In The Name of God. The Merciful, The Compassionate.

PMBP: PatchMatch Belief Propagation for Correspondence Field Estimation

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1 Abstract and Introduction

This paper draws a new connection between PatchMatch(PM) and Particle Belief Propagation (PBP). The key contributions are as follows:

- 1. description of PM and BP in terms that allow the connection between them be clearly described.
- 2. use of this analysis to define a new algorithm PMBP which is more accurate than PM and faster than BP.

Belief Propagation (BP)

Correspondence field is parametrized by a vector grid $\{\mathbf{u}_s\}_{s=1}^n$ where s indexes nodes (correspondence to image pixels) and $\mathbf{u}_s \in \mathbb{R}^d$ parametrizes the correspondence vector at s.

Problems with the data term for weighted patch flow are as follows:

- 1. it implicitly assumes a constant correspondence field in the $(2h+1) \times (2h+1)$ patch surrounding every pixel (?). Large h over-smooths the output. More complex parametrization of flow field can be suggested. However, they are not computationally tractable.
- 2. h may be reduced. This causes the data term to be ambiguous. This causes the introduction of pairwise terms.

For discrete problems, where \mathbf{u} live in finite set of size D, energy can be minimized in O(nD) time, while with pairwise terms, the worst case complexity is $O(D^n)$. BP finds good minimizers in times far below the worst case. However, for correspondence problems, where \mathbf{u} lives in an effective continuous space, D must be very large. So, even minimizing unary only costs is too expensive.

PatchMatch

An efficient way to compute a nearest neighbour field (NNF) between 2 images. It is considered as an efficient global minimizer for unary term only energies.

In PatchMatch Stereo [3] disparity is over-parametrized by 3D vector $\mathbf{u}_s = [a_s, b_s, c_s]^T$, parametrizing planar disparity surface $\Delta_s(x, y) = a_s(x - x_s) + b_s(y - y_s) + c_s$.

A key deficiency of PM is that it lack an explicit smoothness control on output field (has deficiency in finding reliable correspondences in very large smooth regions). A related deficiency is tendency of PM to require a form of early stopping: global optimum of unary energy is not necessarily the best solution in terms of image error $(?) \rightarrow error\ versus\ energy\ trade-off$.

$$f(S) := \{f(s)|s \in S\}$$
 fargmin_K(S, f) := S_K \(\sigma S \) s.t. |S_K| = \(\min(K, |S|) \) and \(\max f(S_K) \) \(\le \min(S \setminus S_K) \)

1.1 PatchMatch with Particles