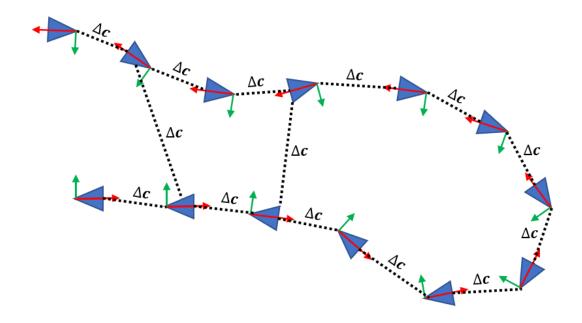
# Vision Aided Navigation 2022 - Exercise 7

### Prefix:

In exercise 6 we summarized the information from the Bundle optimizations in a Pose Graph.

We use the pose graph as a concise description of the trajectory. This will enable us to recognize that the current location of the vehicle is potentially similar to some past location and initiate a search for the exact relative pose between two frames.

When we find such connection to a past frame, we'll use it to add a **Loop Closure** constraint to the pose graph, thus greatly reducing the drift of the trajectory estimation.



Pose Graph: Relative poses  $\Delta c$  between consecutive poses and distant poses (loop closure)

#### 7

For each key frame  $c_n$  in the pose graph loop over previous keyframes  $c_i$ , i < n, and perform steps 7.1-7.4:

# 7.1 Detect Loop Closure Candidates

### a. Relative Covariance

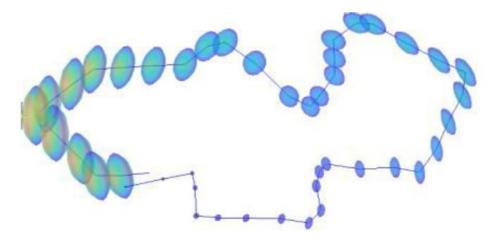
find the shortest path from  $c_n$  to  $c_i$  and sum the covariances along the path to get an estimate of the relative covariance  $\Sigma_{n|i}$ .

- What are reasonable choices for the edge weights? i.e. in what way is the chosen path the shortest?
  - What did you use as edge weights?
- How did you implement the shortest path algorithm?

### **b.** Detect Possible Candidates

Choose the most likely candidate to be close to the pose  $c_n$  by applying a Mahalanobis distance test  $\Delta c_{ni}^T \Sigma_{nli}^{-1} \Delta c_{ni}$  with  $c_{ni}$  the relative pose between  $c_n$  and  $c_i$ .

Choose a threshold to determine if the candidate advances to the next (expensive) stage.



Relative Covariance

Note that the last frame uncertainty threshold includes the 1st frame location

# 7.2 Consensus Matching

Perform consensus match between the two candidate frames. (See exercise 3) Set a threshold for the number of inliers that indicates a successful match. Note that this is typically a more difficult match than that of two consecutive frames.

What was your chosen threshold?



Two similar frames from different times with a successful consensus match (inlier in cyan)

## 7.3 Relative Pose Estimation

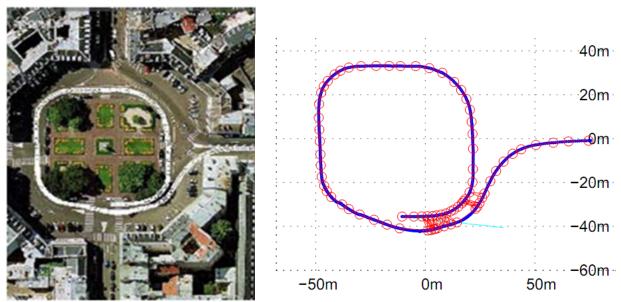
Using the inlier matches perform a small Bundle optimization to extract the relative pose of the two frames as well as its covariance.

What is a reasonable initial solution for the Bundle?

How did you extract the appropriate covariance?

# 7.4 Update the Pose Graph

Add the resulting synthetic measurement to the pose graph and optimize it to update the trajectory estimate.



Trajectory around a square. Estimation on the right – keyframes marked in circles, loop closure edges in red

### 7.5

- How many successful loop closures were detected?
- Plot the match results of a single successful consensus match of your choice. (For the left images, inliers and outliers in different colors)
- Choose 5 versions of the pose graph along the process and plot them (including location covariance).
  - Explain at what points you chose to plot the graph.
- Plot a graph of the absolute location error for the whole pose graph both with and without loop closures.
- Plot a graph of the location uncertainty size for the whole pose graph both with and without loop closures. (What measure of uncertainty size did you choose?)

## **GTSAM**

- pose prior = gtsam.PriorFactorPose3(key, pose, uncertainty)
- Factor error for particular values: pose prior.error(gtsam.Values())

- gtsam.noiseModel.Gaussian.Covariance(S)
- relative\_pose = pose\_c0.between(pose\_c1)
- gtsam.BetweenFactorPose3(c0, c1, relative\_pose, noiseCov)