

OPEN DATA SCIENCE CONFERENCE



@ODSC

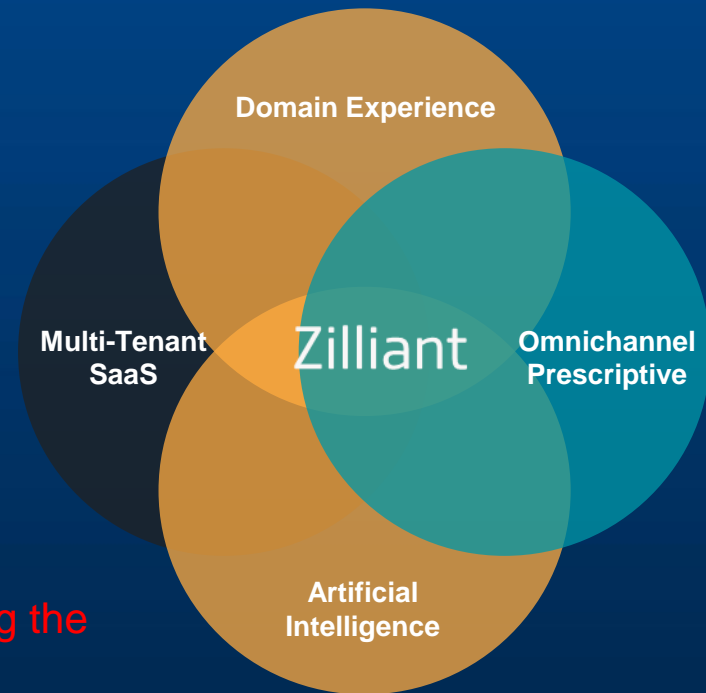
Boston | May 1 - 4 2018

Bayesian Hierarchical Model for Predictive Analytic

Amir Meimand
Director of R&D, Pricing Science, Zilliant

About Zilliant

- Founded in 1998
- Headquartered in Austin, Texas
- 200 employees & contractors
- Serving B2B Distribution, Manufacturing & Industrial Services
- 120+ customers around the world. 100's of implementations
- Investors: ABS Ventures, Houston Ventures, Trellis Partners, and Goldman Sachs



The world's leading AI-enriched SaaS platform for maximizing the lifetime value of B2B customer relationships.

About Zilliant

Zilliant IQ

Converting Strategic Insights into Account Specific Action Plans

Ex. Data In

Product
Master

Customer
Master

Transaction
Data

Win / Loss
Data

3rd Party
Data

Competitor
Price Data

Zilliant IQ – Multi-Tenant SaaS Platform

Cloud Infrastructure: Highly Scalable – Secure – Collaborative – In-Memory Reporting

Action IQ – Actionable Intelligence & Sales Guidance

Account
Potential

Account
Health

Dashboards &
Collaboration

Action Plans
& Campaigns

Quotes

Agreements

IQ Engines – AI & Prescriptive & On-Demand Insights

Cart IQ

Cost IQ

Price IQ

Profit IQ

Sales IQ

Zilliant IQ Anywhere – Integration & Omnichannel Activation

Omnichannel
Activation

Email

Mobile

Browser

CRM / CPQ

eCom

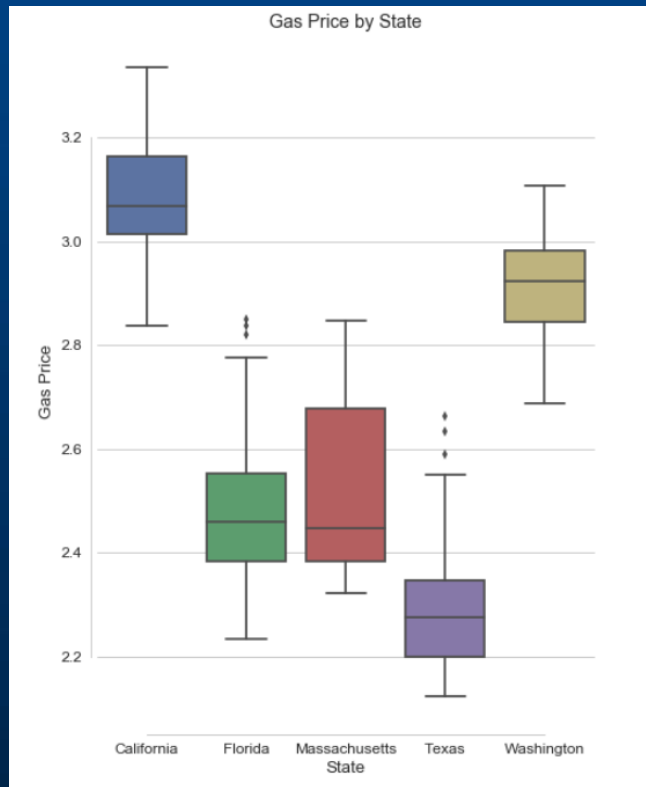
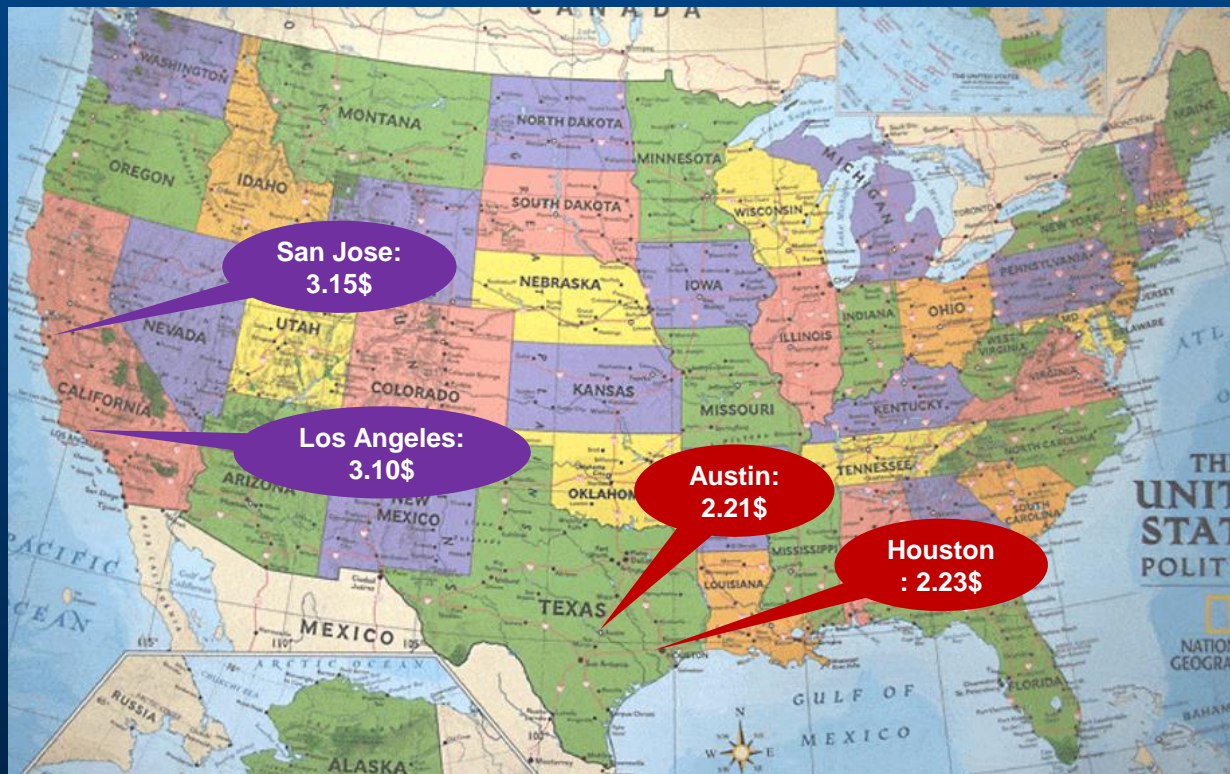
Quoting
Tools

ERP

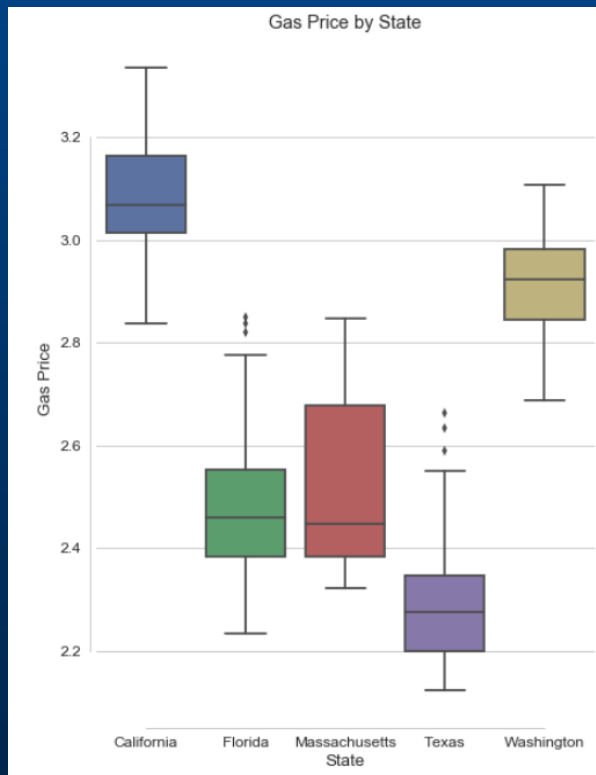
Zilliant Apps

Enterprise Integration...

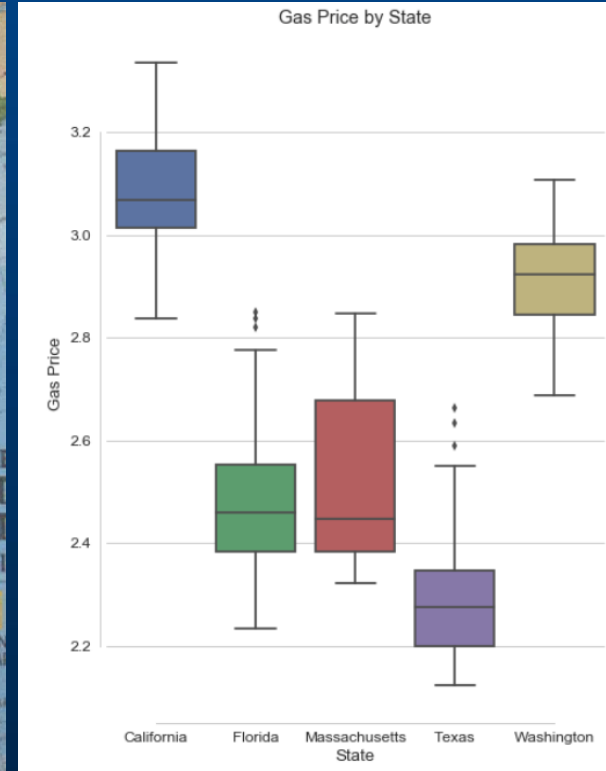
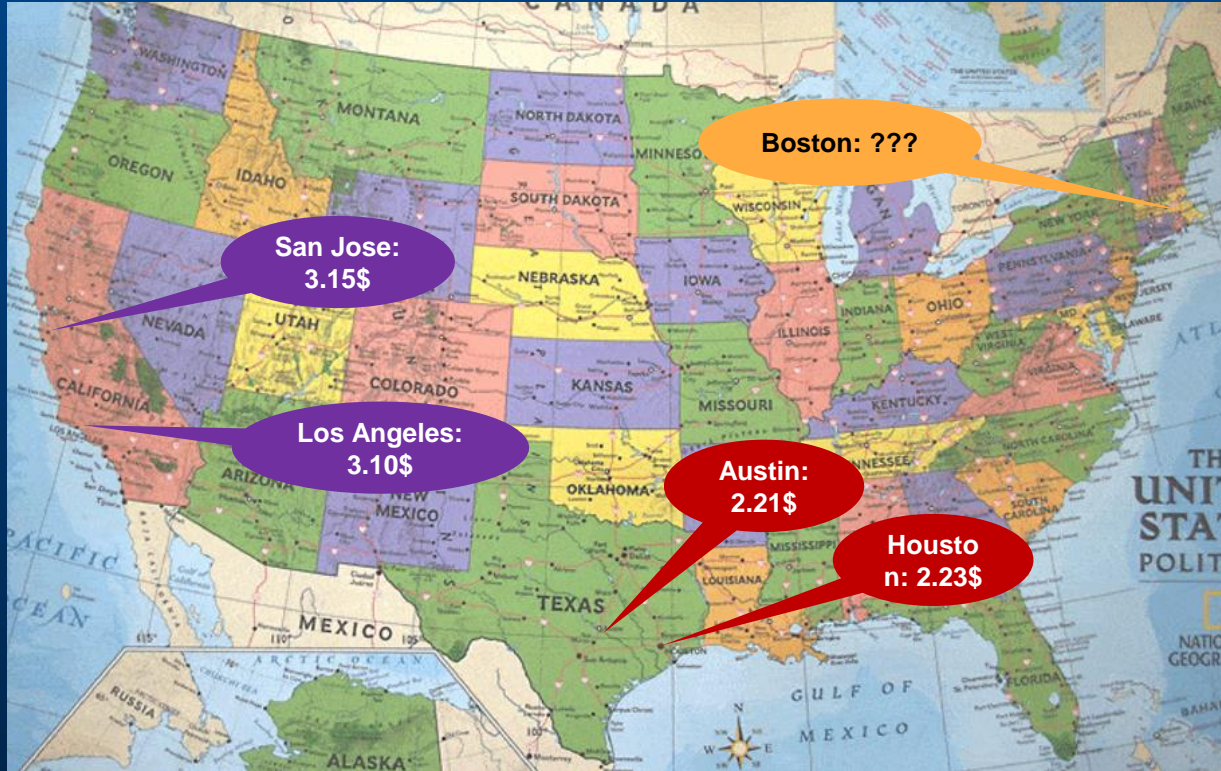
Gas Price:



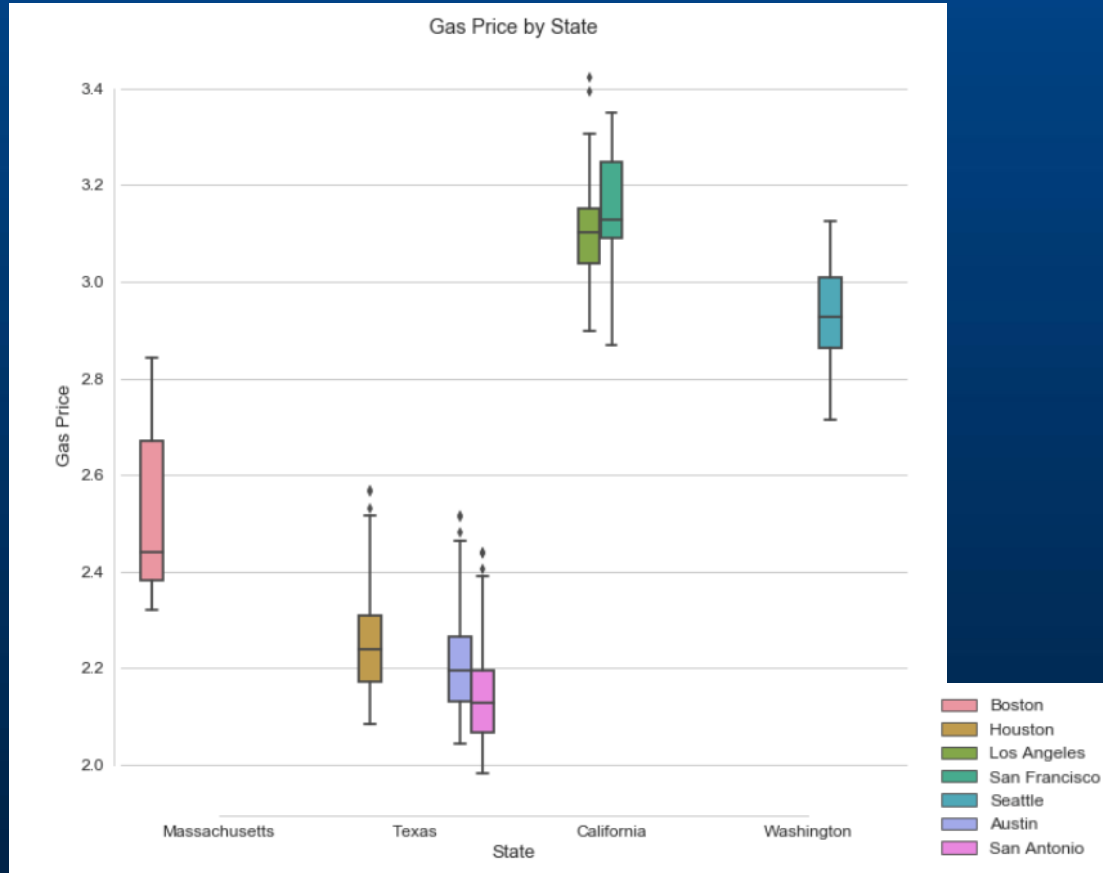
Gas Price:



Gas Price:



Gas Price:



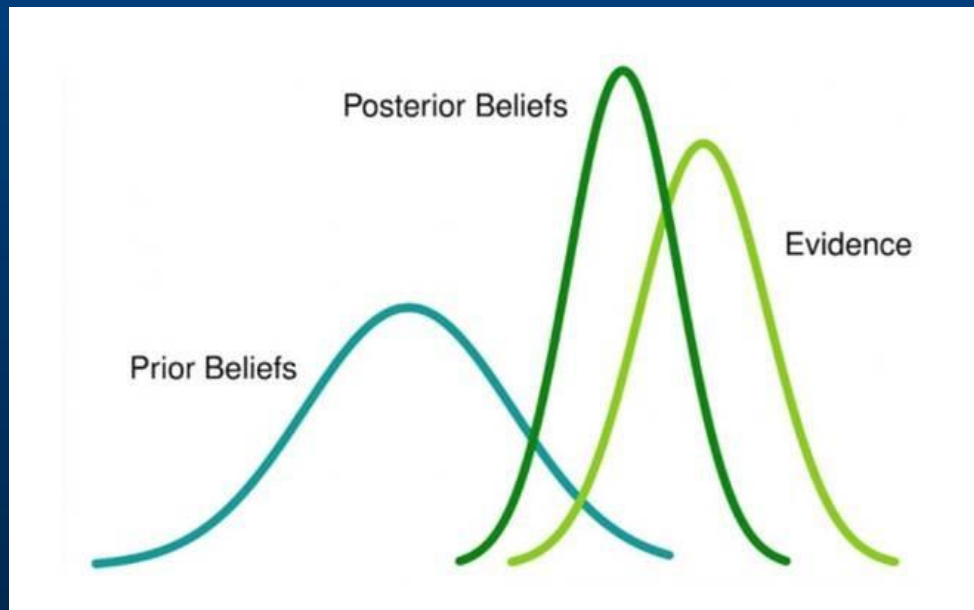
Gas Price:



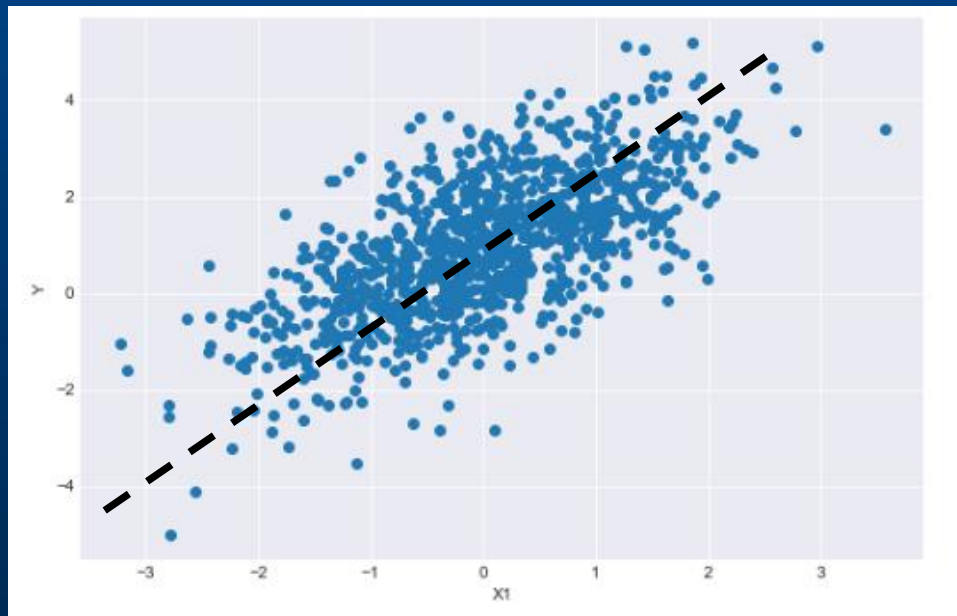
San Antonio:

- Station 1: 3.5\$
- Station 2: 3.8\$

Bayesian Models



Bayesian Regression



Assumed relationship: $y = \alpha + \beta x$

Priors:

$$\alpha \sim N(0, 10)$$

$$\beta \sim N(1, 5)$$

What other assumption(s) we have?

Bayesian Regression

- 1- What is the target variable? **Y which depends on Alpha and Beta**
- 2- What is assumed (potential distribution)? **Normal Distribution**
- 3- Define priors **Alpha and/or Beta distribution**

Bayesian Regression

```
regression_model = pm.Model()
```

```
with regression_model:
```

```
    alpha = pm.Normal('alpha', mu=0, sd=10)
```

```
    beta = pm.Normal('beta', mu=1, sd=5)
```

```
    sigma = pm.HalfNormal('sigma', sd=1)
```

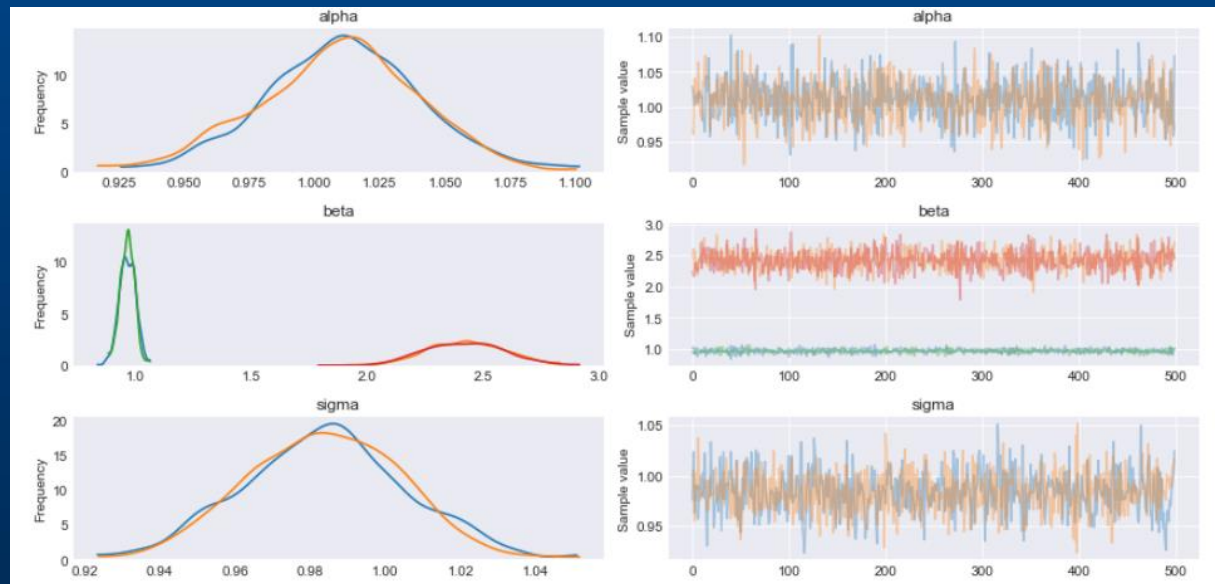
Create stochastic variables

```
    mu = alpha + beta*X1
```

Create deterministic variable

```
    Y_obs = pm.Normal('Y_obs', mu=mu, sd=sigma, observed=Y)
```

Bayesian Regression

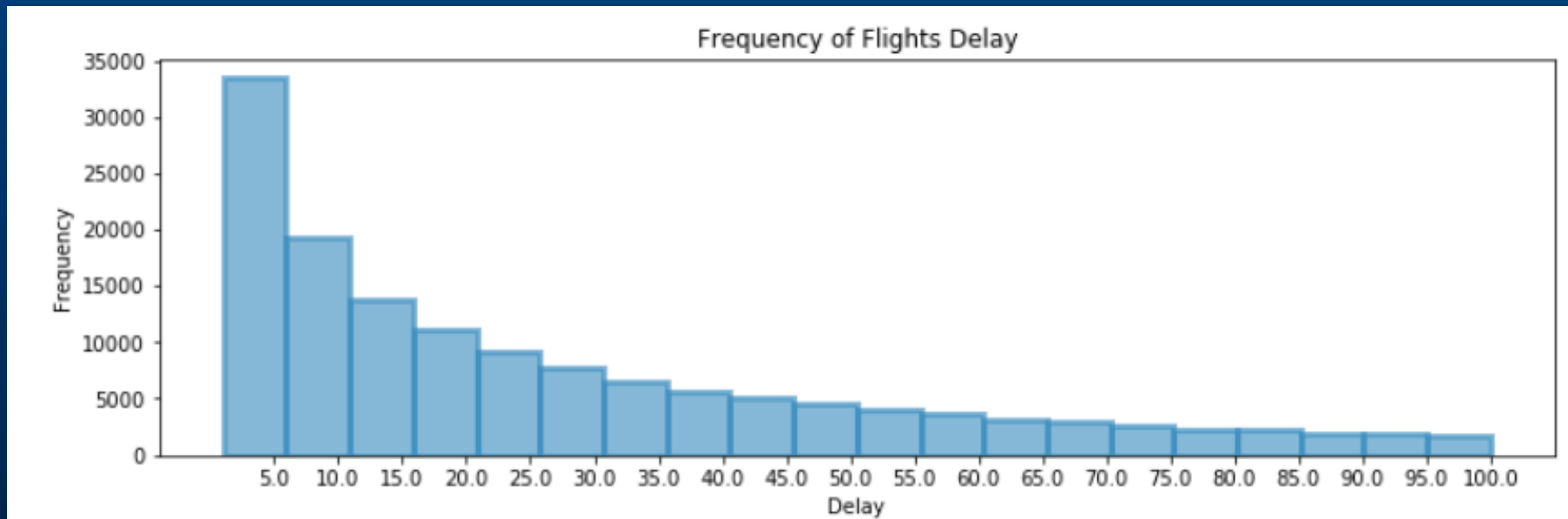


	mean	sd	mc_error	hpd_2.5	hpd_97.5	n_eff	Rhat
alpha	1.009507	0.029933	0.000790	0.950972	1.065191	1515.745188	1.000558
beta__0	0.967910	0.032986	0.000856	0.905172	1.032044	1451.511508	0.999007
beta__1	2.420182	0.164576	0.004431	2.120133	2.747157	1641.803594	0.999708
sigma	0.983615	0.021083	0.000603	0.945488	1.024915	1201.344314	0.999019

Flight Delay Prediction

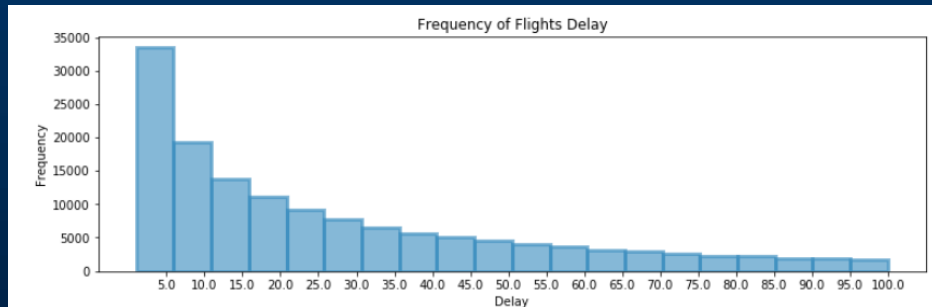
Flight Delay Prediction:

Evidence (IAH Airport)

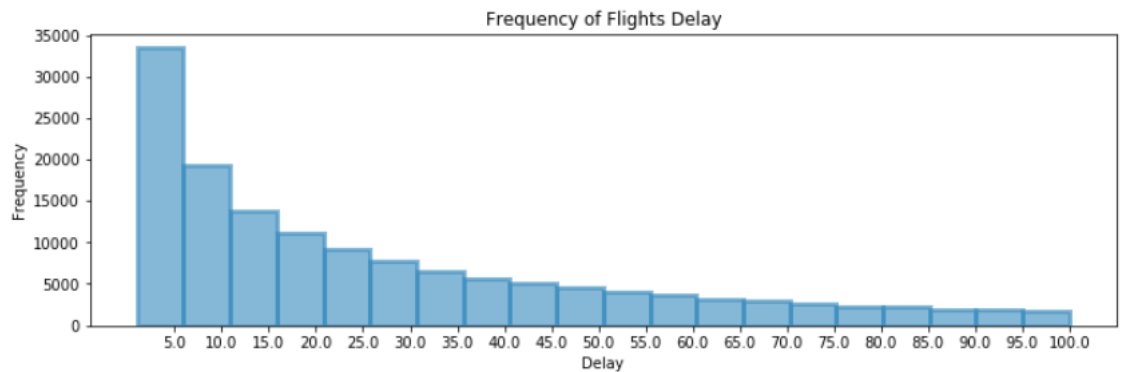


Modeling Step

- 1- What is the target variable?
- 2- What is assumed (potential distribution)?
- 3- Define priors

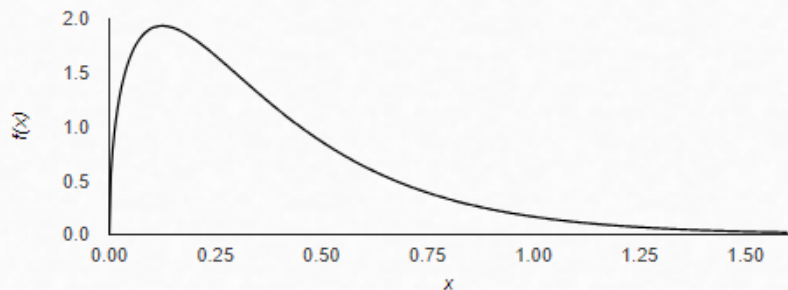


Flight Delay Prediction:



Evidence (IAH Airport)

$$f(x; \lambda) = \lambda e^{-x\lambda}$$



Prior Belief

Flight Delay Prediction:

```
Flight_Delay = pm.Model()

with Flight_Delay:
    # Prior Distribution

    rate = pm.Gamma('rate', 2, 2)

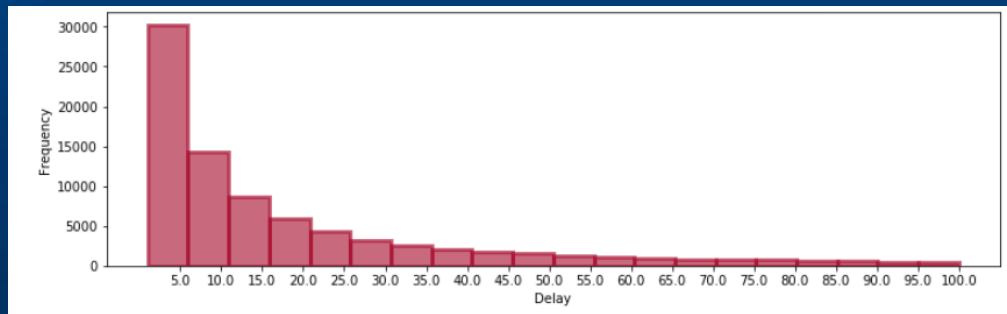
    # Likelihood (sampling distribution) of observations
    Y_obs = pm.Exponential('Y_obs', rate, observed=x)
```

Prior Distribution of target variable

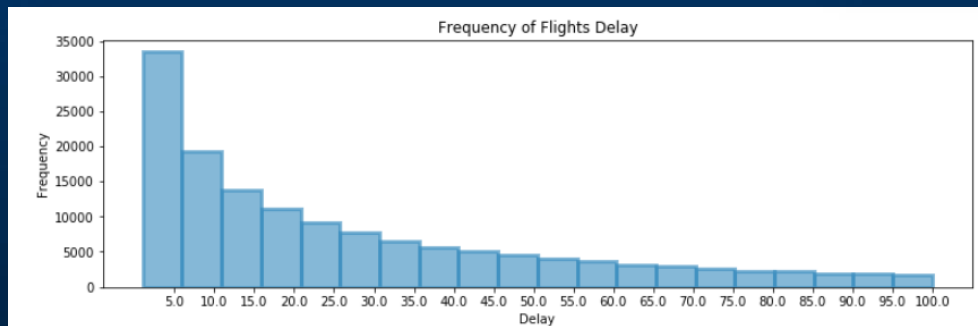
Relationship between

Flight Delay Prediction:

Evidence (ORD Airport)

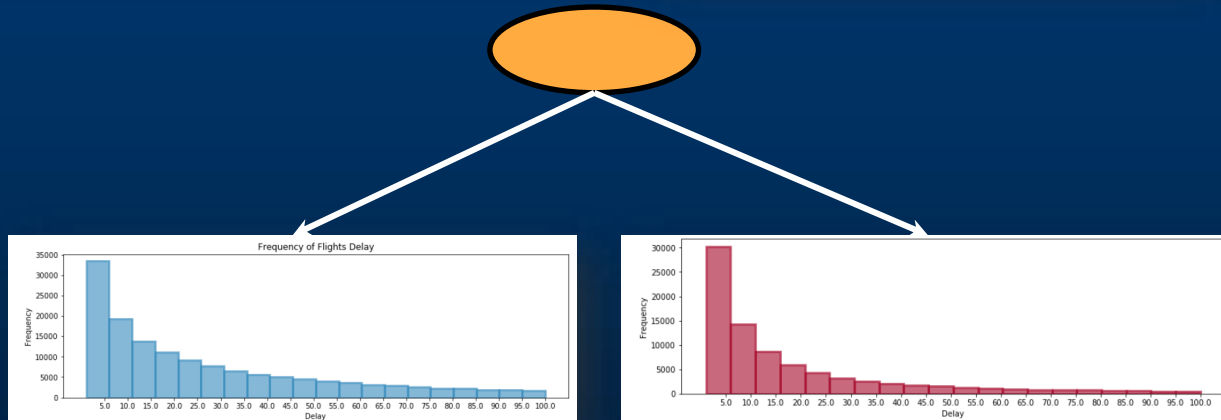
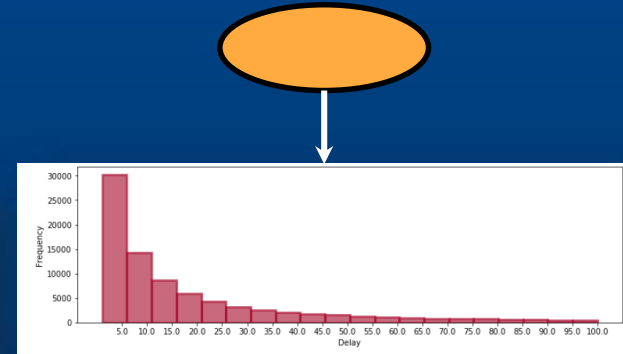
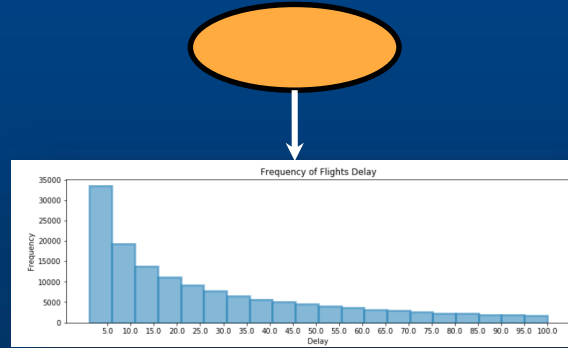


Evidence (IAH Airport)



Flight Delay Prediction:

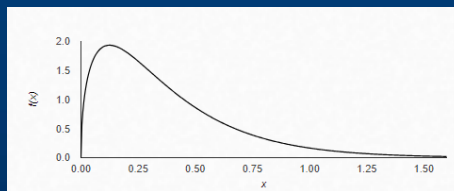
Every one has its own model!



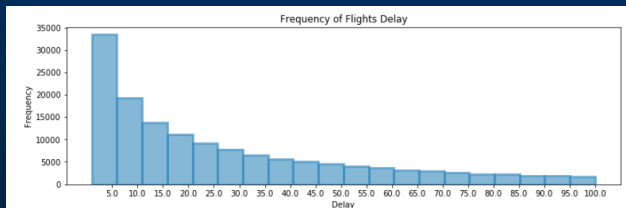
All have one model!

Flight Delay Prediction:

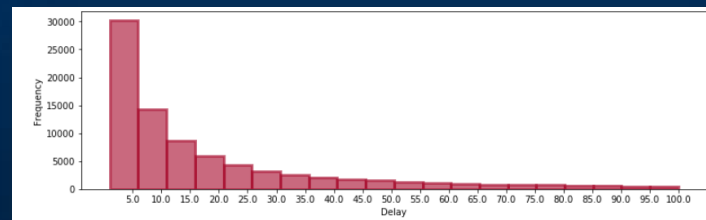
Gamma(α_1, β_1)



$$f(x; \lambda_1) = \lambda_1 e^{-x\lambda_1}$$



$$f(x; \lambda_2) = \lambda_2 e^{-x\lambda_2}$$



Flight Delay Prediction:

```
Flight_Delay = pm.Model()

with Flight_Delay:
    # Prior Distribution
    rate = pm.Gamma('rate', alpha, beta, shape=2)

    rate_hat=rate[airport]
    # Likelihood (sampling distribution) of observations
    Y_obs = pm.Exponential('Y_obs', rate_hat, observed=Delay)
```

Artificial Intelligence – A Definition for B2B

The capability of a machine to imitate intelligent human behavior

What if your best...

Sales Person

Pricer

Buyer

Product Manager

Financial Analyst

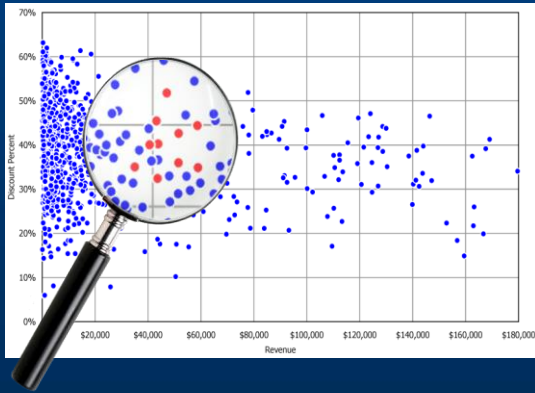
...could evaluate every customer relationship, every day and recommend action?

How would that impact customer lifespan, revenue and profit?

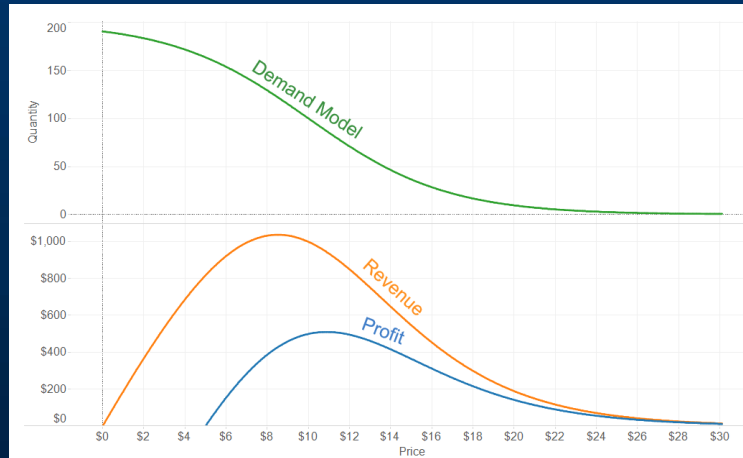
Price Optimization

Machine learning for market segmentation, price sensitivity, and price optimization.

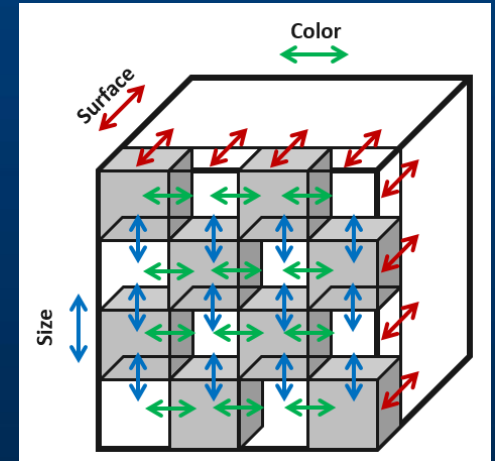
Segment Clustering



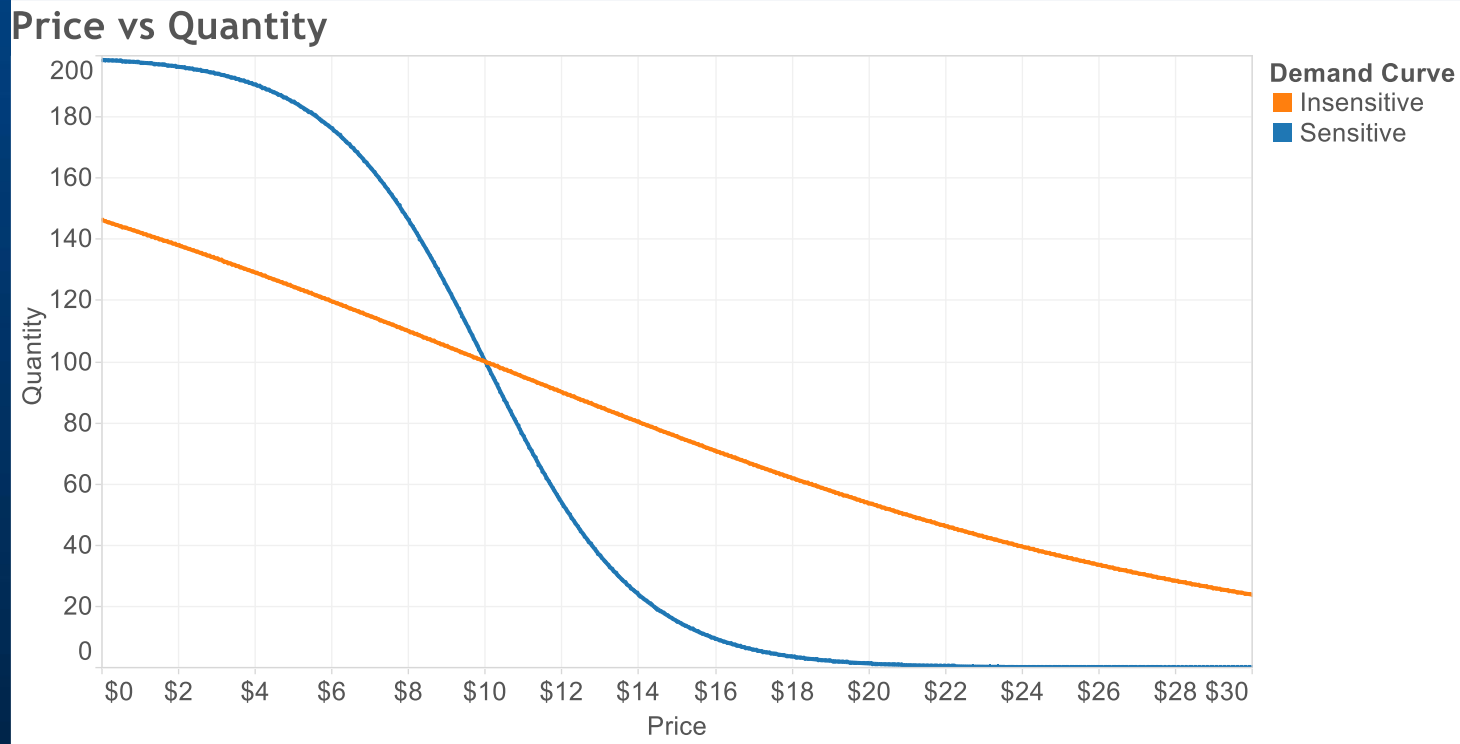
Convex Optimization



Pricing Constraints



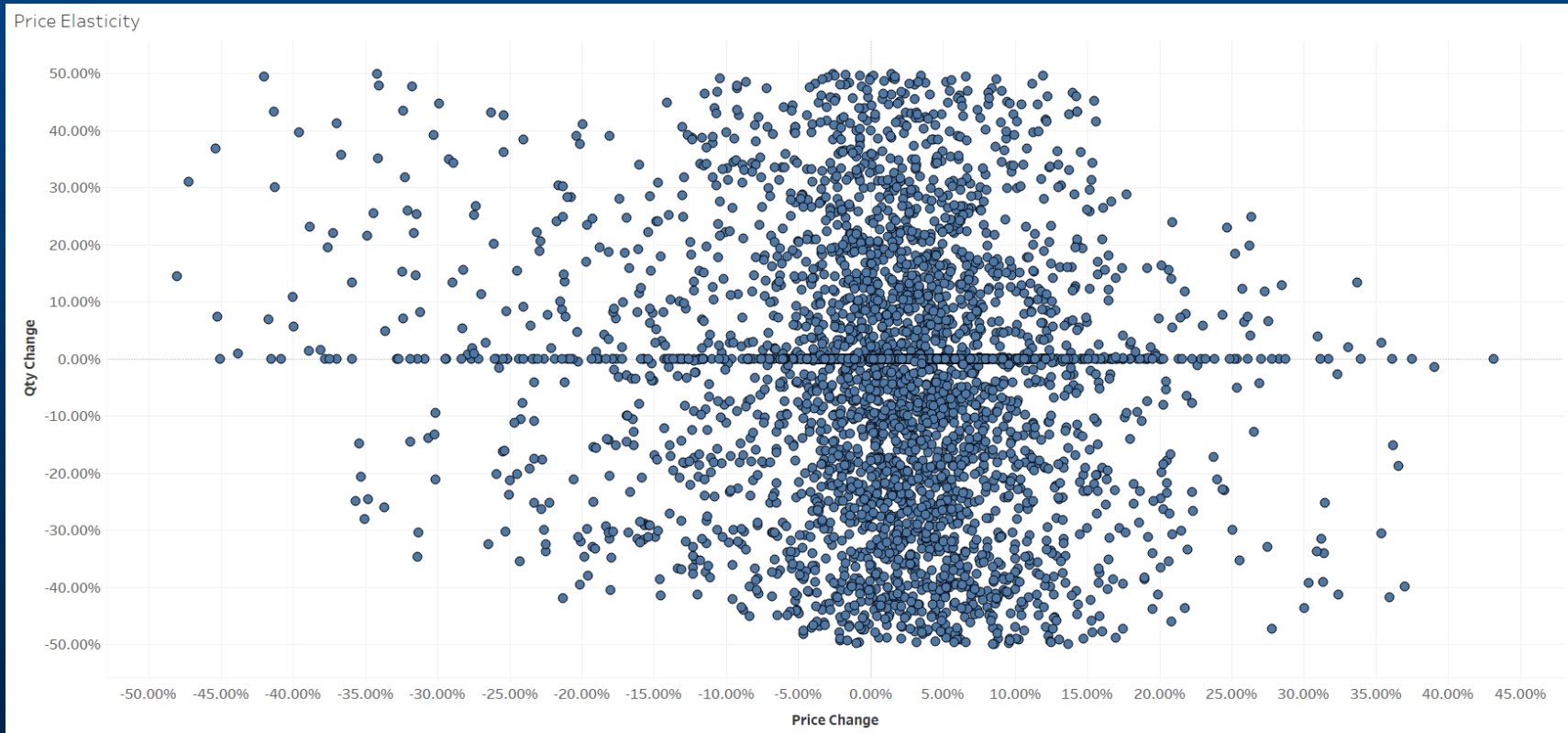
Price Elasticity



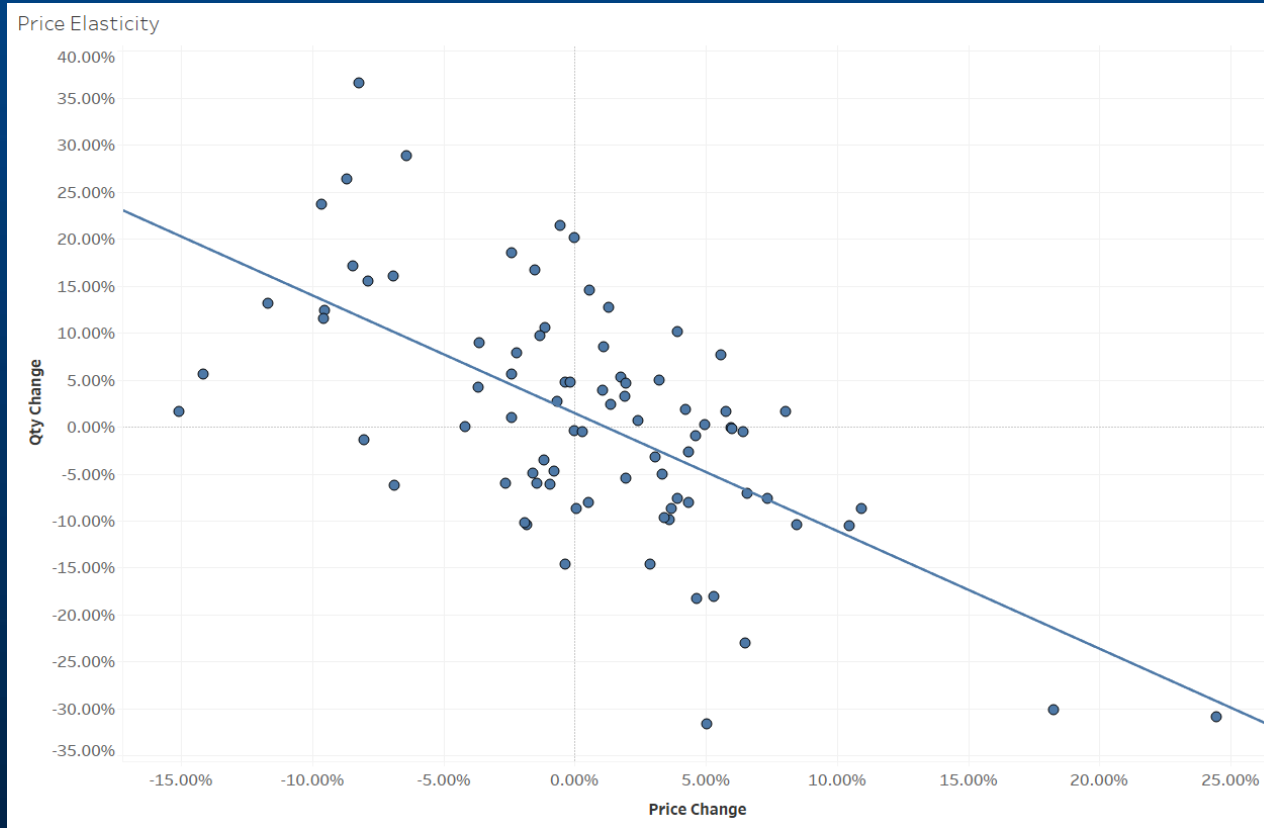
What we hope to see (Dream)



What we see (Reality!)

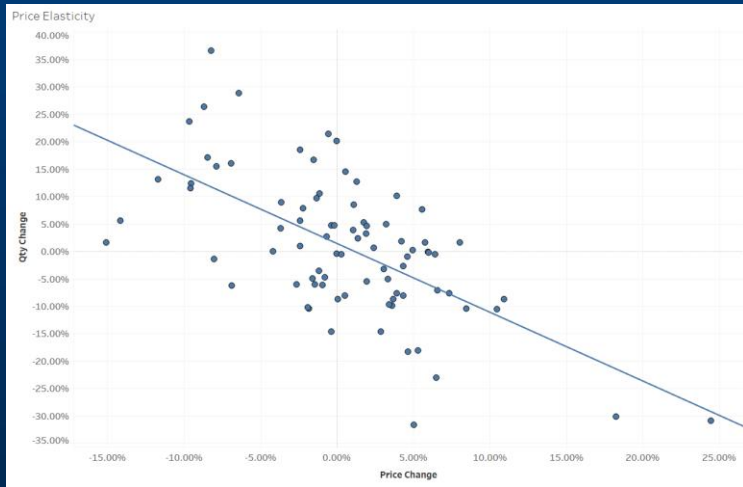


Fix it!



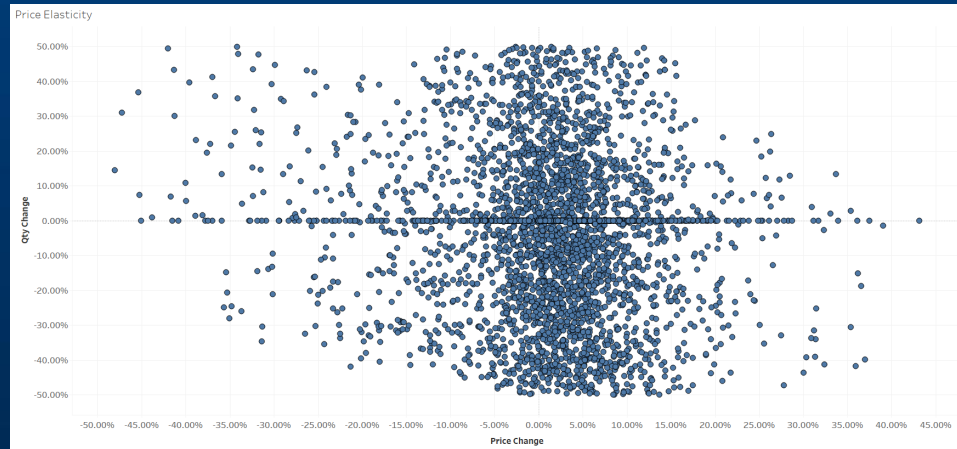
Why Hierarchical Model?

Clean Data, Less Data Points

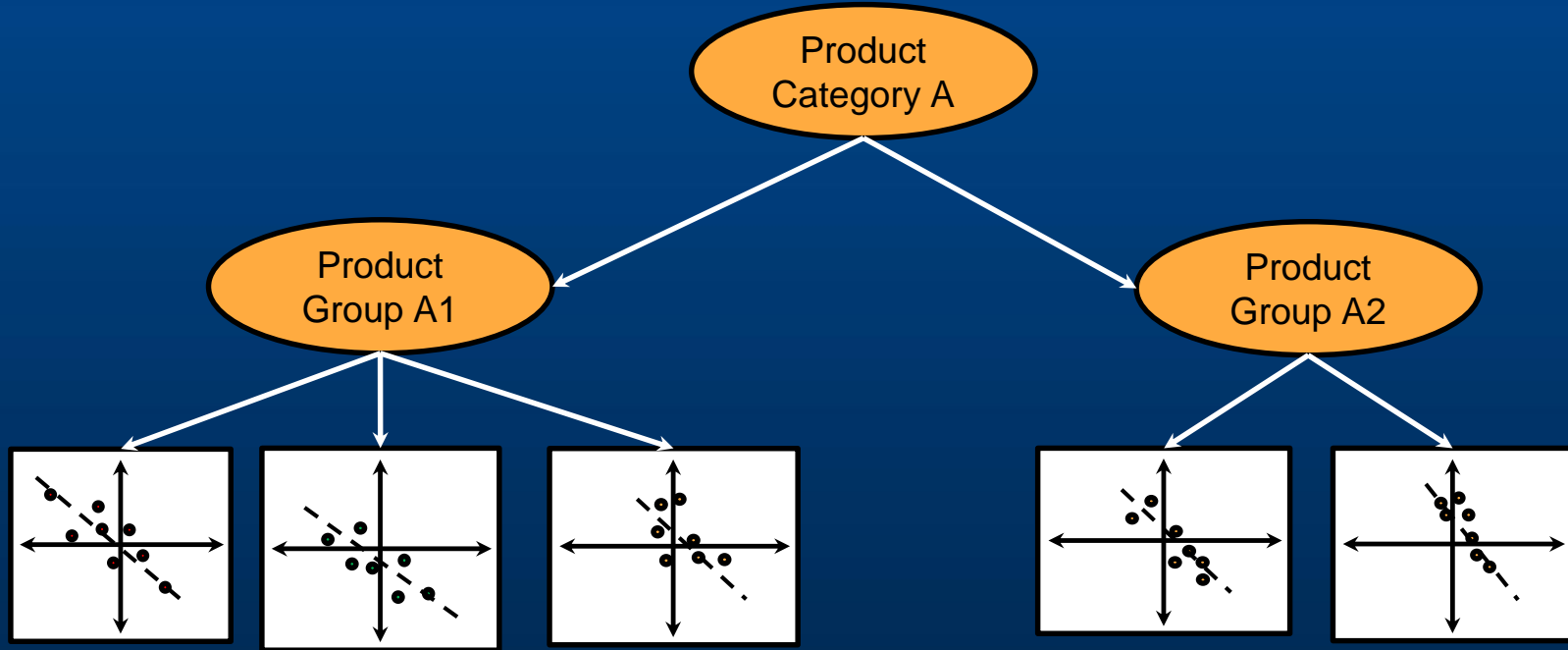


Vs.

Noisy Data, Many Data Points



Why Hierarchical Model?



Zilliant ML Platform (Point and Click!)

Step 1- Define Hierarchical Levels

Segmentation Trees: PSE

Segmentation Tree Name

Purpose Time-Based Metrics

Segmentation Tree Levels

Use	Order	Attribute	Entity
<input checked="" type="checkbox"/>	0	zProduct_Id	Transaction
<input checked="" type="checkbox"/>	1	Customer_Program	Transaction
<input checked="" type="checkbox"/>	2	CompetitiveRegion_Bin	Transaction
<input checked="" type="checkbox"/>	3	zRegion	Transaction
<input type="checkbox"/>	4	CustomerSpend_Bin	Transaction
<input type="checkbox"/>	5	Customer_Loyalty	Transaction
<input type="checkbox"/>	6	OrderSize_Bin	Transaction
<input type="checkbox"/>	7	Price_Change_Group	Transaction
<input type="checkbox"/>	8	Region	Transaction

Step 2- Set Model Parameters

Regression Parameters

Enable Trace Debug ☐

Delta Days

Delta Lag Days

Max Price Delta (%)

Max Quantity Delta (%)

Transaction Threshold

MuA

MuB

SigA

SigB

SigEpsHB

SigEpsLB

Number of Samples

Burn-in (%)

Calculation Time Limit (hours)

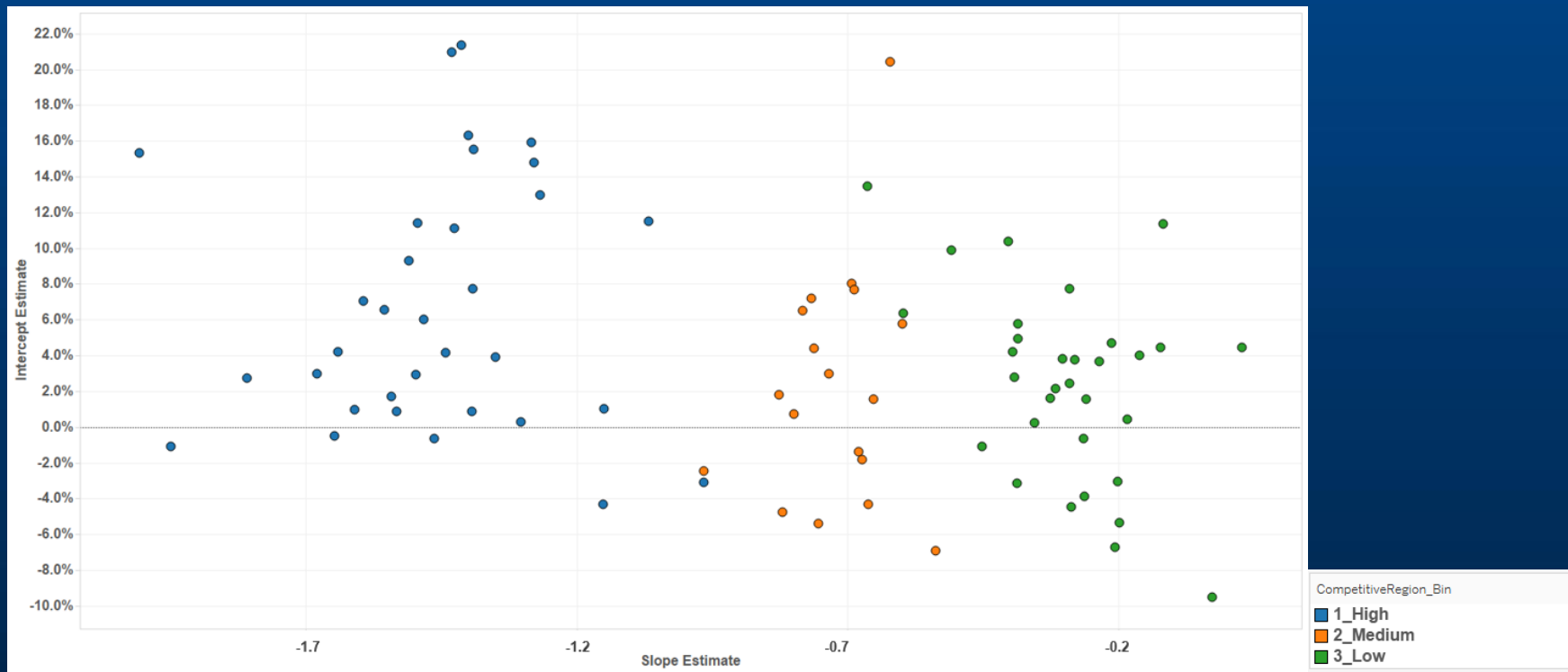
Attribute for Partitioning

Step 3- Run the job!

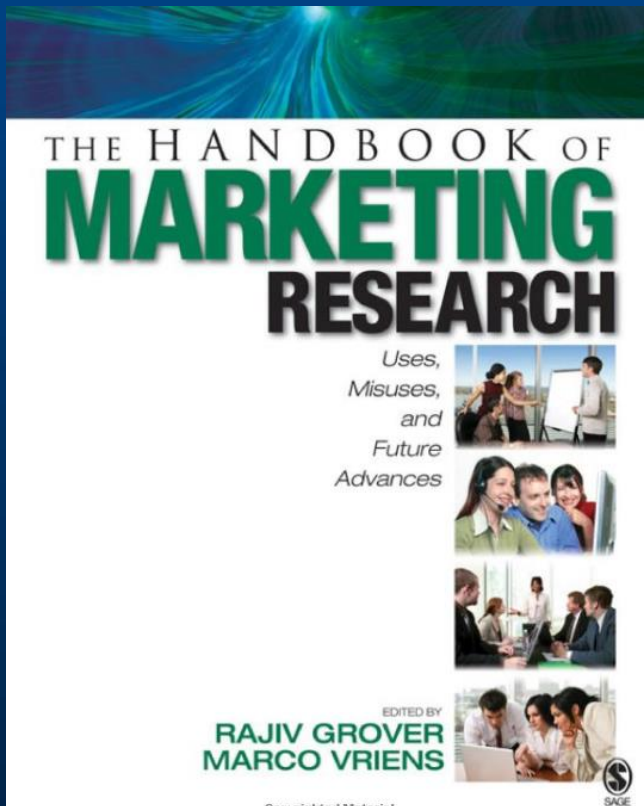
Jobs

- Compute regression

Output



Learn more?



20

HIERARCHICAL BAYES MODELS

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Ohio State University

PETER E. ROSSI
University of Chicago

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Hierarchical Bayes Models • 419

include the relationship of needs to desired attributes or wants, wants to brand beliefs and consideration sets, and consideration sets to preference orderings and choice. These extended models are often conceptualized in a hierarchical manner, where movement from one model component to the next proceeds in a logical manner. Estimation of these new integrated models is not possible without Bayesian methods.

The nature and determinants of heterogeneity have also received much attention over the past 10 years. Across dozens of studies, the distribution of heterogeneity has been shown to be better represented by a continuous, not a discrete, distribution (e.g., from a finite mixture model) of heterogeneity (Allenby, Arora, & Ginter, 1998). This has important implications for analysis connected with market segmentation, where researchers often incorrectly assert the existence of a small number of homogeneous groups. Bayesian methods are being used to identify new basis variables that point to brand preferences (Yang, Allenby, & Fennell, 2002), new ways of dealing with respondent heterogeneity in scale usage (Rossi, Gilula, & Allenby, 2001), and new ways of characterizing social networks and their impact on demand (e.g., interdependent preferences; Yang & Allenby, 2003). These developments would again not be possible without modern Bayesian methods.

In this chapter, we provide an introduction to hierarchical Bayes models and an overview of successful applications. Underlying assumptions are discussed in the next section, followed by an introduction to the computational arm of

look behind the data requires models that reflect associations of interest. Consider, for example, an analysis designed to determine the influence of price on the demand for a product or service. If the offering is available in continuous units (e.g., minutes of cell phone usage), then a regression model (see Chapter 13) can be used to measure price sensitivity using the following model:

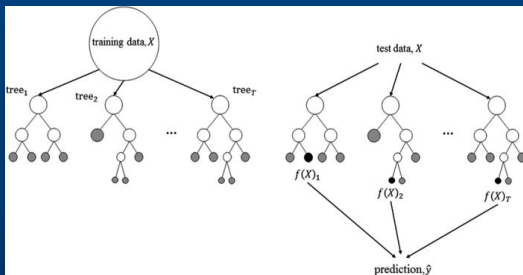
$$y_t = \beta_0 + \beta_1 \text{price}_t + \epsilon_t; \epsilon_t \sim \text{Normal}(0, \sigma^2) \quad (1)$$

where y_t denotes demand at time t , price_t is the price at time t , and β_0 , β_1 , and σ^2 are parameters to be estimated from the data. The parameters β_0 and β_1 define the expected association between price and demand. Given the price at any time, t , one can compute $\beta_0 + \beta_1 \text{price}_t$ and obtain the expected demand, y_t . The parameter σ^2 is the variance of the error term ϵ_t and reflects the uncertainty associated with relationship. Large values of σ^2 are associated with noisy predictions, and small values of σ^2 indicate an association without much uncertainty.

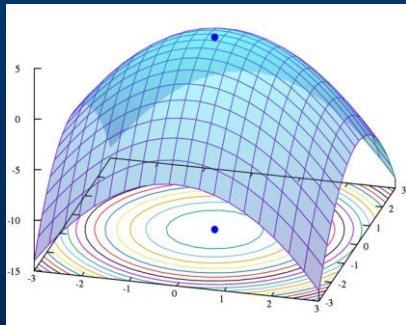
Individual-level demand, however, is rarely characterized by such a smooth, continuous association. The most frequently observed quantity of demand at the individual level is 0, and the next most frequently observed quantity is 1. Marketing data, at the individual level, are inherently discrete and noncontinuous. One approach to dealing with the discreteness of marketing data is to assume that the observed demand is a censored realization of an underlying continuous model:

The Zilliant IQ Platform Brings Best-In-Class AI to B2B

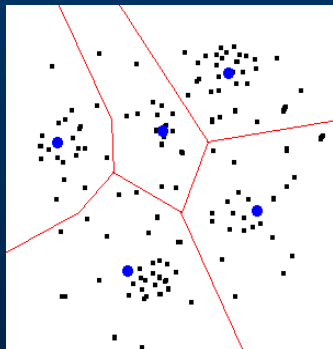
Random Forest



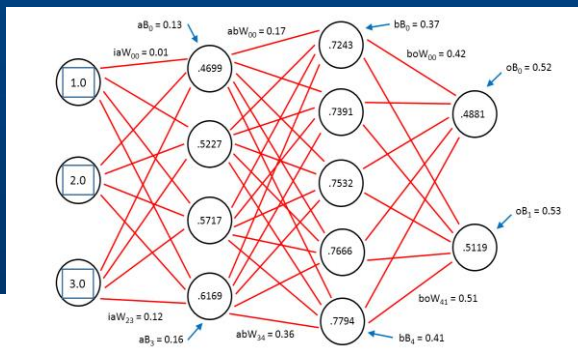
Convex Optimization



Clustering



Neural Network / Deep Learning



Association Rules

$$\begin{aligned} \text{Rule: } X \Rightarrow Y & \begin{cases} \text{Support} = \frac{frq(X, Y)}{N} \\ \text{Confidence} = \frac{frq(X, Y)}{frq(X)} \\ \text{Lift} = \frac{\text{Support}}{\text{Supp}(X) \times \text{Supp}(Y)} \end{cases} \end{aligned}$$

Codes and Slides:

<https://github.com/AmirMK/ODSC>

Question and/or Discussion:

Amir.Meimand@Zilliant.com