

Computer Fundamentals

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Lecture 6





Binary Logic Operations

- > Also called Boolean logic operations
- > Boolean variable can have only two possible values i.e. 0 or 1
- Logic operations or functions of Boolean variables
 - E.g. AND, OR, NOT etc.





Binary Logic Operations

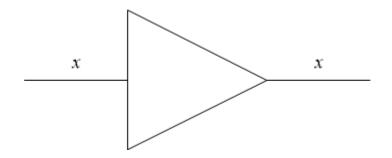
Name	Example	Symbolically
Buffer	y = x	\mathcal{X}
NOT	y = NOT(x)	$\overline{\mathcal{X}}$
AND	z = x AND y	x.y
OR	z = x OR y	x + y
XOR	z = x XOR y	$x \oplus y$
NAND	z = x NAND y	$\overline{x.y}$
NOR	z = x NOR y	$\overline{x+y}$
XNOR	z = x XNOR y	$\overline{x \oplus y}$



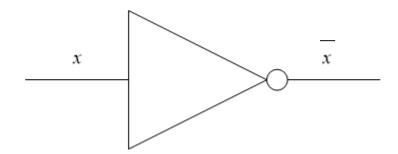


Diagrammatic Representation

> Buffer



> NOT

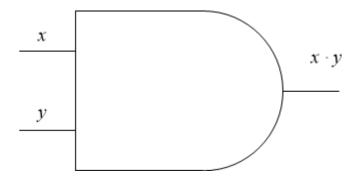




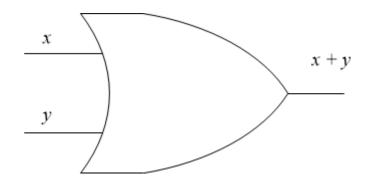


Diagrammatic Representation (cont.)

> AND



> OR

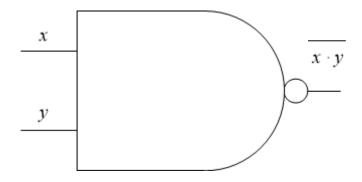




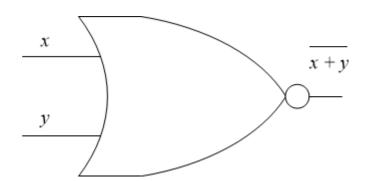


Diagrammatic Representation (cont.)

> NAND



> NOR

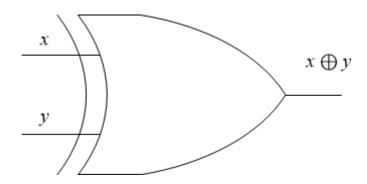




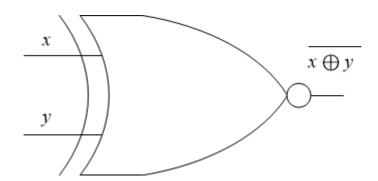


Diagrammatic Representation (cont.)

> XOR



> XNOR







Truth Table

- Defines the output of a logic function for all possible inputs
 □ 2ⁿ rows in a truth table (n is the number of inputs)
- > Truth table for NOT

\mathcal{X}	\overline{x}
О	1
1	0





> Truth table for OR

X	У	x + y
0	0	
0	1	
1	0	
1	1	





> Truth table for AND

\mathcal{X}	У	x.y
0	0	
0	1	
1	0	
1	1	





> Truth table for XOR

X	y	$x \oplus y$
0	0	
0	1	
1	0	
1	1	





> Truth table for NOR

X	У	x + y	${x+y}$
0	0		
0	1		
1	0		
1	1		





> Truth table for NAND

X	У	x.y	$\overline{x.y}$
0	0		
0	1		
1	0		
1	1		





> Truth table for XNOR

X	У	$x \oplus y$	$\overline{x \oplus y}$
0	0		
0	1		
1	0		
1	1		





Boolean Laws

> AND

$$0 \cdot x = 0$$

$$1 \cdot x = x$$

> OR

$$0 + x = x$$

$$1 + x = 1$$





> AND

$$x \cdot x = x$$

$$x \cdot x = 0$$

> OR

$$x + x = x$$

$$x + x = 1$$





> AND

Commutativity

$$x \cdot y = y \cdot x$$

Associativity

$$(x \cdot y) \cdot z = x \cdot (y \cdot z)$$

☐ Distributivity

$$x \cdot (y+z) = (x \cdot y) + (x \cdot z)$$





> OR

Commutativity

$$x + y = y + x$$

Associativity

$$(x+y)+z=x+(y+z)$$

□ Distributivity

$$x + (y \cdot z) = (x + y) \cdot (x + z)$$





> DeMorgan's Law

■ NAND

$$\overline{x \cdot y} = \overline{x} + \overline{y}$$

■ NOR

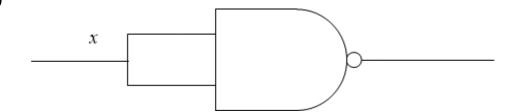
$$\overline{x+y} = \overline{x} \cdot \overline{y}$$





NAND for Every Gate

- Possible to emulate any gate
 - ☐ Using combination of NAND gates
- > NOT gate with NAND
 - □ Compare with NOT



\boldsymbol{x}	x.x	<u></u>
0	0	1
1	1	0

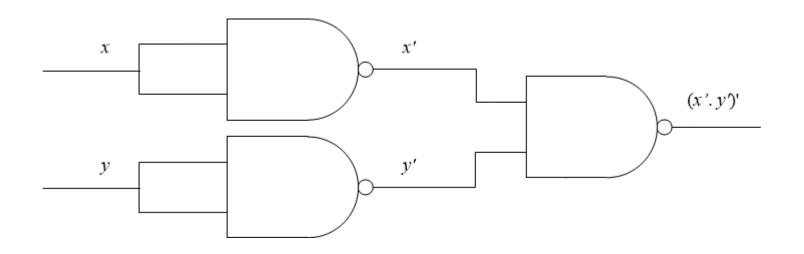




NAND for Every Gate (cont.)

- > OR gate with NAND
 - □ Recall DeMorgan's Law

$$x + y = \overline{x}.y$$







NAND for Every Gate (cont.)

- > OR gate with NAND
 - □ Recall DeMorgan's Law

$$x + y = \overline{x}.y$$

□ Compare with OR

X	у	$\overline{x.x} = \overline{x}$	$\overline{y.y} = \overline{y}$	= $x.y$
0	0	1	1	0
0	1	1	0	1
1	0	0	1	1
1	1	0	0	1



Exercise

> Design AND gate using only NAND gates

