

⇒ K Nearest Neighbour (KNN)
Used for both

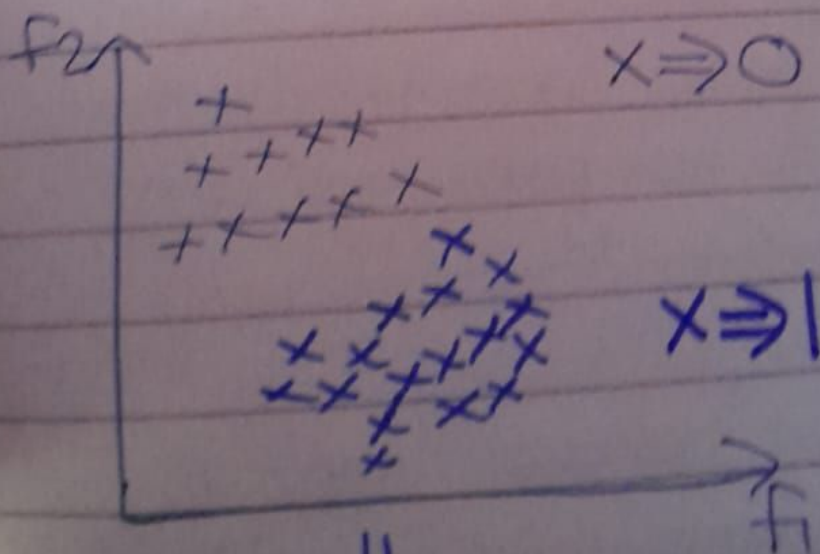
1. Classification
2. Regression

① Classification:

Let we have dataset

Independent		Dependent
f_1	f_2	y (Binary Category)
—	—	1
—	—	0
—	—	0
—	—	1

Let's plot the points of 0 and 1



⇓
Training Dataset

Step 01:

We have to specify K-value

$K > 0 \dots \infty$

i.e $K = 1, 2, 3, 4, 5$ or any

⇒ **Hyperparameter**

(we will try different values of K in cross-validation and pick one which give highest accuracy)

Step 02:

Find the K-nearest neighbours of new test data

i.e we have a new point in the graph drawn on previous page and $K = 5$, we will find 5 nearest neighbours from that new point according to distance.

Step 03:

From nearest neighbours, we found the count that how many of them belongs to 0 class and how many belong to 1 class and we will

assign the majority class to
an new point.

- Distance formulas for
Finding K-nearest neighbours
- ① Euclidean Distance:

$$\text{Distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

- Most of time euclidean distance
is used.

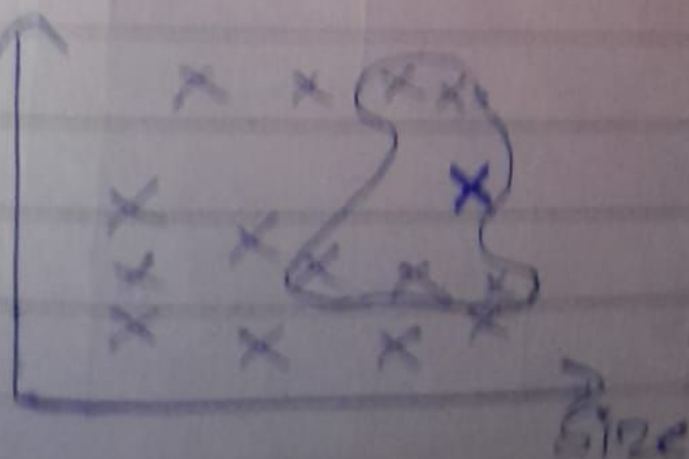
② Manhattan Distance:

In it we will not use
direct tangent like in
roads



② Regression

House
Price



It is similar we will find
nearest neighbours and we will
find average (mean/median) of those.

• Issue:

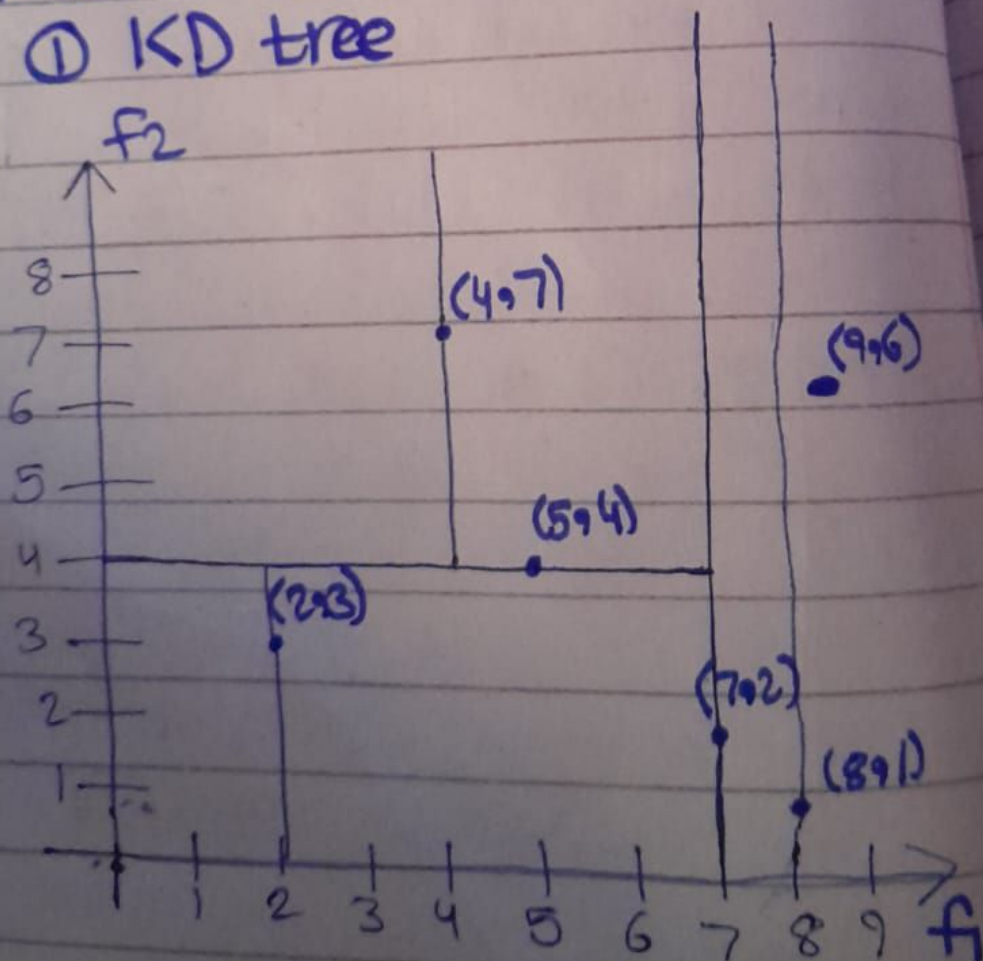
In K-th Nearest Neighbors for prediction we calculate the distance of every point from new point which takes time complexity $O(n)$.

To optimize KNN we use:

- ① KD-tree
- ② Ball tree

⇒ Variants of KNN:

① KD tree



We have dataset

f_1	f_2
7	2
5	4
9	6
2	3
4	7
8	1

Now we will construct KD tree for decreasing time complexity of find K nearest neighbours

- We will take median of f_1 and f_2

$$f_1 = 2, 4, \boxed{5, 7}, 8, 9 \quad (\text{sorted form})$$

$$\text{Median} = \frac{5+7}{2} = \boxed{6.5}$$
 we will

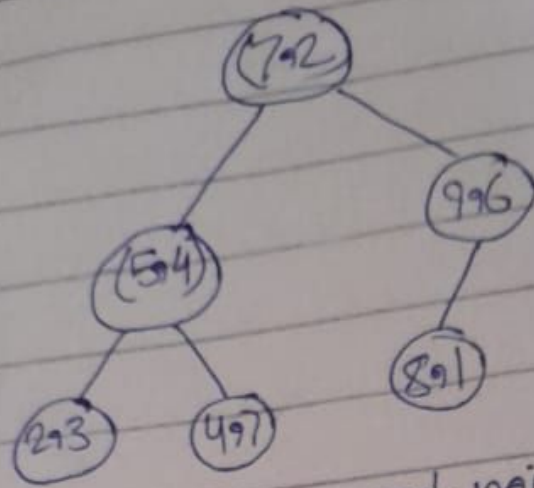
pick 7 from x-axis and draw line as there is no 6.5

$$f_2 = 1, 2, \boxed{3, 4}, 6, 7 \quad (\text{sorted form})$$

$$\text{Median} = \frac{3+4}{2} = \boxed{3.5}$$

We will pick 4 from y-axis and draw line as there is no 3.5

So we will keep making groups by taking median of remaining and construct tree)



We find nearest neighbours using this tree. Backtracking is also involved in it

② Ball tree:

It is better than KD tree and we don't need any backtracking

- In it we try to combine adjacent elements

