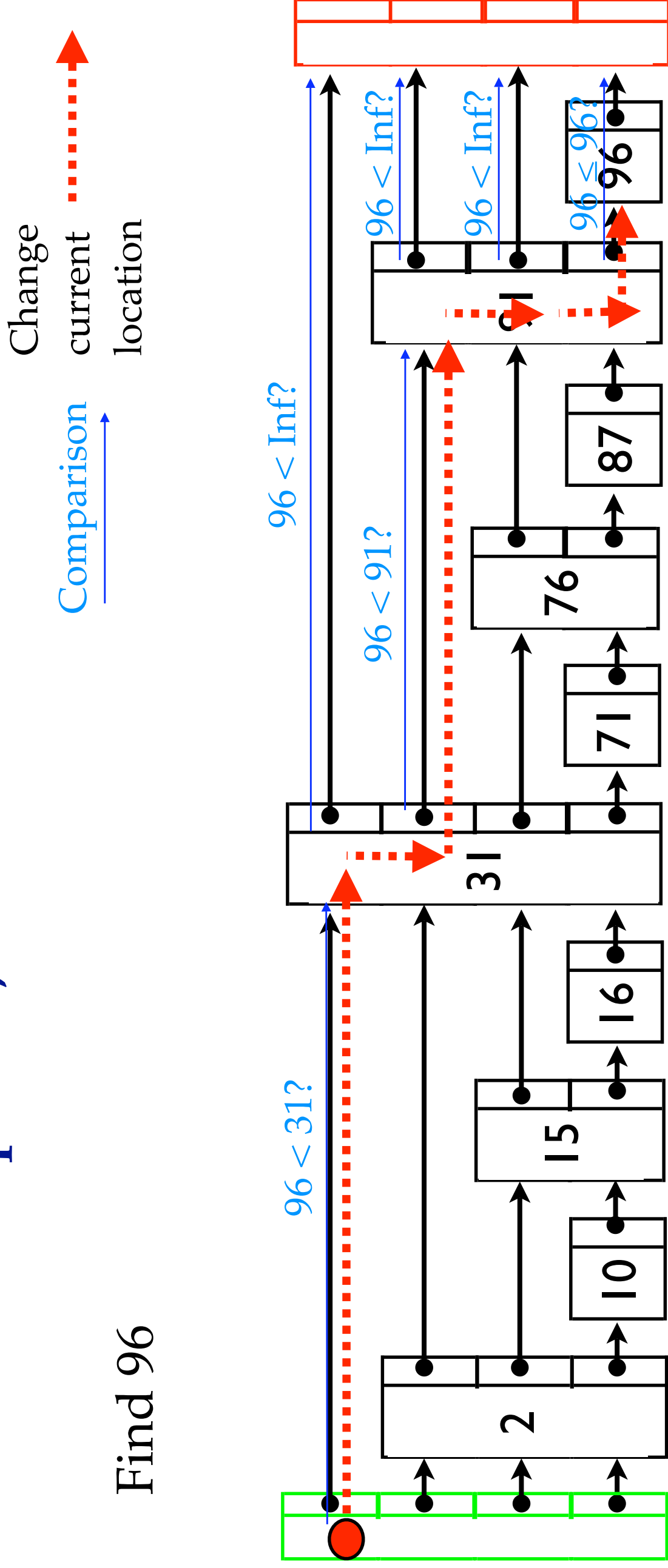


Perfect Skip Lists, continued

Find 96



When search for k:

If $k = \text{key}$, done!

If $k < \text{next key}$, go down a level

If $k \geq \text{next key}$, go right

Search Time:

- $O(\log n)$ levels --- because you cut the # of items in half at each level
- Will visit at most 2 nodes per level:
If you visit more, then you could have done it on one level higher up.
- Therefore, search time is $O(\log n)$.

Insert & Delete

- Insert & delete might need to rearrange the entire list
- Like Perfect Binary Search Trees, Perfect Skip Lists are too structured to support efficient updates.
- Idea:
 - Relax the requirement that each level have exactly half the items of the previous level
 - Instead: design structure so that we expect $1/2$ the items to be carried up to the next level
 - Skip Lists are a randomized data structure: the same sequence of inserts / deletes may produce different structures depending on the outcome of random coin flips.

Randomization

- Allows for some imbalance (like the +1 -1 in AVL trees)
- Expected behavior (over the random choices) remains the same as with perfect skip lists.
- Idea: Each node is promoted to the next higher level with probability $1/2$
 - Expect $1/2$ the nodes at level 1
 - Expect $1/4$ the nodes at level 2
 - ...
- Therefore, expect # of nodes at each level is the same as with perfect skip lists.
- Also: expect the promoted nodes will be well distributed across the list

Randomized Skip List:

