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ROBOTICS DESIGN CAPSTONE 183DB

Off center spinning mass controller for Quad Copters

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Abstract

Your abstract.

1 Symbols

Here is a list of all symbols used in this paper:

- $\boldsymbol{\xi}$ linear position vectors
- η angular position vectors
- α roll angle
- β pitch angle
- γ yaw angle
- V_B linear velocity vectors in Body frame
- ν_B angular velocity vectors in Body frame
- R rotation matrix from body to inertial frame
- $S_x, C_x, T_x = \sin(x), \cos(x), \tan(x)$ respectively

2 Mathematical Derivation

2.1 Free Body Diagram

2.2 Inertial / Body / Controller frame transformation

The Rotation matrix is shown below,

$$\boldsymbol{R} = \begin{bmatrix} C_{\gamma}C_{\beta} & C_{\gamma}S_{\beta}S_{\alpha} - S_{\alpha}C_{\alpha} & C_{\gamma}S_{\beta}C_{\alpha} + S_{\gamma}S_{\alpha} \\ S_{\gamma}C_{\beta} & S_{\beta}S_{\theta}S_{\alpha} + C_{\gamma]}C_{\alpha} & S_{\gamma}S_{\beta}C_{alpha} - C_{\gamma}S_{\alpha} \\ -S_{\beta} & C_{\beta}S_{\alpha} & C_{\beta}C_{\alpha} \end{bmatrix}$$

2.3 Newton-Euler equations

$$m\dot{V}_B + \boldsymbol{\xi}_B \times (mV_B) = \boldsymbol{R}^T\boldsymbol{G} + \boldsymbol{T}_B$$