

$$P(s_i | s_{i-1}, x_1, \dots, x_m) = \frac{\exp(\vec{w} \cdot \vec{\phi}(x_1, \dots, x_m, i, s_{i-1}, s_i))}{\sum_{s' \in S} \exp(\vec{w} \cdot \vec{\phi}(x_1, \dots, x_m, i, s_{i-1}, s'))}$$

Example:

1	2	3	4
The	dog	barks	loudly
DT	NN	VB	ADV

Let's check that  $P(s_4 = \text{ADV} | s_3 = \text{VB}, \text{the, dog, barks, loudly}) > P(s_4 = \text{VB} | s_3 = \text{VB}, \text{the, dog, barks, loudly})$

$$P(s_4 = \text{ADV} | s_3 = \text{VB}, \text{the, dog, barks, loudly}) = \frac{\exp(\vec{w} \cdot \vec{\phi}(\text{the, dog, barks, loudly}, 4, \text{VB}, \text{ADV}))}{\sum_{s' \in S} \exp(\vec{w} \cdot \vec{\phi}(\text{the, dog, barks, loudly}, 4, \text{VB}, s'))}$$

$$P(s_4 = \text{VB} | s_3 = \text{VB}, \text{the, dog, barks, loudly}) = \frac{\exp(\vec{w} \cdot \vec{\phi}(\text{the, dog, barks, loudly}, 4, \text{VB}, \text{VB}))}{\sum_{s' \in S} \exp(\vec{w} \cdot \vec{\phi}(\text{the, dog, barks, loudly}, 4, \text{VB}, s'))}$$