# Bottom Up Parsing

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# LR(0) Parsing

- Build the derivation tree from the bottom
- First build the children, then connect to the parent
- Can handle left recursion
  - Which is common in real-world grammars

# LR(0) Item

An LR(0) item is of the form:

•  $N \rightarrow \alpha . \beta$ 

The **dot** gives us the current location (a local view).

# LR(0) Item

An LR(0) item with the dot at the end is called **reduce** item:

•  $N \rightarrow \alpha \beta$ .

Otherwise, it's a **shift** item:

- $N \rightarrow \alpha \beta$
- $N \rightarrow \alpha.\beta$

# LR(0) Item Closure Set

The LR(0) closure set of an item is it's  $\epsilon$ -closure.

For example, given the following CFG:

- $S \rightarrow E$ \$
- $E \rightarrow ID = X$
- $E \rightarrow \{ID\}$
- $X \rightarrow INT$

the closure set of the  $S \rightarrow E$ \$ contains:

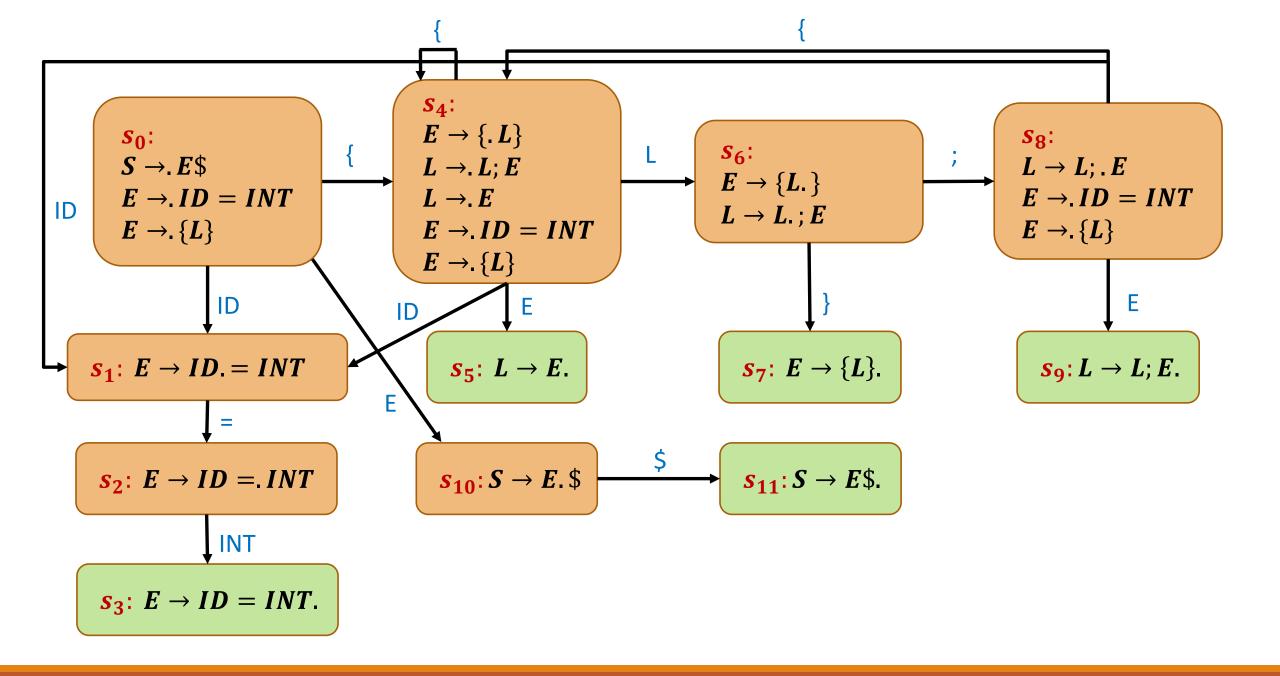
- $S \rightarrow E$ \$
- $E \rightarrow ID = X$
- $E \rightarrow \{L\}$

# LR(0) Parsing

Consider the following CFG:

- $S \rightarrow E$ \$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$
- $L \rightarrow E$
- $L \rightarrow L; E$

What will be the **transition system** of the LR(0) parser for this CFG?



We start with the initial LR(0) item (that comes from the initial rule):

•  $S \rightarrow E$ \$

The initial state is the  $\epsilon$ -closure of that item, which contains:

- $S \rightarrow E$ \$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

#### $S_0$ : $S \rightarrow E$ $E \rightarrow ID = INT$ $E \rightarrow \{L\}$

From  $s_0$ , if we recognized ID, then the next state will contain:

•  $E \rightarrow ID = INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

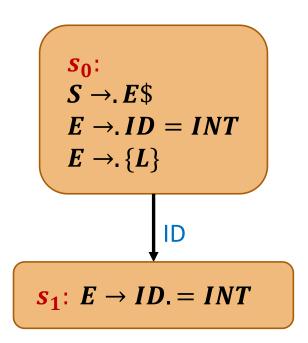
From  $s_0$ , if we recognized ID, then the next state will contain:

•  $E \rightarrow ID = INT$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $E \rightarrow ID = INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_1$ , if we recognized =, then the next state will contain:

•  $E \rightarrow ID = .INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

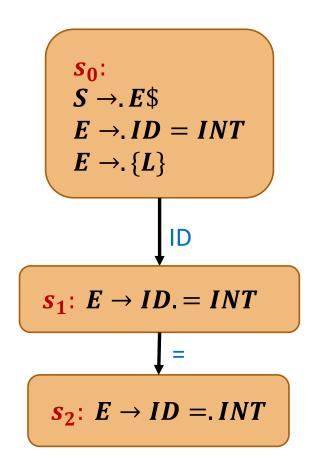
From  $s_1$ , if we recognized =, then the next state will contain:

•  $E \rightarrow ID = .INT$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $E \rightarrow ID = INT$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

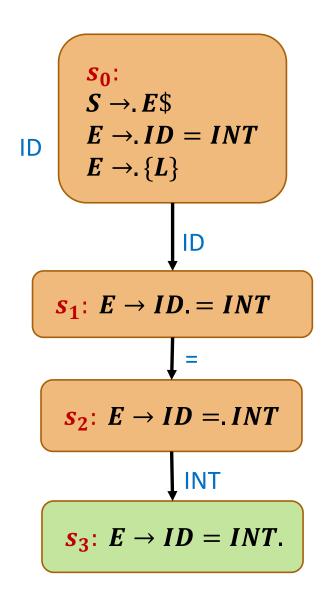


From  $s_2$ , if we recognized INT, then the next state will contain:

•  $E \rightarrow ID = INT$ .

Which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_0$ , if we recognized  $\{$ , then the next state will contain:

• 
$$E \rightarrow \{.L\}$$

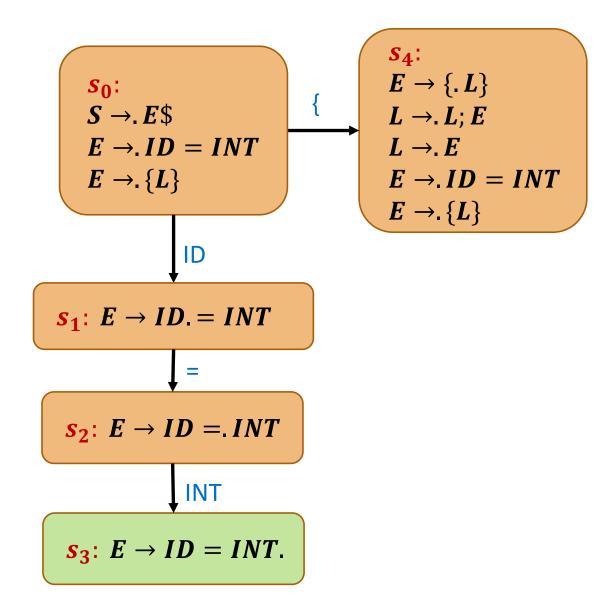
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_0$ , if we recognized  $\{$ , then the next state will contain:

•  $E \rightarrow \{.L\}$ 

- $E \rightarrow \{.L\}$
- $L \rightarrow L; E$
- $L \rightarrow E$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_4$ , if we recognized  $\{$ , then the next state will contain:

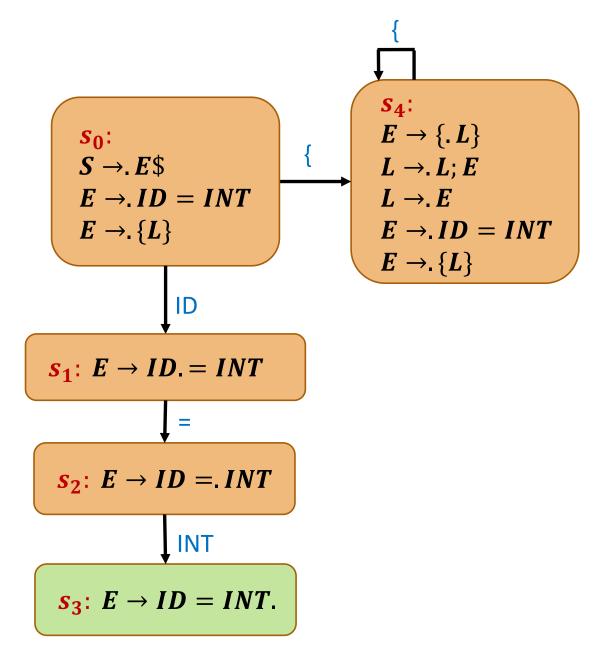
• 
$$E \rightarrow \{.L\}$$

So the next state (the  $\epsilon$ -closure) contains:

- $E \rightarrow \{.L\}$
- $L \rightarrow L; E$
- $L \rightarrow E$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

which was already computed:  $s_4$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_4$ , if we recognized ID, then the next state will contain:

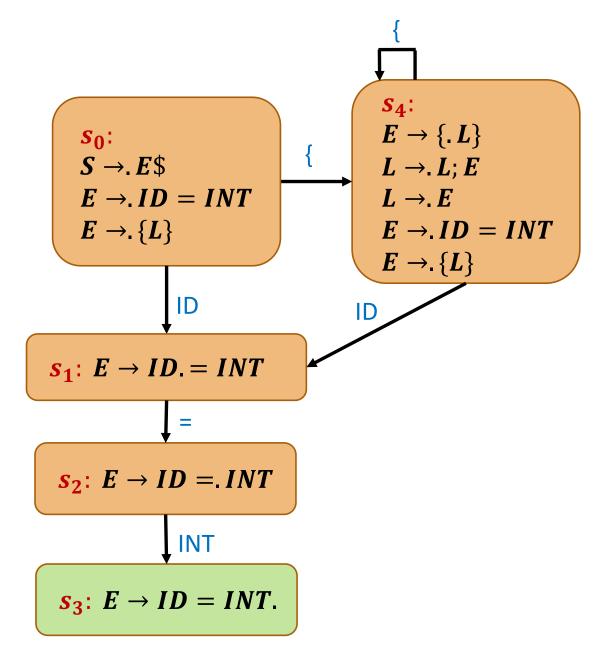
•  $E \rightarrow ID = INT$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $E \rightarrow ID = INT$ 

which was already computed:  $s_1$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

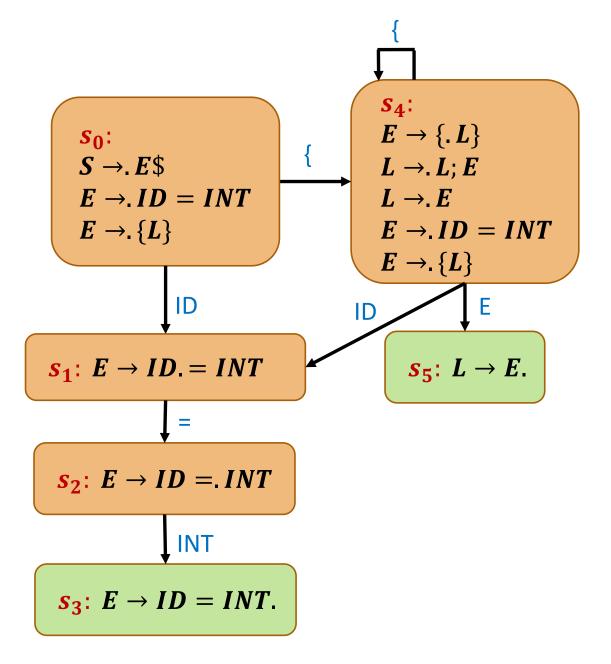


From  $s_5$ , if we recognized E, then the next state will contain:

•  $L \rightarrow E$ .

which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_4$ , if we recognized L, then the next state will contain:

- $E \rightarrow \{L.\}$
- $L \rightarrow L$ ; E

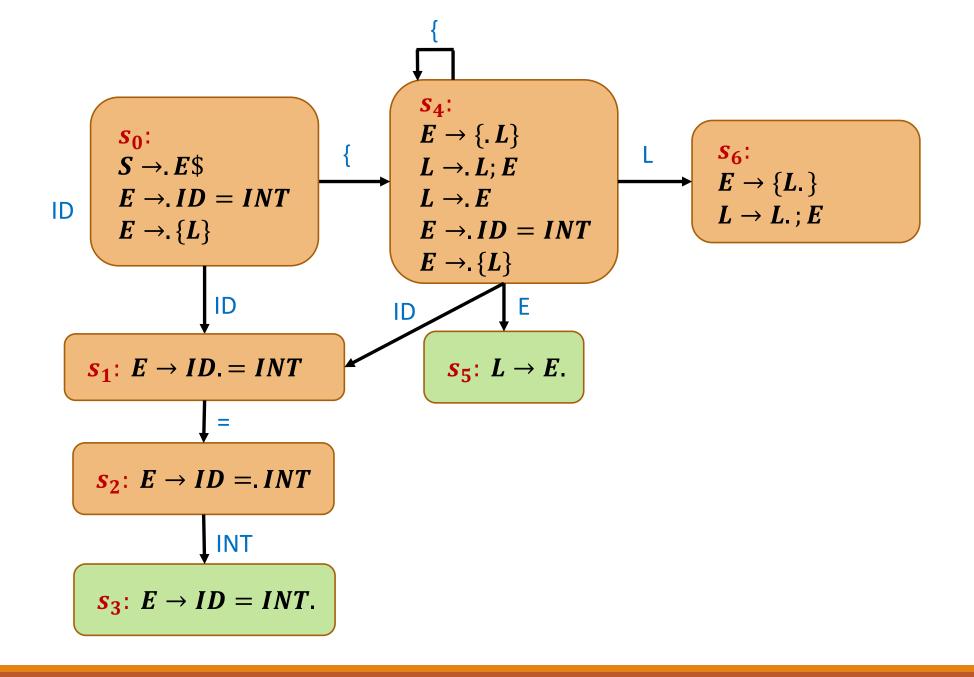
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_4$ , if we recognized L, then the next state will contain:

- $E \rightarrow \{L.\}$
- $L \rightarrow L$ ; E

- $E \rightarrow \{L.\}$
- $L \rightarrow L$ ; E

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

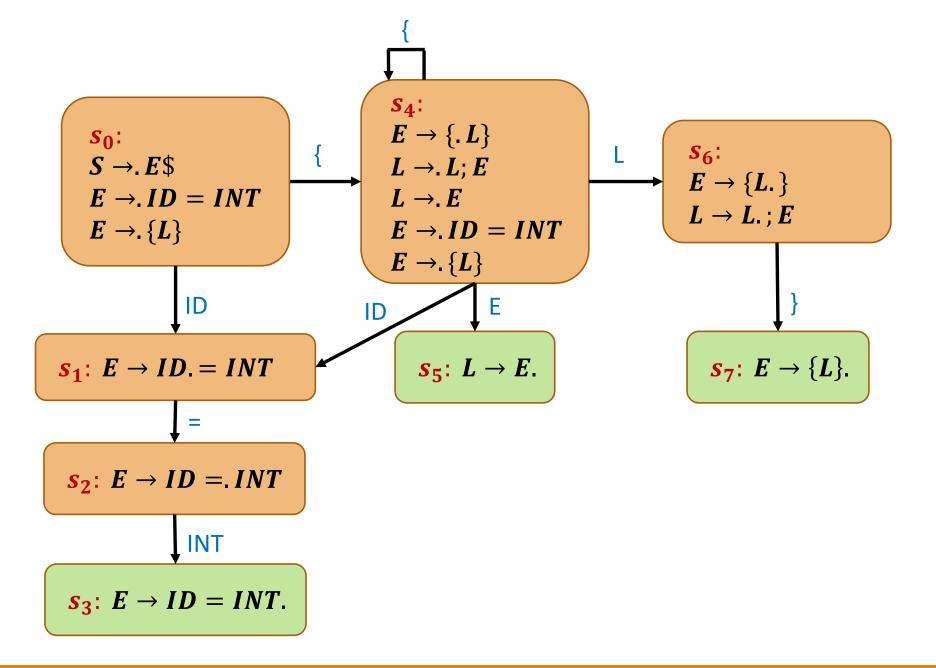


From  $s_6$ , if we recognized }, then the next state will contain:

• 
$$E \rightarrow \{L\}$$
.

Which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_6$ , if we recognized;, then the next state will contain:

• 
$$L \rightarrow L$$
;  $E$ 

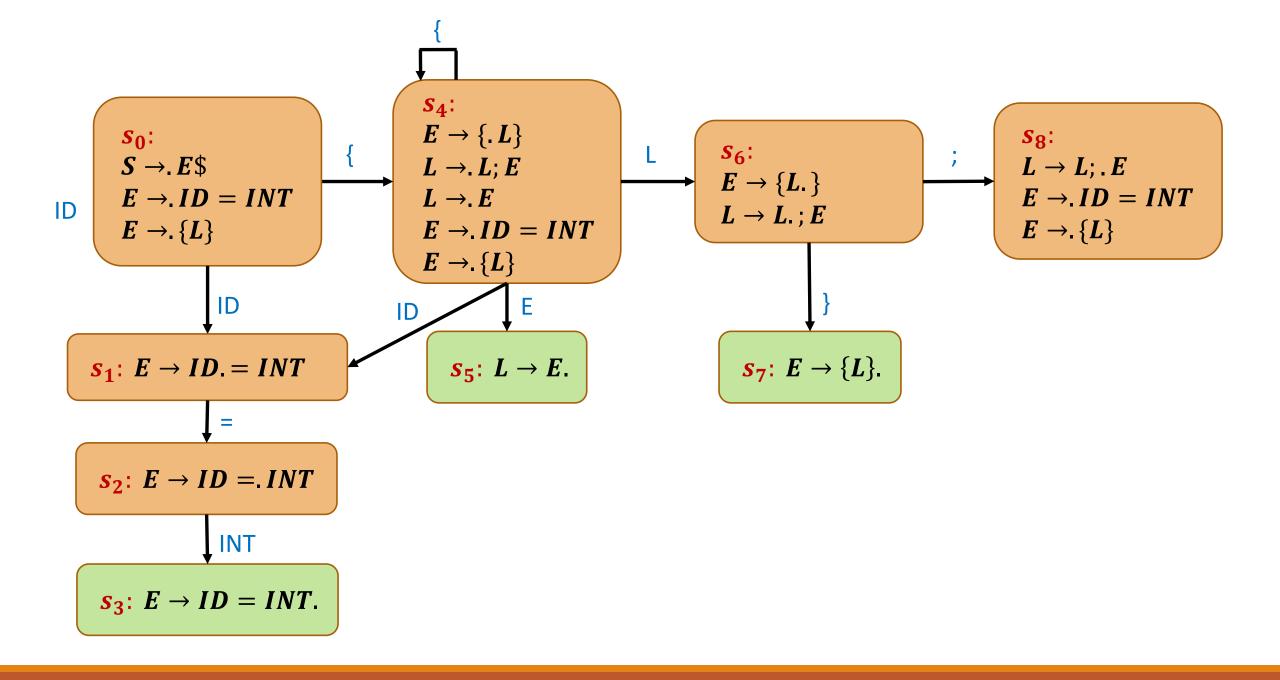
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_6$ , if we recognized;, then the next state will contain:

•  $L \rightarrow L$ ; E

- $L \rightarrow L$ ; E
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

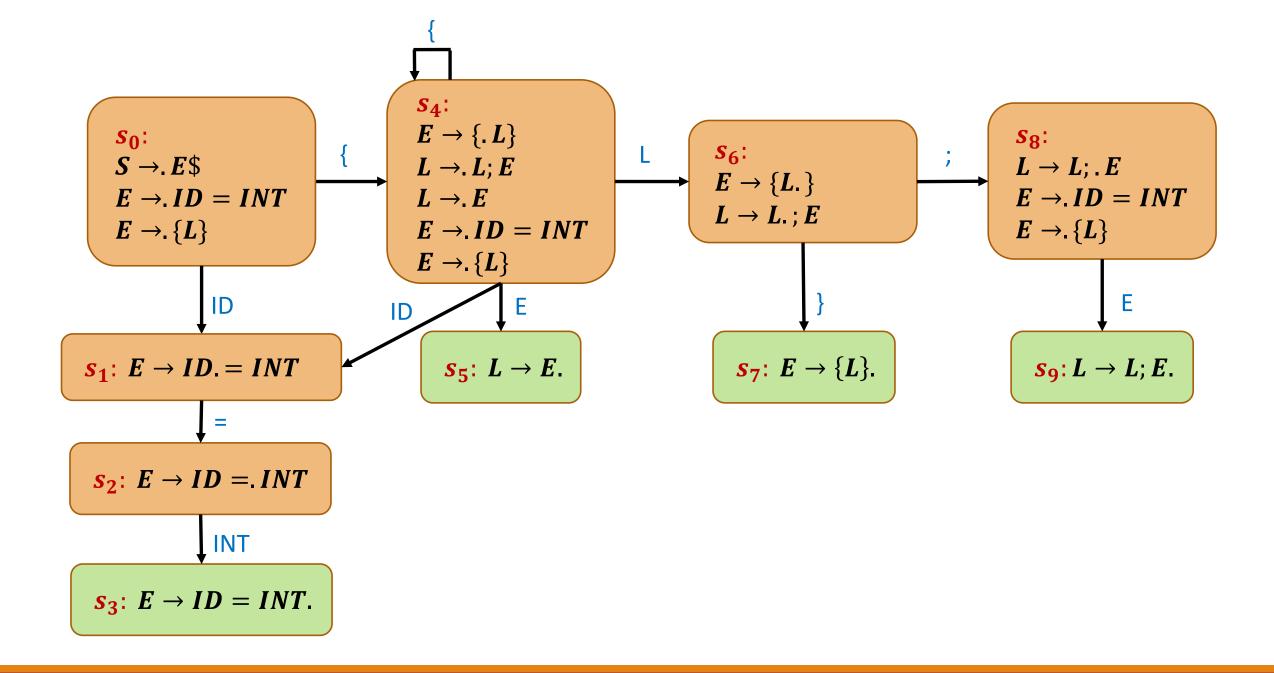


From  $s_8$ , if we recognized E, then the next state will contain:

•  $E \rightarrow L; E$ .

which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_8$ , if we recognized  $\{$ , then the next state will contain:

• 
$$E \rightarrow \{.L\}$$

So the next state (the  $\epsilon$ -closure) contains:

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_8$ , if we recognized  $\{$ , then the next state will contain:

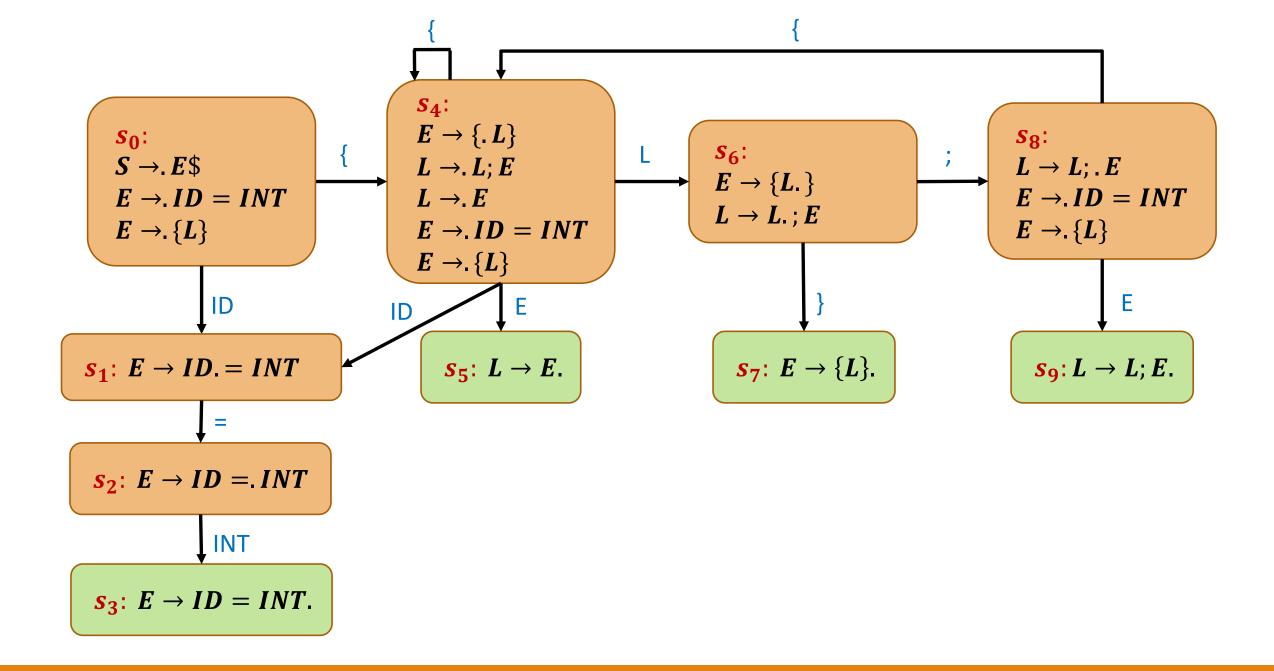
• 
$$E \rightarrow \{.L\}$$

So the next state (the  $\epsilon$ -closure) contains:

- $E \rightarrow \{.L\}$
- $L \rightarrow L; E$
- $L \rightarrow E$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

which was already computed:  $s_4$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_8$ , if we recognized ID, then the next state will contain:

•  $E \rightarrow ID = INT$ 

So the next state (the  $\epsilon$ -closure) contains:

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_8$ , if we recognized ID, then the next state will contain:

•  $E \rightarrow ID = INT$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $E \rightarrow ID = INT$ 

which was already computed:  $s_1$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

From  $s_8$ , if we recognized ID, then the next state will contain:

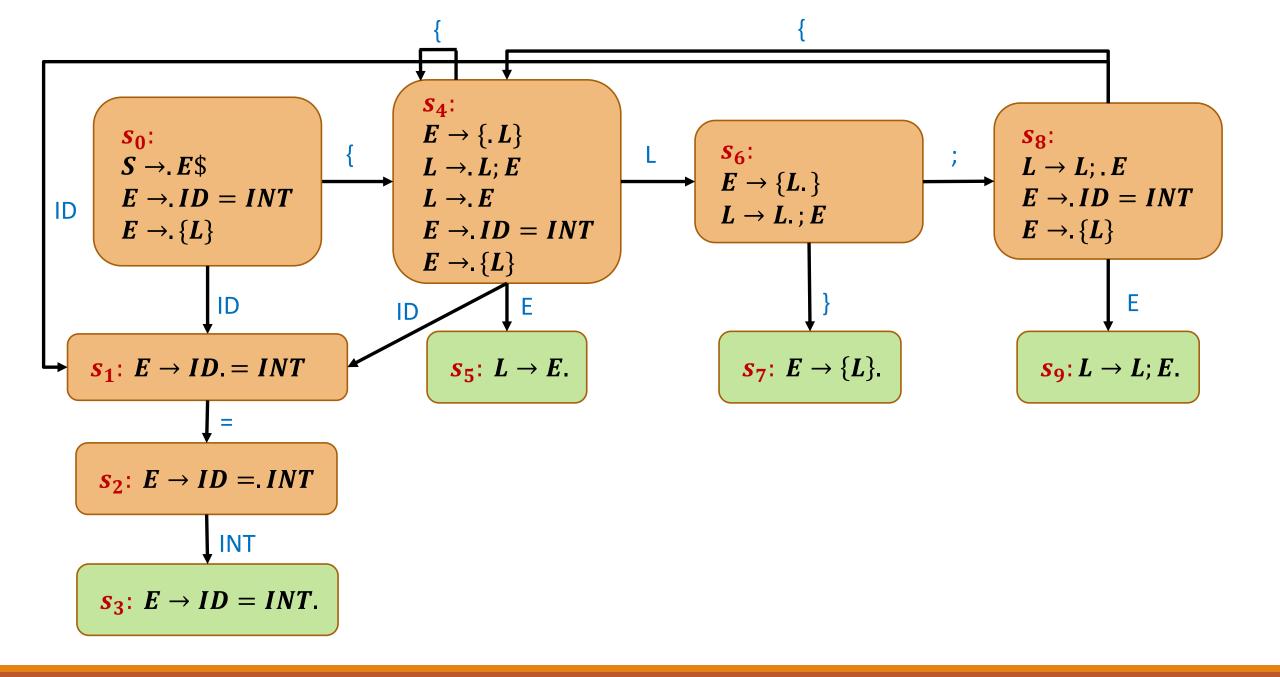
•  $E \rightarrow ID = INT$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $E \rightarrow ID = INT$ 

which was already computed:  $s_1$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 



From  $s_0$ , if we recognized E, then the next state will contain:

• 
$$S \rightarrow E.\$$$

So the next state (the  $\epsilon$ -closure) contains:

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

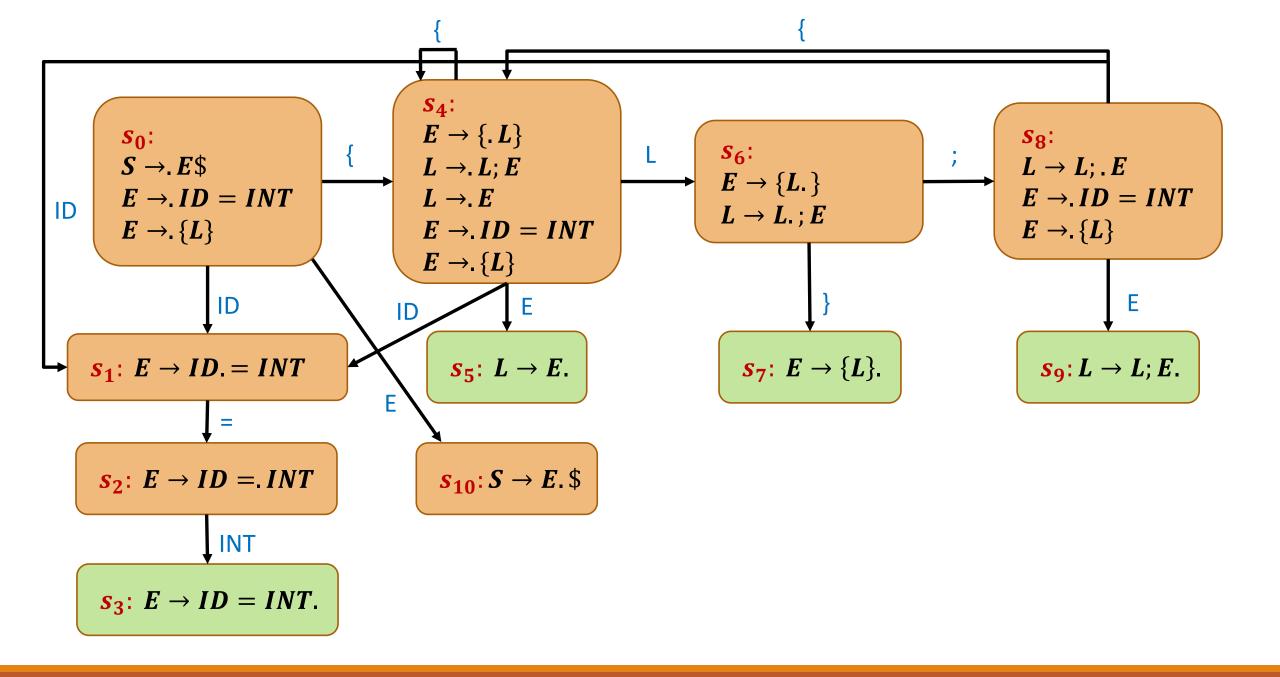
From  $s_0$ , if we recognized E, then the next state will contain:

•  $S \rightarrow E.\$$ 

So the next state (the  $\epsilon$ -closure) contains:

•  $S \rightarrow E.\$$ 

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

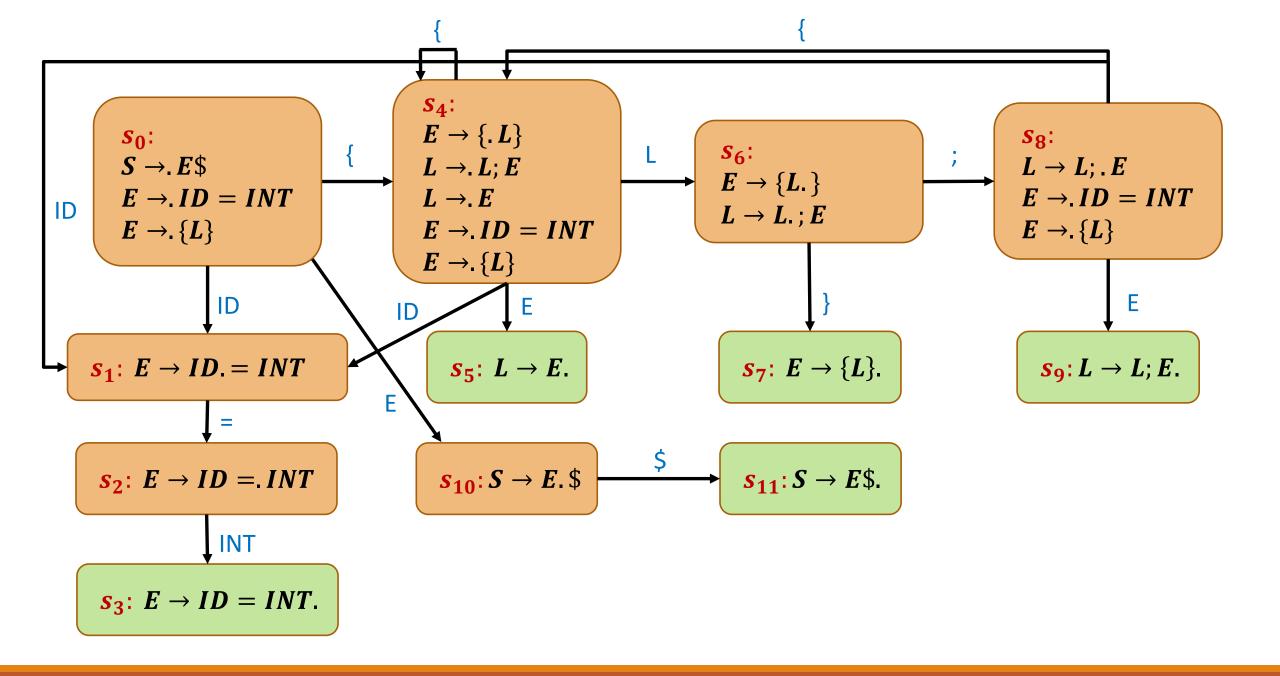


From  $s_0$ , if we recognized E, then the next state will contain:

•  $S \rightarrow E$ \$.

which is a reduce state.

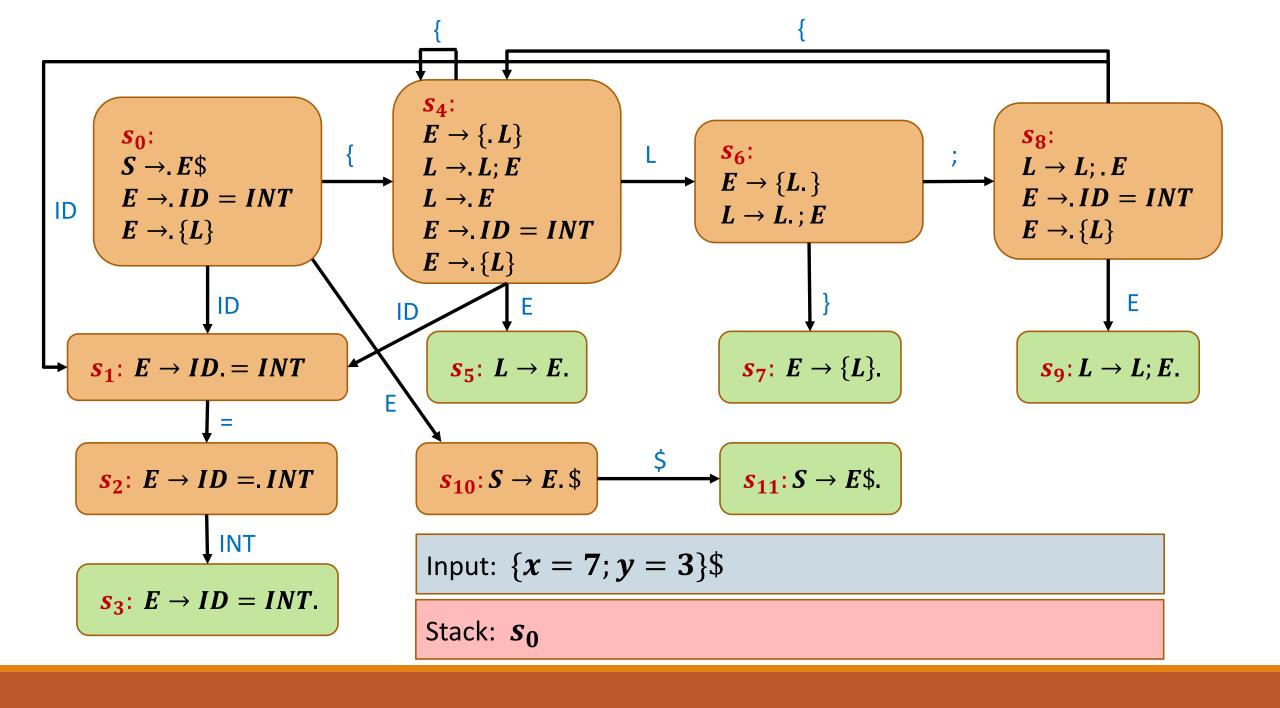
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$ 
 $E \rightarrow \{L\}$ 
 $L \rightarrow E$ 
 $L \rightarrow L; E$ 

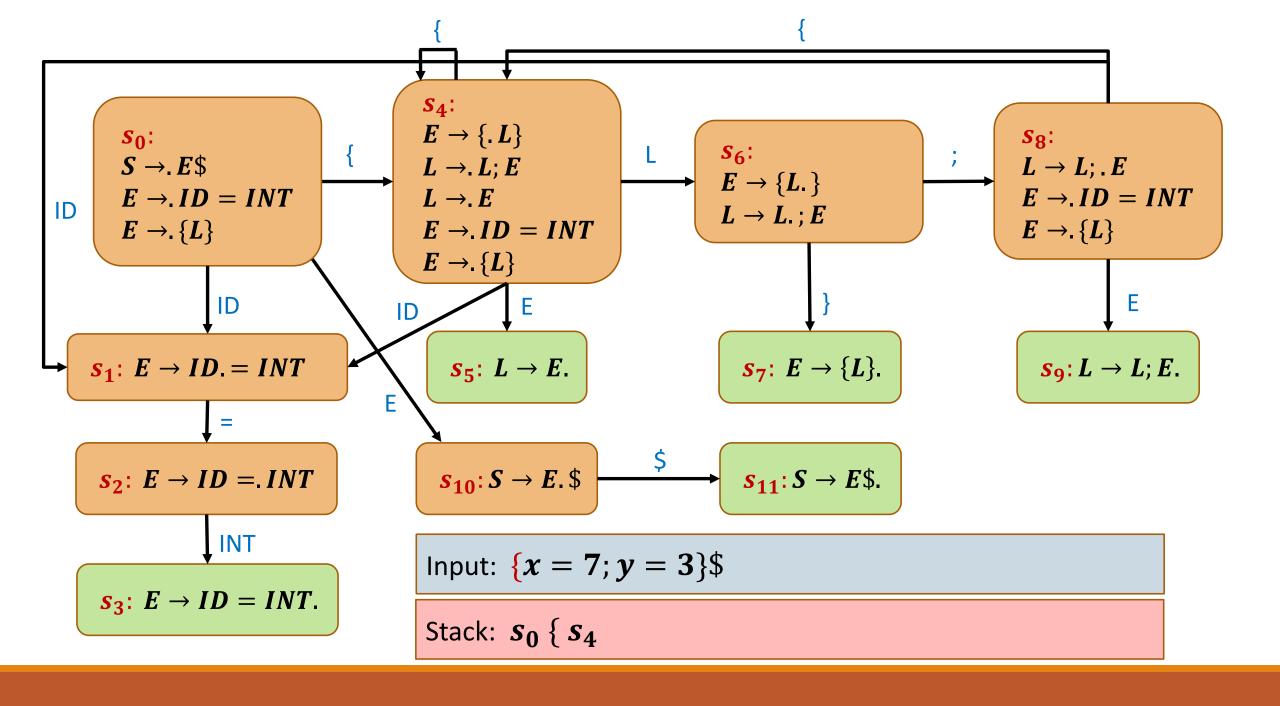


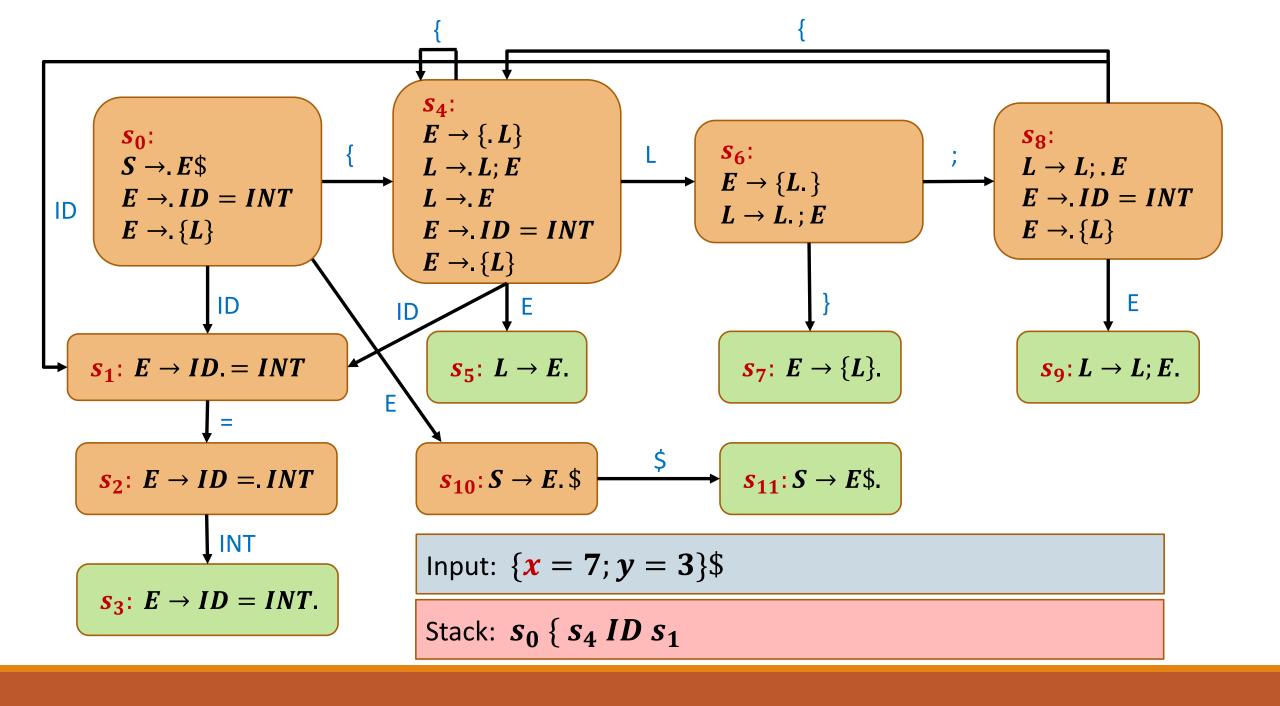
### LR(0) Parser: Running Example

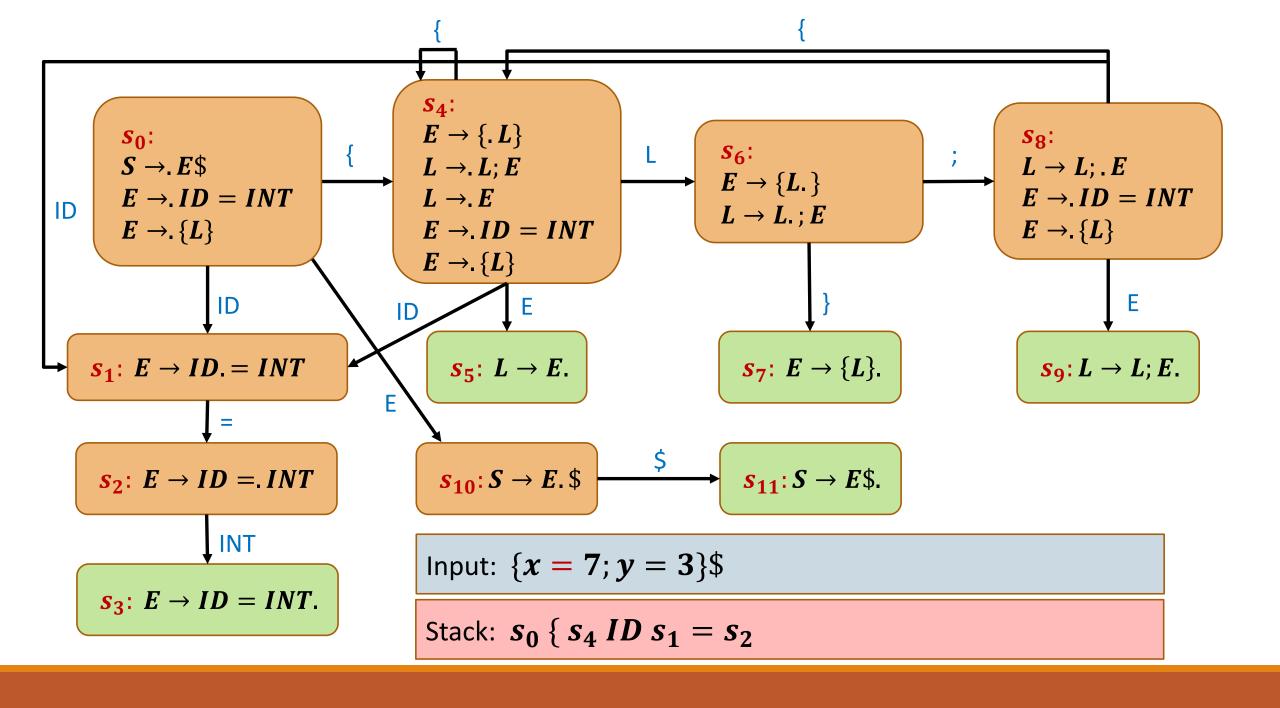
What will happen with the following input:

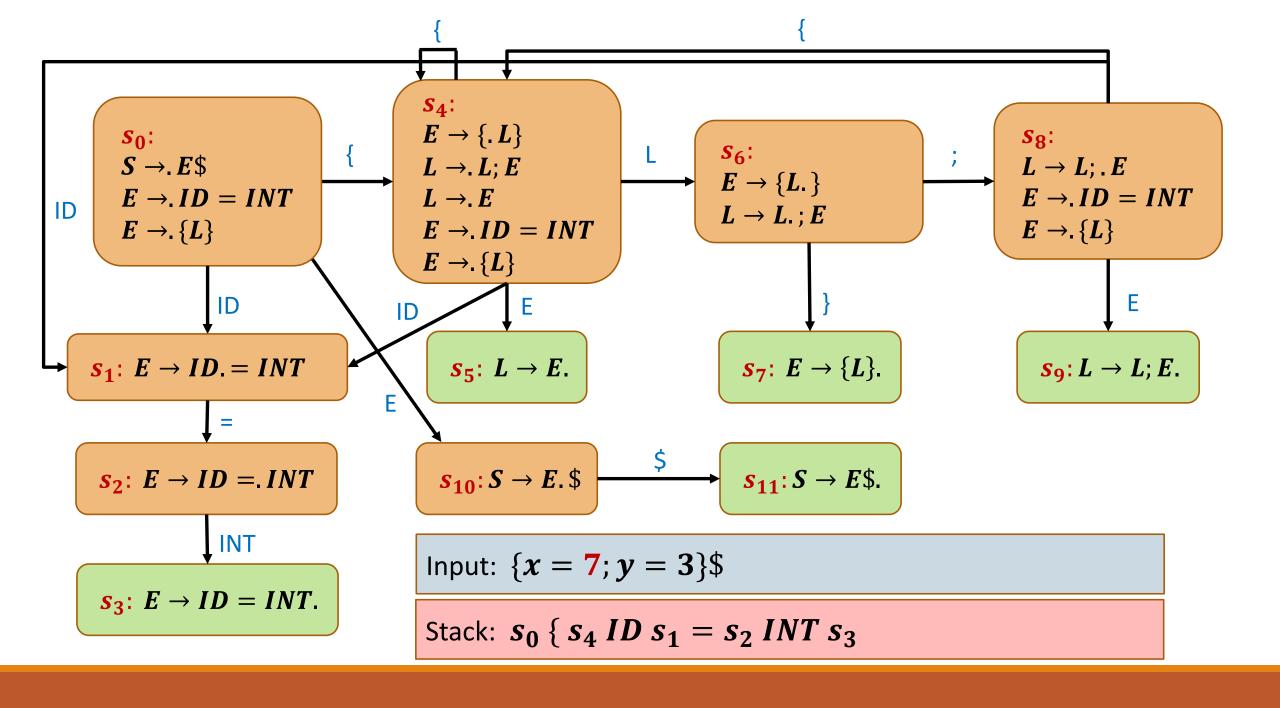
• 
$$x = 7; y = 3$$
\$

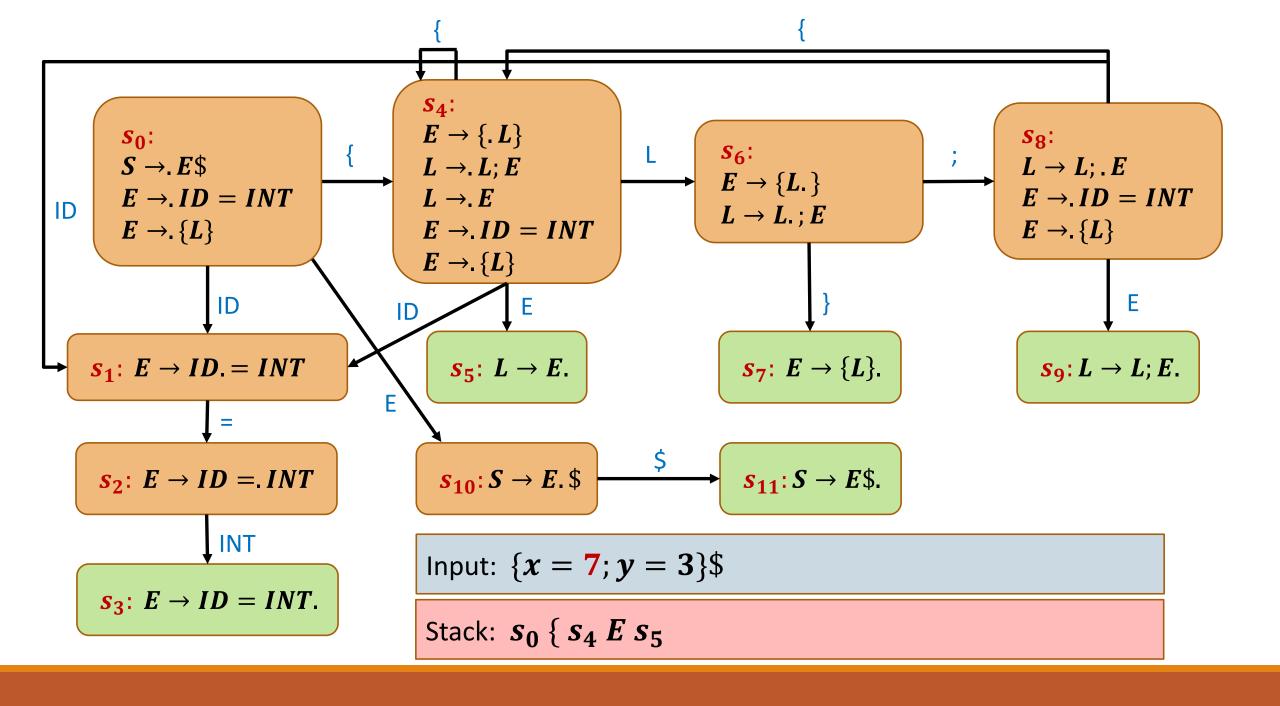


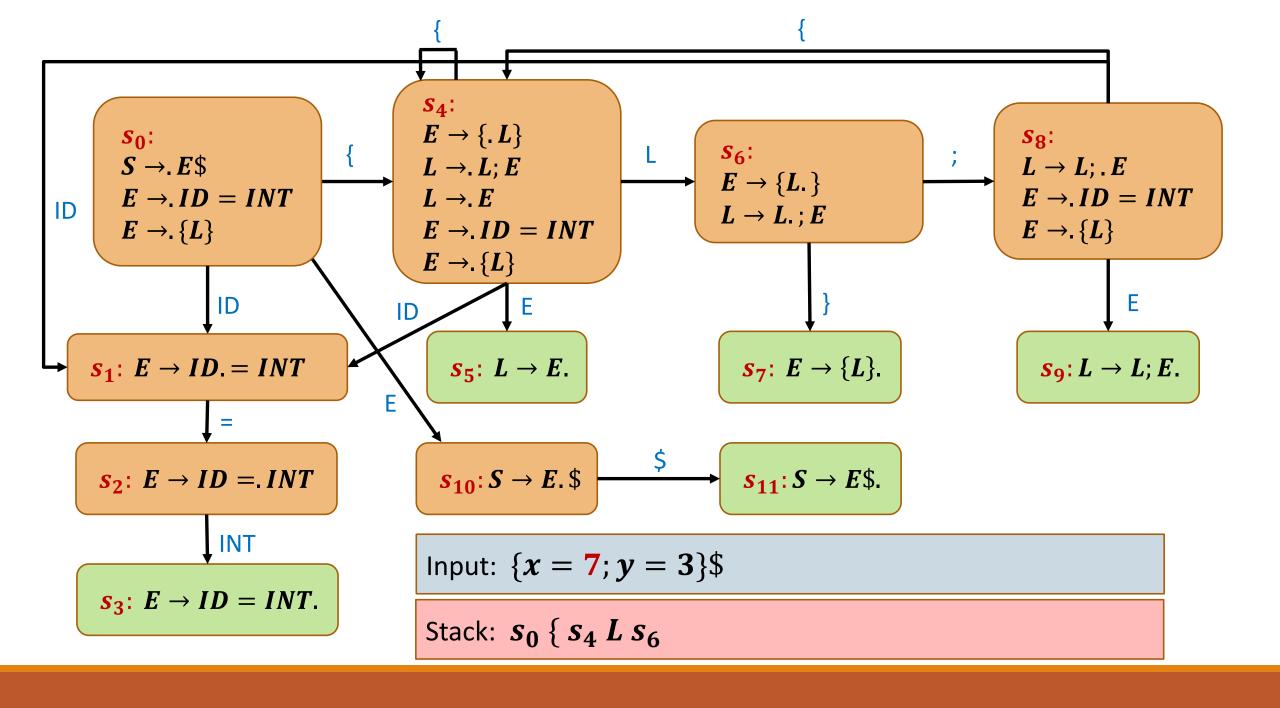


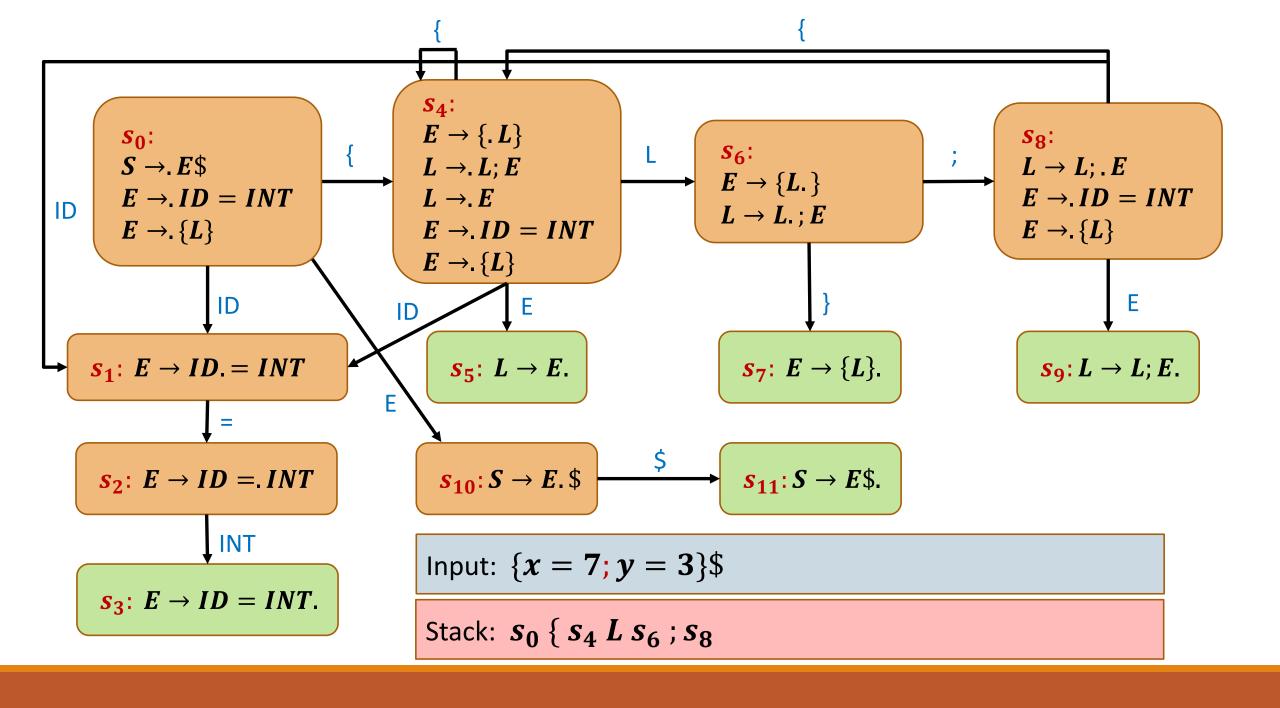


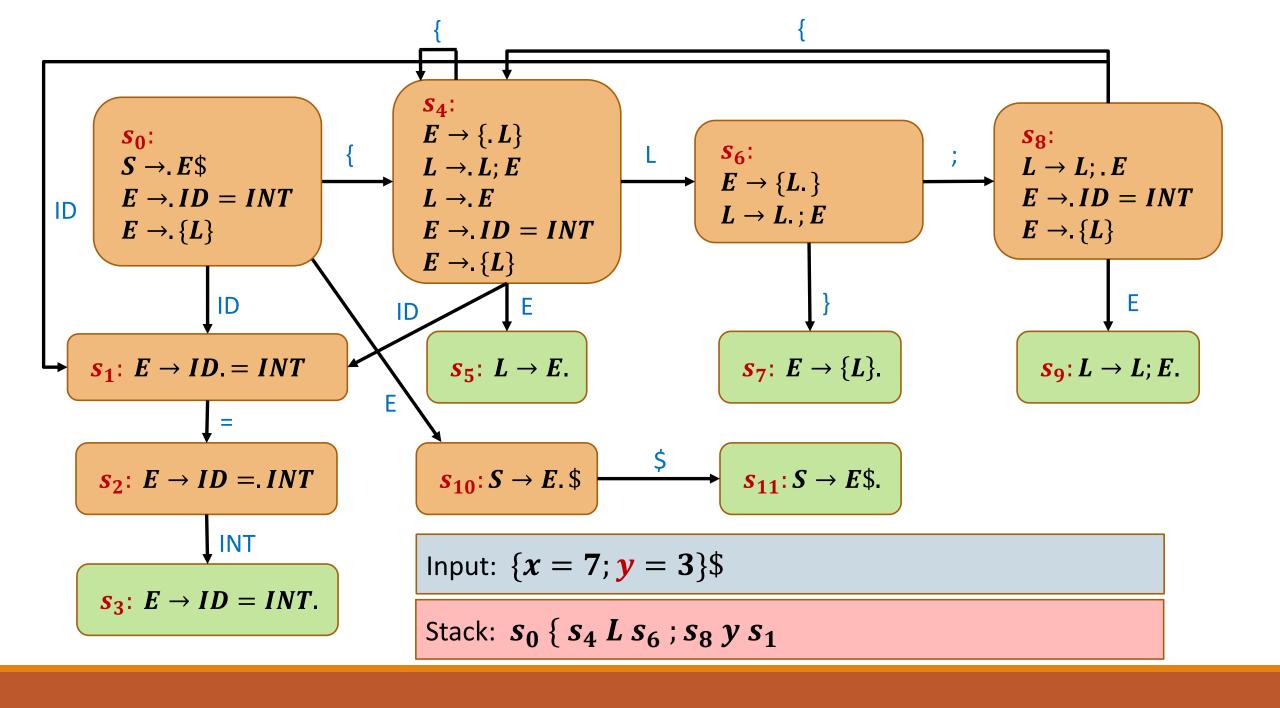


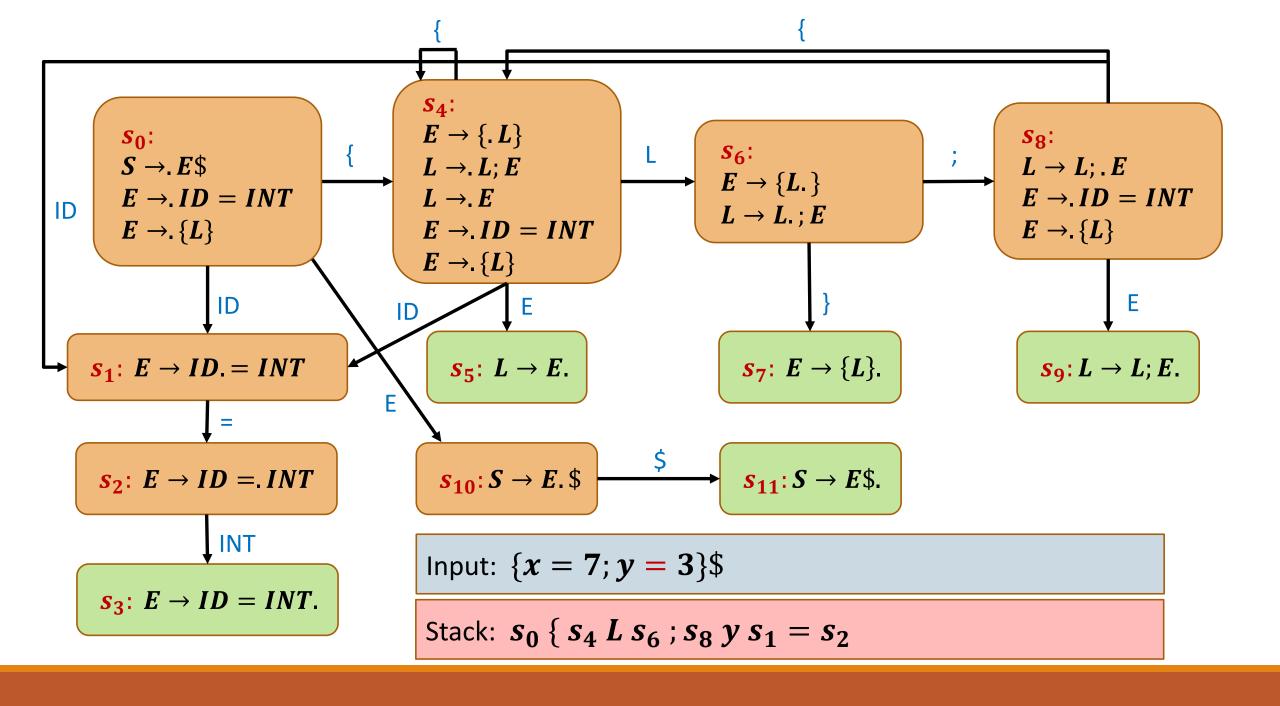


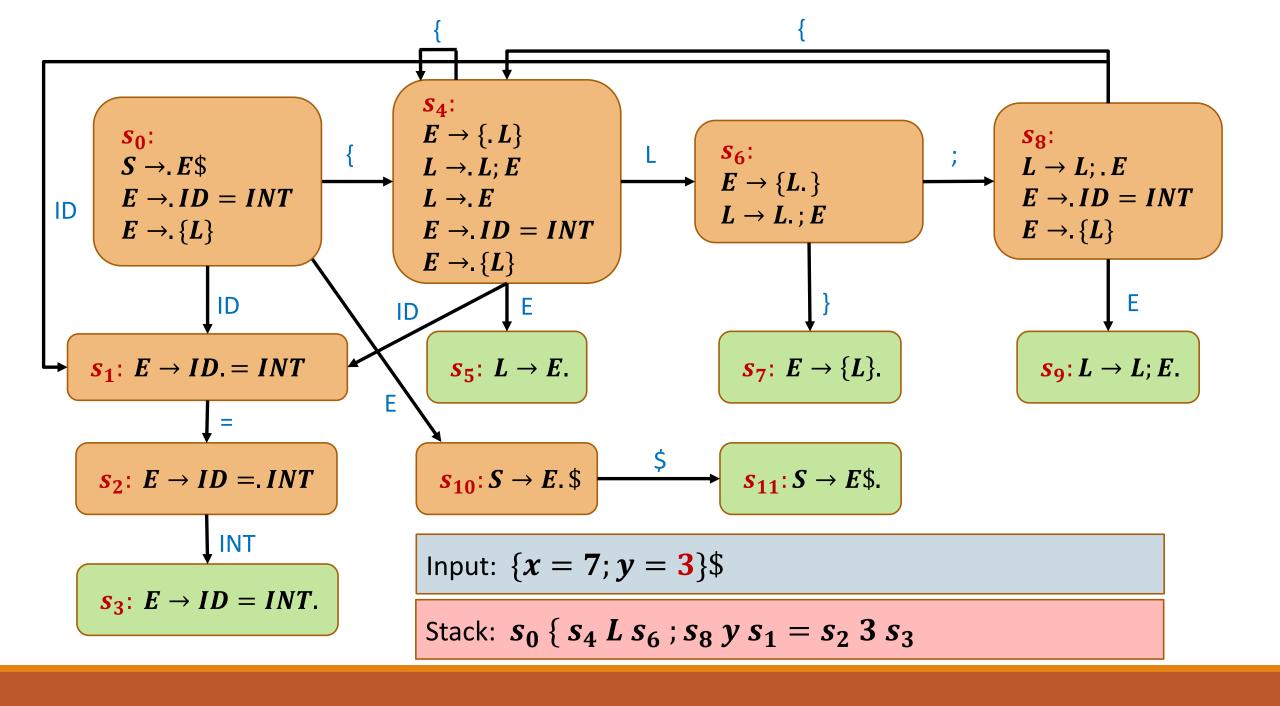


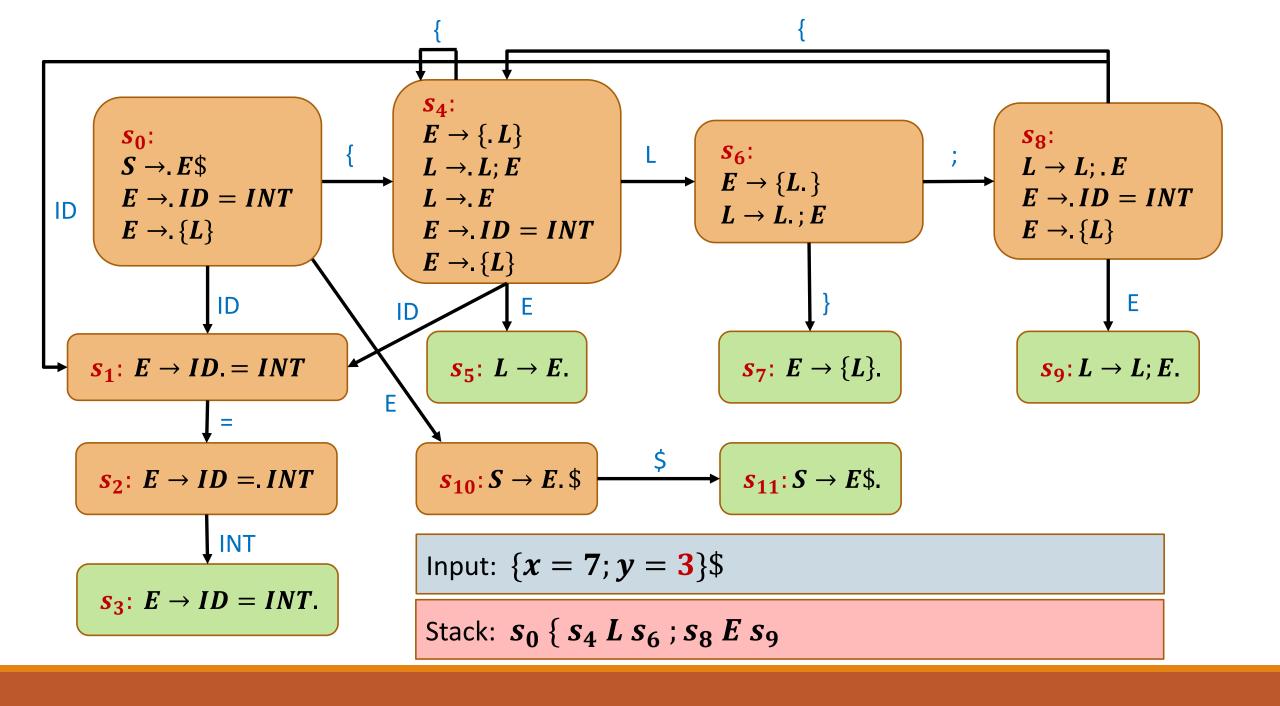


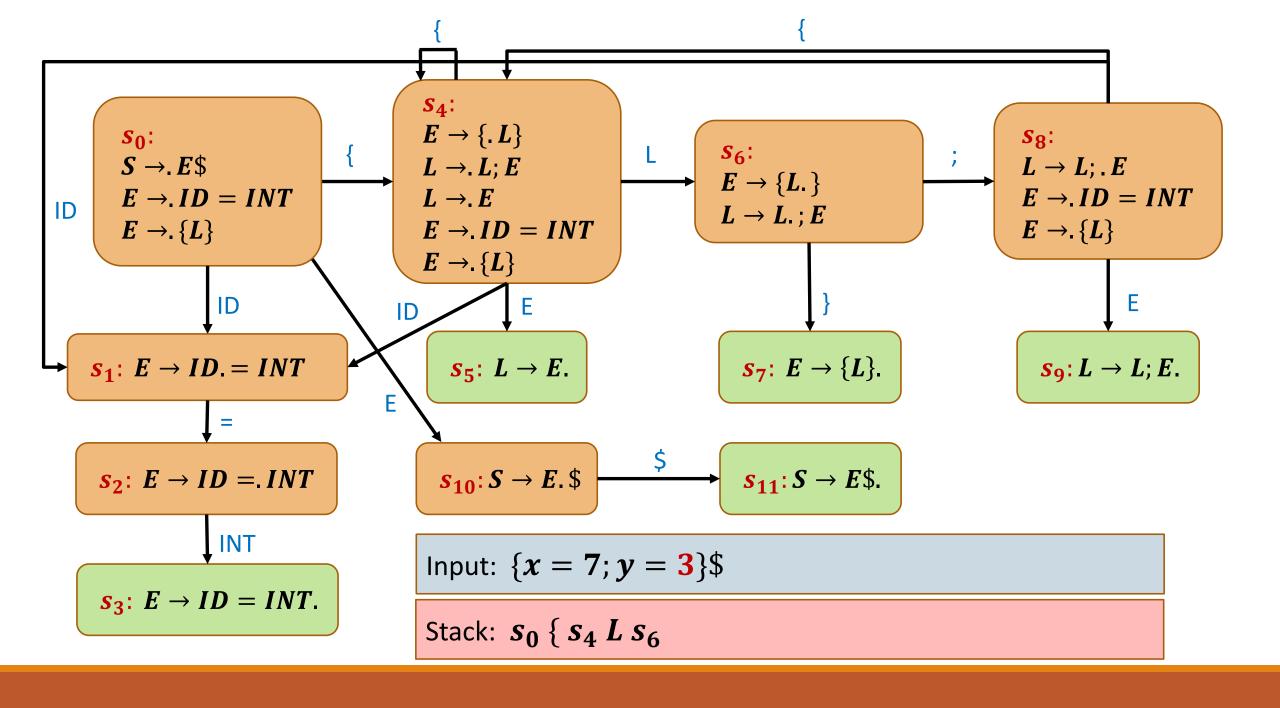


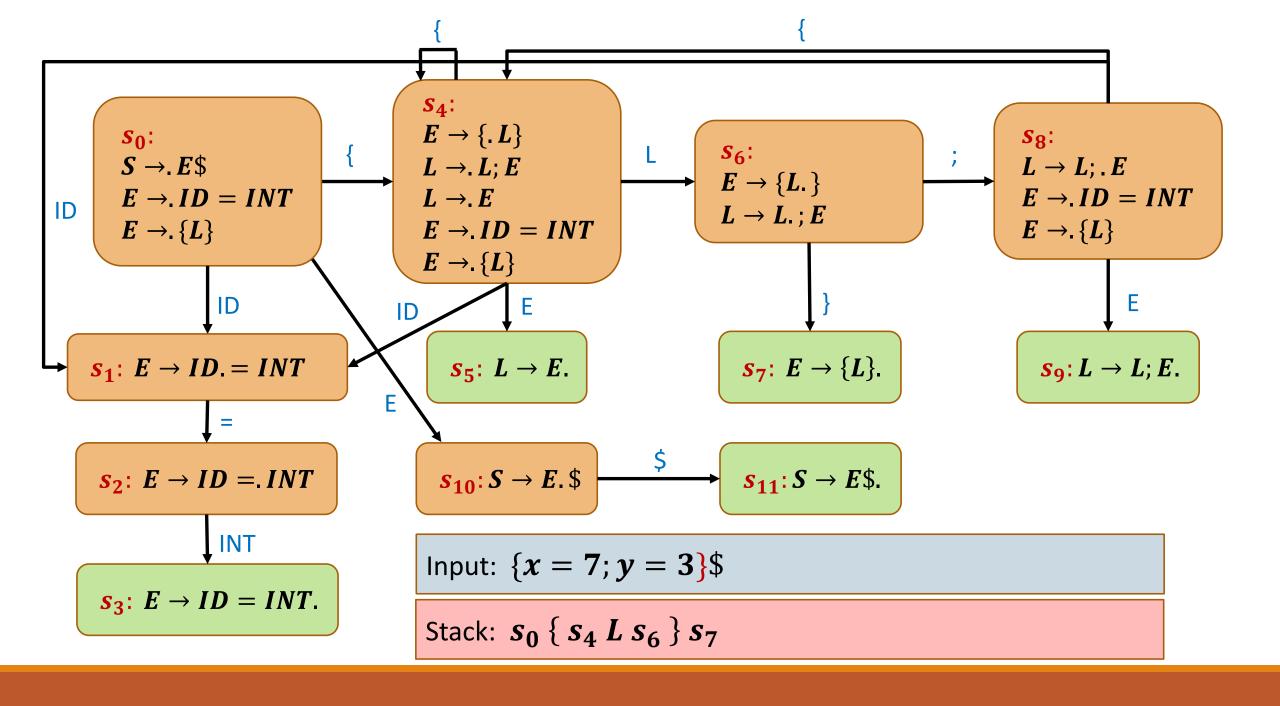


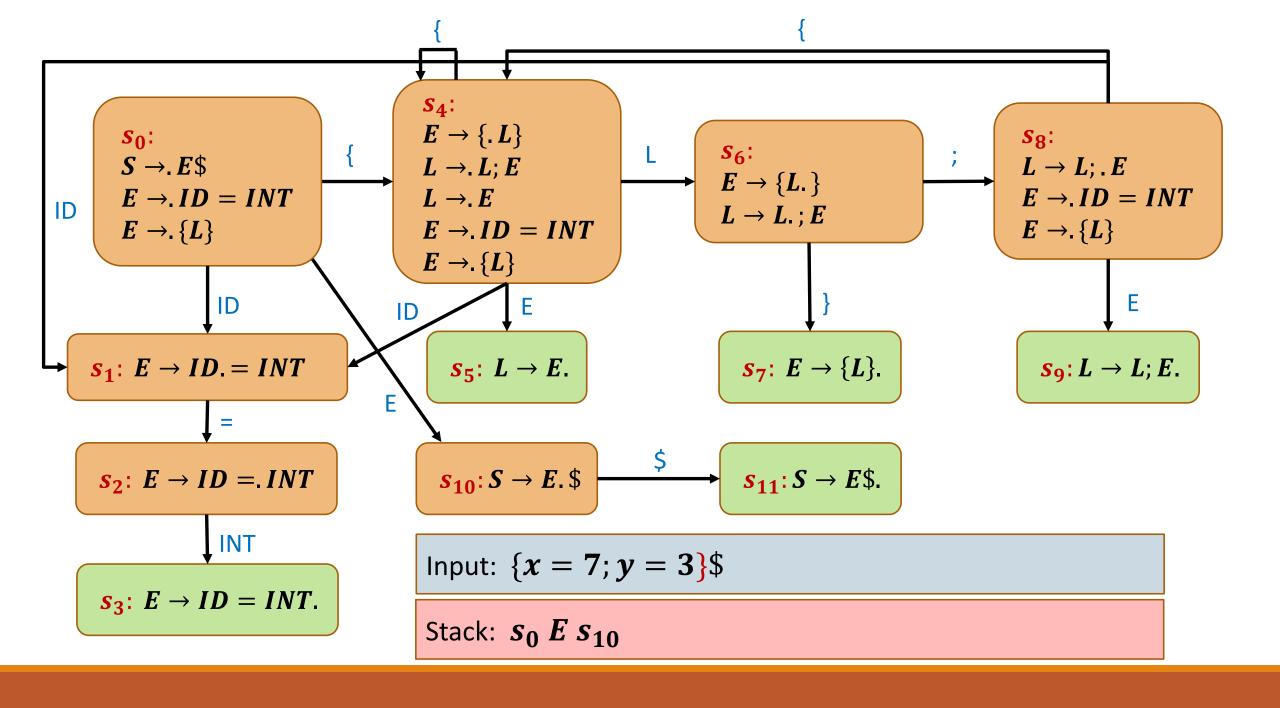


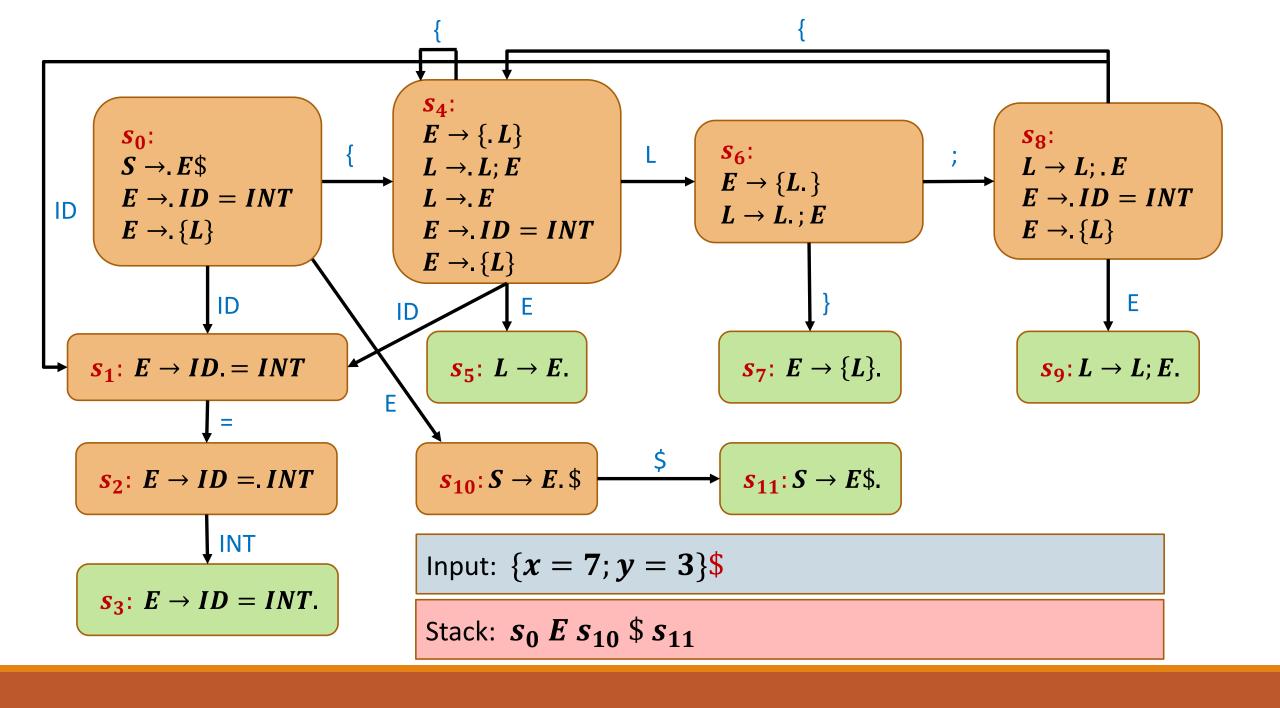


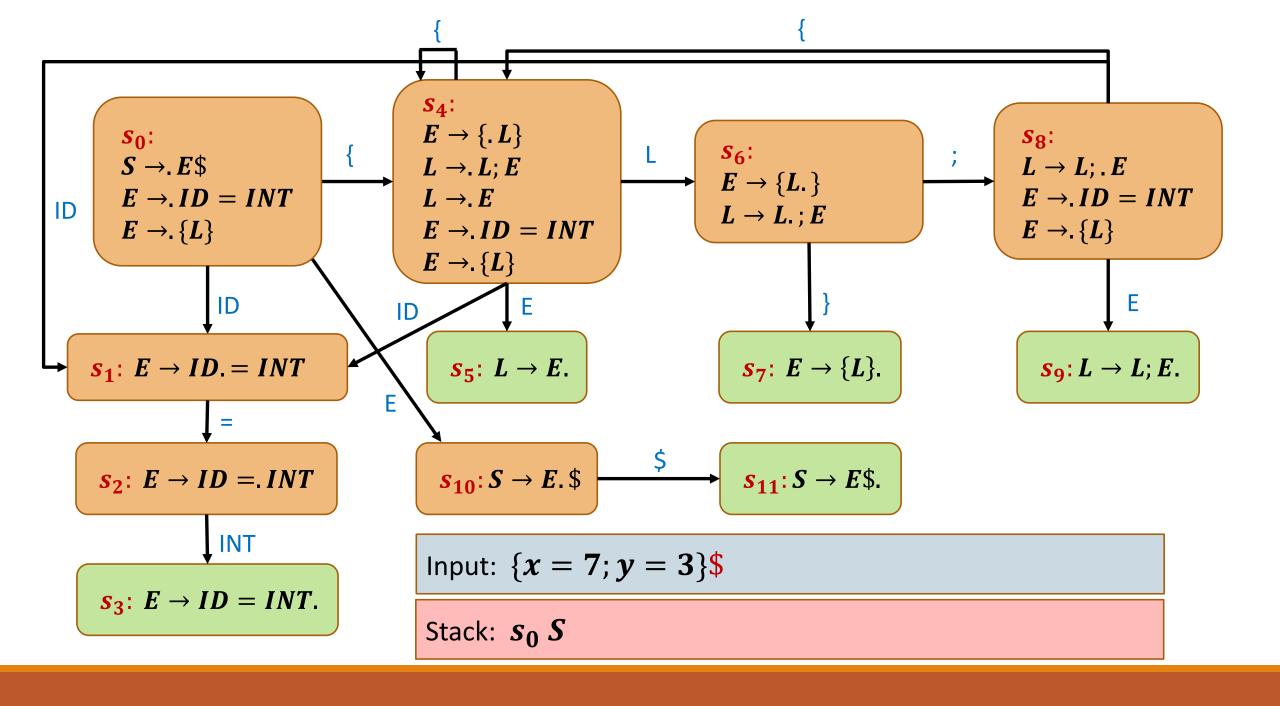










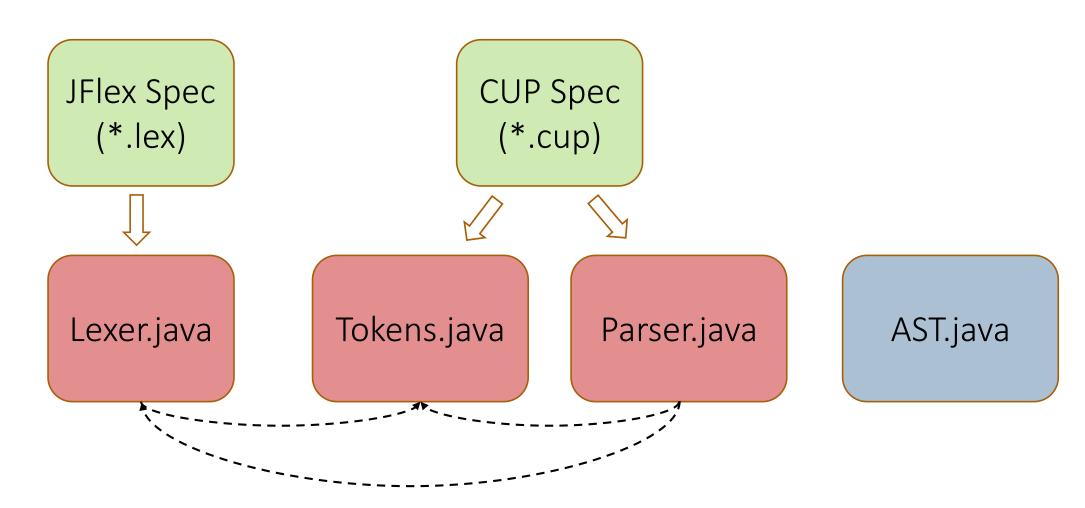


# Parsing with CUP

#### CUP

- Given a user-specified grammar, generates a parser
- Works with Jflex, which provides the parsed tokens
- Other tools:
  - Bison (for C)

# CUP/JFlex Workflow



#### CUP Spec: Parser Setup

```
parser code {:
      public Lexer lexer;
      public Parser(Lexer lexer) {
             super(lexer);
             this.lexer = lexer;
      public void report_error(String message, Object info) {
             System.exit(0);
```

#### CUP Spec: Lexer Setup

```
scan with {:
         Symbol s;
         s = lexer.next_token();
         // print token...
        return s;
:};
```

## **CUP Spec: Terminals**

```
terminal T1;
terminal T2;
terminal T3;
terminal T4;
...
```

### CUP Spec: Non-Terminals

```
non terminal AST_NODE_1 E1;
non terminal AST_NODE_2 E2;
non terminal AST_NODE_3 E3;
...
```

#### CUP Spec: Operator Precedence

```
precedence left OP1;
precedence left OP2;
precedence left OP3;
precedence left OP4;
...
```

These are token names...

#### CUP Spec: Grammar

```
start with S;
S ::=
 E1:e1 E2:e2 {: RESULT = new AST NODE 1(e1, e2); :} |
            {: RESULT = new AST_NODE_2(e3); :};
 E3:e3
E1 ::= ID:id {: RESULT = new AST NODE 3(id); :}
E2 ::= INT:i {: RESULT = new AST NODE 4(i); :}
E3 ::= ...
```

#### CUP Spec: AST Nodes

- We need to decide which node types we have in our AST
- We need to define the classes for these AST nodes.
- For example, for integers (INT) we can do:

```
public class AST_EXP_INT extends AST_EXP {
    public int value;
    public AST_EXP_INT(int value) {
        this.value = value;
    }
    public void PrintMe() { ... }
}
```

# CUP Example

Consider the following CFG:

- $E \rightarrow INT$
- $E \rightarrow V$
- $E \rightarrow E + E$
- $E \rightarrow E E$
- $V \rightarrow ID$
- $V \rightarrow V . ID$

# CUP Example: Terminals

```
terminal Integer INT;
terminal String ID;
terminal PLUS;
terminal MINUS;
Terminal DOT;
```

# CUP Example: Non-Terminals

```
non terminal AST_EXP exp;
non terminal AST_VAR var;
```

# CUP Example: Operator Precedence

```
precedence left PLUS;
precedence left MINUS;
```

### CUP Example: Grammar

```
start with EXP;
EXP ::=
  INT:i {: RESULT = new AST EXP INT(i); :} |
  VAR: \lor \{: RESULT = new AST_EXP_VAR(\lor); :\} 
  EXP:e1 PLUS EXP:e2 {: RESULT = new AST EXP BINOP(e1, e2, 0); :} |
  EXP:e1 MINUS EXP:e2 {: RESULT = new AST EXP BINOP(e1, e2, 1); :};
VAR ::=
  ID:name {: RESULT = new AST VAR SIMPLE(name); :} |
  VAR:v DOT ID:fieldName {: RESULT = new AST VAR FIELD(v, fieldName); :};
```

#### CUP Example: AST Nodes

For the rule *ID:name*:

```
public class AST_VAR_SIMPLE extends AST_VAR {
    public String name;
    public AST_VAR_SIMPLE(String name) {
        this.name = name;
    }
}
```

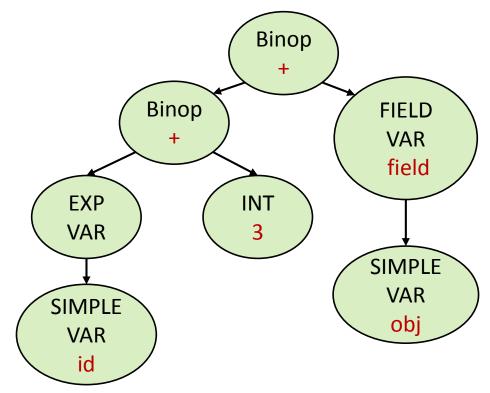
#### CUP Example: AST Nodes

For the rule *var:v DOT ID:fieldname*:

```
public class AST_VAR_FIELD extends AST_VAR {
    public AST_VAR var;
    public String fieldName;
    public AST_VAR_FIELD(AST_VAR var, String fieldName) {
        this.var = var;
        this.fieldName = fieldName;
    }
}
```

# CUP Example: Debugging

We can generate an image of the AST (using the exercise template) For the input foo + 3 + obj.field we have:



# CUP Example: Debugging

CUP enables to dump:

- The automaton
- The goto/action table