

Problem 1

We need to show that a Fibonacci heap contains one tree with a linear chain of  $n$  nodes that can be created from a sequence of Fibonacci heap operation.

$$F_h \rightarrow \text{Fibonacci heap}$$

Creating an algorithm for Fibonacci heap that comprises of only one tree with  $(n-1)$  nodes, starting with empty  $F_h$ . After that one more node is added.

Creating a Fibonacci heap with the height of one with the root key  $R$ , such that  $R$  is the value of Root mode. Now we are adding the nodes with the following keys:  $R-1$  (a value less than the current root's value),  $R+1$  (a value greater than the current root's value) and  $R-2$  (a value which is twice less than the current root's value).

~~Finally remove~~ We need to remove the node  $\text{Key}[R-2]$ .

# Assumption: Number of node should be greater than two.

Linear-heap ( $F_h, R, m$ )

|| Starting with empty  $F_h$

Linear-heap ( $F_h, R+1, m-1$ )

|| Adding a node with a value greater than the current root's value.

Insert ( $F_h, \min(F_h) + 1$ )

|| Adding a node with a value lesser than the current root's minimum value.

Insert ( $F_h, \min(F_h) - 1$ )

|| Adding a node with value twice less than the current root's minimum value

Insert ( $F_h, \min(F_h) - 2$ )

|| Deleting the node with minimum key from the  $F_h$

Delete  $\min(F_h)$

|| Assigning the minimum node's child node to the variable b

$b = \min(F_h)$ . second child

II Decreasing the node's key value by two

Decrease key ( $b, \min(F_h) - 2$ )

Delete  $\min(F_h)$

return

### Proof of correctness

Hypothesis is correct for  $n=1$  as the Fibonacci heap contains one tree with a linear chain of  $n$  nodes.

### Inductive Process

Let us say above demonstration holds for  $n=k$ , now for  $n=k+1$ , the pseudocode creates a linear chain containing  $k$  nodes.

After addition of two child node  $M$  which has a key less than minimum key and one child node  $y$  which has a key greater than minimum key. It adds node  $R$  such that this node's key is smaller than minimum key.

When R is deleted then there remain the chain of the K nodes containing x and y. Since x and y is having zero degree so nodes are joined, then the chain having two element is obtained such that x becomes the root with the degree one.

The chain having height two and other chain with height K are combined.

Hence by removing the node 'y' gives linear chain with n nodes.

## Problem 2

We are assuming that we can print each member of the set in  $O(1)$  time. Here we are going to use circular singly linked list for nodes of each set. We need to iterate circular singly linked list ~~in which the~~ to print all the members of  $n$  where the set is stored until ~~we are~~ same node is occurring.

Pseudo code for Make-set, Union, find-set and print-set are as follows  $\Rightarrow$

### Make-set ( $n$ )

1.  $n.p = 0$
2.  $n.rank = 0$

### Union ( $n, y$ )

1. Link (Find-set ( $n$ ), Find-set ( $y$ ))

### Link ( $n, y$ )

1.  $n.next = y.next$
2.  $y.next = n.next$
3. if ( $n.rank > y.rank$ )  
    4.      $y.p = n$   
5. else      $x.p = y$

6. if  $x.rank = y.rank$
7.  $y.rank = y.rank + 1$

### Find-set ( $n$ )

1. if  $n.p = n$
2.  $n.p = \text{Find-set}(n.p)$
3. return  $n.p$

~~Point~~

### Point-Set ( $n$ )

1. ~~temp =~~   $n$
2.  $\text{point}(n)$
3. while  $\text{temp}.next \neq \text{empty}$   $n$
4. ~~temp.next~~  
 $\text{temp} = \text{temp}.next$
5.  $\text{point}(n)$

Point function is having time complexity of  $O(n)$ .

In the beginning ~~we~~ it is assumed by us that to point each member of set we need  $O(1)$  time. Here we have  $n$  number of ~~no~~ nodes in a set so while iterating  $n$  times to circular linked list time bound to our point set function is  $O(n)$ . (Proved)

### Problem 3

We are going to use accounting method to prove time bound  $O(m)$ , following credits can be assigned to given operations.

$\text{Make-Set}(i) \rightarrow$  We can assign two credits.

For make-set operation we can assign one credit and another one credit can be assigned for when a particular node appears on a find-path for the first time and is turned into child of a root.

$\text{Union}(S_i, S_j) \rightarrow$  We can assign one credit. One credit is used for ~~linkage~~ linking one node to others in union operation.

$\text{Find}(i) \rightarrow$  We can assign one credit. This operation implements the path compression heuristic. It is two pass method as it recurses, it makes one pass up the find path to find root and as the recursion unwinds, it updates each node on the path to point directly to the root. One credit is used for visiting root node and its child and path compression of these two nodes during find set operation. All other nodes on the find path

Can use one credit to visit and path compression.

All nodes on find path becomes children of a root so if they are visited during subsequent find-set, the operation pays for itself.

From above observations we can conclude for  $m$  operations maximum charged amount will be  $2m$  as for each operation either one or two credit is payed. For union by rank, argument is not required for above argument.

Hence, it is proved that  $O(m)$  is the time bound for sequence of  $m$  operation.

For  $q$  such Find-set operation takes time  $O(q+m)$ , where  $m$  is the total number of elements.

### Problem 4

Let us consider a node ( $n$ ) is having two children i.e. its predecessor ( $p$ ) and its successor ( $s$ ). our aim is to show that the successor of  $n$  has no left child. This can be proved by contradiction. Let us assume that  $s$  has left child, then the key  $s$  is greater than that of  $\text{left}[s]$ . the key of  $s$  is also larger than the key of  $n$ , and since  $s$  has a left child the key of  $\text{left}[s]$  is larger than that of  $n$ . thus we can write as below,

∴  $\text{key}[s] \geq \text{key}[\text{left}[s]] \geq \text{key}[m]$  since  $s$

which is a contradiction, since  $s$  is the successor of  $m$ . Hence the predecessor of  $n$  has no left child.

no left child.  
 Likewise, we can show that the predecessor  
 of  $m$  has no right child by contradiction.  
 Let us say  $p$  has a right child and  
 the key of  $p$  is less than that of  
 right  $[p]$ . The key of  $p$  is less than that  
 of right  $[p]$ . The key of  $p$  is less than that of  
 since  $p$  has a right child the key  
 of right  $[p]$  is less than that of  $m$ .  
 $\text{right } [p] \subseteq \text{key } [m]$

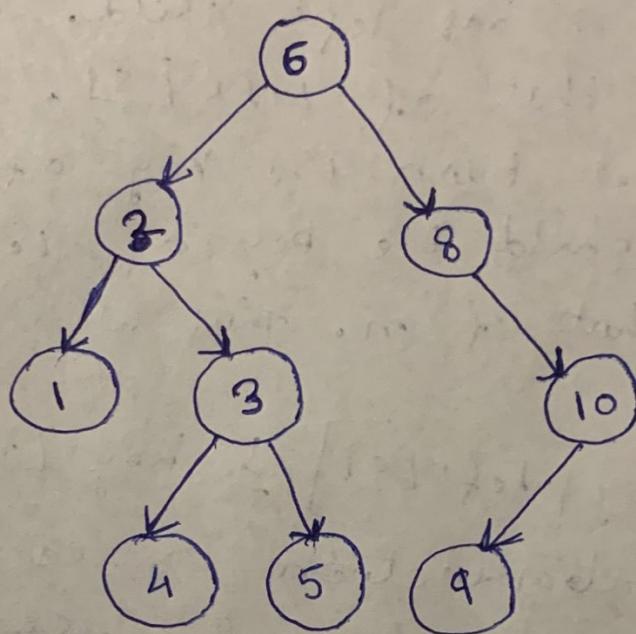
of night [n] is less than  
 thus  $\text{key}[n] \leftarrow \text{key}[\text{night}]$  since n is the  
 first letter.

Thus  $\text{key}[P] \leq \text{key}[L]$   
 which is a contradiction, since  $P$  is the

predecessor of  $n$ . Hence the predecessor of  $n$  has no right child.

Eg

Binary search Tree  $\Rightarrow$



Here 5 is predecessor of  $n$  i.e. 6 and it is not having right child.

Here 8 is successor of  $n$  i.e. 6 and it is not having left child.

# College of Science Academic Integrity Pledge

## Expectations

IIT requires instructors, teaching assistants, and students to maintain the highest standards of academic integrity and honesty. As a student, I will commit to academic integrity by adhering to the following requirements:

- I will ensure that all work I do is solely my own, and will collaborate with others only as is allowed in the course.
- I will make use of external resources only when they are permitted.
- I will properly give credit to any sources I make use of in my work, and will take credit only for work that I have personally produced.
- I will hold other students accountable to do the same.

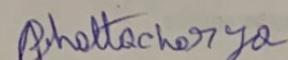
During exams:

- I will not use any additional materials other than pen, pencil, or eraser, unless specifically allowed by the instructor.
- I will not look at another student's paper during the exam, or allow another student to look at mine.
- I will not communicate with anyone other than the TA or instructor during the exam.

## Violations

Cheating, plagiarism, and dishonesty will not be tolerated. In the event that a violation of this policy comes to the attention of the instructor, the incident will be reported to [academichonesty@iit.edu](mailto:academichonesty@iit.edu). According to the campus *Code of Academic Honesty*, a first incident may result in a zero for the assignment, and a second incident may result in failure for the course.

[http://www.iit.edu/student\\_affairs/handbook/information\\_and\\_regulations/code\\_of\\_academic\\_honesty.shtml](http://www.iit.edu/student_affairs/handbook/information_and_regulations/code_of_academic_honesty.shtml)



Signature

I have read and understood this policy.

Name Armitadee Prosad Bhattacharya Date 3/7/19

## I. Code of Academic Honesty

With respect to matters covered by this Article I, students enrolled in or otherwise attending programs of IIT's Chicago-Kent College of Law, and only such students, are subject to the policies, procedures and provisions of the IIT Chicago-Kent College of Law Student Handbook (<http://www.kentlaw.edu/depts/acadadm/handbook.htm>), and all such students should refer to the IIT Chicago-Kent College of Law Student Handbook for policies, procedures and provisions applicable to them.

### A. Code

IIT expects students to maintain high standards of academic integrity. Students preparing for the practice of a profession are expected to conform to a code of integrity and ethical standards commensurate with the high expectations society places upon the practitioners of a learned profession. No student may seek to gain an unfair advantage over another.

It shall be a violation of this Code for a student to engage in conduct that violates the established standards of his or her major academic discipline, the established standards of the academic discipline in which she or he is engaged, the established standards of the profession of which she or he is training, or the standards of IIT set forth herein.

In addition, it is a violation of this Code for a student, whether or not currently enrolled at IIT, to knowingly engage or attempt to engage in the following:

- The misrepresentation of any work submitted for credit or otherwise as the product of a student's sole independent effort, such as using the ideas of others without attribution and other forms of plagiarism;
- The use of any unauthorized assistance in taking quizzes, tests or examinations;
- The acquisition, without permission, of tests, answers sheets, problem solutions or other academic material when such material has been withheld from distribution by the instructor;
- Deliberate and harmful obstruction of the studies, research or academic work of any member of the IIT community;
- Making material misrepresentation in any submission to or through any office of the University to a potential employer, professional society, meeting or organization; or
- The intentional assistance of others in the violation of the standards set forth in this Code.

### B. Academic Discipline

Any member of the IIT community who is aware of a violation of the IIT Code of Academic Honesty, or who has evidence that a violation has occurred, is urged to inform the appropriate course instructor, academic unit head or dean or send an email to [academichonesty@iit.edu](mailto:academichonesty@iit.edu). Faculty members or administrators who are aware of a violation, or who have good evidence of a violation, must inform the Chair of the Academic Honesty Committee for the appropriate academic unit and the Designated Dean for Academic Discipline ("DDAD"). The appropriate academic unit is the unit responsible for the course in which the alleged academic honesty violation occurred.

For the Main Campus, Rice Campus, Moffett and Institute of Design the DDAD is either the Vice Provost for Undergraduate Affairs or the Associate Dean for Graduate Academic Affairs, as appropriate given the status of the student. For Chicago-Kent College of Law, the DDAD is the Assistant Dean of Students, and for the Stuart School of Business it is the Dean.

The DDAD will provide a record of all incidents to the Office of Student Affairs. A student who believes that his or her record is factually inaccurate should inform the Dean of Students, who will investigate, as he or she deems appropriate, and, if he or she determines necessary, in his or her sole discretion, will correct any factual inaccuracies in the record. The decision of the Dean of Students as to such matters shall be final.

If a violation concerns conduct relating to coursework, the course instructor may meet with the student and impose one of the sanctions below if after the meeting the instructor has satisfied himself or herself that a violation has in fact occurred. The meeting may be held in consultation with the academic unit head, or with the Academic Honesty Committee of the academic unit. The course instructor will report the violation, a summary of the facts evidencing the violation and the sanction to the DDAD. Appropriate sanctions include:

- **Expulsion from a course.** The student is assigned a punitive failing grade of 'E' for the course and can no longer participate in the course or receive evaluation of coursework from the instructor.
- **Reduction in grade.** A reduction in grade for the assignment or exam involved or for the course may be applied.

Upon receipt of information about a violation of the Code, the DDAD will review the report and any record of prior violation of the Code by the student. If there are one or more prior violations, the DDAD will consult with the Chair of the Academic Grievance Committee of the University Faculty Council to determine whether the matter should be referred to a hearing before the Academic Grievance Committee for further sanctions. The DADD's decision to refer a matter to the Academic Grievance Committee shall be made in his or her sole discretion and shall be final. If the matter is referred for a hearing, the Academic Grievance Committee shall supplement its membership as necessary so that the Committee includes at least one faculty member from the Academic Honesty Committee of the academic unit where the violation occurred, one member of the student's major faculty, one other faculty member, two students and the Dean of Students or his or her designee. The Academic Grievance Committee so supplemented will form a disciplinary committee for the purpose of investigating the matter and making findings and a recommendation to the DDAD. The chair of the Academic Grievance Committee shall chair this disciplinary committee.

A student who is to appear before such a disciplinary committee shall be notified in writing by the Dean of Students of the charges, in summary fashion, placed against him or her and the time and place of the hearing. This notice shall be delivered to the student at least five days before the hearing. A student appearing before the disciplinary committee has the right to be accompanied by an advisor, witnesses on his or her behalf, and his or her parents. The advisor is limited to advising the student and may not participate in presenting the case, questioning witnesses, or making statements during the hearing. A student shall have the right to make an oral statement both at the start and the conclusion of the hearing and to submit written evidence to the committee. Further, as a general rule, a student shall have the right (i) to present and to question any witnesses of his or her choosing that have information relevant to the charges against him or her, provided that the chair may, in his or her sole discretion, disallow witnesses whose testimony would be redundant or not germane to the charges; and (ii) to cross-examine any witness that is called to testify in support of the charges, provided that the chair may, in his discretion, limit such cross-examination to the extent it is not germane to the charges, is redundant or becomes abusive or harassing. Members of the committee may, as each deems appropriate, ask questions of any witness called or regarding any evidence submitted. To the extent deemed necessary

to maintain decorum or to protect students from harassment or to ensure the integrity of the process, the chair may require a student to direct questions to the chair who will then ask them of a witness or witnesses.

An audio tape recording of the hearing will be made. The audio tape will remain the sole property of the University. No other record of the hearing may be made.

Once proper notification has been given, the University reserves the right to hold the hearing whether or not the student elects to participate. Email correspondence will be considered sufficient written notification in all instances where written notification is required.

Upon receipt of the findings of the disciplinary committee, which findings may include recommended sanctions, the DDAD shall determine the appropriate action to be taken and shall so notify the student. The disciplinary committee may recommend, and the DDAD may impose, any of the following sanctions:

- **Expulsion from a course.** The student is assigned a punitive failing grade of 'E' for the course and can no longer participate in the course or receive evaluation of coursework from the instructor.
- **Suspension.** Suspension is a status assigned for various periods of time in which a student's enrollment is interrupted. A suspended student may not attend day or evening classes, participate in student activities, or live in campus housing. A suspended student may apply for reinstatement at the end of the period of suspension. If reinstated, the student may be placed on disciplinary probation for a period of time designated by the DDAD.
- **Expulsion.** Expulsion is the complete severance of association with the University. Notation of the violation of the Code is made on the student's transcript.

In any matter where the DDAD's determination is to impose a sanction of suspension or expulsion, the DDAD's determination shall automatically be stayed and the matter referred to the Provost for review. With respect to such a proposed determination by the DDAD, the Provost may make any of the determinations set forth under the Appeals Procedures heading immediately following. Once the Provost's review has been completed, the DDAD's determination, as it may have been modified by the Provost, shall become effective. Notwithstanding any other provision of this Student Handbook, no matter so referred to the Provost shall be subject to any further appeals on the basis that the sanction imposed was inappropriate to the offense.

### C. Appeal Procedures

An appeal of a decision on academic honesty must be submitted in writing to the Office of Student Affairs within five business days of notification of the decision. Supporting information must be submitted with the appeal. An appeal or submission made after this deadline will not be considered. Decisions rendered by the DDAD without referral to the University Faculty Council's Academic Grievance Committee and sanctions, excluding non-punitive grades, imposed by a course instructor may be appealed to the Academic Grievance Committee, which in the latter instance only may either affirm or overturn the course instructor's finding of academic dishonesty. Upon such an appeal, the Academic Grievance Committee will supplement its membership to form a disciplinary committee that is composed as described above and that follows hearing procedures as described above.

Decisions of the DDAD following a disciplinary committee hearing and decisions of a disciplinary committee hearing upholding a course instructor's finding of academic dishonesty may be appealed to the Provost, whose decision shall be final. An appeal to the Provost is limited to the following reasons:

- Appropriate procedures were not followed;
- The sanction imposed was inappropriate for the offense; and
- New evidence that was not available at the time of the original decision, not due to the fault of the student, has become available.

The Provost may make one of the following determinations:

- Uphold the decision and the sanction;
- Reverse the decision and the sanction; or
- Uphold the decision, but return the matter to the DDAD to reconsider the sanction.

Last modified: April 29, 2014