## 1 Question

Proof by Induction: Sum of the First n Natural Numbers The sum of the first n natural numbers is:

$$1+2+3+\cdots+n = \frac{n(n+1)}{2}$$

## 2 Answer

Consider the sum of the first n numbers:

$$1 + 2 + \ldots + n. \tag{1}$$

Now, let us write the sum from n to 1:

$$n+n-1+\ldots+1. (2)$$

The sum of both sequences is the same; the only difference is the order of the addition. Next, add the first element of the first sequence to the first element of the second sequence, which is (1+n). Do the same for each of the two elements of both sequences. The result is the following:

$$(1+n), (2+(n-1)), \dots, (n+1).$$
 (3)