Machine Learning (CE 40717)

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1. Introduction
2. Multi-Layer Perceptron (MLP)
3. Neural Networks
4. Training Neural Networks
5. References

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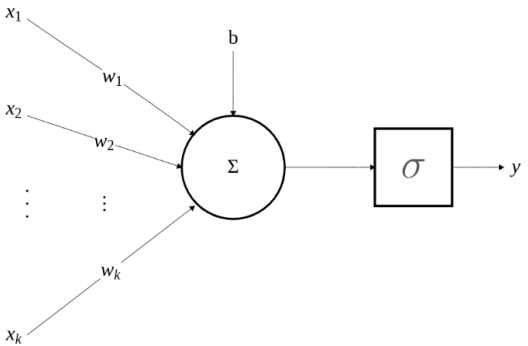
Perceptron Reminder

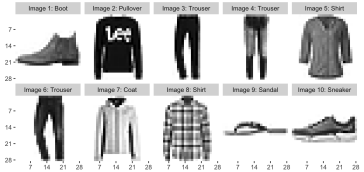
The building block of each neural network is the perceptron:

- $\{x_1, x_2, \ldots, x_k\}$: input features
- $\{w_1, w_2, \ldots, w_k\}$: feature weights
- b : bias term
- $\sigma(\cdot)$: activation function
- y : output of the neuron



Why Neural Networks?

- We can find explicit formulas for some problems (no machine learning)
  - $\Delta x = \frac{1}{2} a \cdot t^2 + v_0 \cdot t$
- We can model some problems by assuming simple relationships (classical machine learning)
  - House price as a linear function of its features
  - $y = a_1 \cdot x_1 + a_2 \cdot x_2 + \ldots + a_p \cdot x_p$
- How can we classify these images?



Why Neural Networks? Cont.

- **No explicit formula** exists to recognize a sneaker
- We intuitively recognize any sneaker
- Our brains use a **complex function** for this recognition
- **Deep neural networks** can learn this complex function

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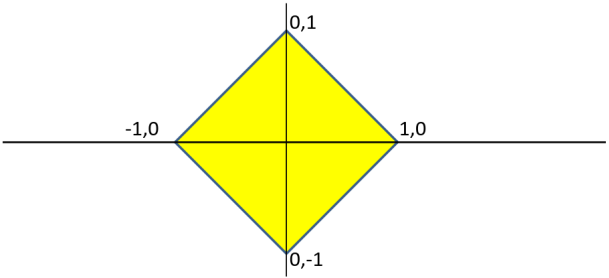
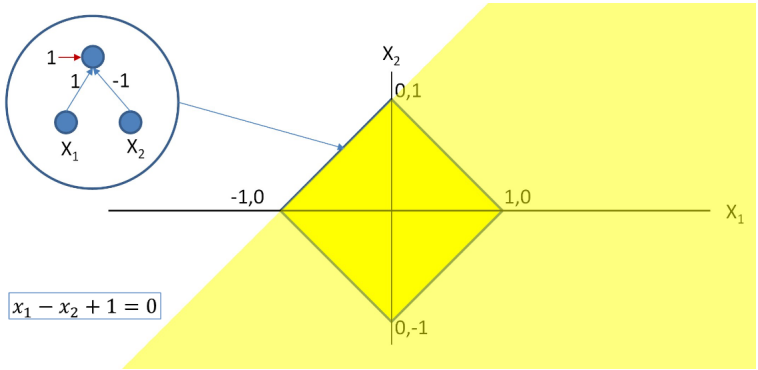
Example: MLP for Complex Patterns

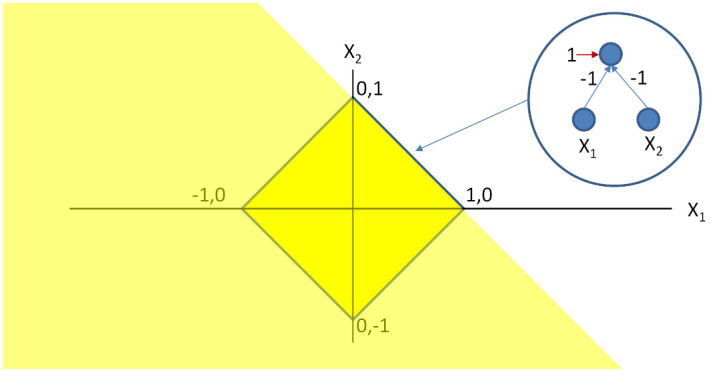
- What network to learn this area?
- Example is adapted from [1].



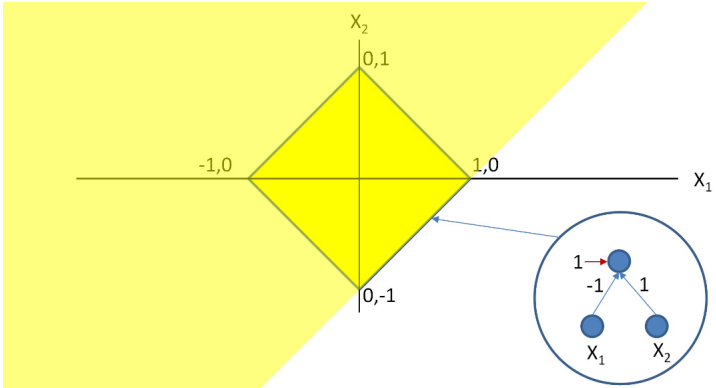
Example: MLP for Complex Patterns Cont.



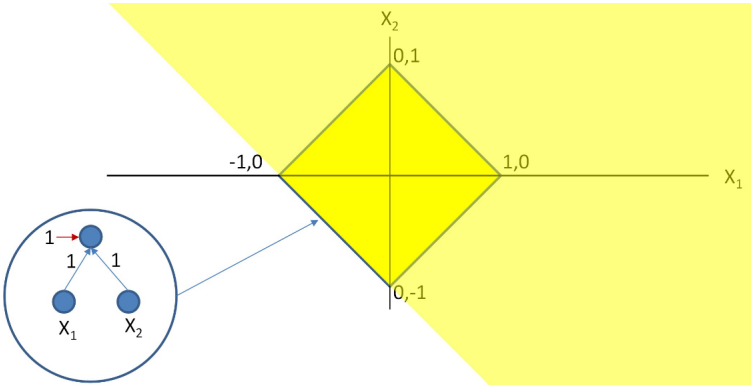
Example: MLP for Complex Patterns Cont.



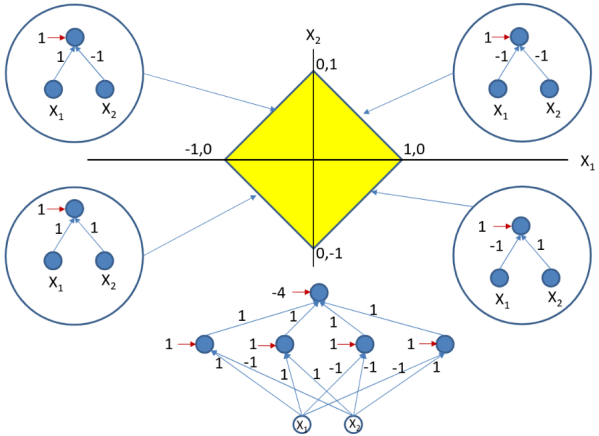
Example: MLP for Complex Patterns Cont.



Example: MLP for Complex Patterns Cont.

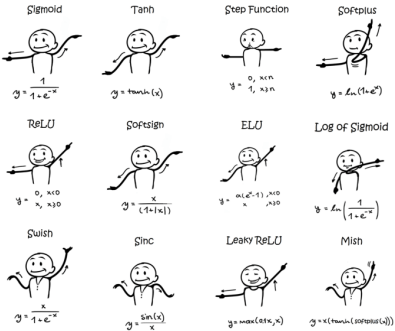


Example: MLP for Complex Patterns Cont.



MLP Capacity

- Increasing **width and depth** allow us to approximate **complex decision boundaries**
- An **activation function** makes a neuron's output **non-linear**, allowing the network to learn complex pattern
- It is **not limited** to Boolean or step functions
- With appropriate activation functions, neural networks can **approximate any real-valued function** (More details later)



Adapted from Sefiks

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Single Hidden Layer Neural Network

- Hidden layer pre-activation:

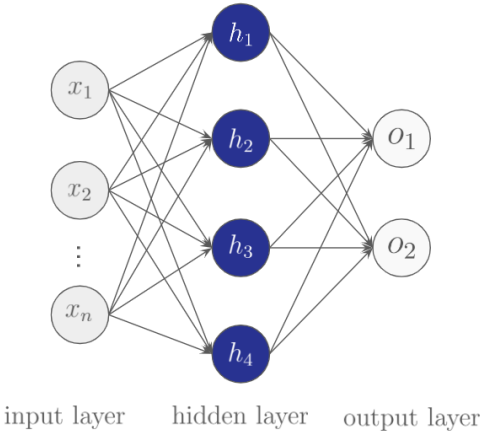
$$a_i(x) = b_i^{(1)} + \sum_j W_{ij}^{(1)} \cdot x_j$$

- Activated hidden layer:

$$h(x) = \sigma^{(1)}(a(x))$$

- Output layer:

$$o(x) = \sigma^{(2)}\left(b^{(2)} + W^{(2)} h^{(1)}(x)\right)$$



Multi-Hidden Layer Neural Network

- Let $h_i^0 = x_i$ for $i \in \{1, 2, \ldots, n\}$
- For $\ell \in \{0, 1, \ldots, L\}$:

$$a_j^{(\ell+1)} = b_j^{(\ell)} + \sum_i W_{ij}^{(\ell)} \cdot h_i^{(\ell)}$$

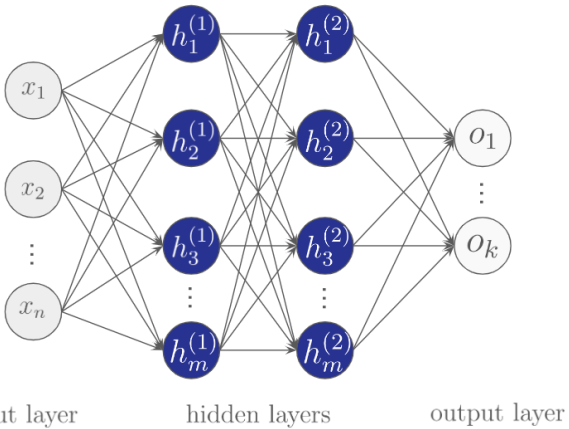
$$h_j^{(\ell+1)} = \sigma^{(\ell+1)}(a_j^{(\ell+1)})$$

- Learnable parameters:

$$b_j^{(\ell)}, W_{ij}^{(\ell)}$$

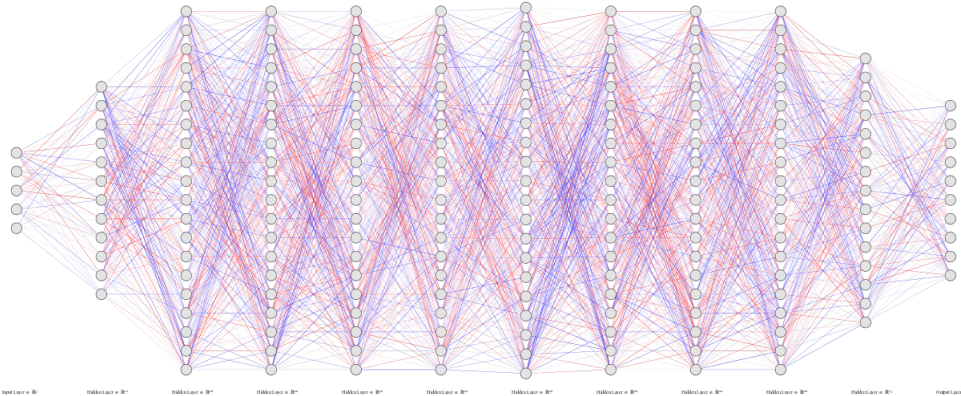
- Number of learnable parameters:

$$(n+1)m_1 + (m_1+1)m_2 + \ldots + (m_L+1)k$$



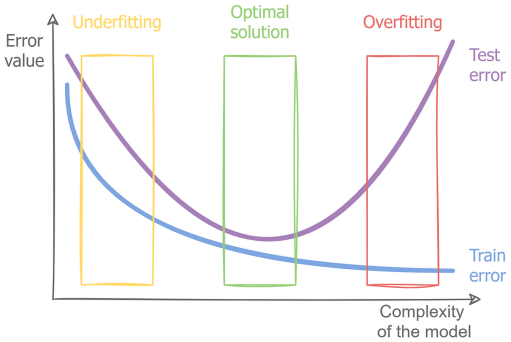
Deep Neural Network Architecture

- More than a few hidden layers: **Deep Neural Network (DNN)**
- Designing neural network architecture is **more of an art than a science**.



Network Width and Depth

- **Width:** More neurons, more complexity
- **Depth:** More layers, more abstraction
- **Balance:**
  - Too narrow/shallow: risk of underfitting
  - Too wide/deep: risk of overfitting



Adapted from Towards Data Science

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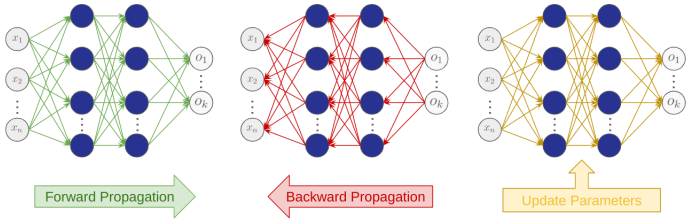
Training Phases

- **Initialize weights and biases**: These values control how the network initially processes information (more details later)
- **Forward pass**: Pass the input through the network to get an output
- **Calculate the error**: Compare the network's output to the correct answer to measure the difference (called the 'loss' – more details later)
- **Backpropagation**: Use the loss value to adjust the weights and biases to improve the network's accuracy

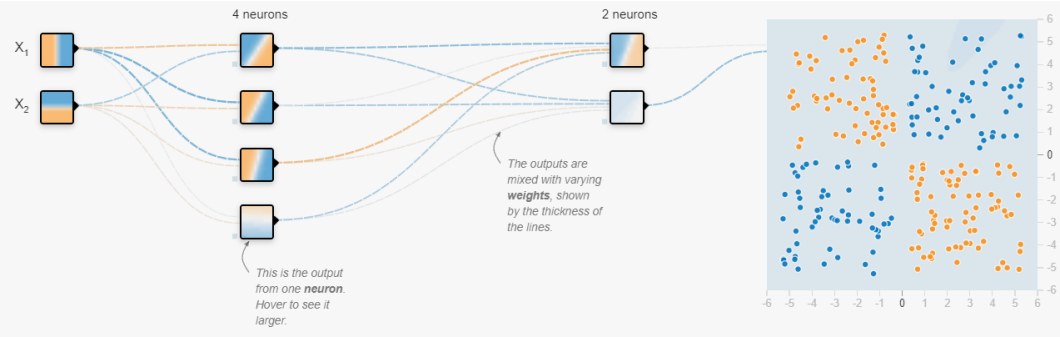


Forward Propagation

- This is the pass where we send input data through the network to make a prediction (likely inaccurate at first).
- The prediction is made by calculating weighted sums and applying an activation function in each layer

$$o(x) = a^{(L)} = \sigma^{(L)}\left(b^{(L)} + W^{(L)}\sigma^{(L-1)}\left(\dots\sigma^{(1)}(b^{(1)} + W^{(1)}x)\dots\right)\right)$$

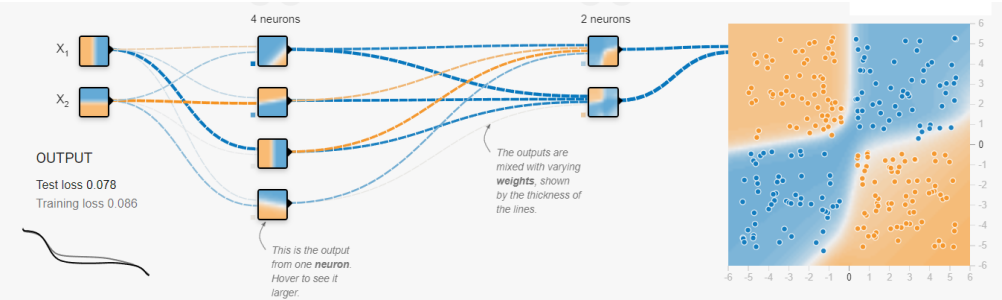
Forward Propagation Cont.



Before making predictions. Adapted from TensorFlow playground: Daniel Smilkov and Shan Carter.

Forward Propagation Cont.

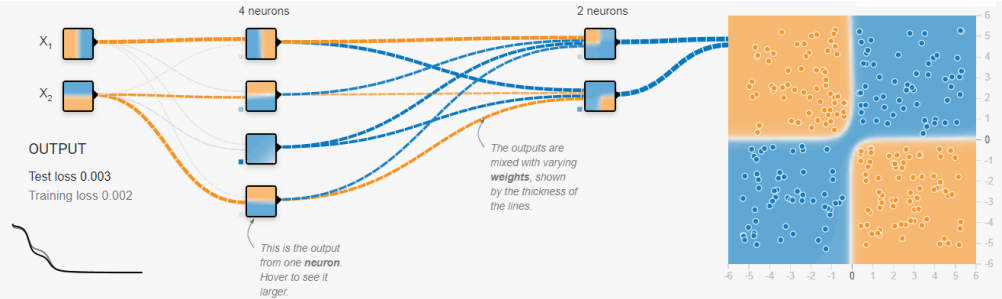
- The goal is to adjust the network's parameters to improve the predictions
- The loss is calculated after the forward pass, indicating how far off our predictions are from the true values



Loss values for predictions. Adapted from TensorFlow playground: Daniel Smilkov and Shan Carter.

BackPropagation and Parameter Update

- The network uses the **loss** to adjust its **weights and biases** through a process known as **backpropagation**
- Backpropagation calculates how much weights should change to reduce the error
- This will be explained in more detail in the following lecture



Predictions improve as the weights get updated. Adapted from TensorFlow playground: Daniel Smilkov and Shan Carter.

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Contributions

These slides are authored by:

- Sogand Salehi
- Erfan Sobhaei

[1] R. Ramakrishnan, "Deep learning course at carnegie mellon university." https://deeplearning.cs.cmu.edu/F23/index.html, 2023. Accessed: 2024–09-04.

[2] E. Mousavi and K. Alishahi, "Deep learning course at sharif university of technology." https://https://dnncourse.github.io/lectures, 2023. Accessed: 2024–09-04.

[3] D. Smilkov and S. Carter, "A neural network playground." playground.tensorflow.org, 2022. Accessed: 2024-10-14.

[4] I. Goodfellow, Y. Bengio, and A. Courville, *Deep Learning*. MIT Press, 2016.

[5] A. Géron, *Hands-On Machine Learning with Scikit-Learn, Keras, and TensorFlow: Concepts, Tools, and Techniques for Building Intelligent Systems*. O'Reilly Media, 2019.