

* Probability Distribution

Type of Pro. Dist.

① Discrete probability Dist.

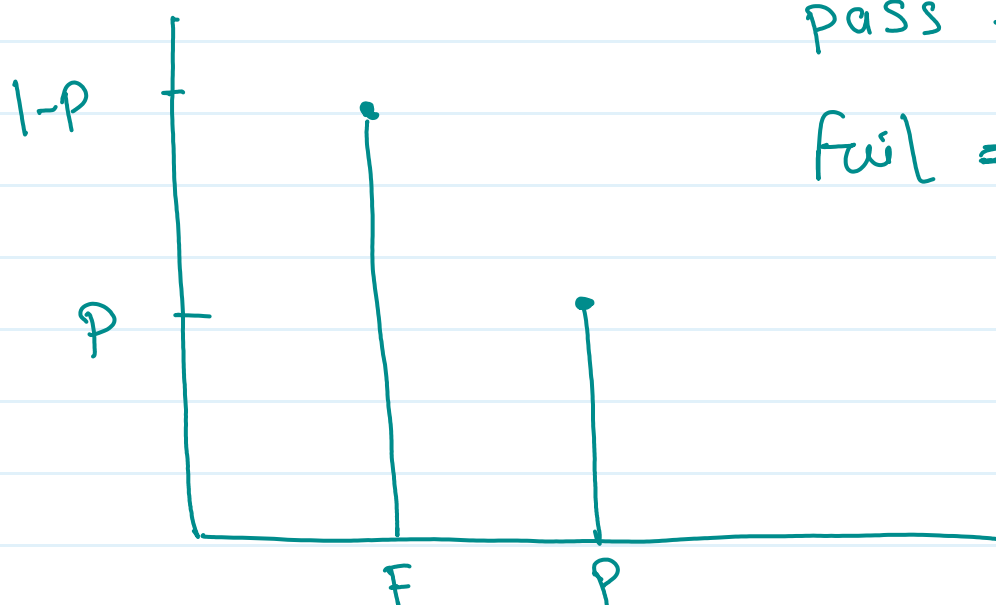
② Continuous probability Dist.

① Discrete probability Distribution

① Bernoulli Dist. -

experiment - single time

Result - fix



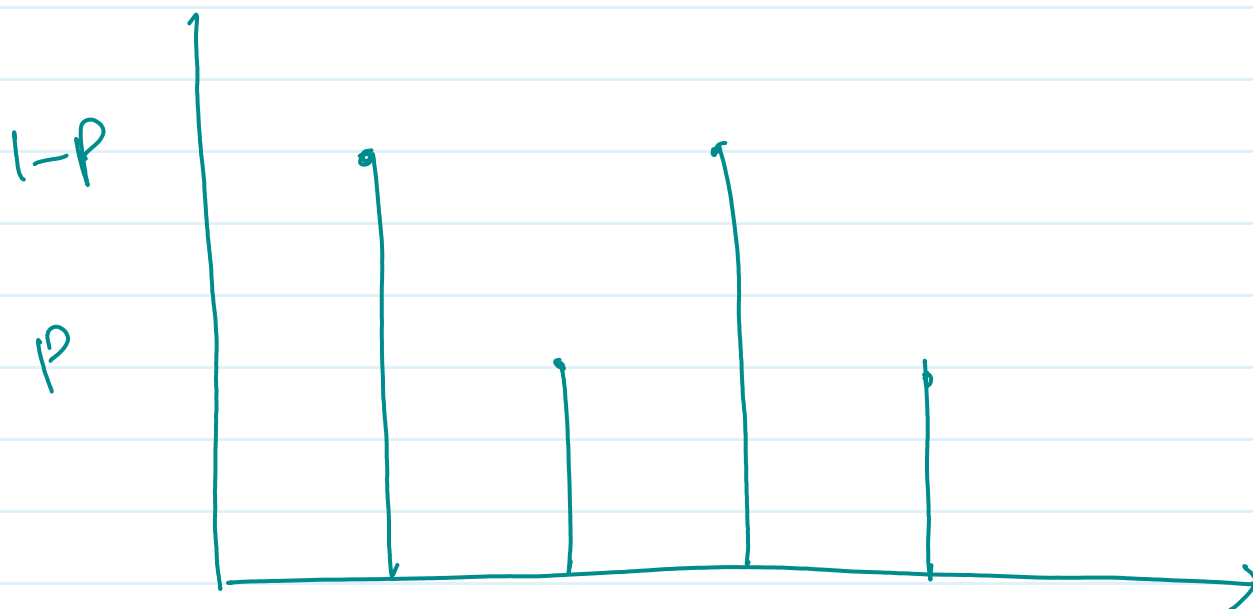
pass = p

fail = $1-p$

⑥ Binomial Distribution:-

experiment = fix no. of times

Result = fix



$$P(X=r) = {}^n C_r (p)^r (1-p)^{n-r}$$

$${}^n C_r = \frac{n!}{(r!(n-r)!)}$$

n = no. of trials

p = prob success in 1 trial

r = no. of success of n trial.

eg:- total no of trials $n=4$ prob.
getting a red ball 1 trials $p=0.6$.

$$\text{Sol}^n \Rightarrow P(X=r) = {}^4C_r (0.6)^r (0.4)^{4-r}$$

$$P(X=0) = {}^4C_0 (0.6)^0 (0.4)^{4-0} = 0.0256$$

$$P(X=1) = {}^4C_1 (0.6)^1 (0.4)^3 = \underline{0.1536}$$

© Poisson Distribution:-

Poisson distribution is used to model the number of events that occur in a fixed interval of time or space, given the average rate of occurrence, assuming that the events happen independently and at a constant rate.

It deals with **discrete random variables**, meaning the number of events can only take on non-negative integer values (0, 1, 2, 3,...). Each event is considered to be independent of others and they are assumed to occur at a constant average rate (λ) over the given interval.

$$P(X=k) = \frac{e^{-\lambda} \lambda^k}{k!}$$

$\lambda = \text{Average.}$ $e = 2.718$

Egⁿ. In a hospital Avg¹⁴ call received in a single day. What is the probability to receive 7 calls in a day.

Solⁿ \Rightarrow

$$k = 7$$

$$\lambda = 14$$

$$= \frac{e^{-14} 14^7}{7!}$$

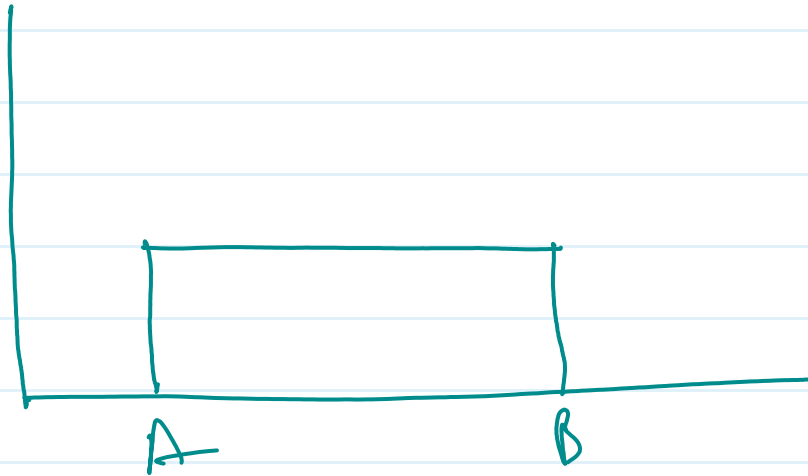
$$P(X=7) = \frac{(8.31 \times 10^{-7}) \times 105413504}{5040}$$

$$= 0.017/100$$

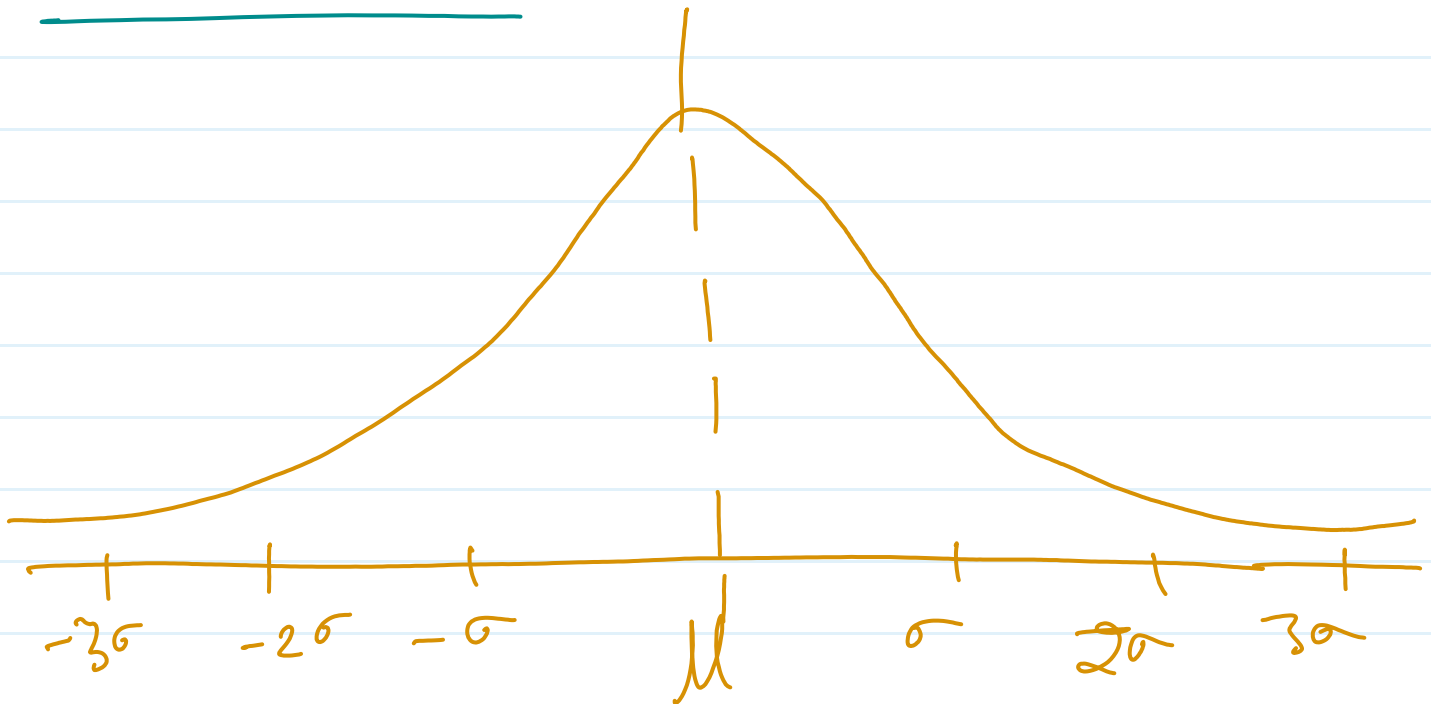
$$\Rightarrow \underline{\underline{1.7\%}}$$

② Continuous probability Dist.

① Uniform Dist. :-



② Normal Dist. -



© standard normal Dist. -

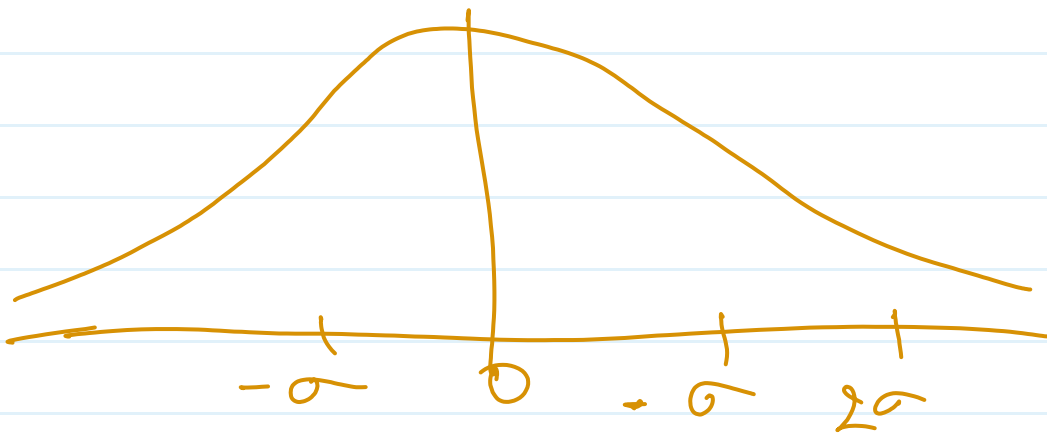
$$\mu = 0$$

$$SD = 1$$

nor. to SD. nor

Z-score formula.

$$Z = \frac{X_i - \mu}{\sigma}$$



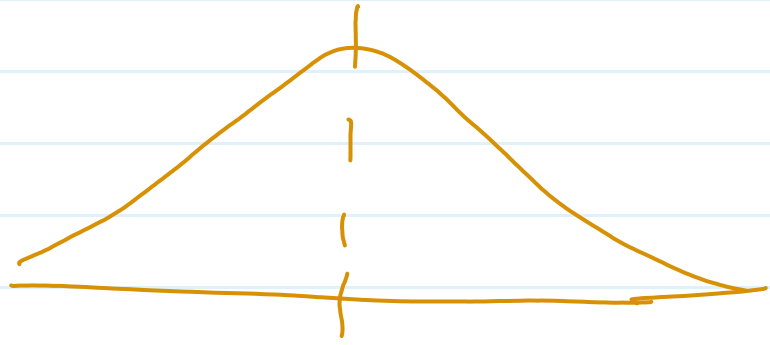
eg:- [1, 2, 3, 4, 5, 6, 7]

$$\mu = 4$$

$$\sigma = 1$$

$$x_i - \mu$$

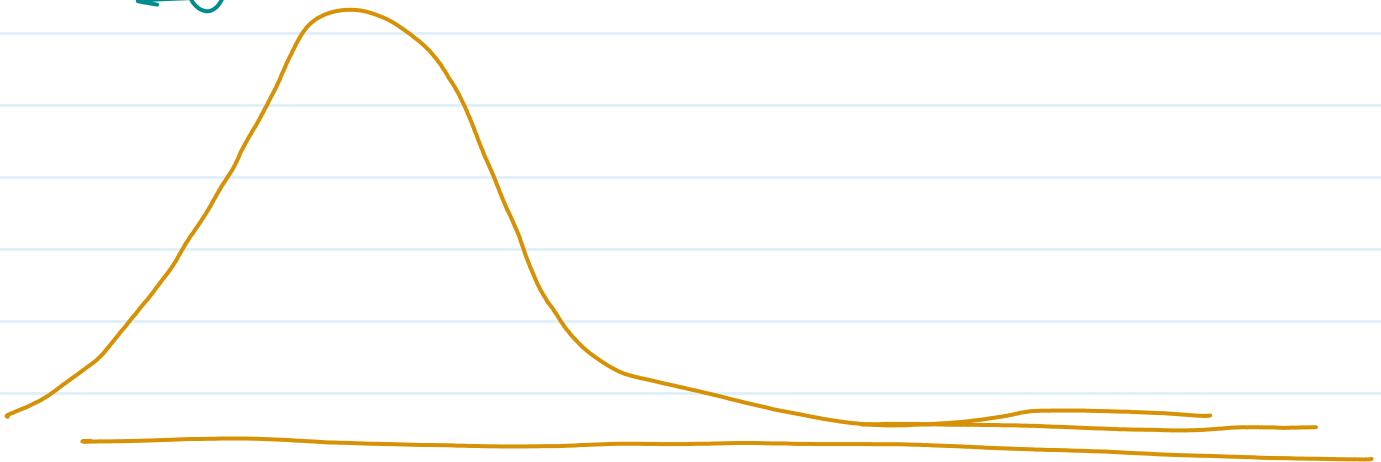
$$\left. \begin{array}{rcl} 1-4 & = & -3 \\ 2-4 & = & -2 \\ 3-4 & = & -1 \\ 4-4 & = & 0 \\ 5-4 & = & 1 \\ 6-4 & = & 2 \\ 7-4 & = & 3 \end{array} \right\}$$



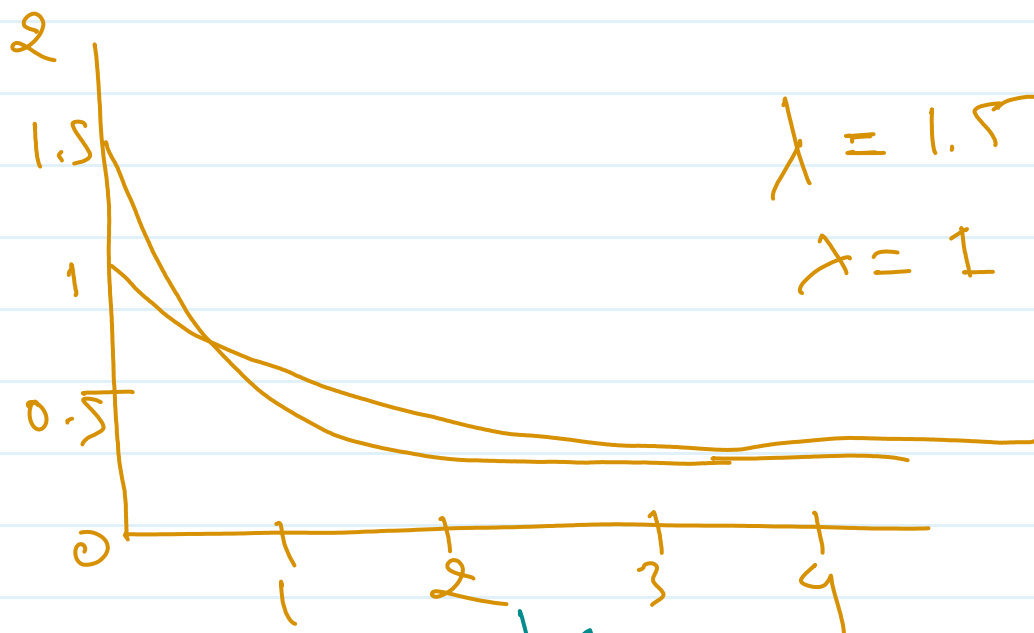
$$\mu = 0$$

$$SD = 1$$

① log Normal Dist



e) exponential Dist.



$$f(x) = \lambda e^{-\lambda x}$$