# Lecture 10

Maximum likelihood Botany 563 — Spring 2022

- Previous class check-up:
  - We studied the different models of evolution
- Learning Objectives: At the end of today's session, you will be able to
  - Explain how the likelihood of a tree is computed
  - Explain the steps in maximum likelihood phylogenetic inference
- Pre-class work
  - Read HAL 1.2 and canvas quiz

### Phylogenetic inference

Step 1: Choose the criterion to use: distances, parsimony, likelihood

Step 2: Search the space of trees until you find the optimum

### Phylogenetic inference

Step 1: Choose the criterion to use: distances, parsimony, likelihood

Step 2: Search the space of trees until you find the optimum

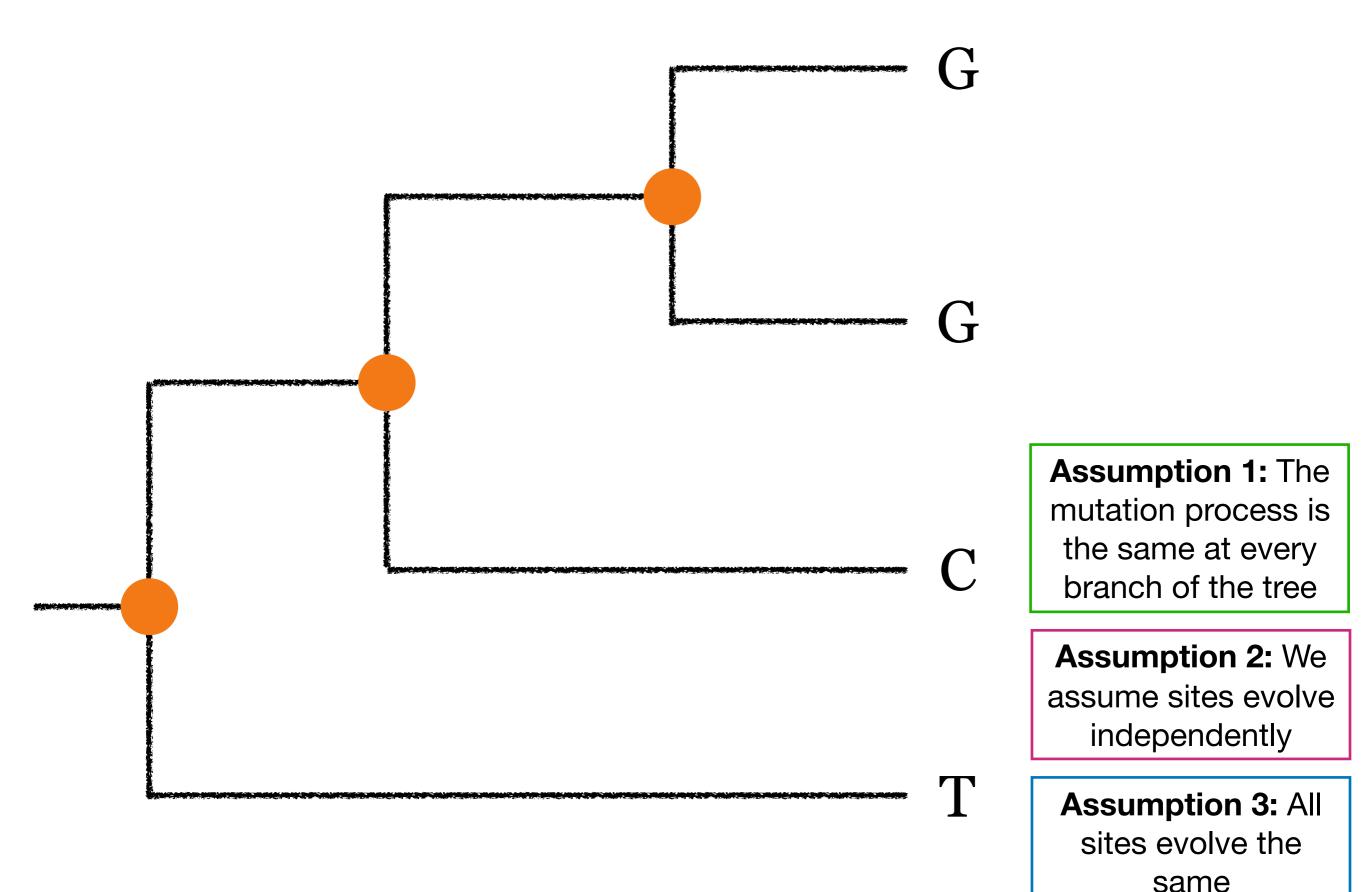
You know how to calculate the likelihood for a given tree

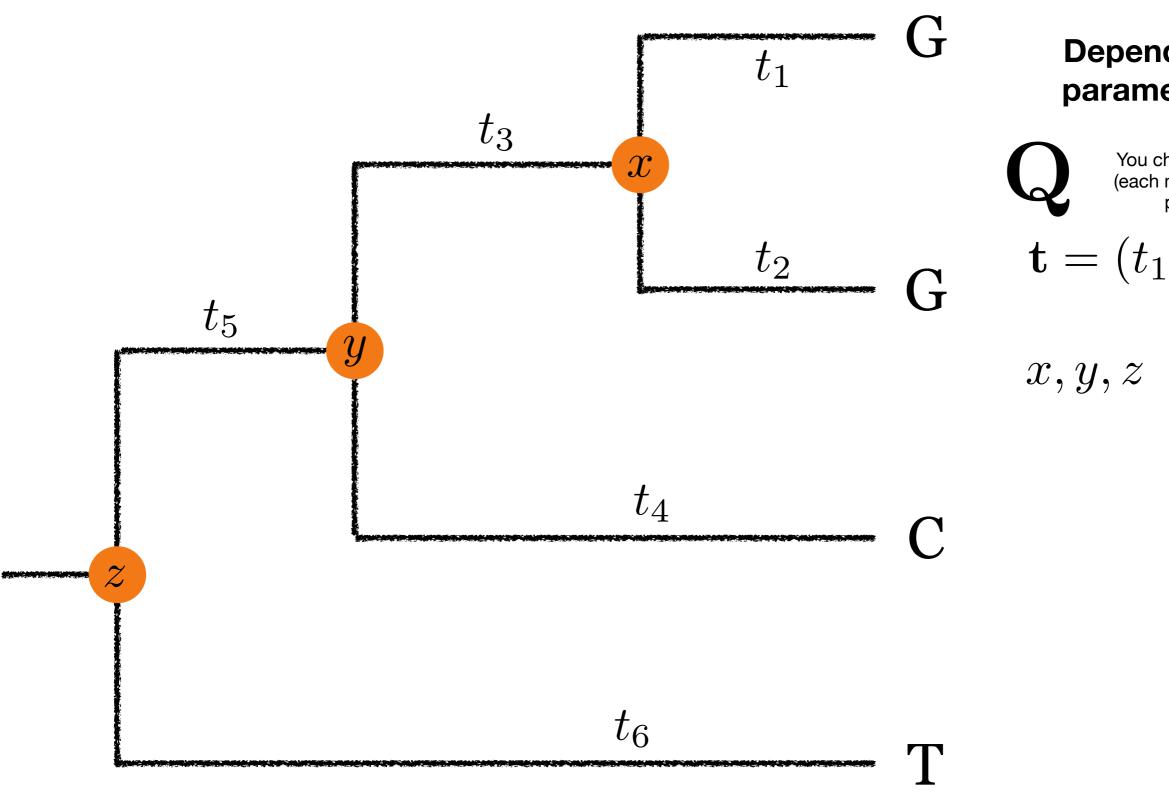
Choose a substitution model

$$\mathbf{P}(t) = \begin{bmatrix} A & C & G & T \\ A & & & & \\ C & & & & \\ G & & & & \end{bmatrix} = e^{\mathbf{Q}\mu t}$$

2. For a given tree, calculate the likelihood given the data and the substitution model

3. Search the space of trees using the tree moves (NNI, SPR, TBR) until you find the maximum likelihood tree





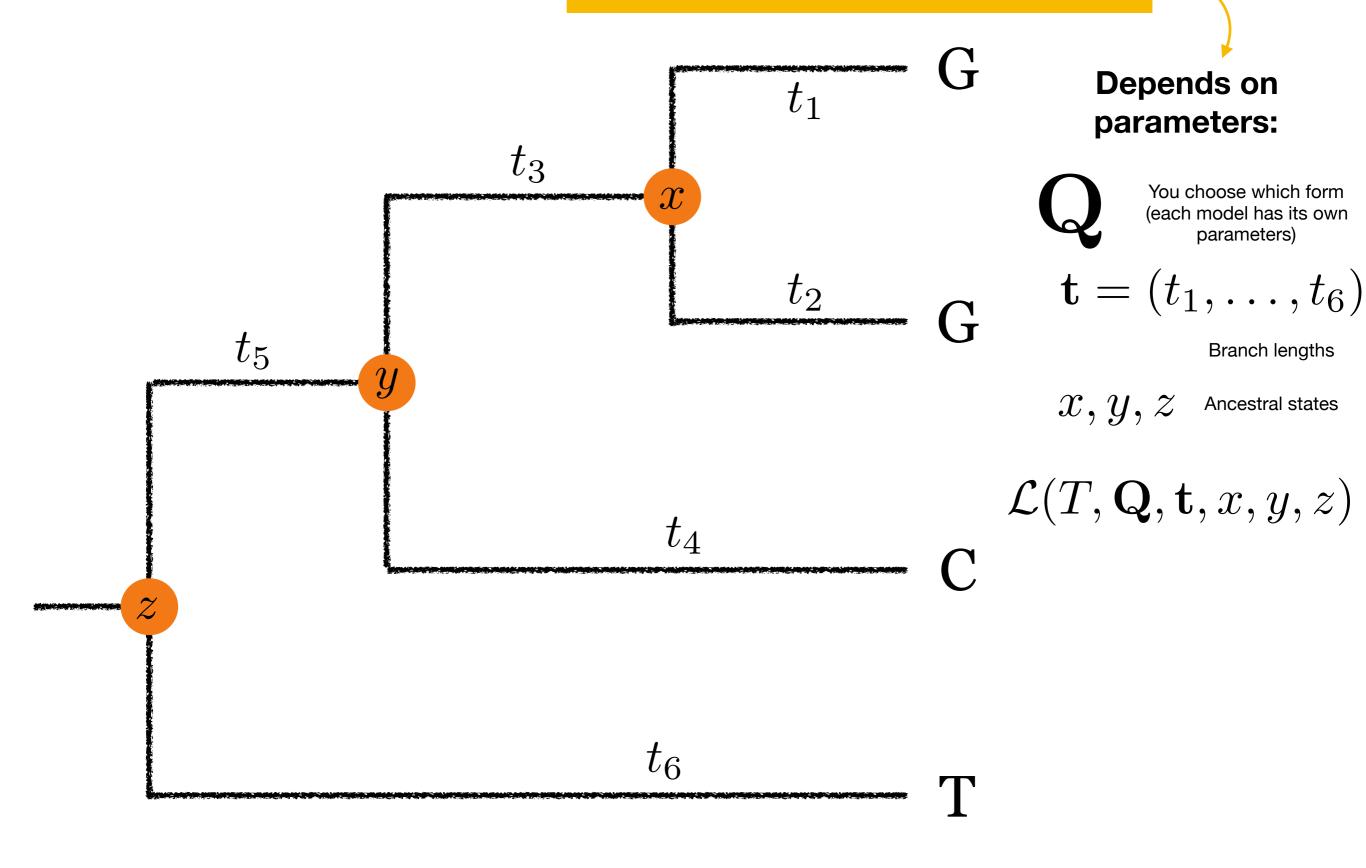
#### **Depends on** parameters:

You choose which form (each model has its own parameters)

$$\mathbf{t}=(t_1,\ldots,t_6)$$

Branch lengths

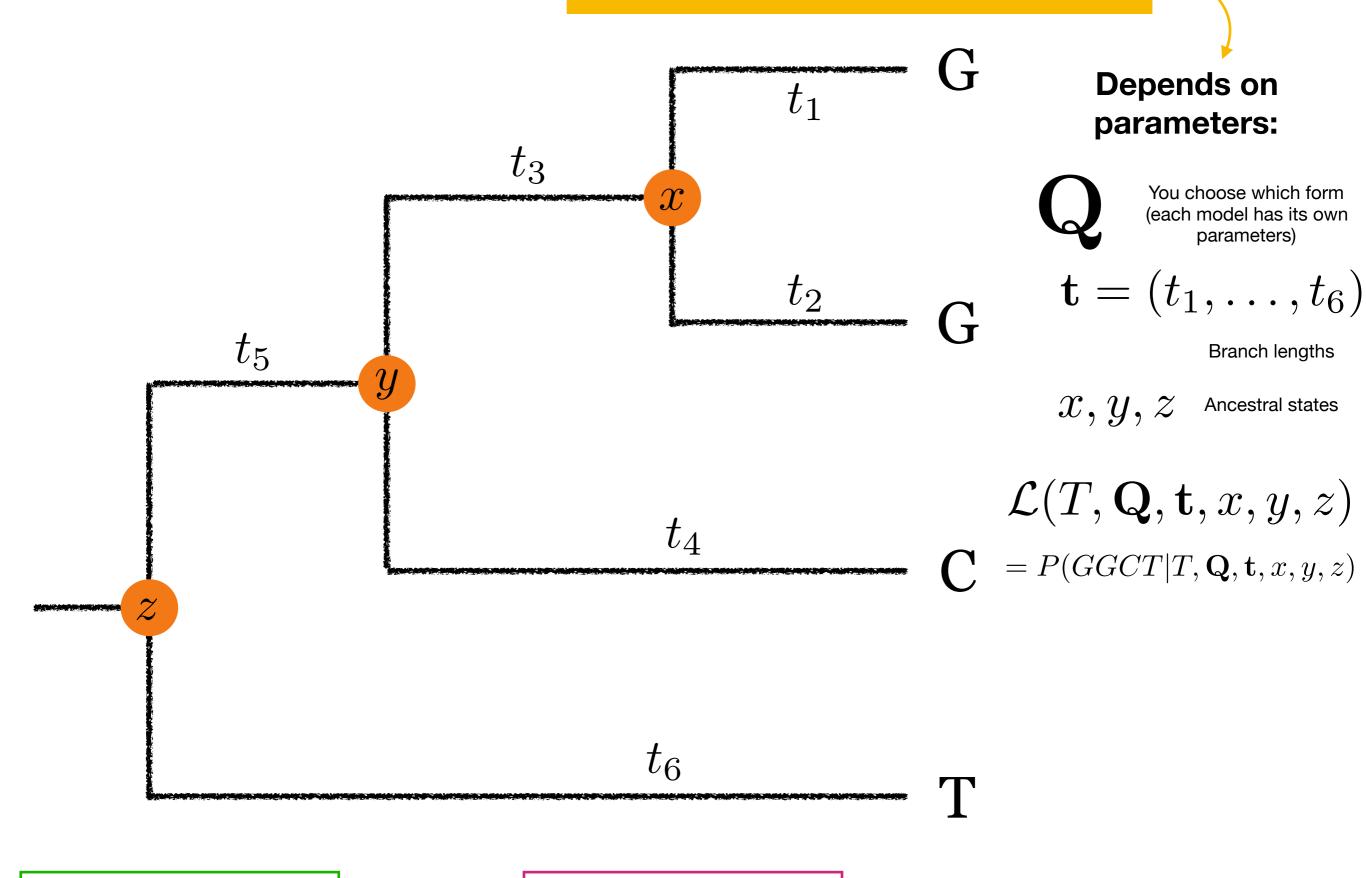
Ancestral states



**Assumption 1:** The mutation process is the same at every branch of the tree

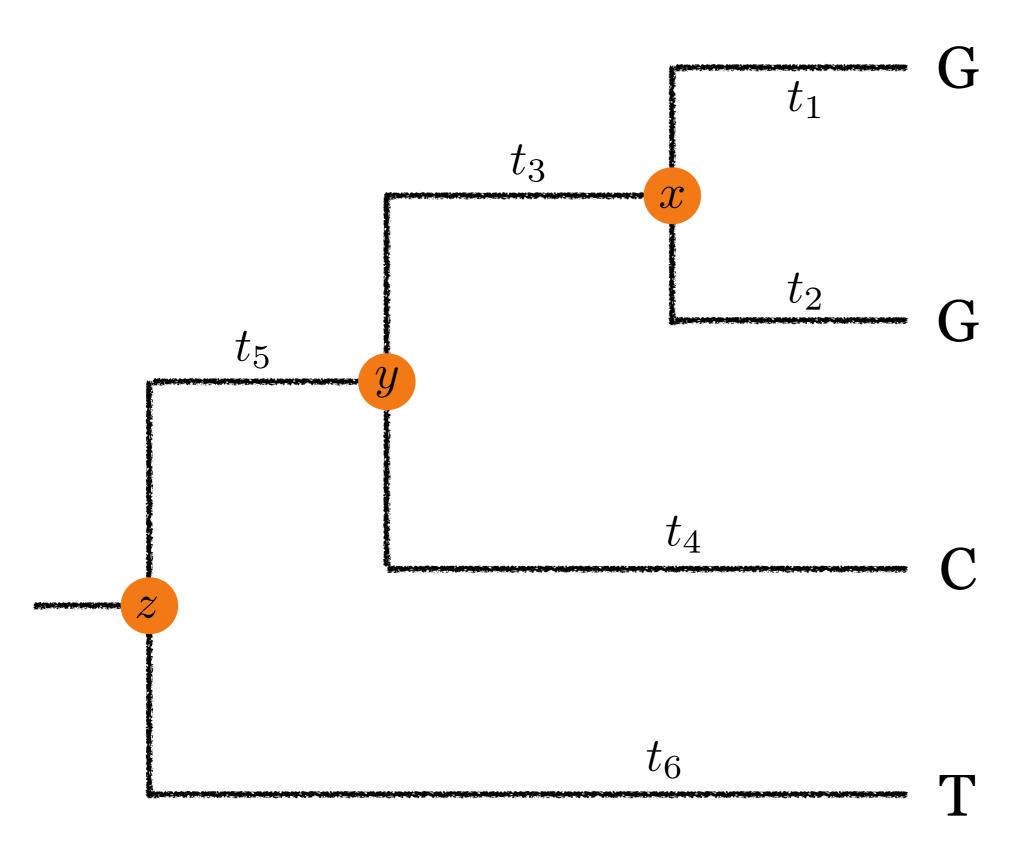
**Assumption 2:** We assume sites evolve independently

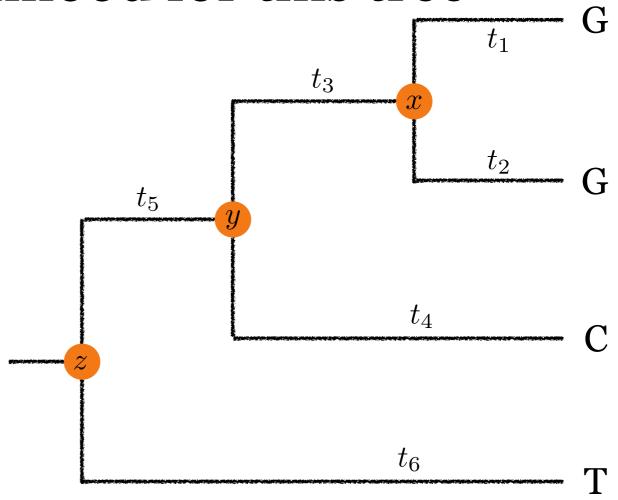
Assumption 3: All sites evolve the same

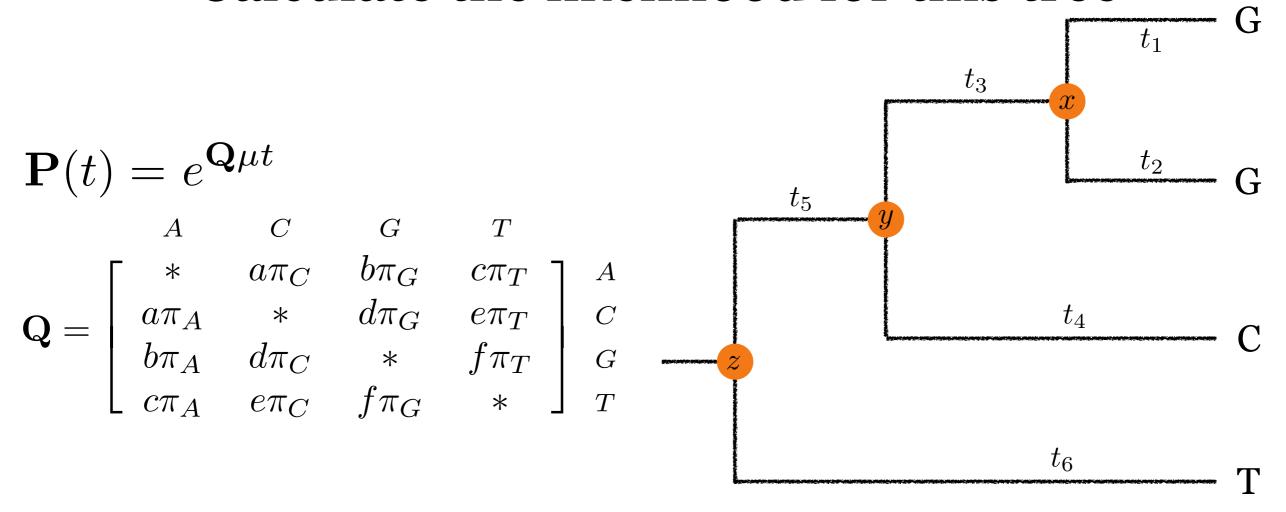


**Assumption 1:** The mutation process is the same at every branch of the tree

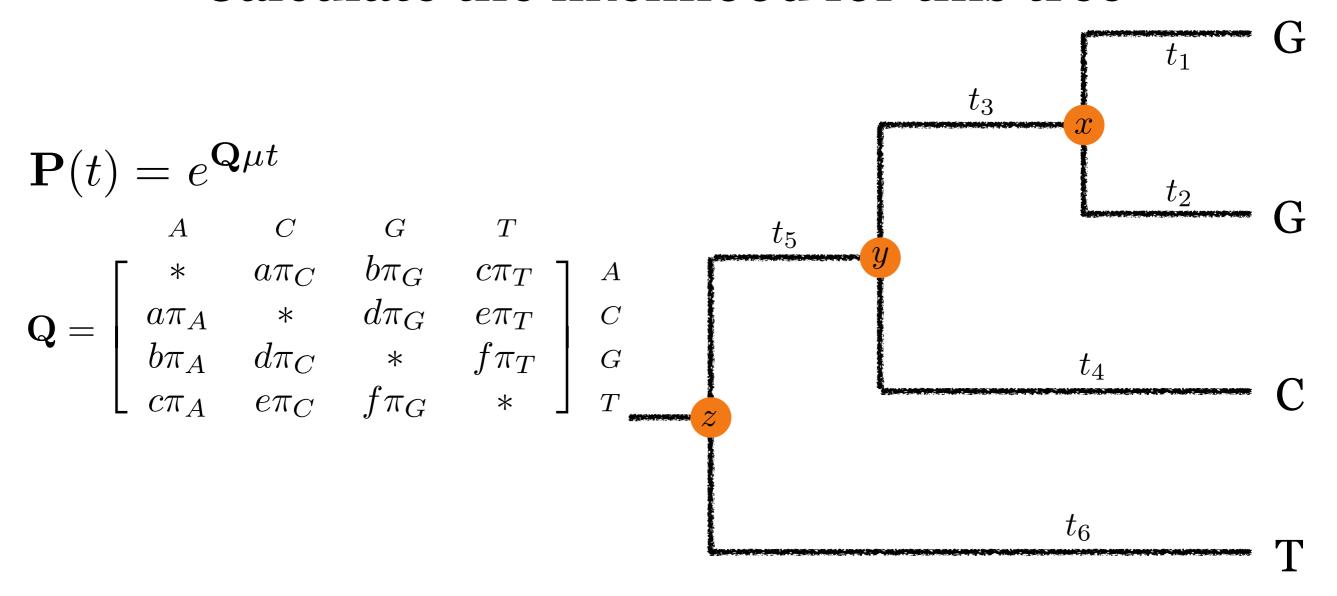
**Assumption 2:** We assume sites evolve independently







$$L = \sum_{z} \sum_{u} \sum_{x} \pi(z) P_{t_6}(z, T) P_{t_5}(z, y) P_{t_4}(y, C) P_{t_3}(y, x) P_{t_2}(x, G) P_{t_1}(x, G)$$



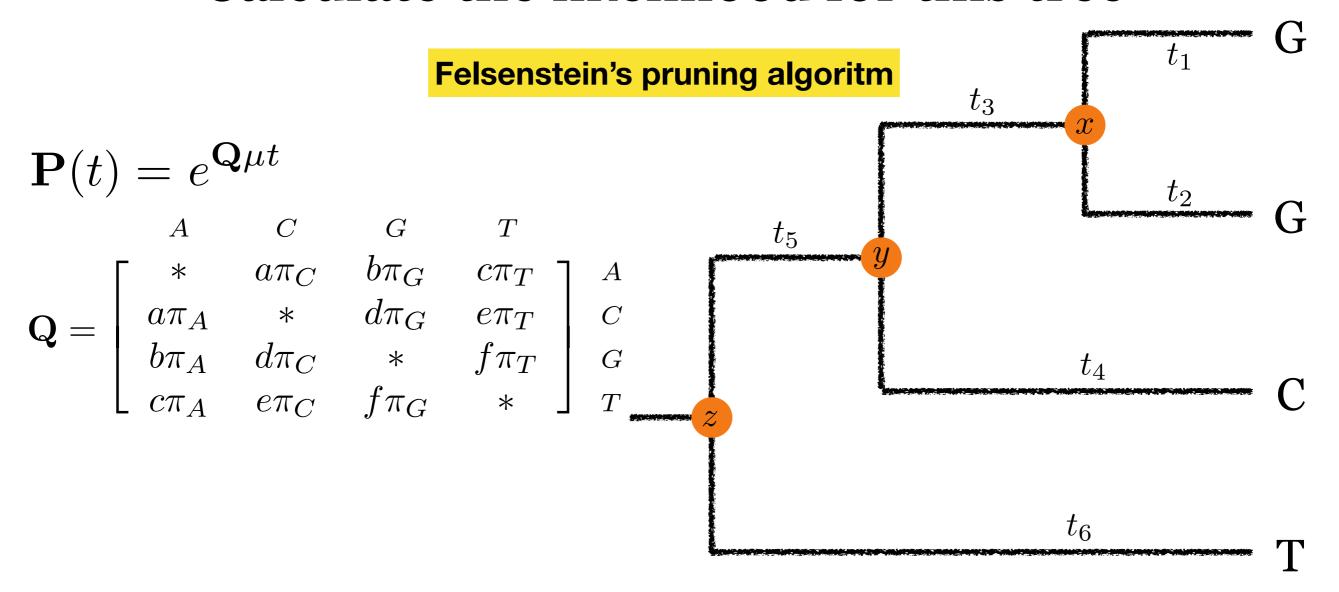
$$L = \sum_{z} \sum_{y} \sum_{x} \pi(z) P_{t_6}(z, T) P_{t_5}(z, y) P_{t_4}(y, C) P_{t_3}(y, x) P_{t_2}(x, G) P_{t_1}(x, G)$$

#### Where do the assumptions play a role?

**Assumption 1:** The mutation process is the same at every branch of the tree

**Assumption 2:** We assume sites evolve independently

**Assumption 3:** All sites evolve the same



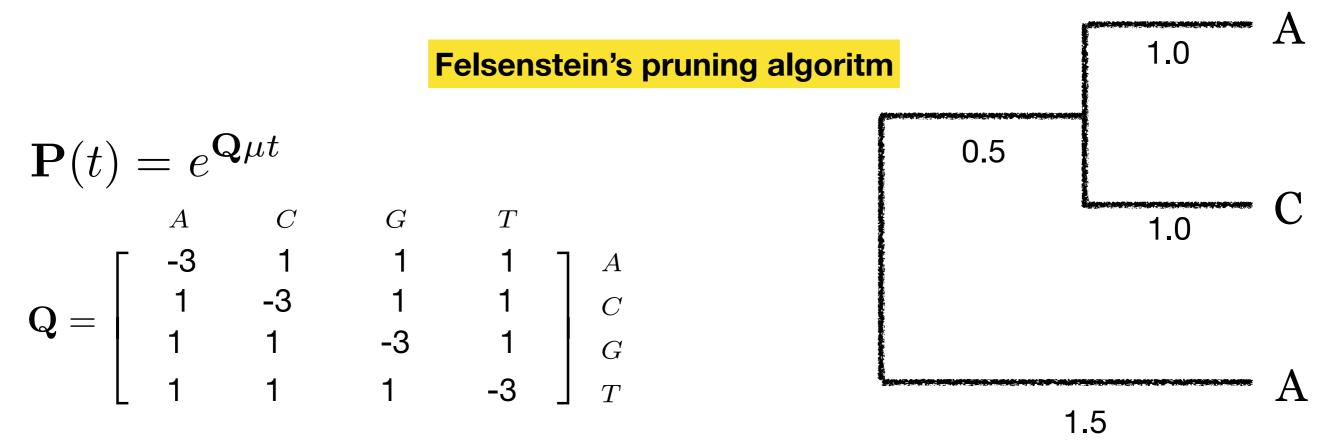
$$L = \sum_{z} \sum_{y} \sum_{x} \pi(z) P_{t_6}(z, T) P_{t_5}(z, y) P_{t_4}(y, C) P_{t_3}(y, x) P_{t_2}(x, G) P_{t_1}(x, G)$$

#### Where do the assumptions play a role?

**Assumption 1:** The mutation process is the same at every branch of the tree

**Assumption 2:** We assume sites evolve independently

**Assumption 3:** All sites evolve the same



1. Choose a substitution model

$$\mathbf{P}(t) = \begin{bmatrix} \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{C} & \mathbf{G} & \mathbf{T} \end{bmatrix} = e^{\mathbf{Q}\mu t}$$

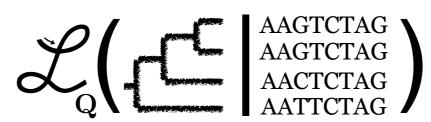
2. For a given tree, calculate the likelihood given the data and the substitution model

 Search the space of trees using the tree moves (NNI, SPR, TBR) until you find the maximum likelihood tree

1. Choose a substitution model

$$\mathbf{P}(t) = \begin{bmatrix} \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{C} & \mathbf{G} & \mathbf{T} \end{bmatrix} = e^{\mathbf{Q}\mu t}$$

2. For a given tree, calculate the likelihood given the data and the substitution model



3. Search the space of trees using the tree moves (NNI, SPR, TBR) until you find the maximum likelihood tree

## Depends on parameters:

Q

You choose which form (each model has its own parameters)

$$\mathbf{t} = (t_1, \dots, t_6)$$

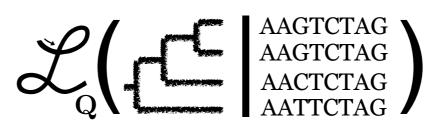
Branch lengths

x,y,z Ancestral states

1. Choose a substitution model

$$\mathbf{P}(t) = \begin{bmatrix} \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{C} & \mathbf{G} & \mathbf{T} \end{bmatrix} = e^{\mathbf{Q}\mu t}$$

2. For a given tree, calculate the likelihood given the data and the substitution model



3. Search the space of trees using the tree moves (NNI, SPR, TBR) until you find the maximum likelihood tree

## Depends on parameters:

Q

You choose which form (each model has its own parameters)

$$\mathbf{t} = (t_1, \dots, t_6)$$

Branch lengths

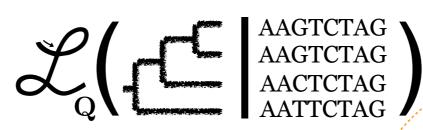
x,y,z Ancestral states

Average across them

1. Choose a substitution model

$$\mathbf{P}(t) = \begin{bmatrix} \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{C} & \mathbf{G} & \mathbf{G} \end{bmatrix} = e^{\mathbf{Q}\mu t}$$

2. For a given tree, calculate the likelihood given the data and the substitution model



- 3. Search the space of trees using the tree moves (NNI, SPR, TBR) until you find the maximum likelihood tree
  - At each proposed tree, we maximize Q and t

## Depends on parameters:

You choose which form (each model has its own parameters)  $\mathbf{t}=(t_1,\ldots,t_6)$ 

Branch lengths

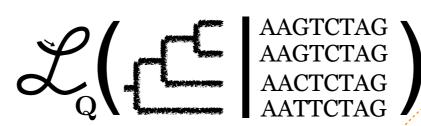
x,y,z Ancestral states

Average across them

1. Choose a substitution model

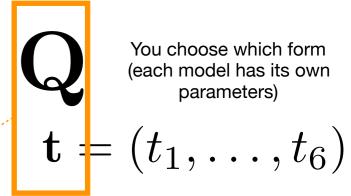
$$\mathbf{P}(t) = \begin{bmatrix} \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{A} & \mathbf{C} & \mathbf{G} & \mathbf{T} \\ \mathbf{C} & \mathbf{G} & \mathbf{C} & \mathbf{C} \end{bmatrix} = e^{\mathbf{Q}\mu t}$$

2. For a given tree, calculate the likelihood given the data and the substitution model



3. Search the space of trees using the tree moves (NNI, SPR, TBR) until you find the maximum likelihood tree

Depends on parameters:

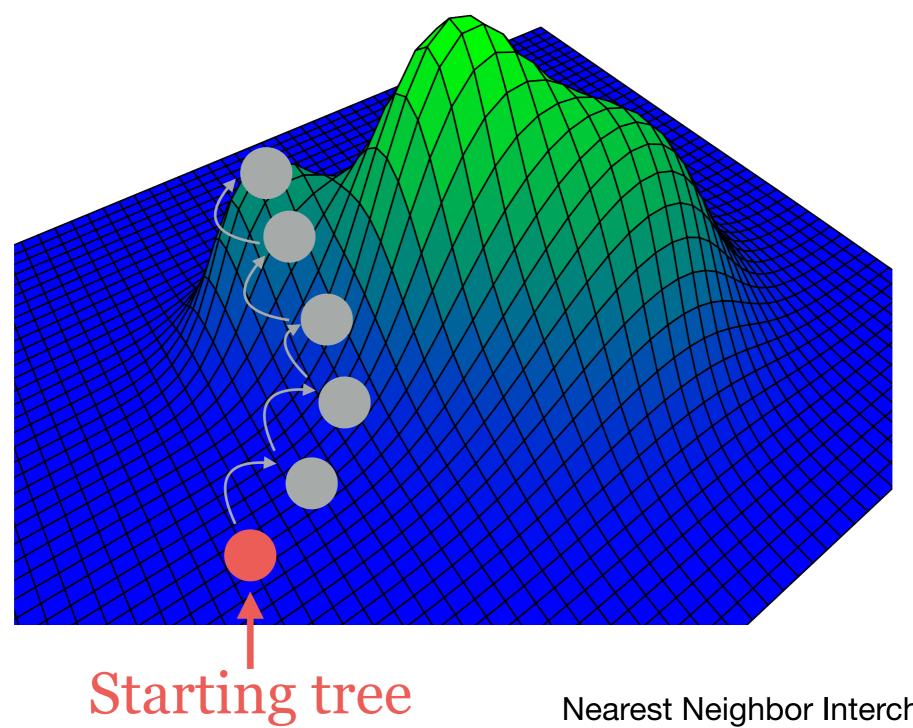


Branch lengths

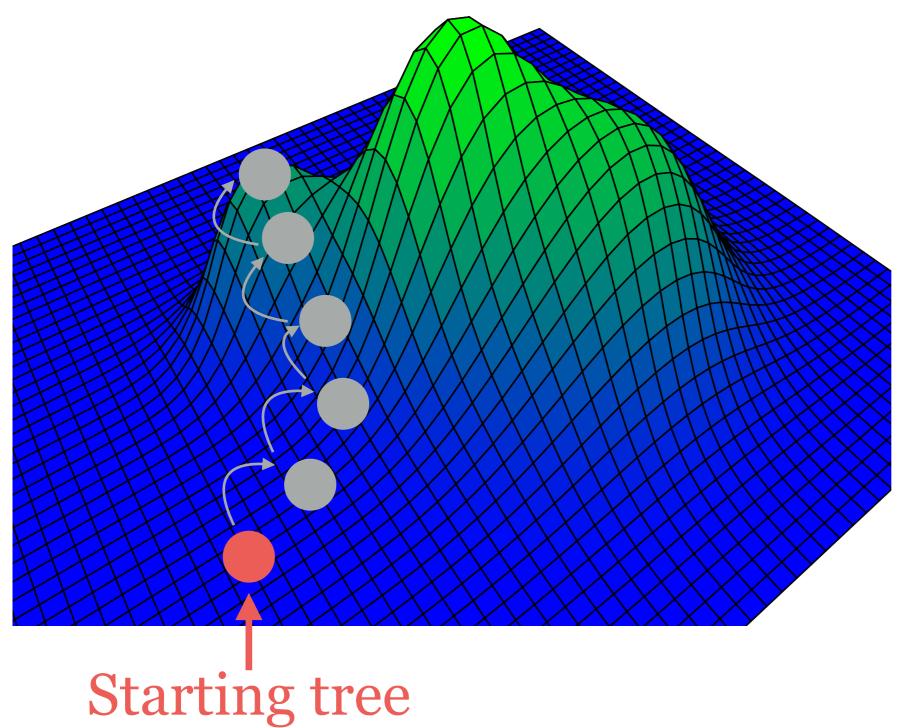
x,y,z Ancestral states

Average across them

Need to optimize

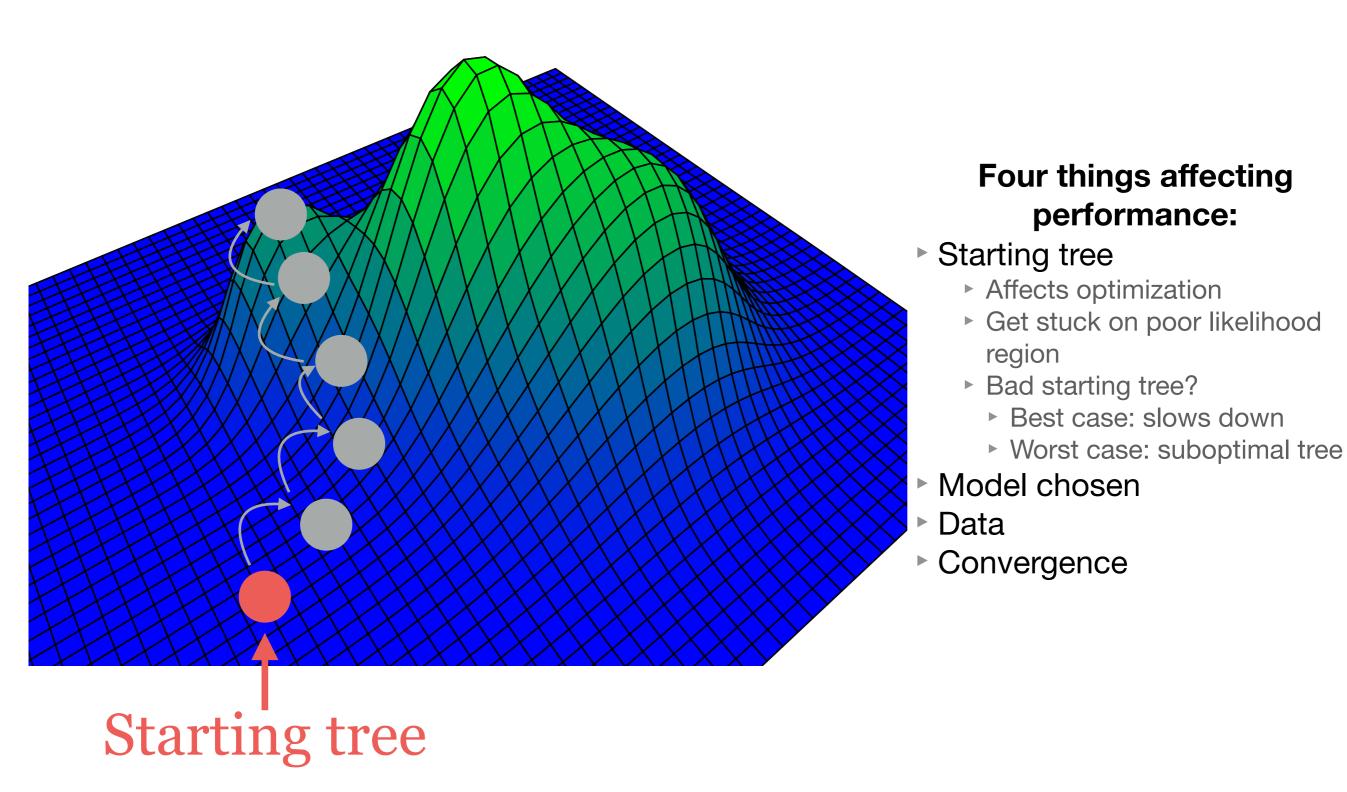


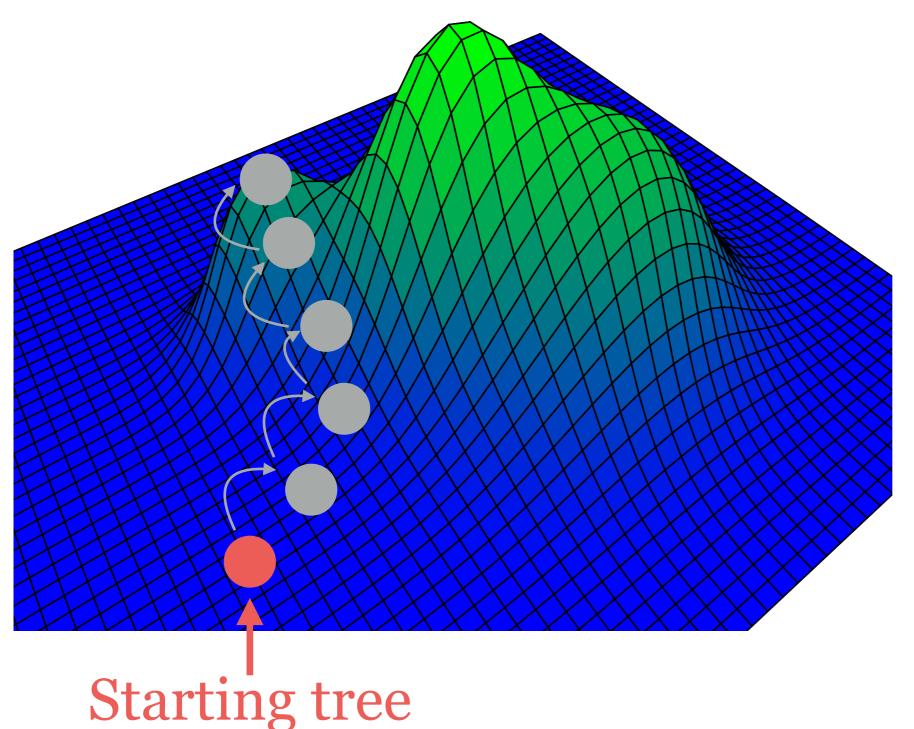
Nearest Neighbor Interchange (NNI)
Subtree Pruning and Regrafting (SPR)
Tree Bisection and Reconnection (TBR)



## Four things affecting performance:

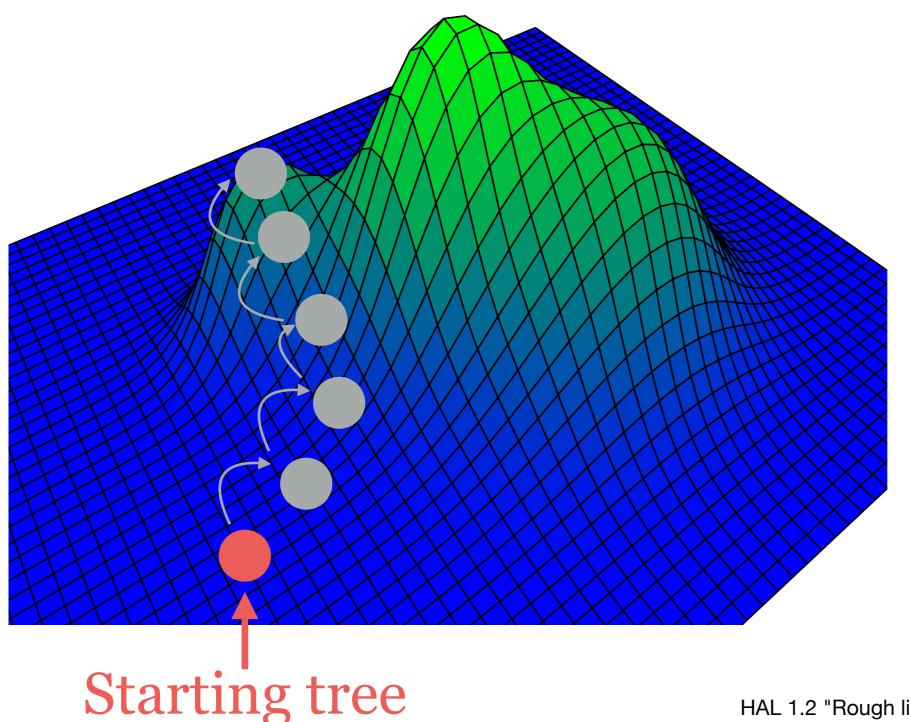
- Starting tree
- Model chosen
- Data
- Convergence





## Four things affecting performance:

- Starting tree
  - Affects optimization
  - Get stuck on poor likelihood region
  - Bad starting tree?
    - Best case: slows down
    - Worst case: suboptimal tree Model chosen
  - Affects shape of the surface we optimize
  - You might be optimizing the wrong function
  - Identifiability
- Data
- Convergence

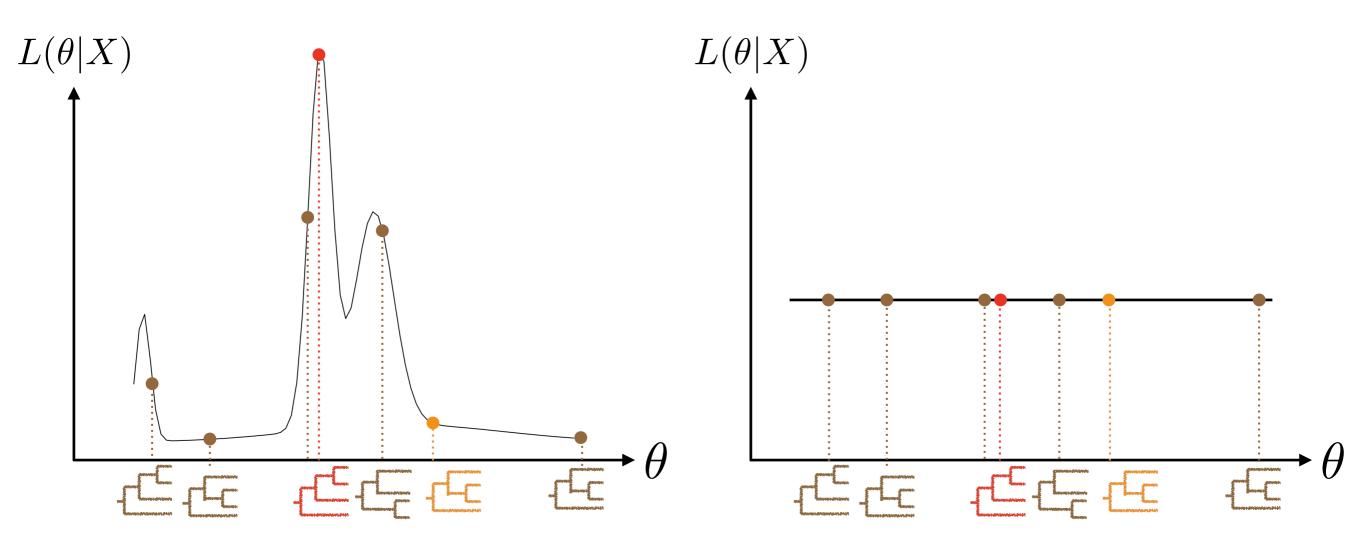


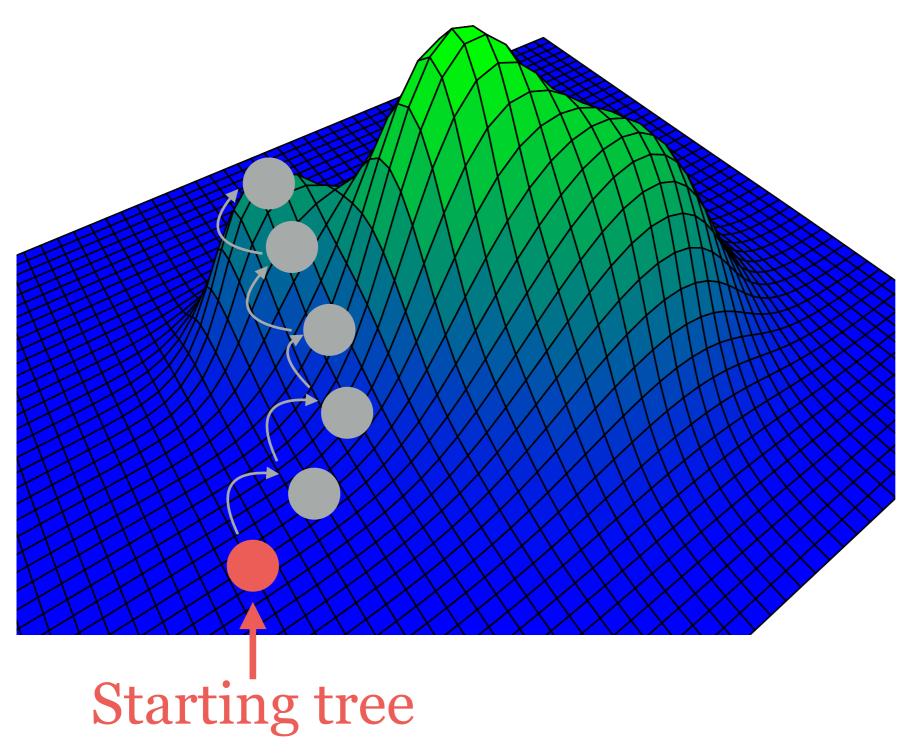
## Four things affecting performance:

- Starting tree
  - Affects optimization
  - Get stuck on poor likelihood region
  - Bad starting tree?
    - Best case: slows down
    - Worst case: suboptimal tree
- Model chosen
  - Affects shape of the surface we optimize
  - You might be optimizing the wrong function
  - Identifiability
- Data
- Convergence

HAL 1.2 "Rough likelihood surface: when analyzing datasets with comparatively few sites and a large number of taxa. The key challenge with such datasets is that 100 distinct ML searches are likely to yield 100 topologically substantially different, but statistically indistinguishable trees."

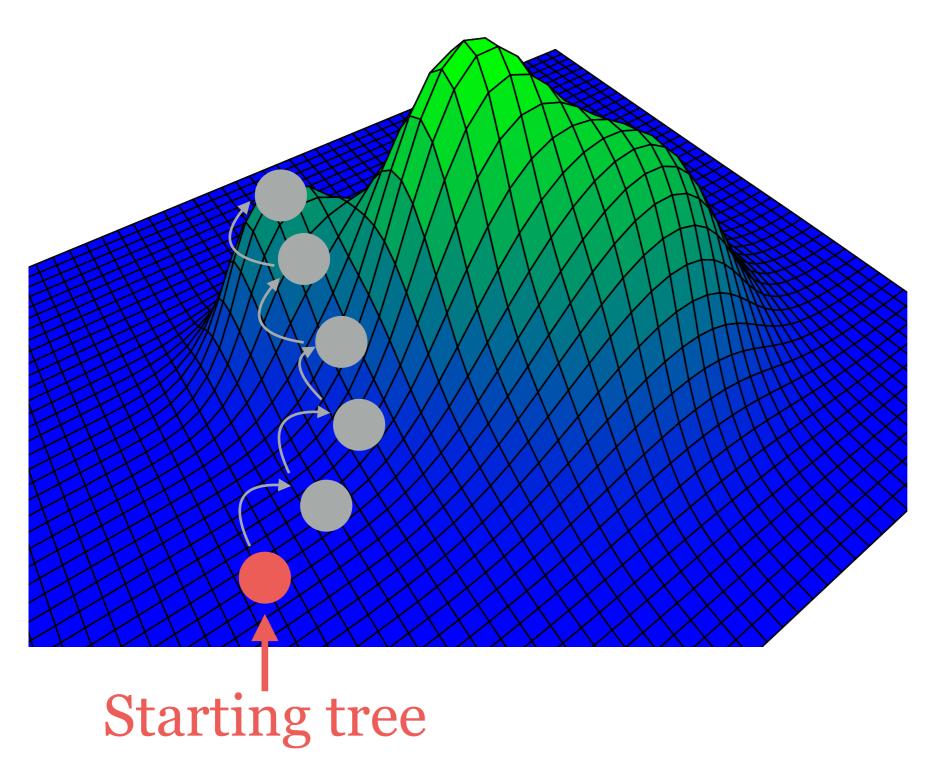
# Identifiability





## Four things affecting performance:

- Starting tree
  - Affects optimization
  - Get stuck on poor likelihood region
  - Bad starting tree?
    - Best case: slows down
    - Worst case: suboptimal tree
- Model chosen
  - Affects shape of the surface we optimize
  - You might be optimizing the wrong function
  - Identifiability
- ▶ Data
  - Lack of signal (sample size or poorly chosen region)
  - Difference between data and information
  - Identifiability
- Convergence



## Four things affecting performance:

#### Starting tree

- Affects optimization
- Get stuck on poor likelihood region
- Bad starting tree?
  - Best case: slows down
  - Worst case: suboptimal tree

#### Model chosen

- Affects shape of the surface we optimize
- You might be optimizing the wrong function
- Identifiability

#### ▶ Data

- Lack of signal (sample size or poorly chosen region)
- Difference between data and information
- Identifiability

#### Convergence

- When do you stop the traversal of tree space?
- Affects optimization

# Statistical Consistency

- Maximum likelihood (and Bayesian), neighbor joining, ME
   OLS are all statistically consistent methods
- UPGMA and maximum parsimony are not statistically consistent methods

# For next class:

- We will go over IQ-Tree and RAxML
- Each student is assigned to one software and has to read two papers for that software (software papers are short: two papers are fewer than 9 pages combined)
- Focus on the 4 things affecting performance: starting tree, model chosen, data, convergence
- We will have a class discussion followed by installing and using the software