Bottom Up Parsing

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LR(0) Parsing

- Build the derivation tree from the bottom
- First build the children, then connect to the parent
- Can handle left recursion
 - Which is common in real-world grammars

LR(0) Item

An LR(0) item is of the form:

• $N \rightarrow \alpha . \beta$

The **dot** gives us the current location (a local view).

LR(0) Item

An LR(0) item with the dot at the end is called **reduce** item:

• $N \rightarrow \alpha \beta$.

Otherwise, it's a **shift** item:

- $N \rightarrow \alpha \beta$
- $N \rightarrow \alpha.\beta$

LR(0) Item Closure Set

The LR(0) closure set of an item is it's ϵ -closure.

For example, given the following CFG:

- $S \rightarrow E$ \$
- $E \rightarrow ID = X$
- $E \rightarrow \{ID\}$
- $X \rightarrow INT$

the closure set of the $S \rightarrow E$ \$ contains:

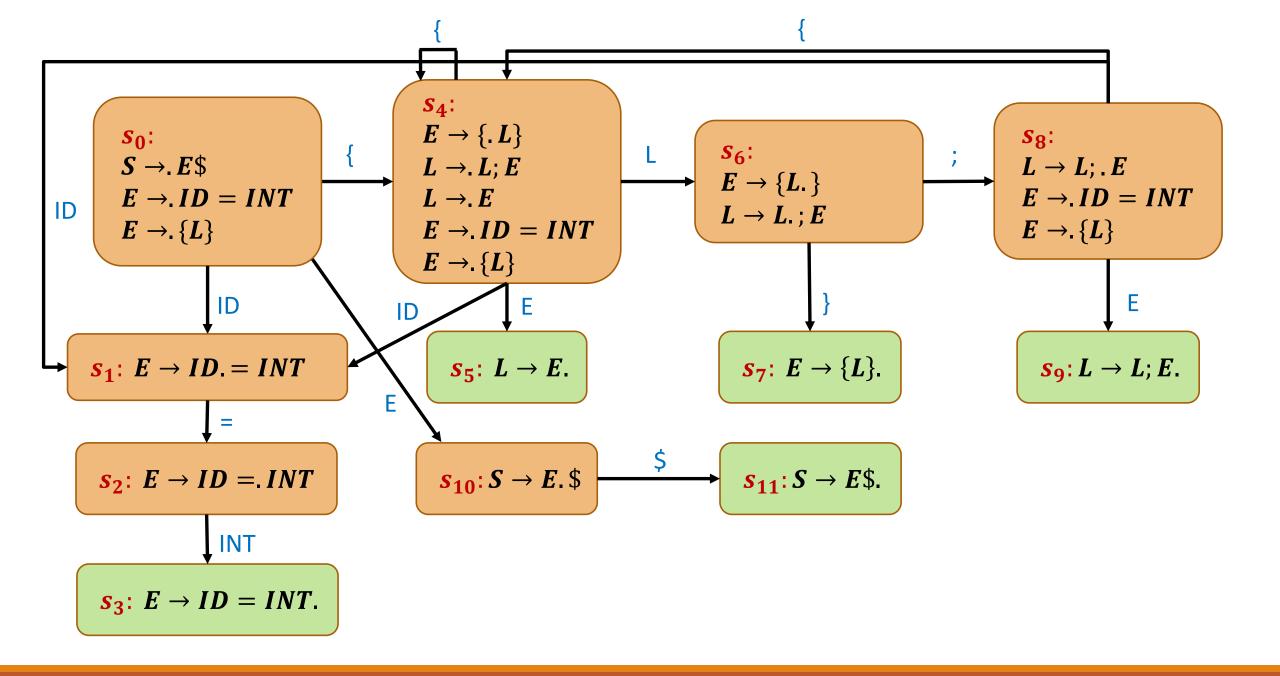
- $S \rightarrow E$ \$
- $E \rightarrow ID = X$
- $E \rightarrow \{L\}$

LR(0) Parsing

Consider the following CFG:

- $S \rightarrow E$ \$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$
- $L \rightarrow E$
- $L \rightarrow L; E$

What will be the **transition system** of the LR(0) parser for this CFG?



We start with the initial LR(0) item (that comes from the initial rule):

• $S \rightarrow E$ \$

The initial state is the ϵ -closure of that item, which contains:

- $S \rightarrow E$ \$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

S_0 : $S \rightarrow E$ $E \rightarrow ID = INT$ $E \rightarrow \{L\}$

From s_0 , if we recognized ID, then the next state will contain:

• $E \rightarrow ID = INT$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

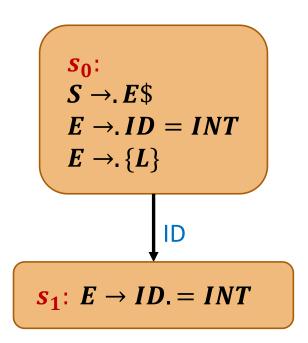
From s_0 , if we recognized ID, then the next state will contain:

• $E \rightarrow ID = INT$

So the next state (the ϵ -closure) contains:

• $E \rightarrow ID = INT$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$



From s_1 , if we recognized =, then the next state will contain:

• $E \rightarrow ID = .INT$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

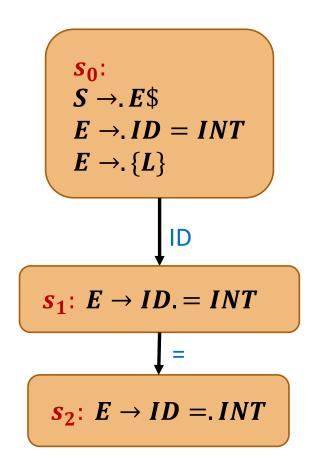
From s_1 , if we recognized =, then the next state will contain:

• $E \rightarrow ID = .INT$

So the next state (the ϵ -closure) contains:

• $E \rightarrow ID = INT$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

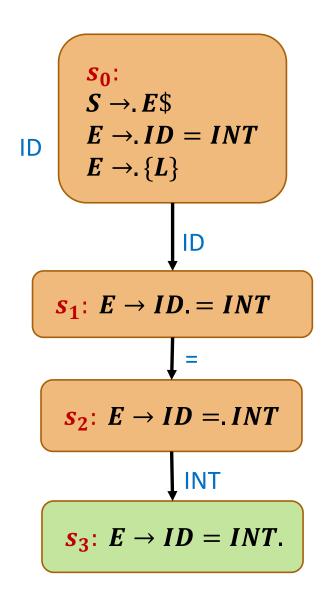


From s_2 , if we recognized INT, then the next state will contain:

• $E \rightarrow ID = INT$.

Which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$



From s_0 , if we recognized $\{$, then the next state will contain:

•
$$E \rightarrow \{.L\}$$

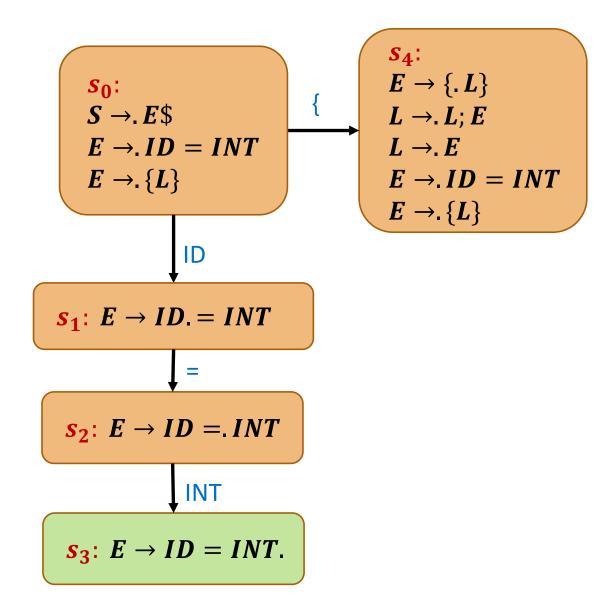
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

From s_0 , if we recognized $\{$, then the next state will contain:

• $E \rightarrow \{.L\}$

- $E \rightarrow \{.L\}$
- $L \rightarrow L; E$
- $L \rightarrow E$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$



From s_4 , if we recognized $\{$, then the next state will contain:

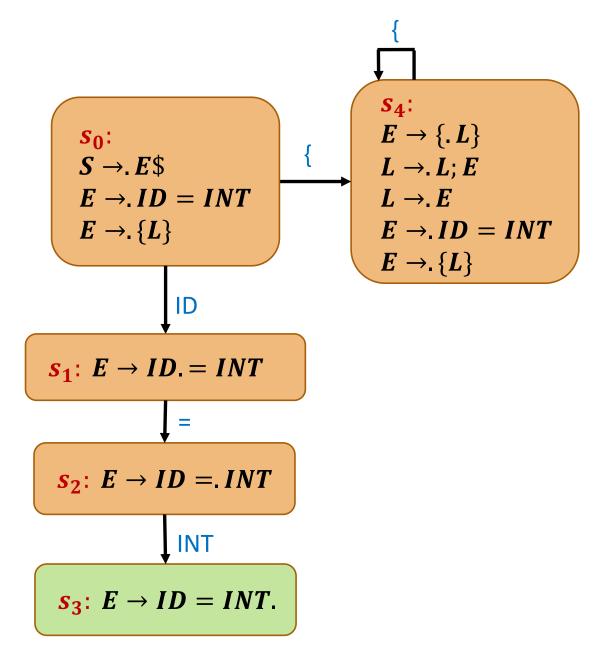
•
$$E \rightarrow \{.L\}$$

So the next state (the ϵ -closure) contains:

- $E \rightarrow \{.L\}$
- $L \rightarrow L; E$
- $L \rightarrow E$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

which was already computed: s_4

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$



From s_4 , if we recognized ID, then the next state will contain:

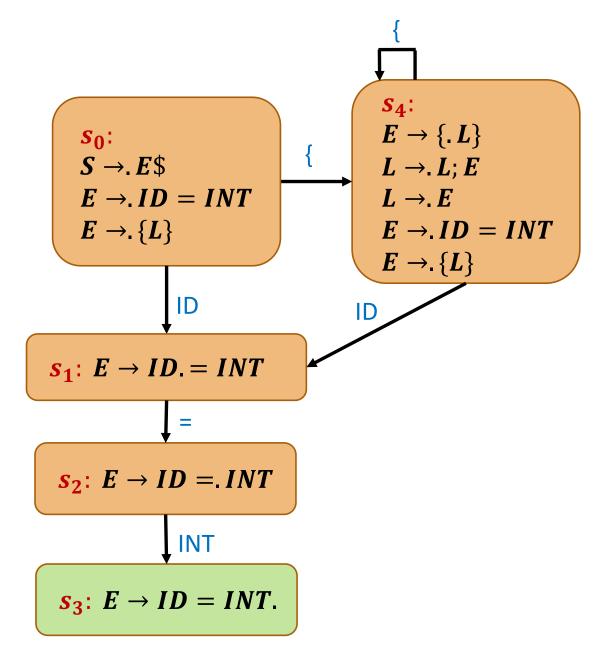
• $E \rightarrow ID = INT$

So the next state (the ϵ -closure) contains:

• $E \rightarrow ID = INT$

which was already computed: s_1

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

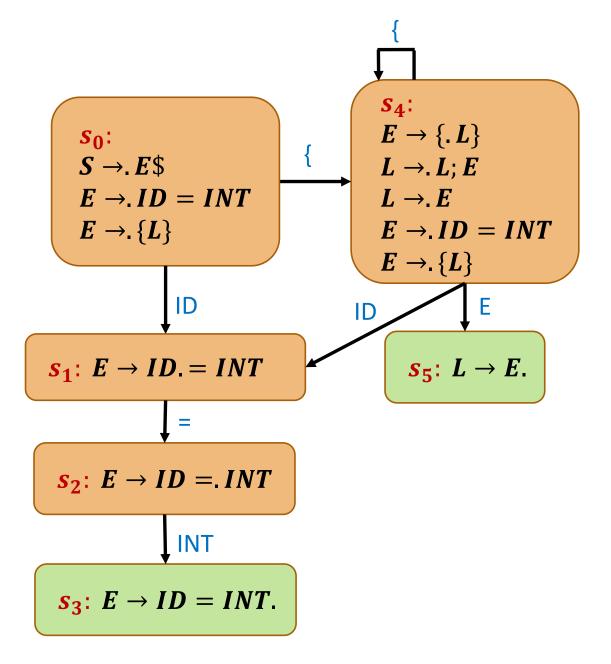


From s_5 , if we recognized E, then the next state will contain:

• $L \rightarrow E$.

which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$



From s_4 , if we recognized L, then the next state will contain:

- $E \rightarrow \{L.\}$
- $L \rightarrow L$; E

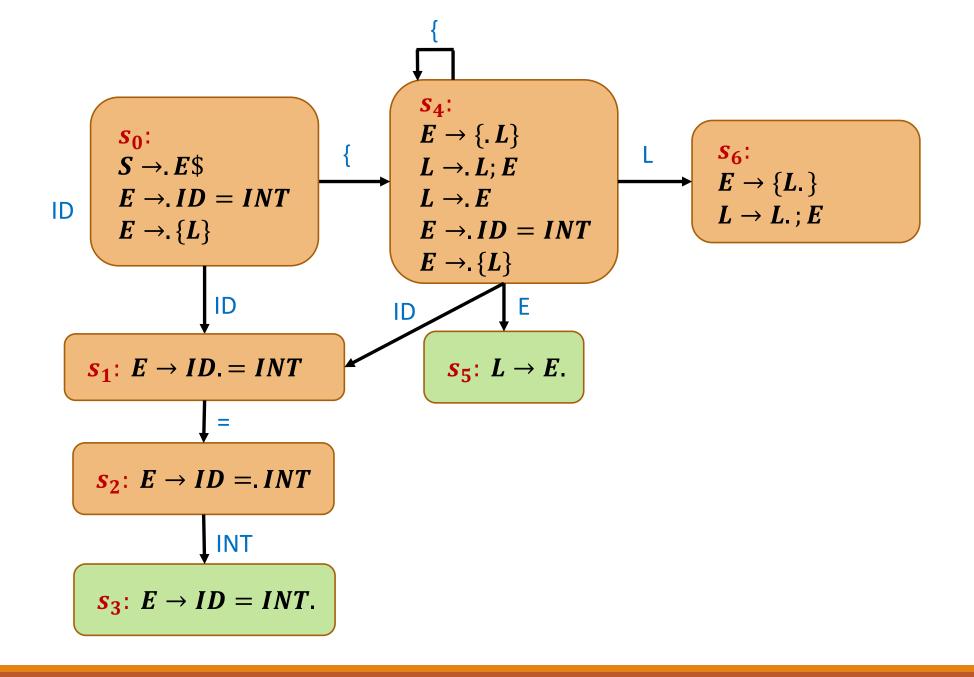
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

From s_4 , if we recognized L, then the next state will contain:

- $E \rightarrow \{L.\}$
- $L \rightarrow L$; E

- $E \rightarrow \{L.\}$
- $L \rightarrow L$; E

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

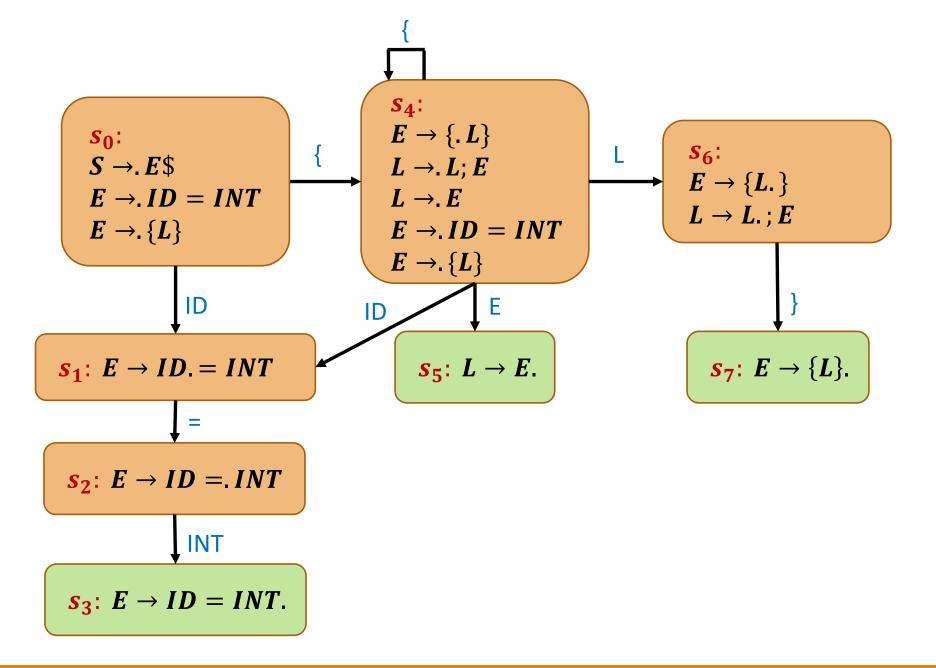


From s_6 , if we recognized }, then the next state will contain:

•
$$E \rightarrow \{L\}$$
.

Which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$



From s_6 , if we recognized;, then the next state will contain:

•
$$L \rightarrow L$$
; E

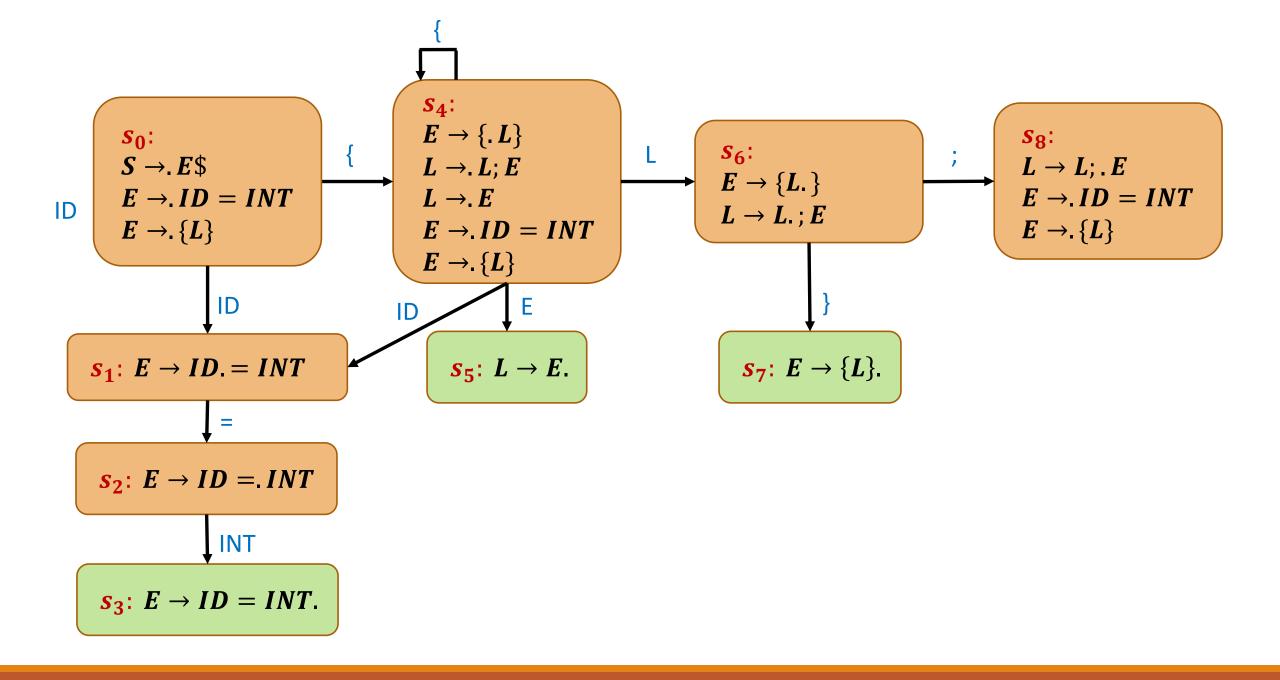
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

From s_6 , if we recognized;, then the next state will contain:

• $L \rightarrow L$; E

- $L \rightarrow L$; E
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

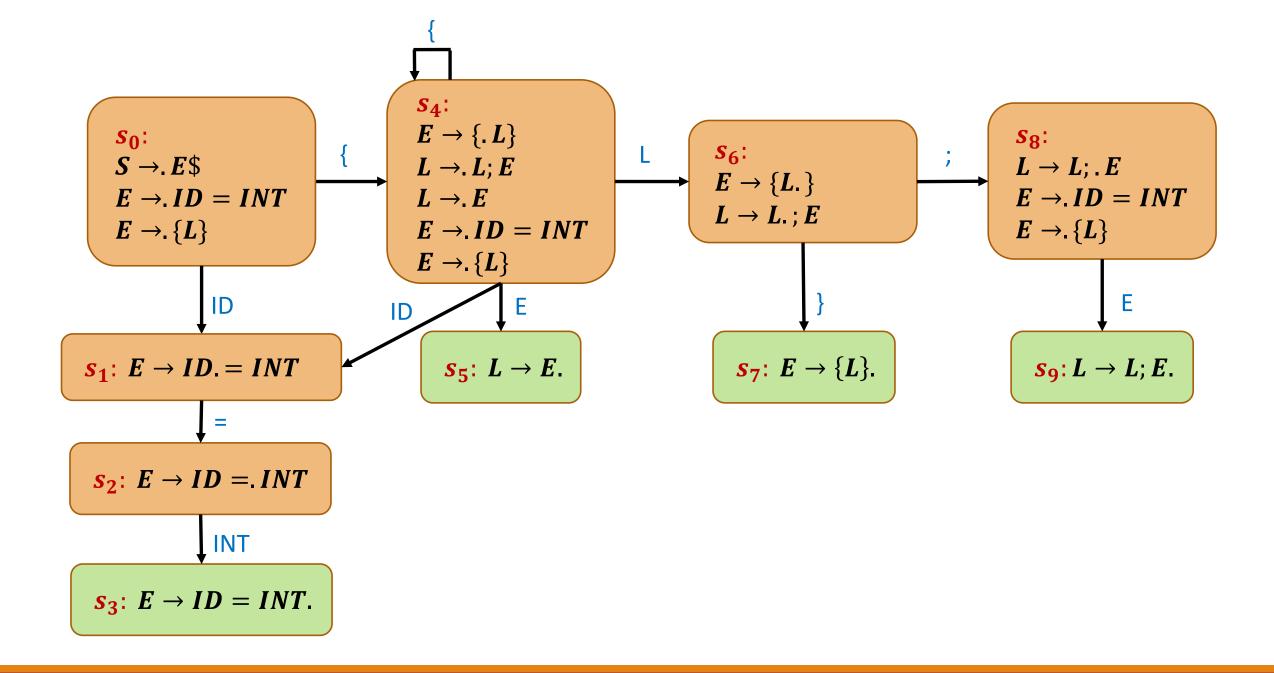


From s_8 , if we recognized E, then the next state will contain:

• $E \rightarrow L; E$.

which is a reduce state.

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$



From s_8 , if we recognized $\{$, then the next state will contain:

•
$$E \rightarrow \{.L\}$$

So the next state (the ϵ -closure) contains:

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

From s_8 , if we recognized $\{$, then the next state will contain:

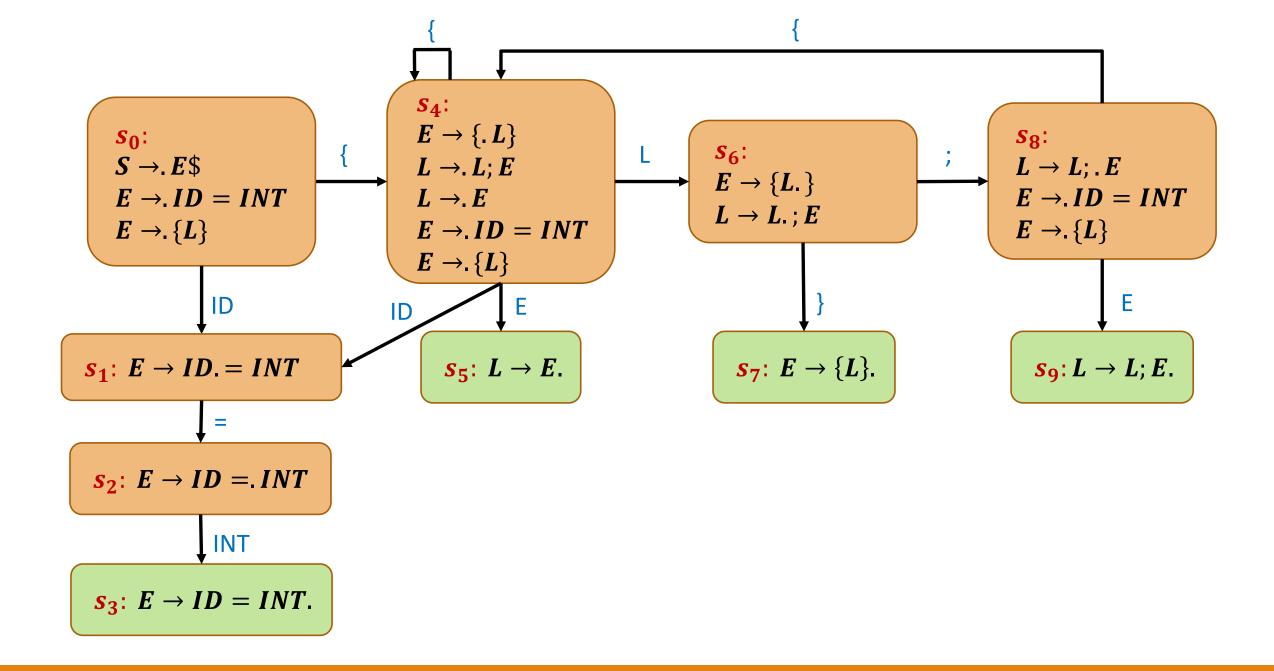
•
$$E \rightarrow \{.L\}$$

So the next state (the ϵ -closure) contains:

- $E \rightarrow \{.L\}$
- $L \rightarrow L; E$
- $L \rightarrow E$
- $E \rightarrow ID = INT$
- $E \rightarrow \{L\}$

which was already computed: s_4

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$



From s_8 , if we recognized ID, then the next state will contain:

• $E \rightarrow ID = INT$

So the next state (the ϵ -closure) contains:

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

From s_8 , if we recognized ID, then the next state will contain:

• $E \rightarrow ID = INT$

So the next state (the ϵ -closure) contains:

• $E \rightarrow ID = INT$

which was already computed: s_1

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

From s_8 , if we recognized ID, then the next state will contain:

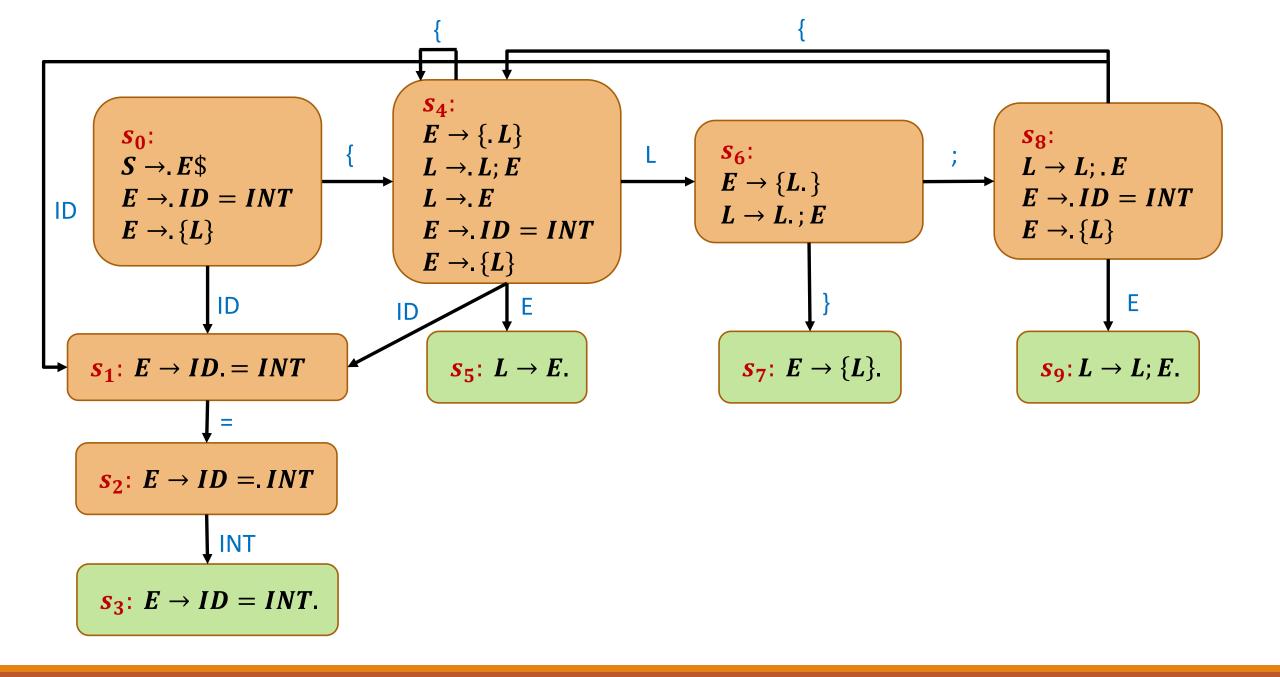
• $E \rightarrow ID = INT$

So the next state (the ϵ -closure) contains:

• $E \rightarrow ID = INT$

which was already computed: s_1

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$



From s_0 , if we recognized E, then the next state will contain:

•
$$S \rightarrow E.\$$$

So the next state (the ϵ -closure) contains:

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

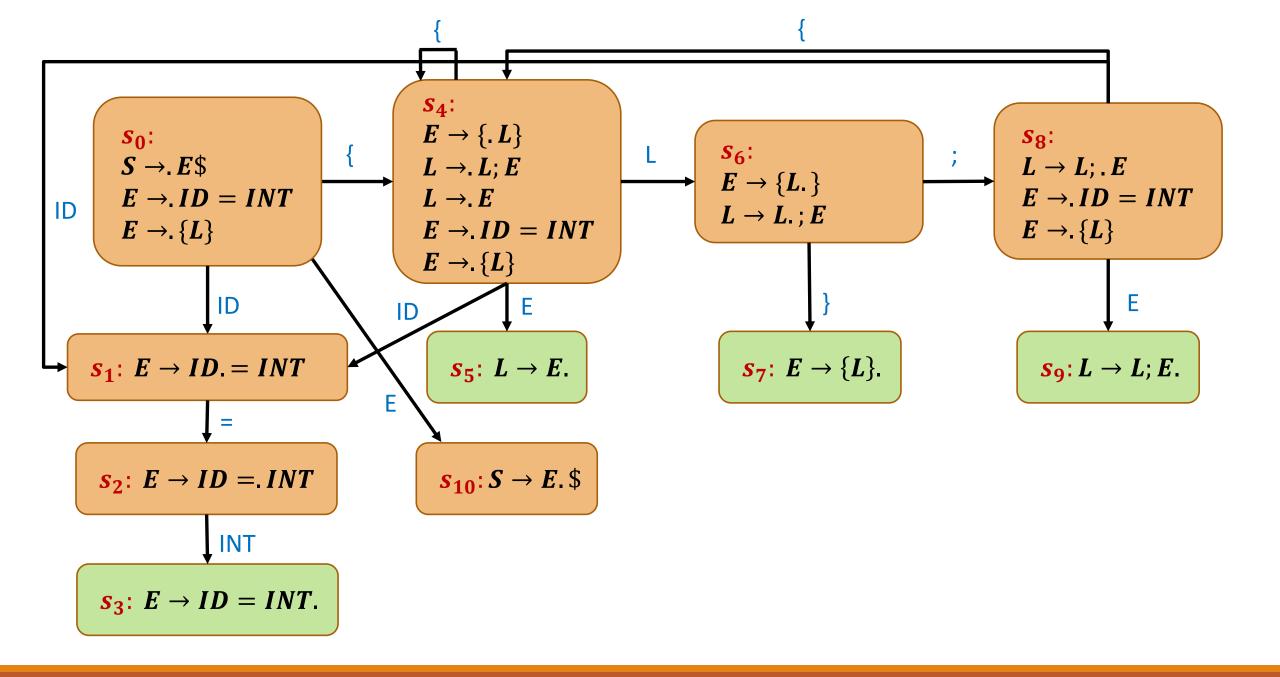
From s_0 , if we recognized E, then the next state will contain:

• $S \rightarrow E.\$$

So the next state (the ϵ -closure) contains:

• $S \rightarrow E.\$$

$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

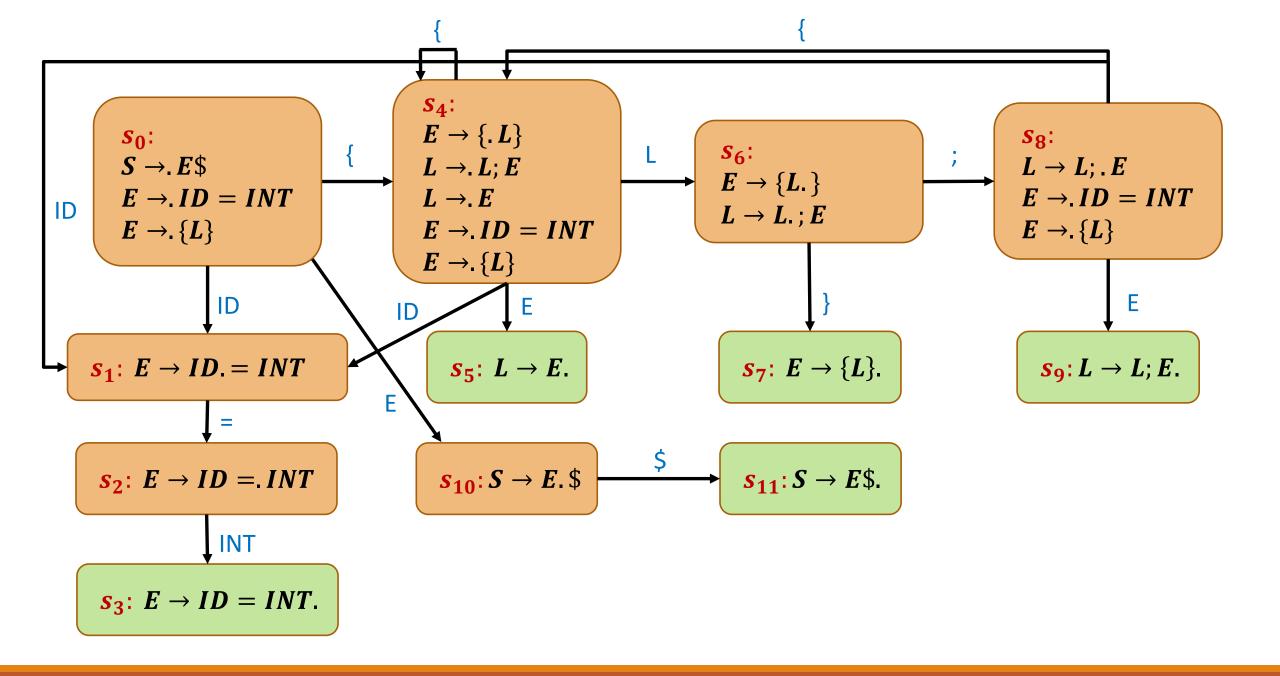


From s_0 , if we recognized E, then the next state will contain:

• $S \rightarrow E$ \$.

which is a reduce state.

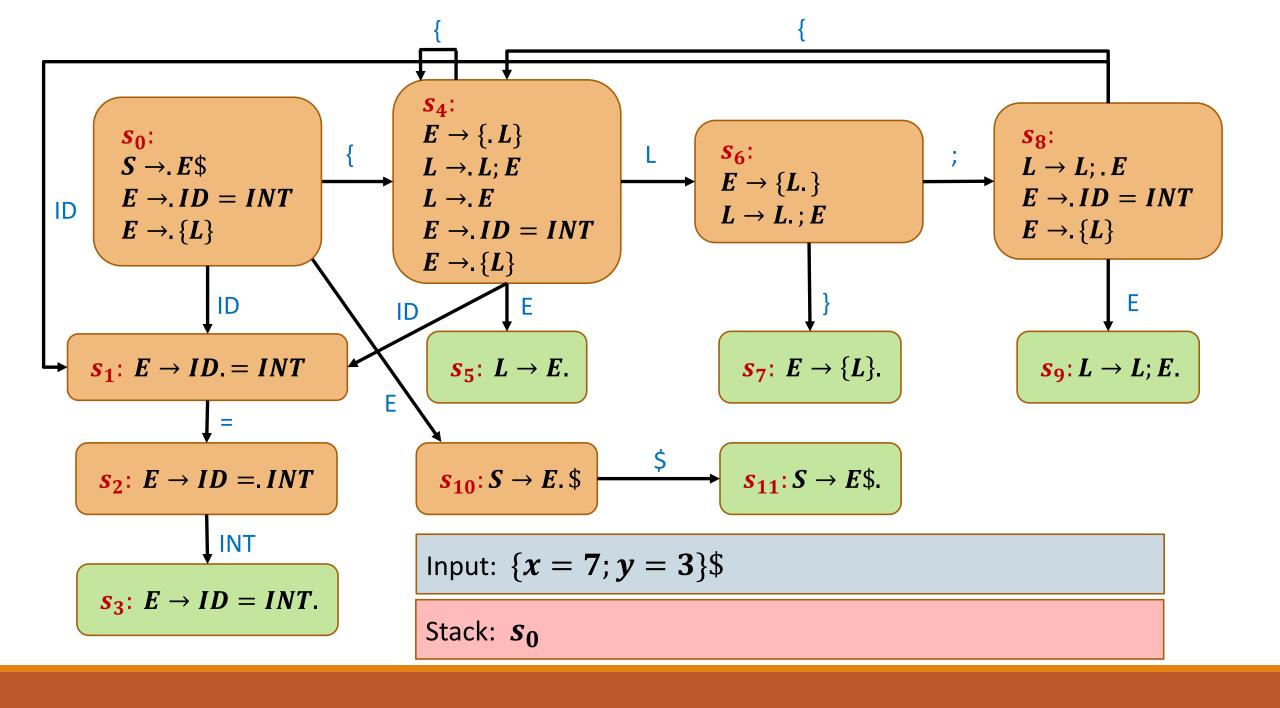
$$S \rightarrow E\$$$
 $E \rightarrow ID = INT$
 $E \rightarrow \{L\}$
 $L \rightarrow E$
 $L \rightarrow L; E$

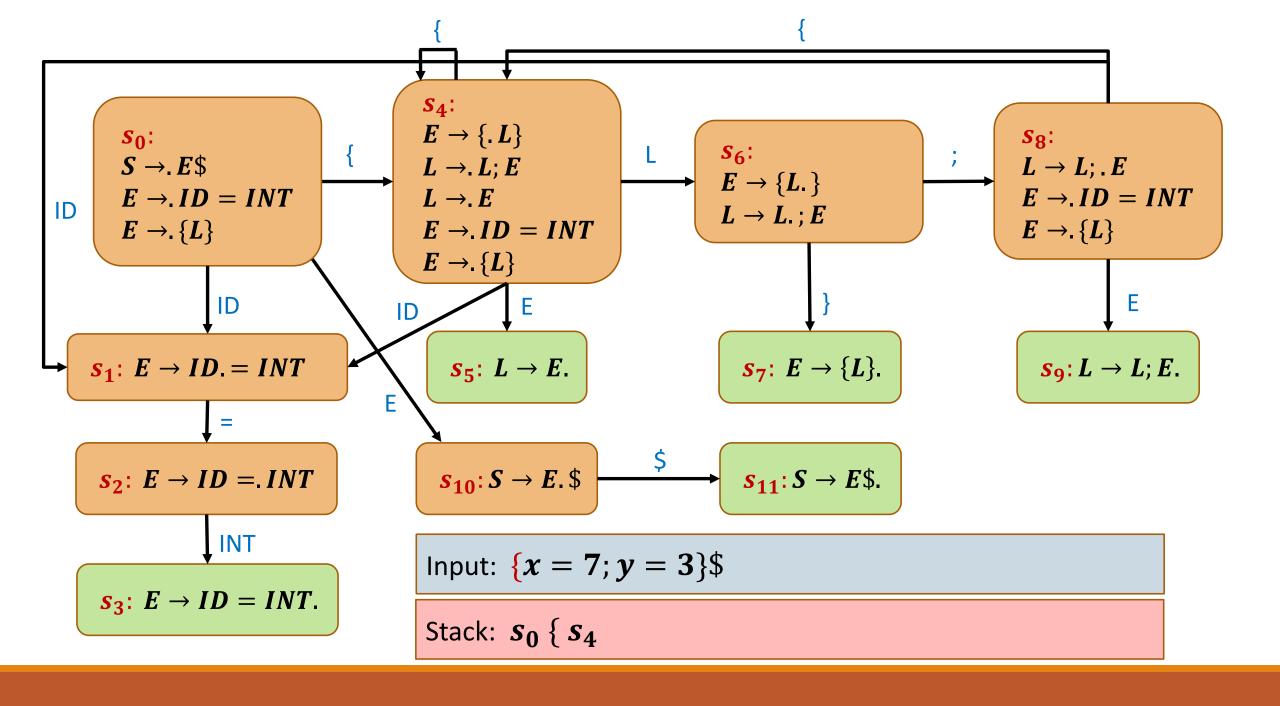


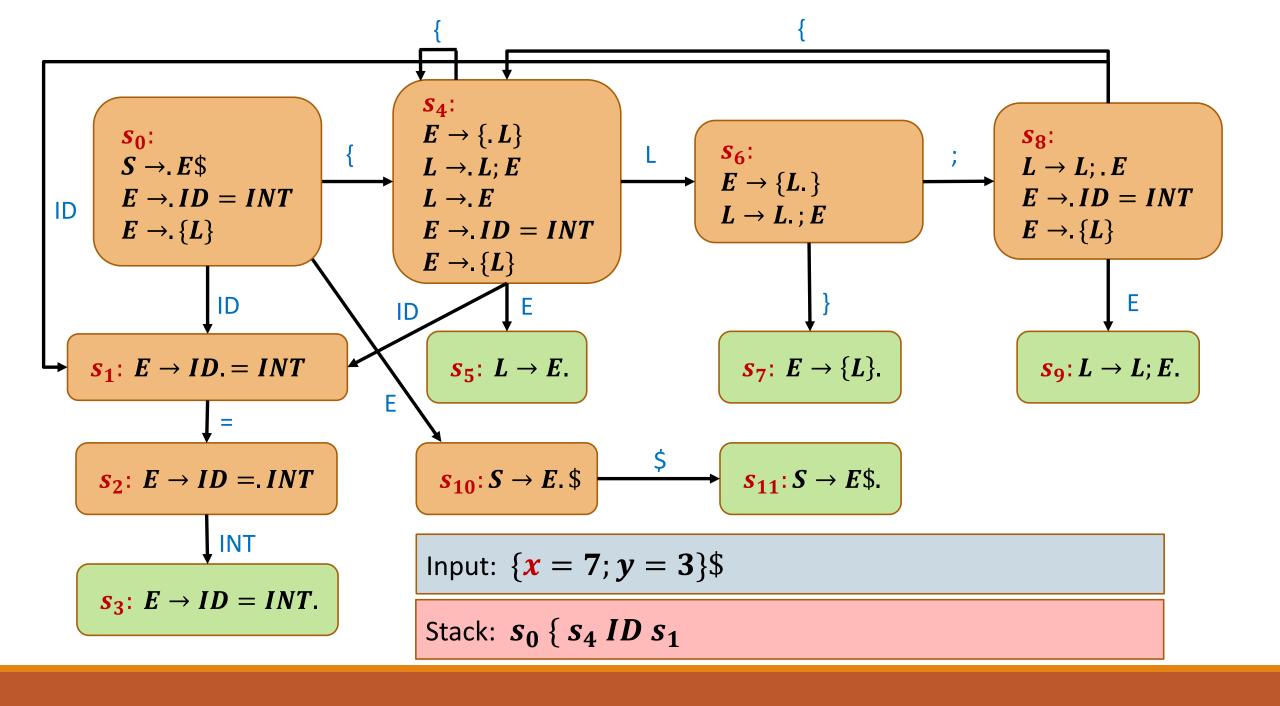
LR(0) Parser: Running Example

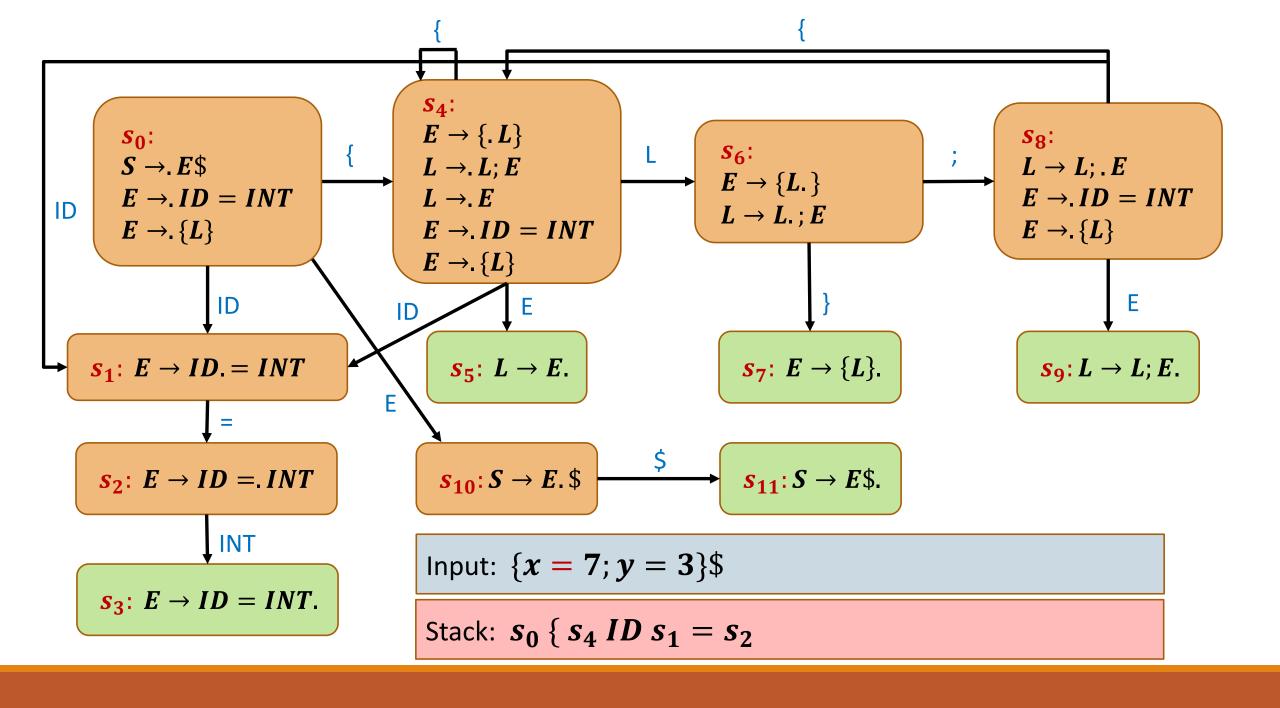
What will happen with the following input:

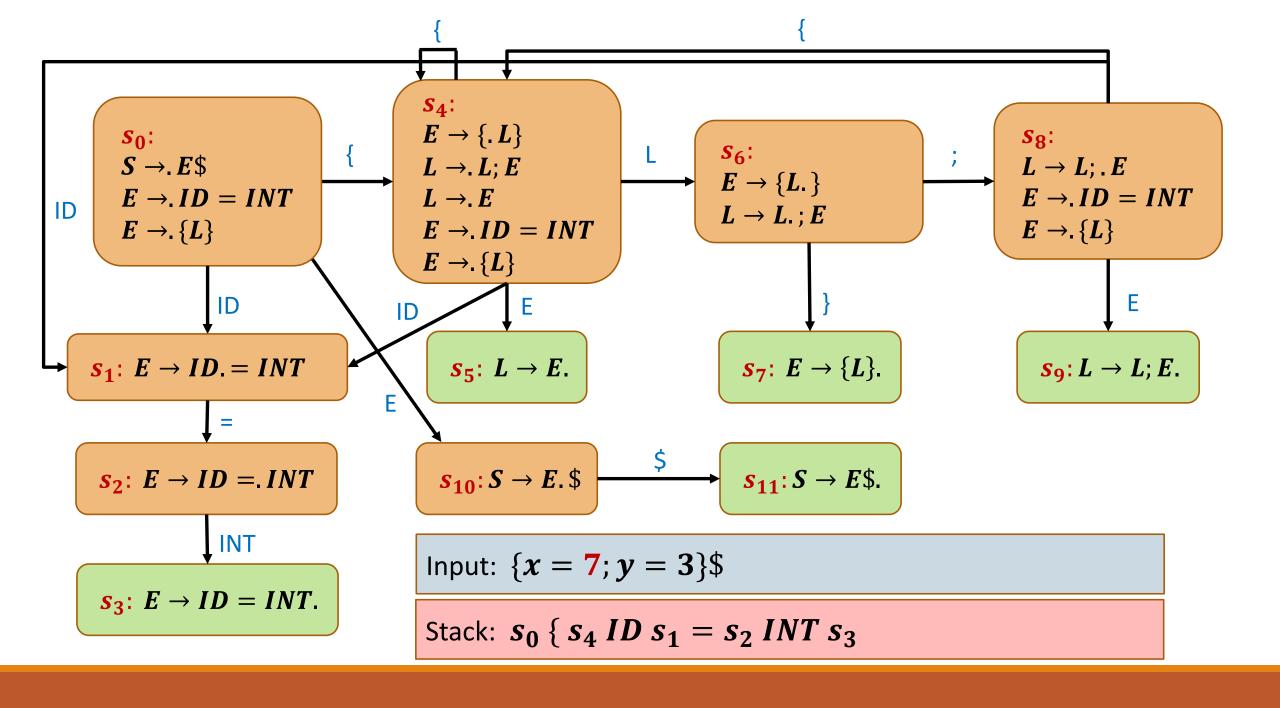
•
$$x = 7; y = 3$$
\$

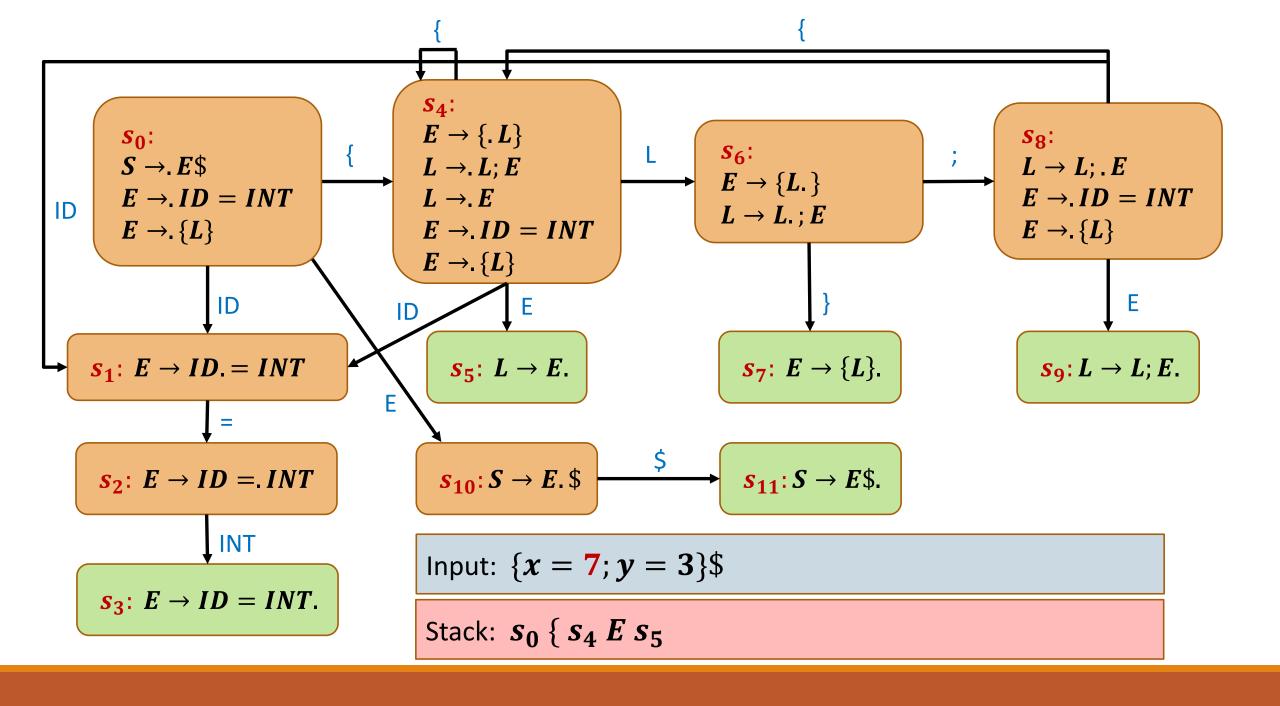


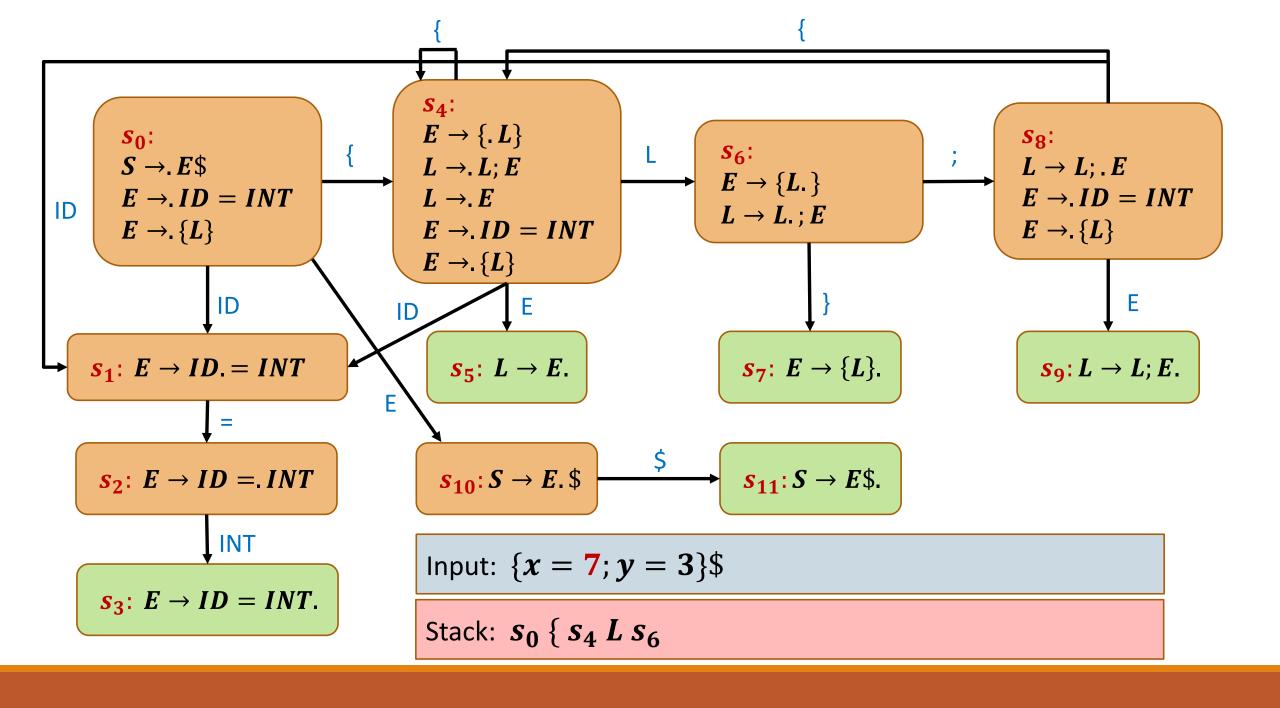


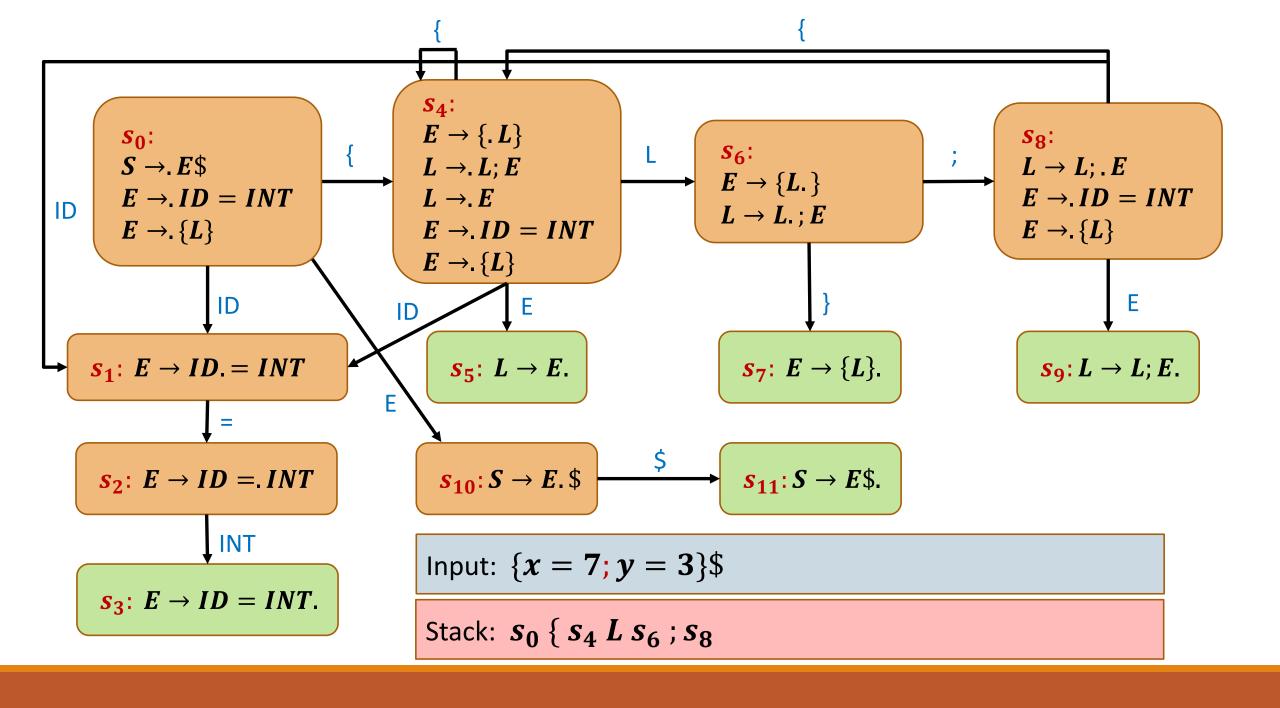


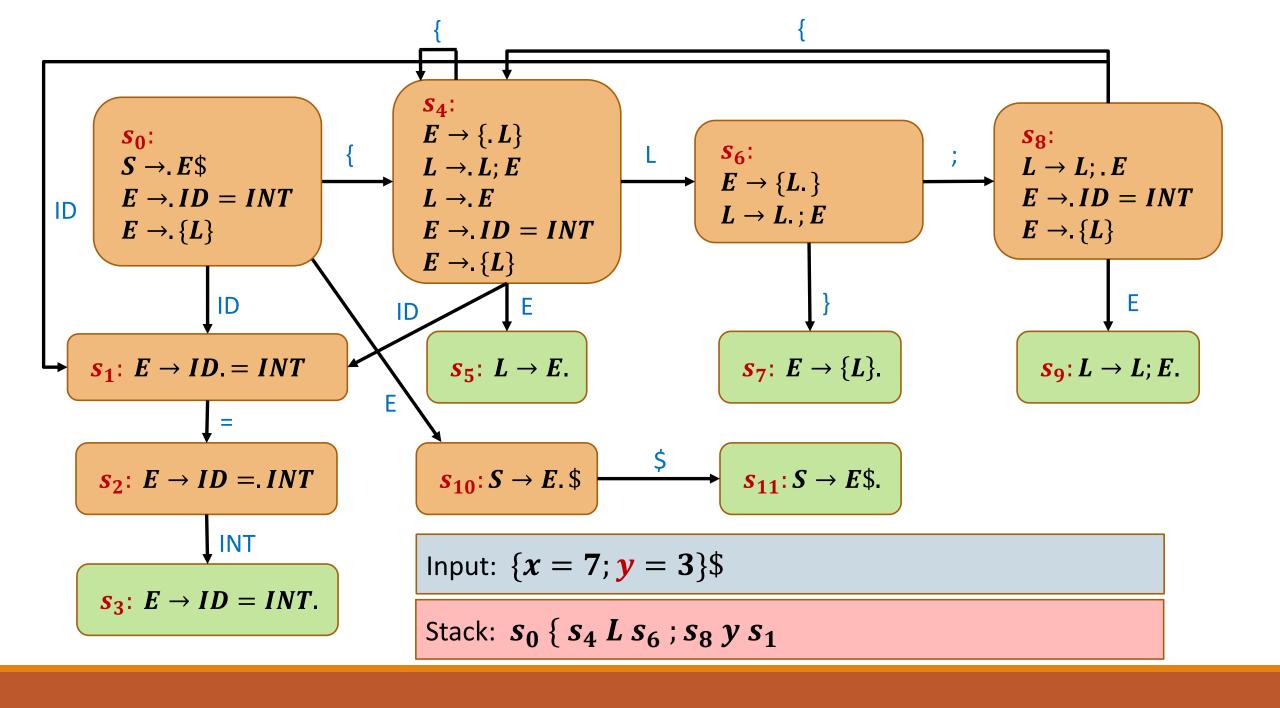


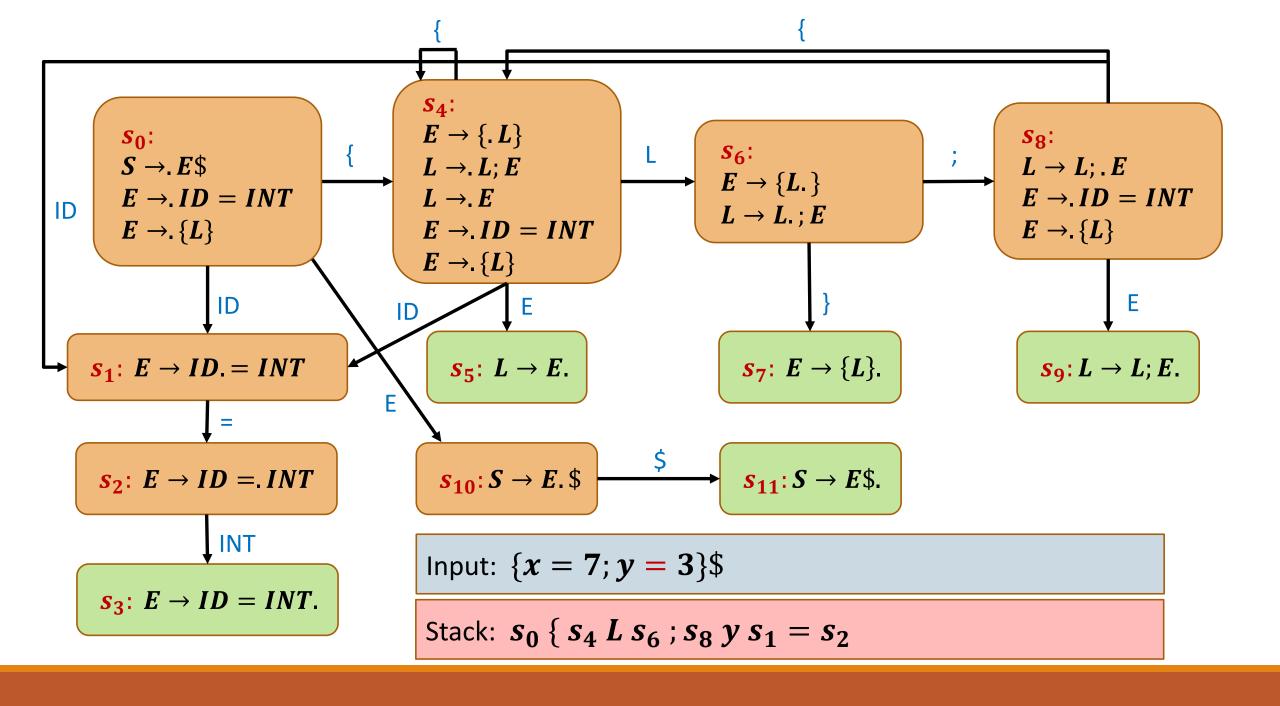


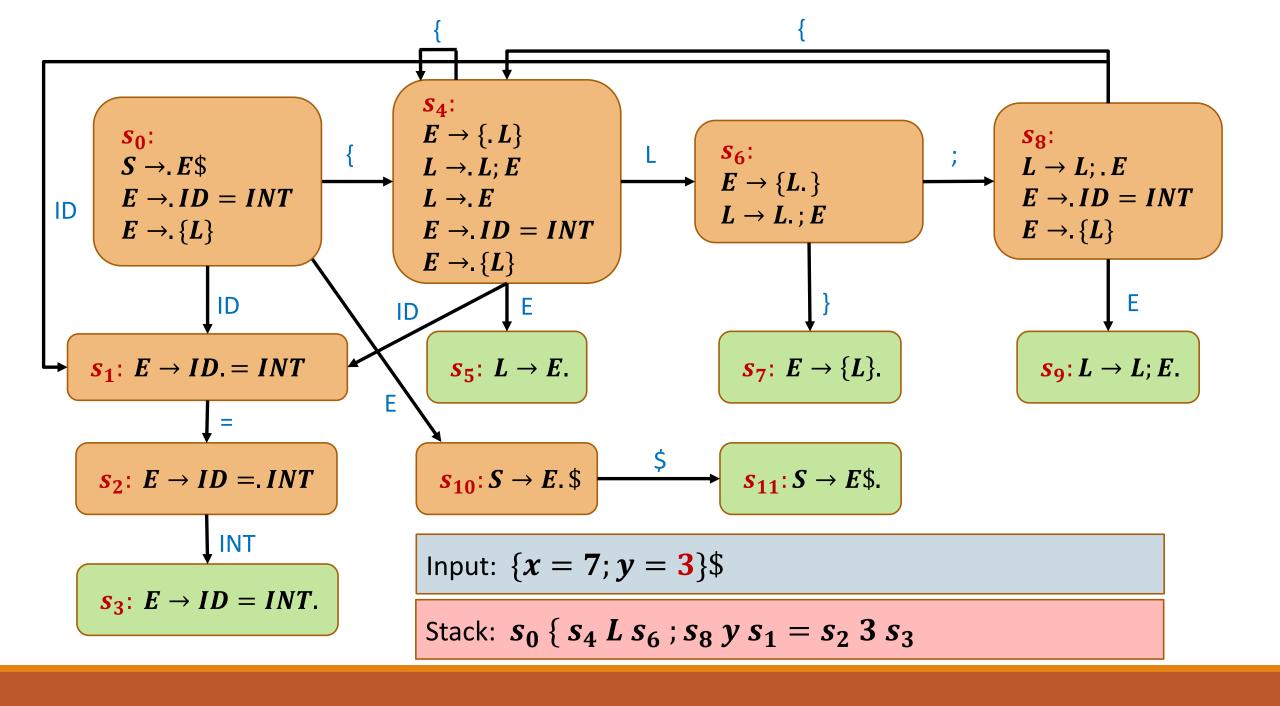


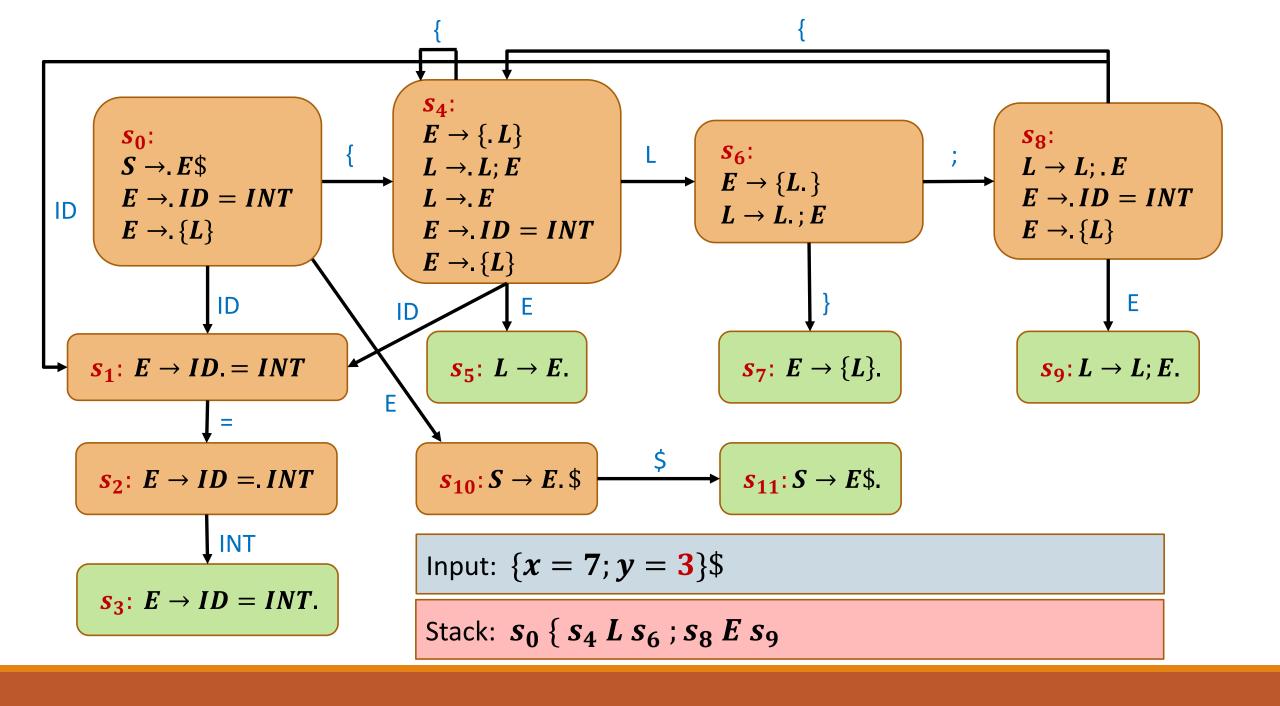


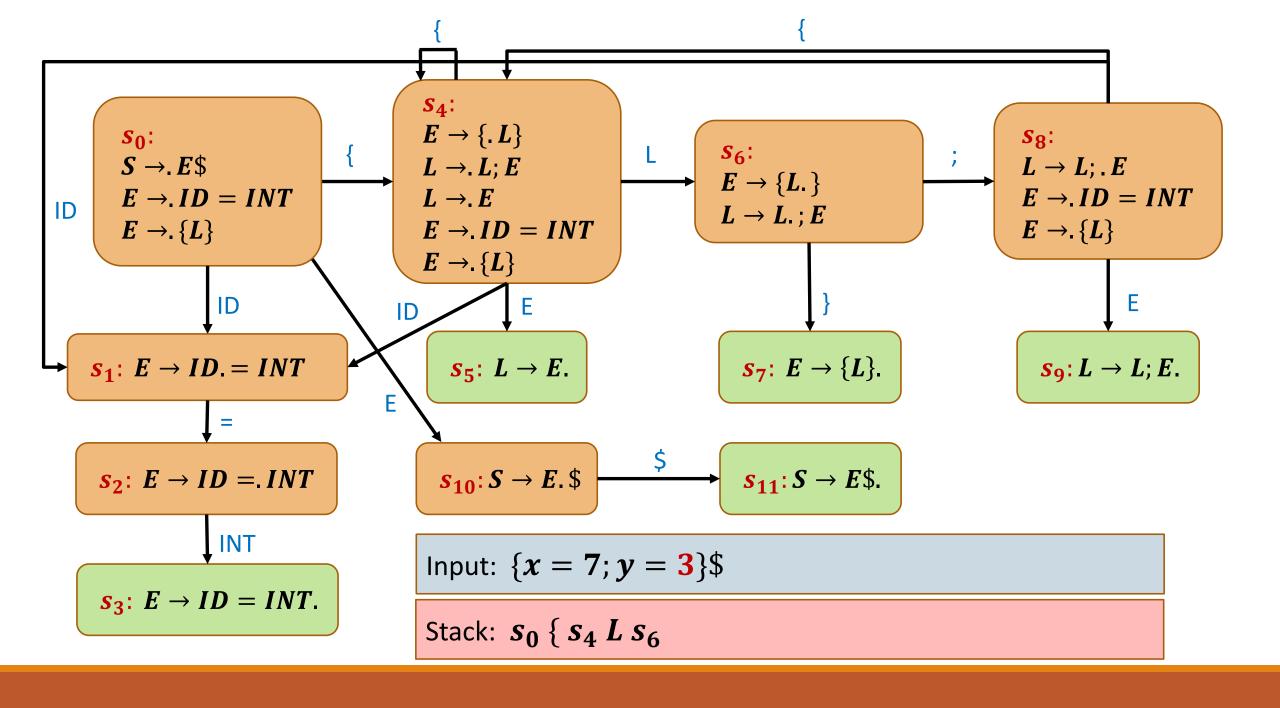


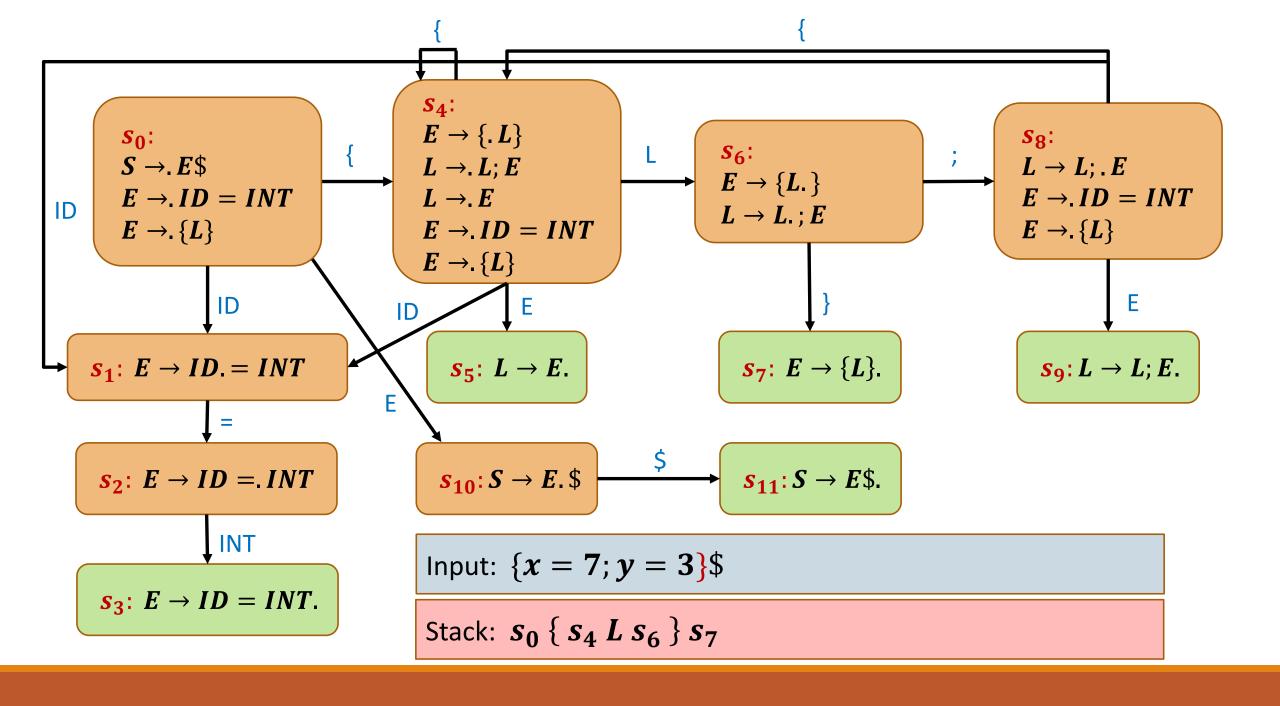


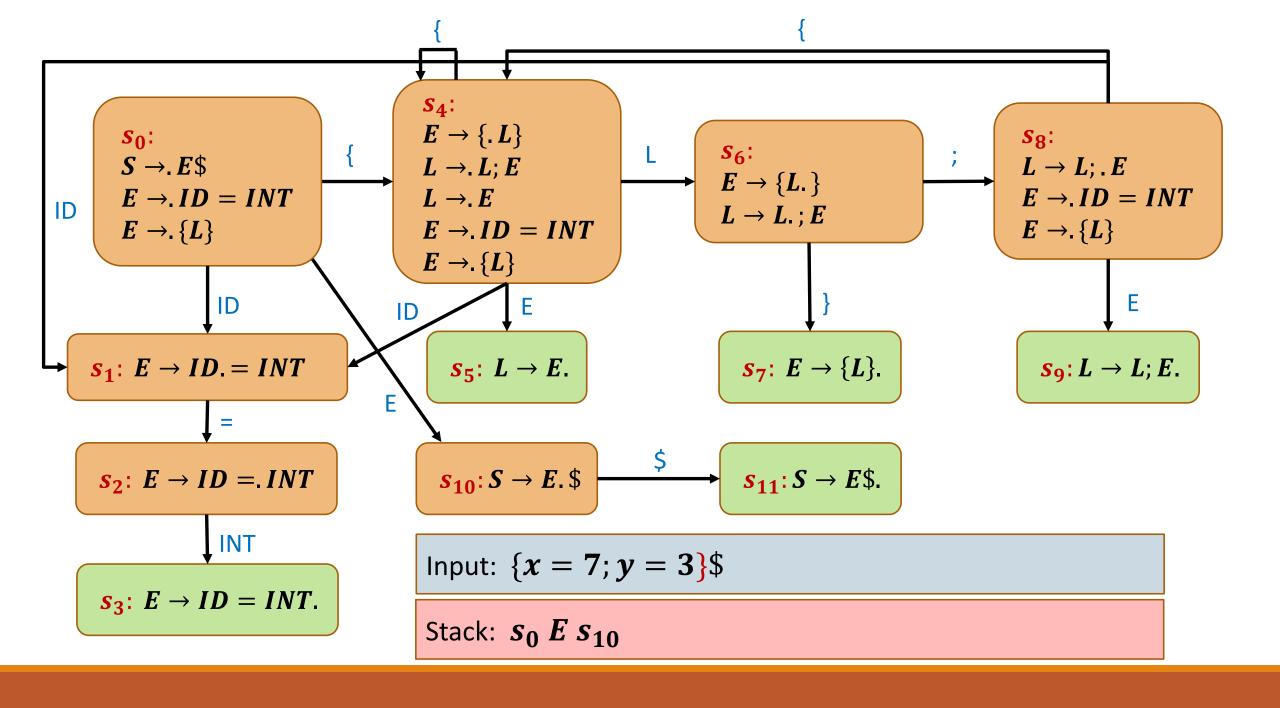


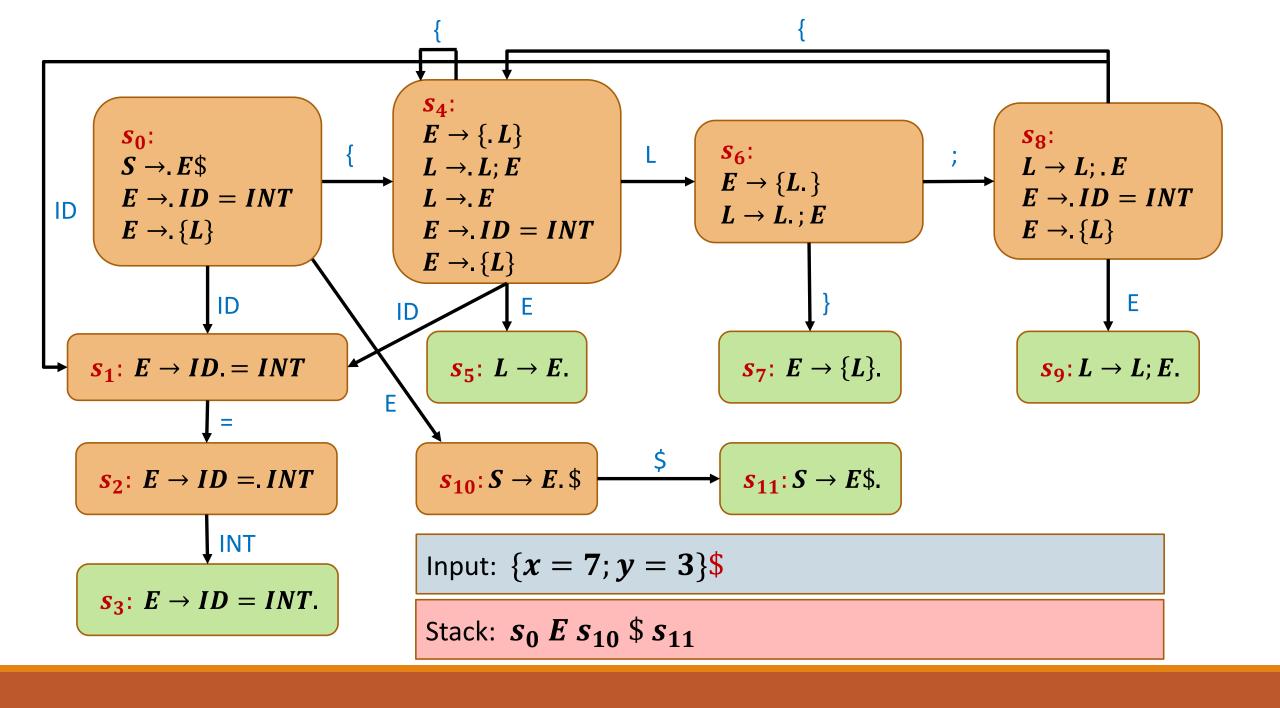


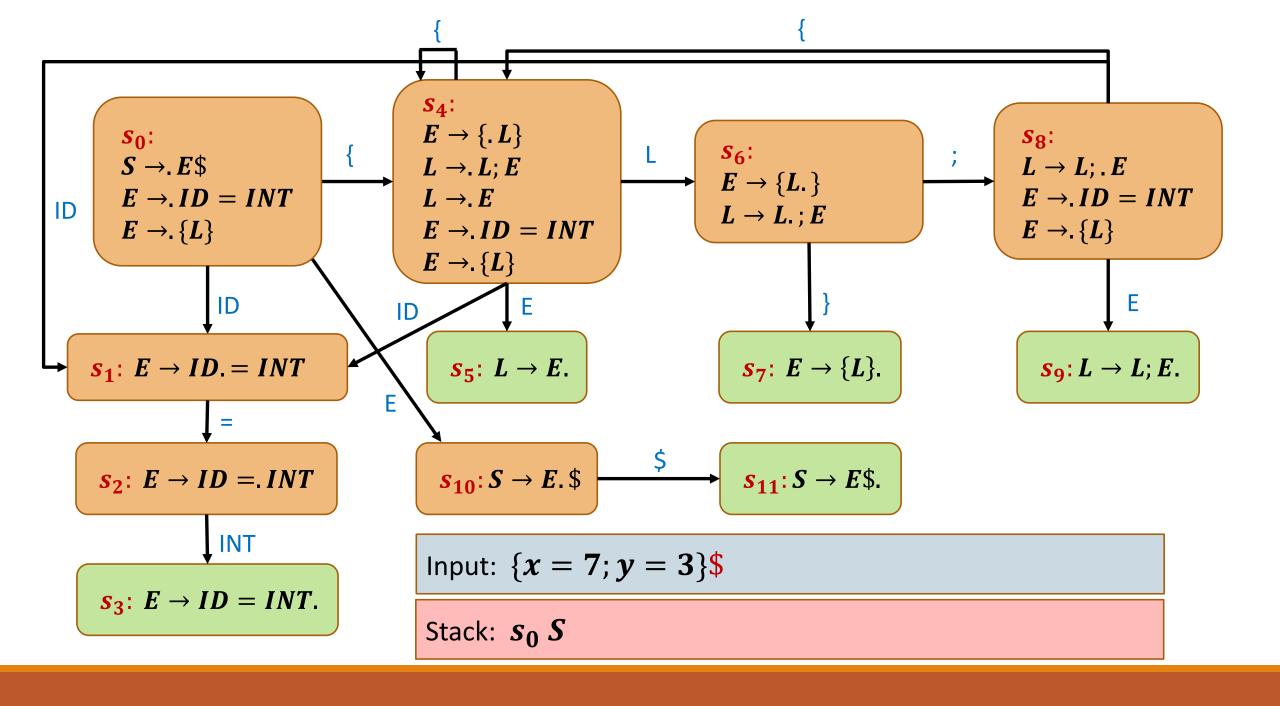










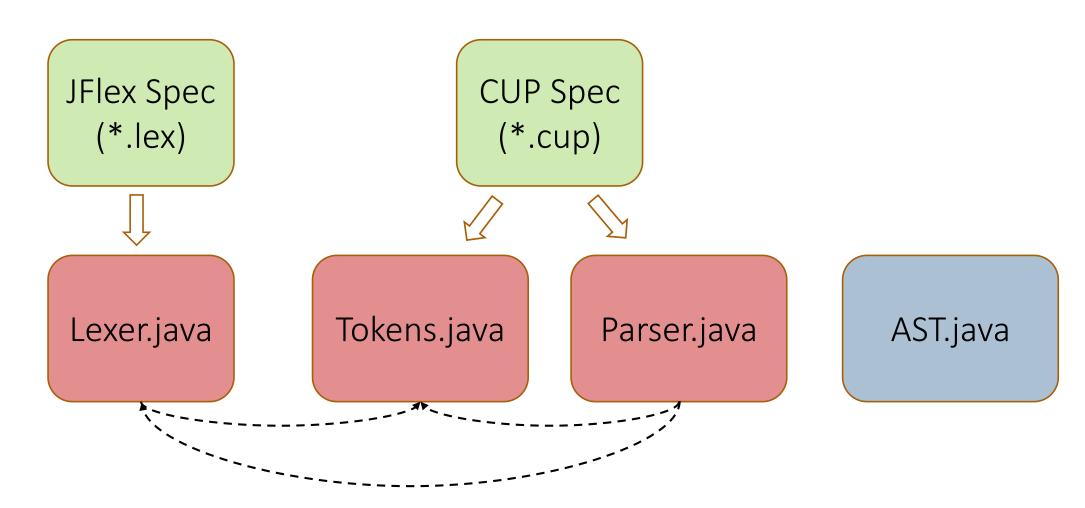


Parsing with CUP

CUP

- Given a user-specified grammar, generates an LALR parser
- Works with JFlex, which provides the parsed tokens
- Other tools:
 - Bison (for C)

CUP/JFlex Workflow



CUP Spec: Parser Setup

```
parser code {:
      public Lexer lexer;
      public Parser(Lexer lexer) {
             super(lexer);
             this.lexer = lexer;
      public void report_error(String message, Object info) {
             System.exit(0);
```

CUP Spec: Lexer Setup

```
scan with {:
         Symbol s;
         s = lexer.next_token();
         // print token...
        return s;
:};
```

CUP Spec: Terminals

```
terminal T1;
terminal T2;
terminal T3;
terminal T4;
...
```

CUP Spec: Non-Terminals

```
non terminal AST_NODE_1 E1;
non terminal AST_NODE_2 E2;
non terminal AST_NODE_3 E3;
...
```

CUP Spec: Operator Precedence

```
precedence left OP1;
precedence left OP2;
precedence left OP3;
precedence left OP4;
...
```

These are token names...

CUP Spec: Grammar

```
start with S;
S ::=
 E1:e1 E2:e2 {: RESULT = new AST NODE 1(e1, e2); :} |
            {: RESULT = new AST_NODE_2(e3); :};
 E3:e3
E1 ::= ID:id {: RESULT = new AST NODE 3(id); :}
E2 ::= INT:i {: RESULT = new AST NODE 4(i); :}
E3 ::= ...
```

CUP Spec: AST Nodes

- We need to decide which node types we have in our AST
- We need to define the classes for these AST nodes.
- For example, for integers (INT) we can do:

```
public class AST_EXP_INT extends AST_EXP {
    public int value;
    public AST_EXP_INT(int value) {
        this.value = value;
    }
    public void PrintMe() { ... }
}
```

CUP Example

Consider the following CFG:

- $E \rightarrow INT$
- $E \rightarrow V$
- $E \rightarrow E + E$
- $E \rightarrow E E$
- $V \rightarrow ID$
- $V \rightarrow V . ID$

CUP Example: Terminals

```
terminal Integer INT;
terminal String ID;
terminal PLUS;
terminal MINUS;
Terminal DOT;
```

CUP Example: Non-Terminals

```
non terminal AST_EXP exp;
non terminal AST_VAR var;
```

CUP Example: Operator Precedence

```
precedence left PLUS;
precedence left MINUS;
```

CUP Example: Grammar

```
start with EXP;
EXP ::=
  INT:i {: RESULT = new AST EXP INT(i); :} |
  VAR: \lor \{: RESULT = new AST_EXP_VAR(\lor); :\} 
  EXP:e1 PLUS EXP:e2 {: RESULT = new AST EXP BINOP(e1, e2, 0); :} |
  EXP:e1 MINUS EXP:e2 {: RESULT = new AST EXP BINOP(e1, e2, 1); :};
VAR ::=
  ID:name {: RESULT = new AST VAR SIMPLE(name); :} |
  VAR:v DOT ID:fieldName {: RESULT = new AST VAR FIELD(v, fieldName); :};
```

CUP Example: AST Nodes

For the rule *ID:name*:

```
public class AST_VAR_SIMPLE extends AST_VAR {
    public String name;
    public AST_VAR_SIMPLE(String name) {
        this.name = name;
    }
}
```

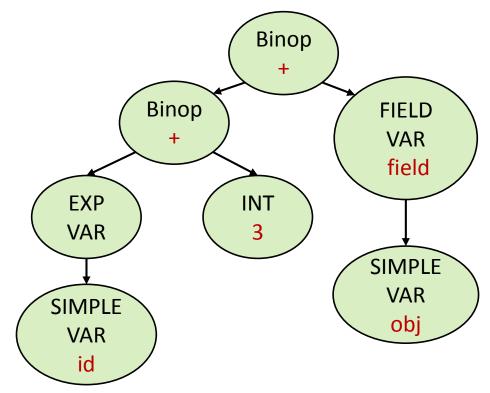
CUP Example: AST Nodes

For the rule *var:v DOT ID:fieldname*:

```
public class AST_VAR_FIELD extends AST_VAR {
    public AST_VAR var;
    public String fieldName;
    public AST_VAR_FIELD(AST_VAR var, String fieldName) {
        this.var = var;
        this.fieldName = fieldName;
    }
}
```

CUP Example: Debugging

We can generate an image of the AST (using the exercise template) For the input foo + 3 + obj.field we have:



CUP Example: Debugging

- Can dump he automaton (and goto/action table)
- Can detect conflicts:
 - shift-reduce, ...