s$ . An optimization problem is solved, in which every noisy measurement in  $L_e$  is mapped to its closest counterpart on the sphere, in terms of the Euclidean distance. Formally, for a given noisy coordinate  $(x_e, y_e, \text{ and } z_e) \in L_e$ , the matched clean coordinate  $(x_s, y_s, \text{ and } z_s) \in L_s$  is obtained by solving the following non-convex optimization problem:

$$(x_s, y_s, z_s) = \underset{(x,y,z): x^2+y^2+z^2=B^2}{\operatorname{argmin}} J(x, y, z, x_e, y_e, z_e) \quad (3)$$

where  $J = (x - x_e)^2 + (y - y_e)^2 + (z - z_e)^2$  and  $B$  stands for the earth's magnetic field. To ensure a non-trivial solution, the cross-correlation between  $L_e$  and  $L_s$  is given in Fig. 3, for

each of the three-axial components. To emphasize the existing difference between these curves, the rms error (RMSE) is also generated.

In recent years, NNs have re-gained popularity due to an increase in the amount of available data and computational capabilities [29], [30]. In this paper, we attempt to perform calibration by learning the mapping from the set  $L_e$  to the set  $L_s$  with an artificial NN. The network comprises two hidden layers of three nodes each. Thus, the output layer, which holds the perfectly calibrated three-axial magnetic measurements in  $L_s$ , is given by the multiplication of the input layer by two  $3 \times 3$  matrices. These matrices are notated as  $S_{\text{net}}^{-1}$  and  $R_{\text{net}}$ . Let  $(a_e, b_e, \text{ and } c_e)$  and  $(a_s, b_s, \text{ and } c_s)$  represent the parameter sets of the original ellipsoid and the target sphere, respectively. Then the network learns the following mapping:

$$\Psi : \frac{x_e^2}{a_e^2} + \frac{y_e^2}{b_e^2} + \frac{z_e^2}{c_e^2} \rightarrow \frac{(x_s - a_s)^2 + (y_s - b_s)^2 + (z_s - c_s)^2}{B^2}. \quad (4)$$

Namely, the mapping  $\Psi$  has an intrinsic linear nature. By taking this fact and the noisy measurements that lay on the ellipsoid into account, the activation chosen for the network is linear and the objective function is the mean-squared error. By integration of the drop-out approach on two neurons every 30 epochs, the network is effectively trained to avoid overfitting [23]. Thus, the mapping between the ellipsoid and the sphere is modeled with maximal generalization ability, and the statistical properties of the noise do not affect the model. Given an unseen coordinate  $x_e^{\text{test}} \in L_e$ , the following mapping is applied to generate  $x_s^{\text{test}} \in L_s$ :

$$x_s^{\text{test}} = \Psi(x_e^{\text{test}}) : x_e^{\text{test}} S_{\text{net}}^{-1} R_{\text{net}} + b_{\text{net}} \quad (5)$$

where  $b_{\text{net}}$  stands for a bias component.

#### IV. EXPERIMENTAL

Through this section, both the authentic (*in situ*) and synthetic datasets are considered in order to accomplish valid, real-world applicable results on one hand and demonstrate the potential of the suggested AI method on a variety of setups on the other.

##### A. Apparatus

Bartington's Mag648 and Mag 649 low-power fluxgates were used [24]. They were digitized by a 24 bit NI-9239 data acquisition (DAQ) [25]. The sampled signal was then transferred to a computer by LabVIEW data processing application. The national instruments sampling unit was used to simulate high-performance sampling scheme in order to determine the optimal sampling requirements. A practical sampling unit such as TI 1292 [26] was tested as well for low-power optimization. The hardware configuration we used is presented in Fig. 4 [1].

##### B. Measurements and Simulation Setups

To collect genuine calibration data, the sensor is rotated by hand for approximately 2 min in the natural undisturbed earth field. This rotation is performed in a ferromagnetic

TABLE I  
EFFECT OF THE SAMPLE FREQUENCY AND BANDWIDTH ON PTP AND VARIANCE USING THE GEOMETRICAL APPROACH

Configuration	PTP (nT)	Var (nT <sup>2</sup> )
Mag649 (250 Hz)	15	7
Mag649 (3000Hz)	15	3
Mag648 (250 Hz)	38	23
Mag648 (1000 Hz)	29	23

free environment. The collected data are used as an input for the calibration algorithm. The algorithm's output is a correction matrix and an offset, which are specific for each magnetometer. After applying the matrix and the offset on the sensors' raw data, we get the calibrated data. This calibration process can be done in the field in real time "*in situ*" and allow immediate use the magnetometer as a scalar survey tool.

To generate synthetic data, a MATLAB simulation was built. This simulation generates uniformly sampled data points given a set of pre-determined parameters such as the sensors' internal noise level, DAQ time, and analog and digital frequencies. Once again, this data serve as input for the calibration algorithms, which ultimately produce correction matrices to be applied to any new raw data.

##### C. Parameters Optimization

During the calibration process, the sensor is rotated at a rate of 1 r/s with rotation modes at higher frequencies. This revolution rate might be too high for the conventional low sampling frequency [1] and may result in "smearing" of the measurement and thus decreasing the accuracy of the calibration. Thus, the sampling rate and the averaging windows must be optimized in order to maintain signal integrity.

We used a faster sampling hardware to optimize the sampling rate and averaging window, as shown in Table I, which shows the main findings of this paper. A sampling frequency of 3 kHz provides the best results.

Another important parameter is the bandwidth of the sensor. This is because the higher rate of rotation during the calibration introduced artificial signals at frequencies beyond the bandwidth of the sensor. To test this, we have used two variants of the same sensor by Bartington instruments: Mag648 with a bandwidth of 5 Hz and Mag649 with a bandwidth of 1 kHz. Table I shows the main findings of this paper. A sampling frequency of 3 kHz provides the best results.

It appears that Mag649 with the larger bandwidth and frequency response band has lower PTP error and variance compared to Mag648. Furthermore, increasing the sampling rate decreases the calibration error (using the geometric approach algorithm for comparison) in both the narrowband



TABLE II  
CALIBRATION PERFORMANCE OF GEOMETRIC AND NN COMPARED TO  
UNCALIBRATED MEASUREMENT: MAGNITUDE MAX PTP AND  
VARIANCE. MOVING AVERAGE WINDOW WITH 0.1 s WIDTH  
IS APPLIED (MAG649 AT 3 kHz).

Calibration method	PTP (nT)	Var (nT <sup>2</sup> )
Not calibrated	24,055	652
Geometric	15	3
Neural network	8	4

and wideband sensors. Table I shows the main findings of this paper. A sampling frequency of 3 kHz provides the best results.

Averaging of random noise decreases the noise. However, averaging over a long period of time averages not only random noise but also the signal which is changing during the measurement period. As a result, the signal integrity may decrease. We have tested different averaging windows to optimize the tradeoff between signal integrity and noise decrease. The best value was taken to be a moving average window of 0.1 s.

#### D. Experiments

Several experiments are conducted to analyze the performance of both the geometric and AI methods *in situ*, as well as on synthetic simulated data.

Initially, the geometric and AI methods are employed on the authentic data measurements, and their performance is given in Table II.

Next, a set of synthetic measurements is generated using a dedicated simulation. This allows the analysis of the AI approach without the limitations of the dictates from the real-world setups. It should be highlighted that the uniform sampling done in the simulation differs from the random spinning of the sensor done *in situ*. The same coverage amount even if it is random in both cases will give better results for a true uniformly distributed process. This can be achieved easily in simulation but it is more complicated to achieve for manual *in situ* setup. A mechanical mechanism with uniform sampling data points pre-calculated is presented in [27].

To acquire synthetic measurements, two sensor noise levels  $\sigma_n = 0.1$  and  $0.3$  nT, and coverage percentages, ranging from 10% up to 100% are used. The definition of coverage percentage in this paper refers to the area of the sphere covered by the measurements. Let the sphere be parameterized by the set  $\{B, \theta, \phi\}$ , where  $B$  is the magnetic field and  $0 \leq \theta \leq 2\pi, 0 \leq \phi \leq \pi$ . It is known that an area differential value on the spheres' surface is proportional to  $((\Delta\phi\Delta\theta)/B)$ . In this paper, we make use of this and define a coverage of 100% when  $((\Delta\phi\Delta\theta)/B) \leq 10^{-4}$  for all bald areas on the surface of the sphere. Here, the bald area is an area in which no measurement lays. The measurements then undergo the AI calibration process, and their performance output is extracted.

The coverage percentage is highly correlated with the systems' end-to-end calibration process computational time. The

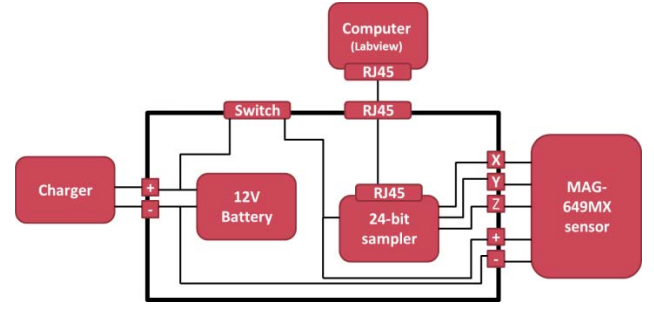


Fig. 4. Hardware configuration scheme.

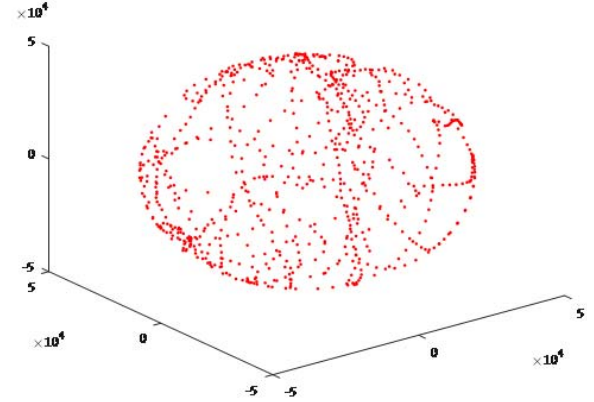


Fig. 5. Points which were created during the sensors' spinning for the calibration process. The axes are the  $x$ -,  $y$ -, and  $z$ -components of the magnetic field. As expected, the low-density ellipsoid shape is observed.

greater the time for calibration, the higher the accuracy, given the environment is noise free. This allows the examination of the effectiveness of uniform sampling DAQ in comparison to its real-world counterpart. In our case, we have physically rotated the sensor for 2 min. The end-to-end calibration process using the simulation was done on a Core-i7-7820HQ CPU 64 bit operating system, x64-based processor.

## V. RESULTS

### A. Measurements

The calibration algorithm transforms the measurements from an ellipsoid to a sphere. The measured ellipsoid can be seen in Fig. 5. An effective calibration algorithm transforms three non-orthogonal axial sensor output to scalar data. The quality of the calibration algorithm may be measured by the data PTP value compared to non-calibrated output, as well as the variance of the calibrated data with respect to  $B$ .

### B. Conventional Geometrical Approach

A graphical demonstration of the input data and the output data of the calibration algorithm can be seen in Fig. 6 (raw data versus calibration results). Here, we present the results for the selected configuration of the system. The configuration yielding the lowest PTP noise and variance was using a wideband sensor (Mag649) with a fast sampling rate of 3000 Hz and averaging over 0.1 s window. Implementing this scheme with

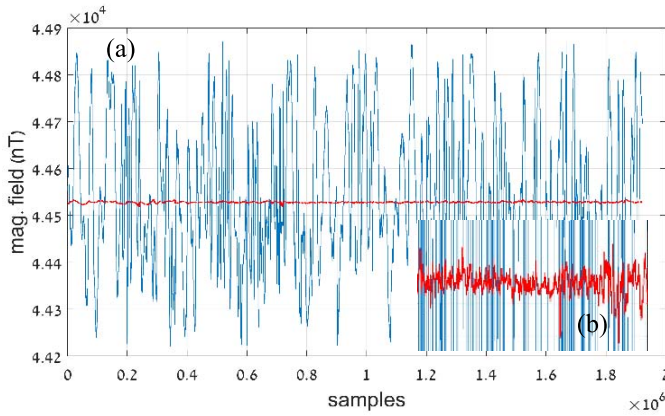


Fig. 6. Magnetic magnitude over 360° sensor spin, before (a) and after applying the geometrical calibration [central line zoomed in (b)]. Sensor used is Mag649 with sample rate of 3 kHz.

a low-power analog-to-digital convertor (ADC) and micro-controller results in power consumption lower than 15 mW, and calibration duration of approximately 2 min. The best result is a maximum PTP value of 15 nT with a variance of 3 nT<sup>2</sup>.

### C. Artificial Intelligence Approach

To demonstrate the performance of the AI method, two sets of calculations are conducted, as extended in Section IV. In the *in situ* experiment, the AI approach shows a better performance over its geometric oriented opponent: a maximum PTP of 8 nT has been obtained (instead of 15 nT for the geometric) and a maximum variance of 4 nT (similar to the one obtained with the previous method).

When considering the simulation related results, a larger set of comparisons can be made. For instance, in Figs. 7 and 8, it is clearly shown that the AI approach highly improves when given a dataset that covers the sphere even by 70%, as long as it is done uniformly. By extending it to 60% coverage, the mean error value approaches to the same order of magnitude that of the natural environmental clutter noise [1].

## VI. DISCUSSION

Several conclusions can be drawn based on these results. First, let us address the results achieved with the experimental *in situ* measurements. As previously stated, the NN learns the linear mapping from the ellipsoid to the sphere. Therefore, the performance of this calibration model is limited in several ways when it comes to nonuniform sampling. First and foremost, a new sample can be mapped by the network to an interval of values with uniform probability, where these values may be distant from  $B$ . This is a direct outcome of the linear fit the network applies on its training data. Second, because the model effectively maps an ellipsoid onto a sphere, the noisy test measurements lead to a non-optimal variance. Also, it can be concluded that using sparse training set, which contains many uncovered regions in the ellipsoid, is limited in its performance and leads to mediocre results considering the vast number of *in situ* recorded samples, ranging up to almost 2 million.

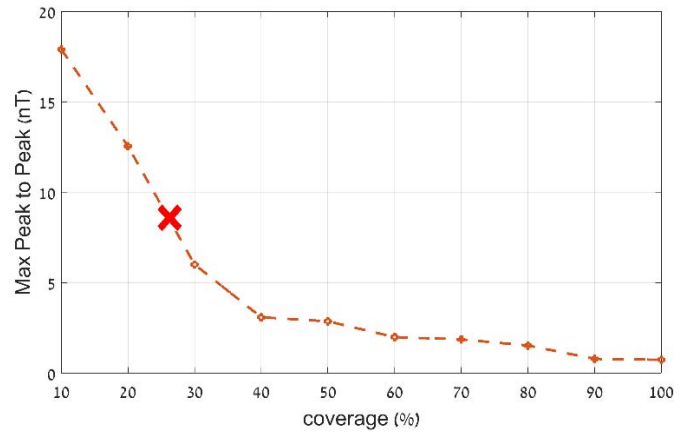


Fig. 7. PTP calibration performance of AI approach for various sphere coverages and two sensor internal noise values. The 'X' mark denotes the experimental PTP. It lies at 26% coverage of the full sphere surface.

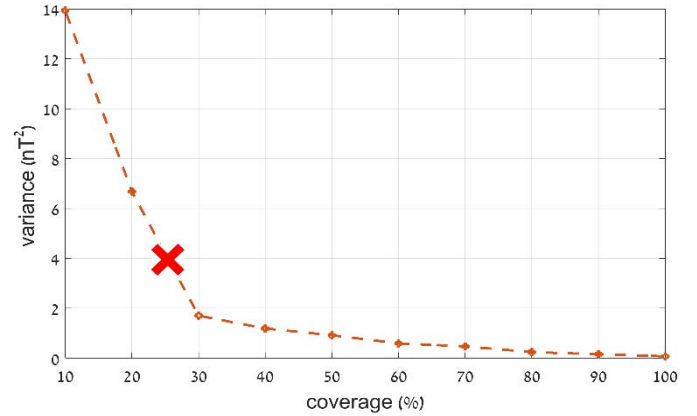


Fig. 8. Variance calibration performance of AI approach for various sphere coverages and two sensor internal noise values. The 'X' mark denotes the experimental PTP. It lies at 26% coverage of the full sphere surface.

When converging to full coverage, one can achieve a performance that approaches the known barrier of the sensors' internal noise. That and more, the presented system can handle authentic data in real time, under the constraint of uniform sampling, e.g., by allowing a delay of 60 min, the achieved error approaches the system' hardware limit with a negligible error variance of less than 0.5 nT<sup>2</sup> (Fig. 8). However, in magnetic surveys, this is not important because the environmental clutter is significantly larger than the sensors' internal noise.

These outcomes highly emphasize the gap in effectiveness between uniform and random data sampling during acquisition, i.e., using the 2 million experimental samples leads to the same performance achieved by using merely 26% uniform sphere coverage (Figs. 7 and 8). This essentially means that if the authentic DAQ is done uniformly, it can save almost 80% of its computational resources and achieve similar performance.

From the measurements and theoretical projections, a practical calibration optimization can be obtained. For example, in our case, in order to reach the same calibration noise as a common environmental clutter noise of 1–2 nT [1], only 60% coverage is required. Extrapolating the calibration

time with the assumption of uniform calibration yields a minimum of 4.2 min of rotating the sensor.

Of course, performing calibration *in situ* cannot cover all orientations due to physical limitations of the human hand. In this case, DAQ should be done systematically in order to approximate a uniform sampling.

## VII. CONCLUSION

A simple, low-cost, low-power method for performing a magnetic survey is presented. The method utilizes a low-power consumption sensor and ADC with a calibration procedure that replaces the very expensive and cumbersome conventional scalar magnetometer. The setup of the survey system is quick and can be performed *in situ* right before performing the magnetic survey, using the same hardware as a surveillance magnetometer. This approach allows an economical dual use of the same hardware as may be used in surveillance applications.

We present an AI-based calibration algorithm and compare it to a conventional geometric calibration method. The AI scheme performs much better than the geometric one and allows us to reach 2 nT PTP value and less than 0.1 nT<sup>2</sup> for the variance. In addition, we analyze the tradeoff between calibration time and the output calibrated noise that can ultimately reach the theoretical sensor internal noise level or the practical environmental clutter.

The experimental results show the capability of using the calibration method for mapping purposes. The calibration procedure reduced the rms noise from the order of 10<sup>4</sup> nT to the order of 10 nT in complete 360° rotation in the natural earth magnetic field with a variance of less than 0.1 nT. In many survey applications, the sensor rotation is controlled manually to within ±10° resulting in a much lower PTP noise than in a complete 360° rotation. Hence, it is even more feasible to achieve magnetic mapping capabilities by using low-cost, low-power fluxgate sensors.

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