

ETHEREUM ZÜRI.CH

Even Faster secp256r1 for Passkeys and SGX

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- Introduction
- A story of secp256r1
- Use cases
 - Passkeys
 - SGX
- Cryptographic Gibberish (optimizations and tradeoffs)
- Call to L2s for DSM (double scalar multiplication) EIP/RIP



0xDECE65 (codename)

Cryptography team-building tools that make self-sovereignty delightful for users and developers.
Our mantra: there is no Web2 or Web3, **just Web**.

Some of our current focus:

- Support of the **secp256r1 (P256)** curve on-chain to enable the use of physical enclaves/keychain
- Support of the ed25559 curve on-chain for the similar reasons
- Support of the FIDO2 framework on-chain, including WebAuthn and the Passkeys
- Development of multi/threshold signature schemes such as FROST, MUSIG2

The Team

1 security/hardware, 1 smarcontract dev, 1 sales, 1 **cryptographer**

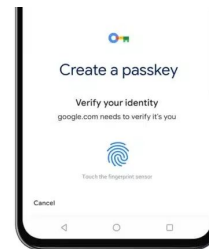
- 17 years in French industry of Defense
- 2 years in Ethereum ecosystem
- **Watch our feet, not our mouth**
 - a. Finalist team at EthGlobal NY 2023
 - b. Rewarded by retroPGF for **fastest** secp256r1 and abstract wallet (invisible wallet on passkeys)
 - c. Granted by Ethereum Foundation for **ECC works (half funded)**

What is it

- secp256r1/P256 is an elliptic curve. Elliptic curve cryptography (ECC) is what enables **signing** and key exchange in modern communications.
- **ECDSA** over P256 secures our daily lives with our TLS exchanges, some Passports; **Intel SGX**, SSH and **passkeys** (TouchID/FaceID).
- Specified in NIST SP186-5, 20 years of existence
- Non native to ethereum (secp256k1 is native), must be **emulated** with EVM instructions
- Natural candidate for Account Abstraction



Passkeys + Account Abstraction : the invisible wallet



Account Abstraction + Secp256r1

What it does:

One click onboarding, invisible for user, vanishing check out churn/difficulties :

- by using the touch ID, creates a keypair stored in Apple/Android stored in keychain/enclave (device bound)
- the related key is written in the UserOp of ERC4337 as the signer
- front translates transaction to sign to the WebAuthn/Passkeys webbrowser



SGX + ZK/optimist Rollup : “2FA” settlement



<https://ethresear.ch/t/2fa-zk-rollups-using-sgx/14462>

(live on scroll)

two state transition proofs to advance the on-chain zk-rollup state root:

1. cryptographic proof: a SNARK/STARK
2. 2FA: additional SGX proof

Intel SGX recently switched from BN curves to secp256r1.

- ZK mechanisms are novel (but the way), and there will be implementation failures (Nova).
- SGX is a way to add an extra layer to buy time for the patch (ZK > SGX)
- Using our precomputation version could save 90% of gas per settlement (scroll, Taiko)



Library	ecaddN (gas)	ecDbl (gas)	ecmulmul (gas)	Prec. Bytes	Test+Analysis
orbs-network	2250	1750	1.06M	0	✓
Androlo	2073	1229	866K	0	✓
Maxrobot	1949	1502	760K	0	Crit Vuln+ KO
Numerology	1973	1003	422K	0	✓
alembich-tech	2250	1750	335K	3.2MB	Malleability
itsobvioustech	946	578	290K	0	Crit Vuln+ KO
Ours(1)	566	522	202K	0M	✓
Ours(3)			61.6 K	3.2MB	✓

<https://eprint.iacr.org/2023/939>

What we did:

Improved by a large factor prior implementations

- Improved by a large factor prior implementations
- Pick optimal formulas according to EVM costs
- Optimize stack
- Use many memory optimization
- Propose precomputations to speed further (complicated for B2C)





Generic

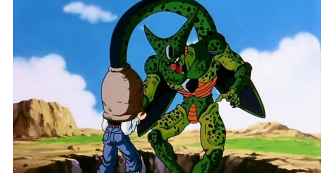
Having a generic precompile would prevent switching or adding endless precompiles

- A seamless tradeoff, only requires to extend the public key by 512 bits (one extra point)
- What we implemented is **DSM (double scalar mul)**, MSM-EIP is a dream, maybe DSM is the way to begin
- Application of this single precompile :
 - All schnorr based wallet without the “hacky-mul” trick (Ambire)
 - Starkcurve, secp256k1, palla, vesta, babyjubjub (circom), **ed25519**, bn254-G1, eecc2024

Even faster

#Bases	ecdbl	ecadd	ecmulmul (measured)	Deployment (Prec.)	Comment
2	256	192	201K	0	2 ¹²⁸ Q in calldata
8	64	64	61.6K	3.2M	
4	128	128	160K	0	

- A seamless tradeoff, only requires to extend the public key by 512 bits (one extra point)



Currently many proposals

- secp256r1 (RIP/EIP7212)
- **ed25519** (EIP665), **ed25519 > secp256r1**
 - not NIST, faster, schnorr (MPC/ZK friendly)
 - farcaster, SGX, IBC
- BN254 (EIP1962)
- BLS12381-G1 (EIP 2537)
- BLS12377 (EIP2539)
- Palla/Vesta
- EECC2024

[illegible][illegible]

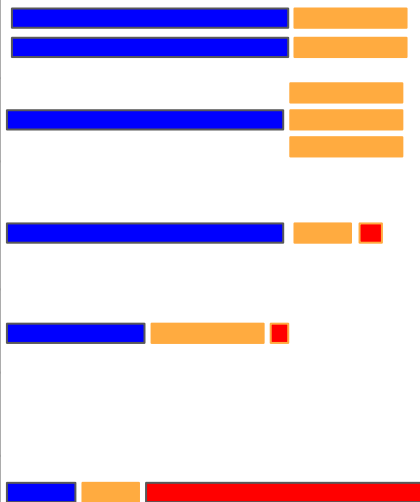
```
b=0x100000000000000002000000005b00000000200000000000000001;
```



Optimizing DSM implementation

4 bases is nearly optimal for 256 bits scalar without precomputations

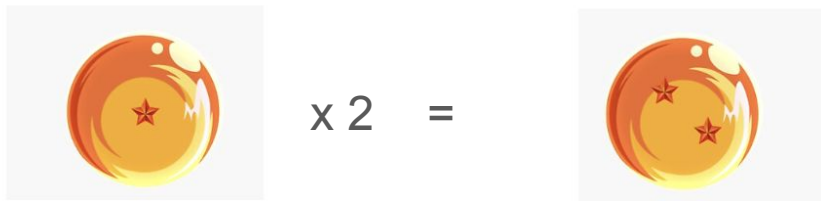
Points	Prec ecAdd	EcAdd	EcD bl	Total DSM	Comment
1		256	512	1024	Double'n Add
2	1	192	256	448+1	Standard Strauss-Shamir DSM
2	14	60	256	326+14	Strauss+Windowing (best RIP-API compliant)
4	11	120	128	248+11	DSM + Precomputed 2^{128} P and Q
6	57	84	85	169+57	Cut scalars by 3 is evil 🤖
8	256	64	64	128+256	



(1 point = 64 bytes = 1K gas call data, 12.8K in contract)

Cryptographic Optimizations

ECC is easy, you have points, you can add them ($P+Q$), or double them ($P+P=2P$) using dedicated formulas.



(harder to resurrect Goku, cause there is more points than atoms in the universe)





The principle

- Double always, Add when '1'

5P (b101) : $P \rightarrow 2P \rightarrow 4P + P$

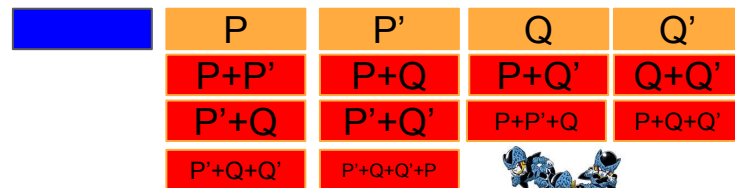
7Q : (b111): $Q \rightarrow 2Q + Q = 3Q, 3Q + Q = 7Q$

- Strauss Shamir : mutualize doubling, compute $H = P + Q$

101 , $(P + Q), 2(P + Q) + Q, 2(2P + 3Q) + P + Q$

111

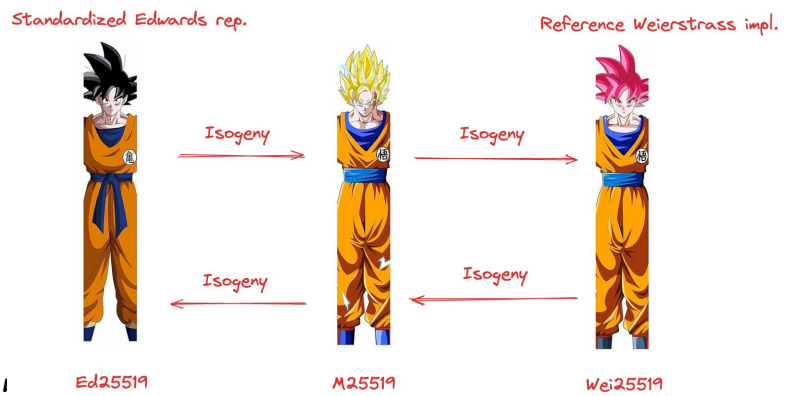
- Higher dimension : choose $2^{(n/2)}P$ and $2^{(n/2)}Q$ as extra points



An isogeny between two elliptic curves is a morphism of curves that sends the origin of E_1 to the origin of E_2 .

It is possible, using those morphisms to convert point from edwards representation to Weierstrass and vice versa:

- babyjub
- ed25519



DSM can be used to implement ed25519

Conclusion

Call for DSM-RIP

- efficient generic ECC progressive precompile
- add generic ECC capacities to the EVM
- release code April, 22th (input to audit)

