

# Computer Security

## Lecture 3: Cryptography

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# CRYPTOGRAPHY

# Polygram substitution

- Using two letters at a time
- If arbitrary chosen:  $(26^2)! = 676!$ 
  - Aa ab ac ad ae af ag ah ai
  - RL TC YB FR UU SN JA IL AP
- The key needs to be formulated via some means

# Playfair Cipher



- not even the large number of keys in a monoalphabetic cipher provides security
- one approach to improving security was to encrypt multiple letters
- the **Playfair Cipher** is an example
- invented by Charles Wheatstone in 1854, but named after his friend Baron Playfair

# Playfair Key Matrix

- a 5X5 matrix of letters based on a keyword
- fill in letters of keyword (no duplicates)
- fill rest of matrix with other letters
- eg. using the keyword MONARCHY

<b>M</b>	<b>O</b>	<b>N</b>	<b>A</b>	<b>R</b>
<b>C</b>	<b>H</b>	<b>Y</b>	B	D
E	F	G	I / J	K
L	P	Q	S	T
U	V	W	X	Z

# Encrypting and Decrypting



- plaintext encrypted two letters at a time:
  1. if a pair is a repeated letter, insert a filler like 'X', eg. "balloon" encrypts as "ba lx lo on"
  2. if both letters fall in the same row, replace each with letter to right (wrapping back to start from end), eg. "ar" encrypts as "RM"
  3. if both letters fall in the same column, replace each with the letter below it (again wrapping to top from bottom), eg. "mu" encrypts to "CM"
  4. otherwise each letter is replaced by the one in its row in the column of the other letter of the pair, eg. "hs" encrypts to "BP", and "ea" to "IM" or "JM" (as desired)

# Security of the Playfair Cipher



- security much improved over monoalphabetic
- since have  $26 \times 26 = 676$  digrams
- would need a 676 entry frequency table to analyse (verses 26 for a monoalphabetic)
- and correspondingly more ciphertext
- was widely used for many years (eg. US & British military in WW1)
- it **can** be broken, given a few hundred letters
- since still has much of plaintext structure

# Polyalphabetic Ciphers

- another approach to improving security is to use multiple cipher alphabets
- called **polyalphabetic substitution ciphers**
- makes cryptanalysis harder with more alphabets to guess and flatter frequency distribution
- use a key to select which alphabet is used for each letter of the message
- use each alphabet in turn
- repeat from start after end of key is reached



- simplest polyalphabetic substitution cipher is the **Vigenère Cipher**
- effectively multiple caesar ciphers
- key is multiple letters long  $K = k_1 k_2 \dots k_d$
- $i^{\text{th}}$  letter specifies  $i^{\text{th}}$  alphabet to use
- use each alphabet in turn
- repeat from start after  $d$  letters in message
- decryption simply works in reverse

# Example



- write the plaintext out
- write the keyword repeated above it
- use each key letter as a caesar cipher key
- encrypt the corresponding plaintext letter
- eg using keyword *deceptive*

```
key:      deceptive
plaintext: wearediscoveredsaveyourself
ciphertext: ZICVTWQNGRZGVTWAVZHCQYGLMGJ
```

# Plain text

Key

	<i>ABCDEFGHIJKLMNOPQRSTUVWXYZ</i>
<i>A</i>	<i>ABCDEFGHIJKLMNOPQRSTUVWXYZ</i>
<i>B</i>	<i>BCDEFGHIJKLMNOPQRSTUVWXYZA</i>
<i>C</i>	<i>CDEFGHIJKLMNOPQRSTUVWXYZAB</i>
<i>D</i>	<i>DEFGHIJKLMNOPQRSTUVWXYZABC</i>
<i>E</i>	<i>EFGHIJKLMNOPQRSTUVWXYZABCD</i>
<i>F</i>	<i>FGHIJKLMNOPQRSTUVWXYZABCDE</i>
<i>G</i>	<i>GHIJKLMNOPQRSTUVWXYZABCDEF</i>
<i>H</i>	<i>HJKLMNOPQRSTUVWXYZABCDEFG</i>
<i>I</i>	<i>IJKLMNOPQRSTUVWXYZABCDEFGH</i>
<i>J</i>	<i>JKLMNOPQRSTUVWXYZABCDEFGHI</i>
<i>K</i>	<i>KLMNOPQRSTUVWXYZABCDEFGHIJ</i>
<i>L</i>	<i>LMNOPQRSTUVWXYZABCDEFGHIJK</i>
<i>M</i>	<i>MNOPQRSTUVWXYZABCDEFGHIJKL</i>
<i>N</i>	<i>NOPQRSTUVWXYZABCDEFGHIJKLM</i>
<i>O</i>	<i>OPQRSTUVWXYZABCDEFGHIJKLMN</i>
<i>P</i>	<i>PQRSTUVWXYZABCDEFGHIJKLMNO</i>
<i>Q</i>	<i>QRSTUVWXYZABCDEFGHIJKLMNOP</i>
<i>R</i>	<i>RSTUVWXYZABCDEFGHIJKLMNOPQ</i>
<i>S</i>	<i>STUVWXYZABCDEFGHIJKLMNOPQR</i>
<i>T</i>	<i>TUVWXYZABCDEFGHIJKLMNOPQRS</i>
<i>U</i>	<i>UVWXYZABCDEFGHIJKLMNOPQRST</i>
<i>V</i>	<i>VWXYZABCDEFGHIJKLMNOPQRSTU</i>
<i>W</i>	<i>WXYZABCDEFGHIJKLMNOPQRSTUV</i>
<i>X</i>	<i>XYZABCDEFGHIJKLMNOPQRSTUVW</i>
<i>Y</i>	<i>YZABCDEFGHIJKLMNOPQRSTUVWX</i>
<i>Z</i>	<i>ZABCDEFGHIJKLMNOPQRSTUVWXY</i>

# Security of Vigenère Ciphers



- have multiple ciphertext letters for each plaintext letter
- hence letter frequencies are obscured
- but not totally lost
- start with letter frequencies
  - see if look monoalphabetic or not
- if not, then need to determine number of alphabets, since then can attach each

- method developed by Babbage / Kasiski
- repetitions in ciphertext give clues to period
- so find same plaintext an exact period apart
- which results in the same ciphertext
- eg repeated “VTW” in previous example
- suggests size of 3 or 9
- then attack each monoalphabetic cipher individually using same techniques as before

- ideally want a key as long as the message
- Vigenère proposed the **autokey** cipher
- with keyword is prefixed to message as key
- knowing keyword can recover the first few letters
- use these in turn on the rest of the message
- but still have frequency characteristics to attack I.e. the key and message share the same frequency distribution.
- eg. given key *deceptive*

```
key:      deceptive
plaintext: wearediscoveredsaveyourself
ciphertext: ZICVTWQNGKZEIIGASXSTSLVWLA
```

# One-Time Pad



- if a truly random key as long as the message is used, the cipher will be secure
- called a One-Time pad
- is unbreakable since ciphertext bears no statistical relationship to the plaintext
- since for **any plaintext** & **any ciphertext** there exists a key mapping one to other
- can only use the key **once** though
- have problem of safe distribution of key

# Transposition Ciphers



- now consider classical **transposition** or **permutation** ciphers
- these hide the message by rearranging the letter order
- without altering the actual letters used
- can recognise these since have the same frequency distribution as the original text



# Rail Fence cipher

- write message letters out diagonally over a number of rows
- then read off cipher row by row

- eg. write message out as:

```
m e m a t r h t g p r y
  e t e f e t e o a a t
```

- giving ciphertext

```
MEMATRHTGPRYETEFETEOAAT
```

# Row Transposition Ciphers

- a more complex scheme
- write letters of message out in rows over a specified number of columns
- then reorder the columns according to some key before reading off the rows

Key:           4 3 1 2 5 6 7

Plaintext: a t t a c k p

o s t p o n e

d u n t i l t

w o a m x y z

Ciphertext: TTNAAPTMTSUOAODWCOIXKNLYPETZ

# Route transposition

t	h	i	s	i
s	a	s	e	c
r	e	t	m	e
s	s	a	g	e
v	w	x	y	z

→ ISCEE IHSME  
ZGTAT SEAYX  
SRSWV

- ciphers using substitutions or transpositions are not secure because of language characteristics
- hence consider using several ciphers in succession to make harder, but:
  - two substitutions make a more complex substitution
  - two transpositions make more complex transposition
  - but a substitution followed by a transposition makes a new much harder cipher
- this is bridge from classical to modern ciphers

- an alternative to encryption
- hides existence of message
  - using only a subset of letters/words in a longer message marked in some way
  - using invisible ink
- has drawbacks
  - high overhead to hide relatively few info bits

- have considered:
  - classical cipher techniques and terminology
  - monoalphabetic substitution ciphers
  - cryptanalysis using letter frequencies
  - Playfair ciphers
  - polyalphabetic ciphers
  - transposition ciphers
  - product ciphers and rotor machines
  - stenography

# END