

* VIF (variance inflation Factor)

Independent variable should not depend on each other

$$VIF = \frac{1}{1 - R^2}$$

* Regularisation

L_1 Lasso

L_2 Ridge

Elasticnet Regularisation

(i) L_1 Lasso

When we have multiple features in data and want to reduce some unrelated features from data while training algorithms.

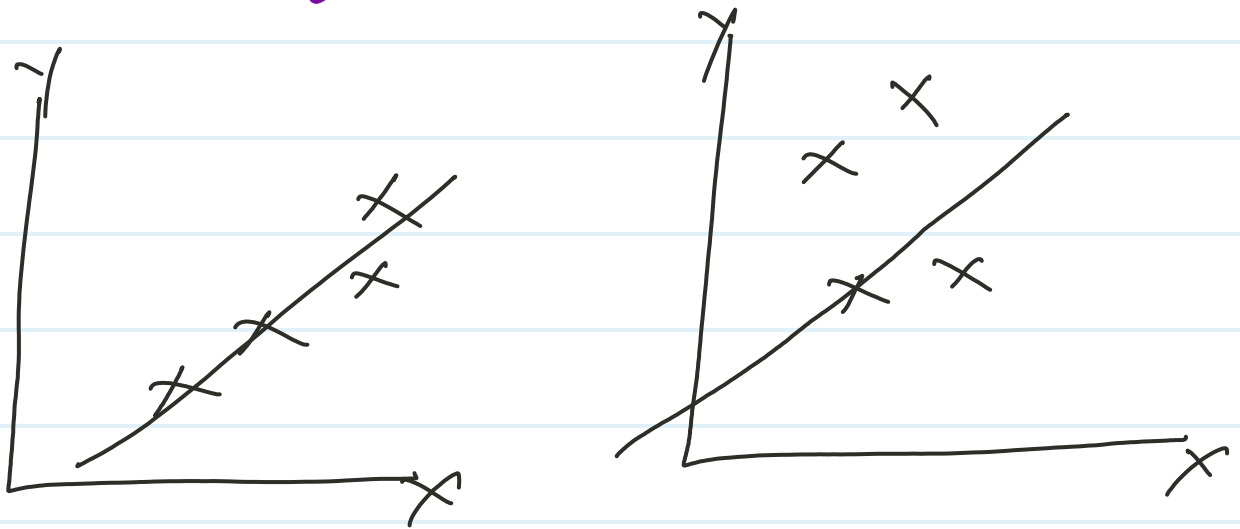
$$x_1 \quad x_2 \quad x_3 \quad x_4 \quad x_5 \quad x_6 \quad x_7 \quad x_8 \quad y$$

$$\Rightarrow \frac{1}{N} \sum_{i=1}^N [h_{\theta}(x^i) - y^i] + \lambda |\text{slope}|$$

$$\begin{aligned} h_{\theta}(x) &= \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3 + \theta_4 x_4 \\ &= \theta_0 + 0.54x_1 + 0.25x_2 + 0.01x_3 + 0.10x_4 \end{aligned}$$

* L₂ Ridge Regularisation

To maintain overfitting and underfitting of model



$$L_2 = \frac{1}{n} \sum_{i=1}^n [h_{\theta}(x^i) - y^i]^2 + \lambda (\text{slop})^2$$

Relationship of λ and slop is inversely proportion.

$$\lambda \uparrow \quad \text{slop} \downarrow \odot$$

$$\lambda \downarrow \quad \text{slop} \uparrow \ominus$$

* Elastic net Regularisation

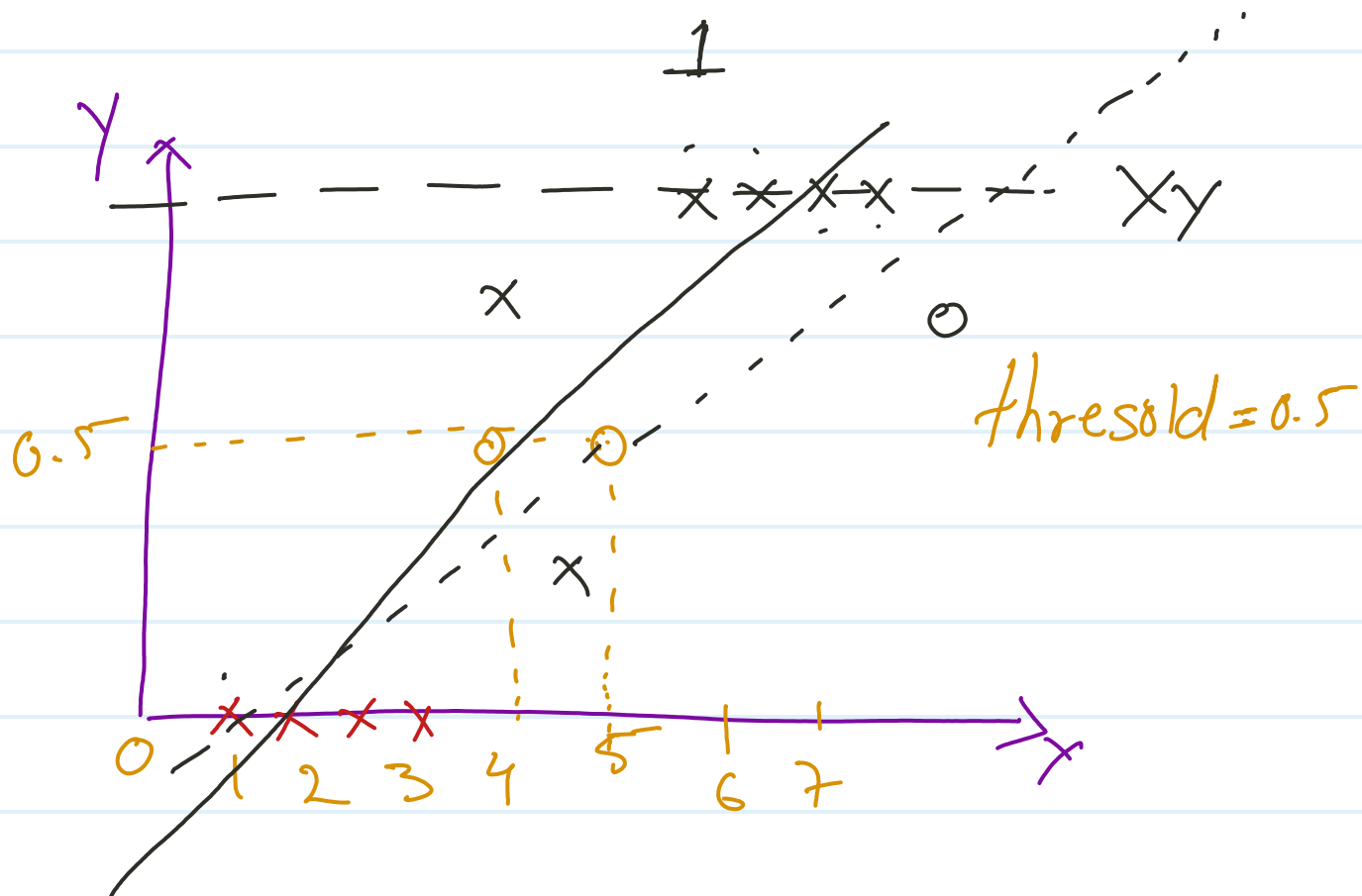
Combination of L_1 and L_2

$$EN = \frac{1}{n} \sum_{i=1}^n [h_{\theta}(x^i) - y^i]^2 + \lambda (\text{slop})^2 + \lambda |\text{slop}|$$

overfitting = low bias
High variance

underfitting = High variance / low variance
= High bias

* Logistic Regression



Binary classification

$$Z = h_{\theta}(x) = \theta_0 + \theta_1 x_1$$

$$\text{Sigmoid Function} = \frac{1}{1 + e^{-Z}}$$

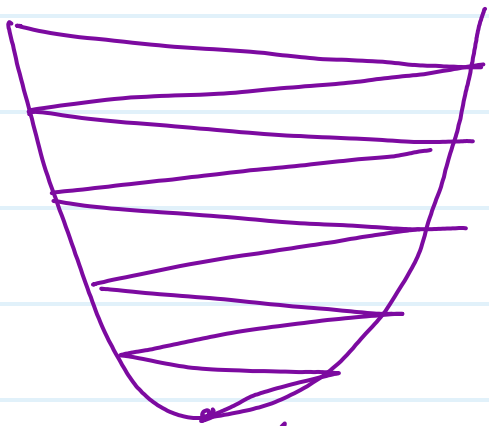
Cost function (convex function)

$$J(\theta_0, \theta_1) = \frac{1}{n} \sum_{i=1}^n (h_{\theta}(x^i) - y^i)^2$$

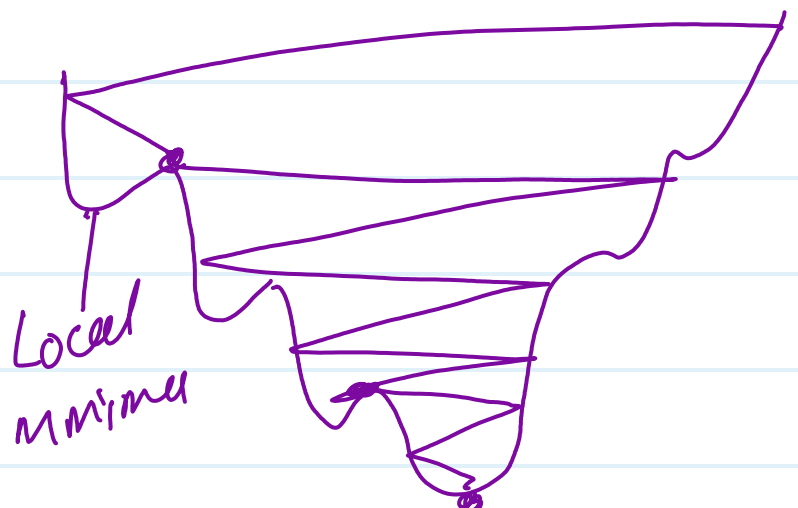
$$h_{\theta}(x) = \sigma(\theta_0 + \theta_1 x)$$

$$\sigma = \frac{1}{1 + e^{-z}}$$

$$\frac{1}{1 + e^{-z}} = \frac{1}{1 + e^{-(\theta_0 + \theta_1 x)}}$$



global minimum



global minimum

cost function of logistic regression

$$J(\theta) = \frac{1}{N} \sum_{i=1}^N \text{cost}(h_{\theta}(x), y)$$

★ Repeat conversion theorem

$$\{ J=0 \text{ and } 1 \}$$

$$\theta_j = \theta_j - \alpha \frac{d}{d\theta_j} \cdot J(\theta_0, \theta_1)$$

α = learning rate

★ logistic Regression - Binary class

★ Sigmoid function

$$\sigma = \frac{1}{1 + e^{-z}}$$