

2D Matrix

Print row wise/ col wise sum

Principal Diagonals

Matrix Transpose

Matrix Inverse

1D arrays : list of elements



2D matrix : 2D array which has a rectangular grid of nos.  $\rightarrow$  element

store elements arranged in row and cols

int mat [N] [M]

$\downarrow$   
data  
type

$\downarrow$   
matrix  
name

$\rightarrow$  rows

$\rightarrow$  cols

Total ele  
 $= N * M$

	0	1	2
0	0,0	0,1	0,2
1	1,0	1,1	1,2
2	2,0	2,1	2,2
3	3,0	3,1	3,2

int mat [4] [3]

$\downarrow$  rows  $\downarrow$  cols

horizontal

$\downarrow$   
vertical

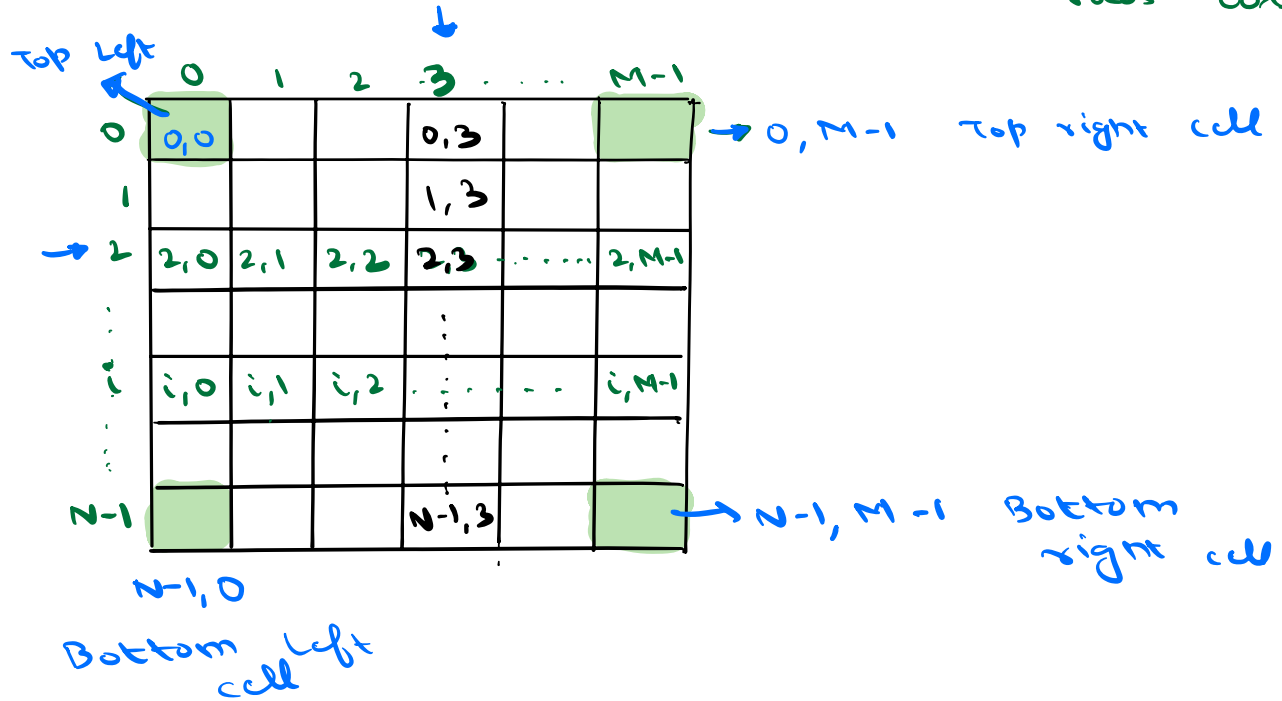
mat [i] [j]

$\downarrow$   
row no

$\downarrow$   
col no

Total ele = 12  
 $= 4 * 3$

int mat[N][M]  
 ↓        ↓  
 rows    cols



mat[N][M]  
 rows col

★ Iterate in a row

1. Row no. is fixed
2. col no.  $\rightarrow [0 \text{ } M-1]$

★ Iterate in a col

1. col no. is fixed
2. Row no.  $\rightarrow [0 \text{ } N-1]$

Given 2D Matrix  $[N][M]$ , print row wise sum.

mat[3][4]

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

10
26
42

output

Traverse each row and while traversing take sum of elements present in that row

mat  $[N][M]$

```

for (row = 0 ; row < N ; row++) {
    sum = 0
    for (col = 0 ; col < M ; col++) {
        sum += mat[row][col]
        // fixed changing
    }
    print (sum)
}

```

TC:  $O(N \times M)$

SC:  $O(1)$

Given 2D Matrix  $[N][M]$ , print col wise sum.

mat[3][4]

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

Output  $\rightarrow$  15 18 21 24

Traverse each col, while traversing, calculate sum of all elements present in that column

```
for (col = 0; col < M; col++) < N x M
```

```

    sum = 0
    for (row = 0; row < N; row++) <
        sum += mat[row][col]
    print (sum)

```

TC:  $O(N \times M)$

SC:  $O(1)$

Given a 2D square matrix  $[N][N]$ ,  
print diagonal elements from left to right.

← rows = cols

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9

2 diagonals in square mat

① Principal Diagonal

Top Left → Bottom Right

1, 5, 9

1 → 5 → 9

0,0 → 1,1 → 2,2 ↗

mat[i][j]

i == j

② Anti Diagonal

Top Right → Bottom Left

3, 5, 7

Print principal diagonal

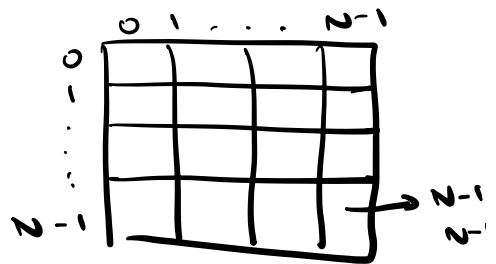
TL  $\xrightarrow{+1}$   $0,0 \rightarrow 1,1 \xrightarrow{+1} 2,2 \rightarrow \dots \rightarrow N-1, N-1$  BR

void print diagonal (int mat[N][N]) {

```

    int i = 0;
    while (i < N) {
        print (mat[i][i]);
        i++;
    }
}

```



```

for (i = 0; i < N; i++) {
    print (mat[i][i]);
}

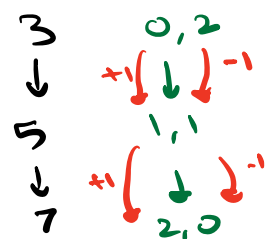
```

TC:  $O(N)$   
SC:  $O(1)$

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9

Print anti-diagonal

row ++, col --



TC:  $O(N)$   
SC:  $O(1)$

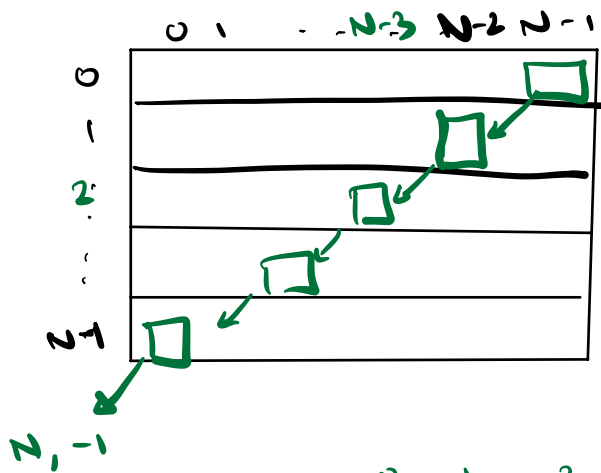
mat[N][N]

```

int i = 0, j = N-1;
while (i < N & j >= 0) {
    print (mat[i][j]);
    i++; j--;
}

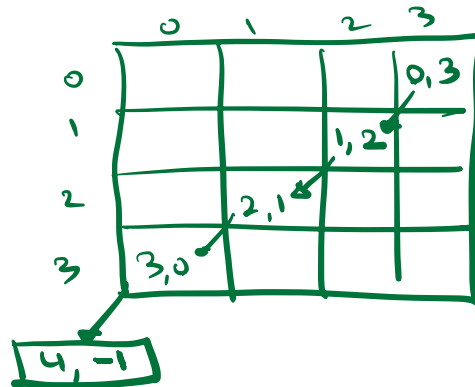
```

i	j
0	N-1
1	N-2
2	N-3



↓  
2  
...  
N-1  
0

0:17



4 x 4  
N=4  
N-1=3

Print all anti diagonals of a non-square matrix. R → L

↓  
rows != cols

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

mat[3][4]

cnt = 6

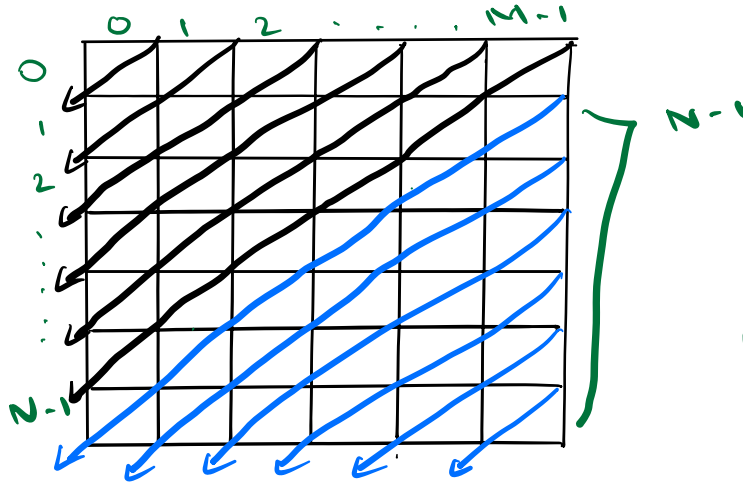
Output

1  
2 5  
3 6 9  
4 7 10  
8 11  
12

N x M  
mat[N][M]

Every cell in 0th row is starting a diagonal

Every cell in last col is starting a diagonal



Total diagonals  
=  $M + N - 1$

mat[N][M]

0<sup>th</sup> row  $\rightarrow$  M cells

Last col  $\rightarrow$  N cells

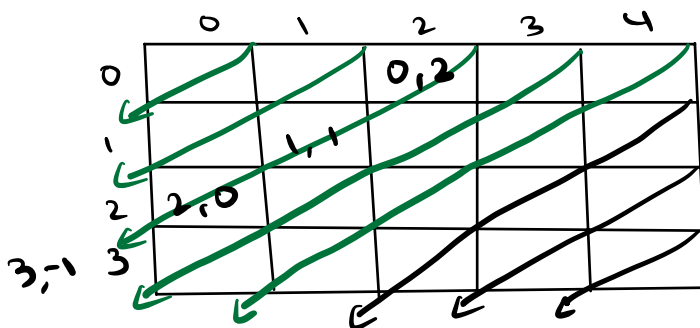
$M +$        $N - 1$   
 $\downarrow$          $\downarrow$   
 0<sup>th</sup> row    last col

Q. Given mat [4][5], cnt of right to left (anti) diagonals?

0<sup>th</sup> row  $\rightarrow$  5 cells  $\rightarrow$  5

Last col  $\rightarrow$  4 cells  $\rightarrow$  3

8 diagonals



① 0<sup>th</sup> row

② Last col



(0,0)

(0,1) → (1,0)

(0,2) → (1,1) → (2,0) → 3,-1 ✓ X

```
for (col = 0 ; col < m ; col++) <
```

```
    i = 0    j = col
```

```
    while ( i < N && j >= 0 ) <
        print ( mat[i][j] )
```

```
        i++    j--
```

```
    print ( \n )
```

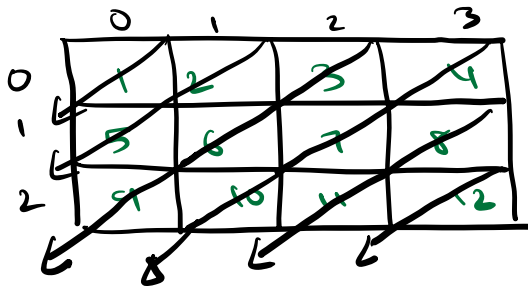
```
for ( row = 0 ; row < N ; row++ ) <
```

```
    i = row    j = M - 1
```

```
    while ( i < N && j >= 0 ) <
        print ( mat[i][j] )
```

```
        i++    j--
```

```
    print ( \n )
```



$\boxed{c=0}$

$N=3 \quad M=4$

$i \quad j$   
(0,0) → (1,-1)

(0,1) → (1,0) → (2,-1)

(0,2) → (1,1) → (2,0)

↓  
(3,-1)

1  
 2 5  
 3 6 9  
 4 7 10  
 8 11  
 12

$(0,3) \rightarrow (1,2) \rightarrow (2,1)$   
 $\downarrow$   
 $(3,0)$

$j = M - 1$      $j = 3$

TC:  $O(N * M)$   
 SC:  $O(1)$

$(1,3) \rightarrow (2,2) \rightarrow (3,1)$

$(2,3) \rightarrow (3,2)$

Q. Given a square mat  $[N][N]$ ,  
 find transpose

4x4

	0	1	2	3
0	1	5	7	9
1	2	6	8	4
2	10	25	41	16
3	18	19	23	21

Mat



	0	1	2	3
0	1	2	10	18
1	5	6	20	19
2	7	8	41	23
3	9	4	16	21

Trans

9  
 $(0,3) \leftrightarrow (3,0)$

5      2  
 $(0,1) \leftrightarrow (1,0)$

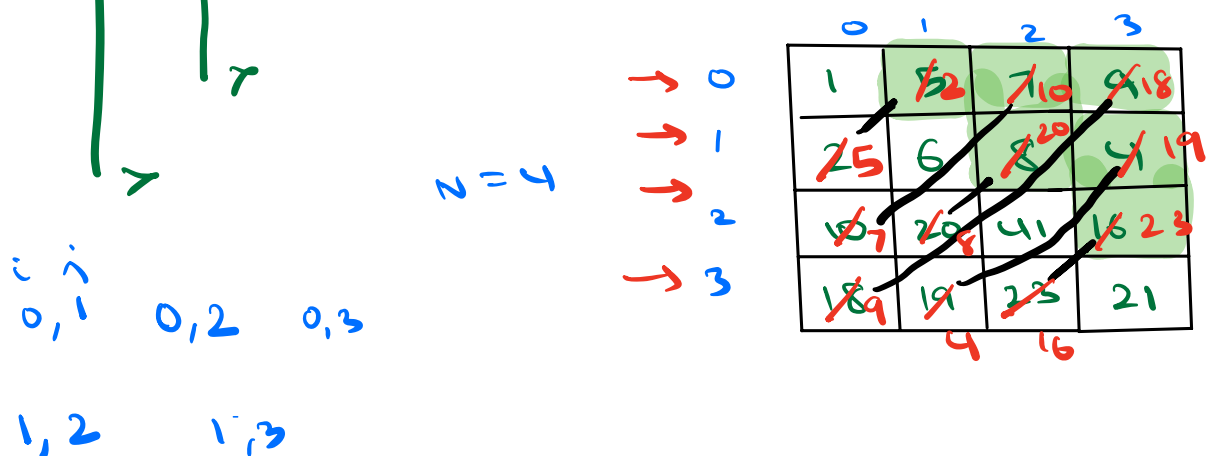
7      10  
 $(0,2) \leftrightarrow (2,0)$

$(i,j) \leftrightarrow (j,i)$

Just swap elements of upper  $\Delta$  or lower  $\Delta$

```

for (i = 0 ; i < N ; i++) <
    for (j = i+1 ; j < N ; j++) <
        swap (mat [i] [j], mat [j] [i])
    
```



2,3  
 $i = N-1, j = N$

$i$  cannot start from 0

$a \quad b$   
 $7 \quad 10$   
 1 swap 10 7  
 2 swap 7 10

1	4	7
2	5	8
3	6	9

Trans

	0	1	2
0	1	2	7
1	4	5	6
2	7	8	9

mat

Total ele =  $N^2$

No. of iter =  $N^2/2$

TC :  $O(N^2)$

SC :  $O(1)$

6. Given mat  $[N][N]$ , rotate by 90° clockwise

18	0	2	1
19	20	9	5
23	41	8	7
21	16	5	9

Rotated  
mat

1	5	7	9
2	6	8	4
10	20	41	16
18	19	23	21

Mat

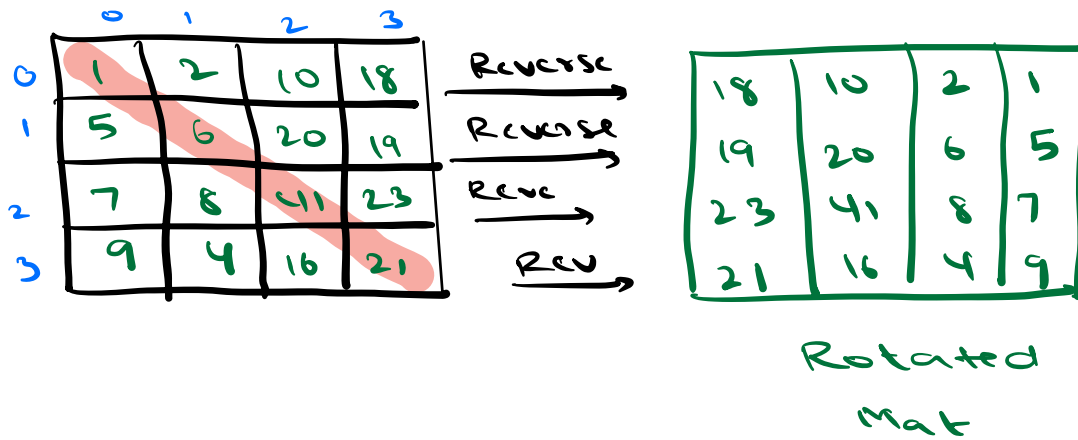


18	10	2	1
19	20	6	5
23	41	8	7
21	16	4	9

Rotated  
Mat

① Transpose

② Reverse each row



- ① Transpose →  $N^2/2$
- ② Go to every row and reverse it. →  $N^2/2$

```

transpose(mat)
for (i=0 ; i<N ; i++) {
    reverse(mat[i])
}

```

TC:  $O(N^2)$   
SC:  $O(1)$

Reverse 1 row →  $\frac{\text{Row size}}{2}$  Iterations

1 row =  $\frac{N}{2}$  iter

N row →  $\frac{N^2}{2}$  iter

---

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

3 x 4



	0	1	2
0	1	5	9
1	2	6	10
2	3	7	11
3	4	10	12

4 x 3

DOUBTS

int mat[N][M] → trans[M][N]

---

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

mat 3x4

r	c	0	
0	1	5	9
1	2	6	10
2	3	7	11
3	4	10	12

Rot 4x3

int mat[N][M] → rot[M][N]

[1, 2, 3]

[ [1], [1, 2], [1, 2, 3] ]

list of list

list of subarrays

for i s →

for e arraylist n  
for idn →  
n. insert (arr[idn])

output. insert(i)

[1, 2, 3]

[ [1]  
[1, 2]  
[1, 2, 3]  
[2]  
[2, 3]  
[3] ]

rows  
 $\frac{n * (n+1)}{2}$   
cols  
n

mat [6][3]

	0	1	2
0	-	-	-
1	-	-	-
2	-	-	-
3	-	-	-
4	-	-	-
5	-	-	-

Ordered - HM

HM

$$\underline{0.01} \rightarrow 2$$

$$0.03 \rightarrow 2$$

$$0.06 \rightarrow 1$$

$$0.7 \rightarrow 1$$

$$\underline{0.9} \rightarrow 1$$

(2)