

Random variable

$$X = 10 \sim$$

$$Y = \text{Pass} \sim$$

age	weight	height	
X_1	X_2	X_3	Y
1	—		
1	—		
1	—		
1	—		

$$X \approx Y$$

Random variable

$$X = \text{Coin (Toss)}$$

$$X = T/H$$

$$X = \text{Dice}$$

$$X = 1/2/3/4/5/6$$

Type of Random variable

1

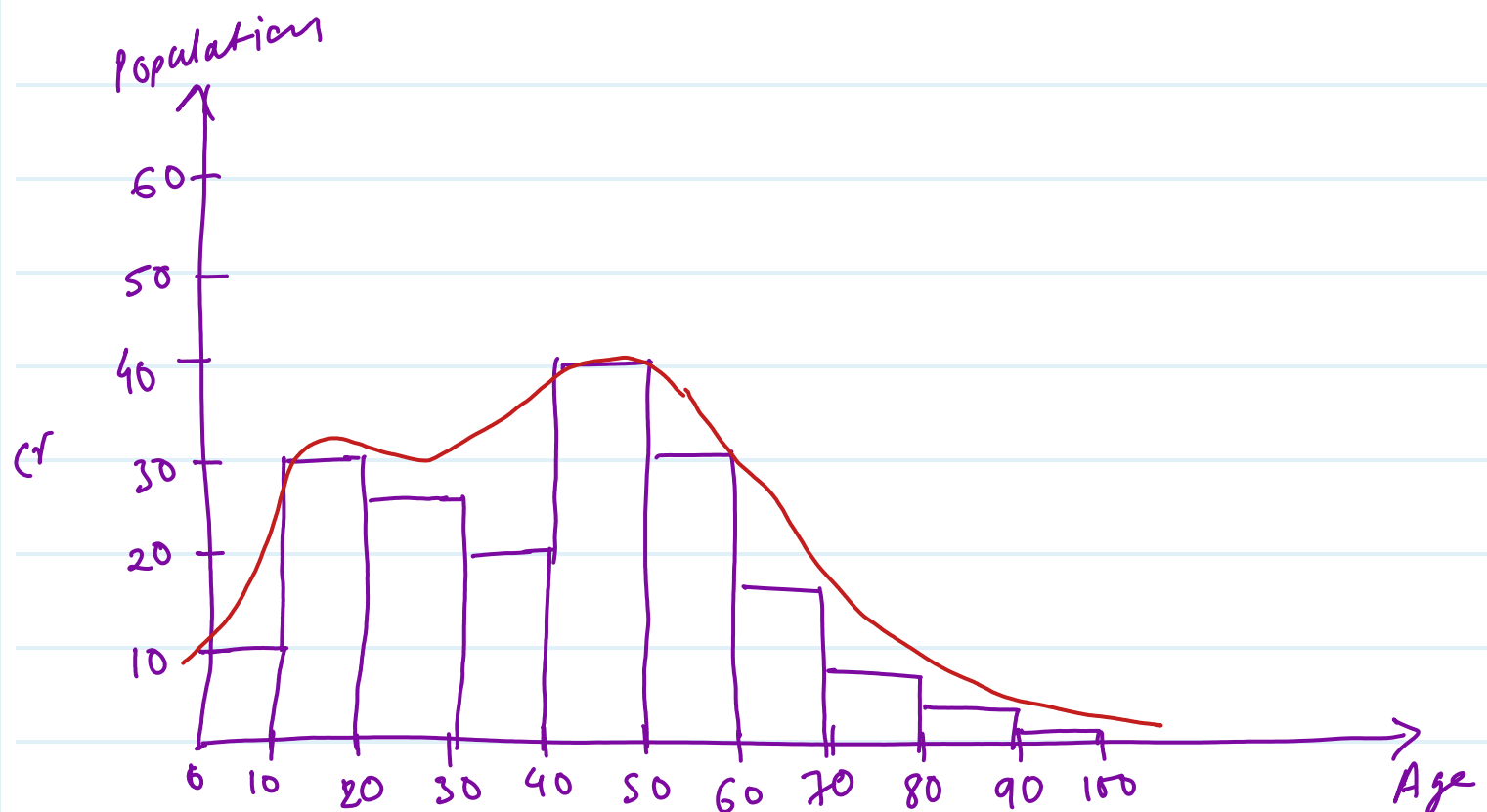
Discrete random variable

Continuous Random variable

$X_1 = \text{Gender}$
 $= M/F/T$

$X_1 = \text{Rain}$
 $(1\text{mm}, 6.5\text{mm})$

$X_2 = \text{Result}$
 (P/F)

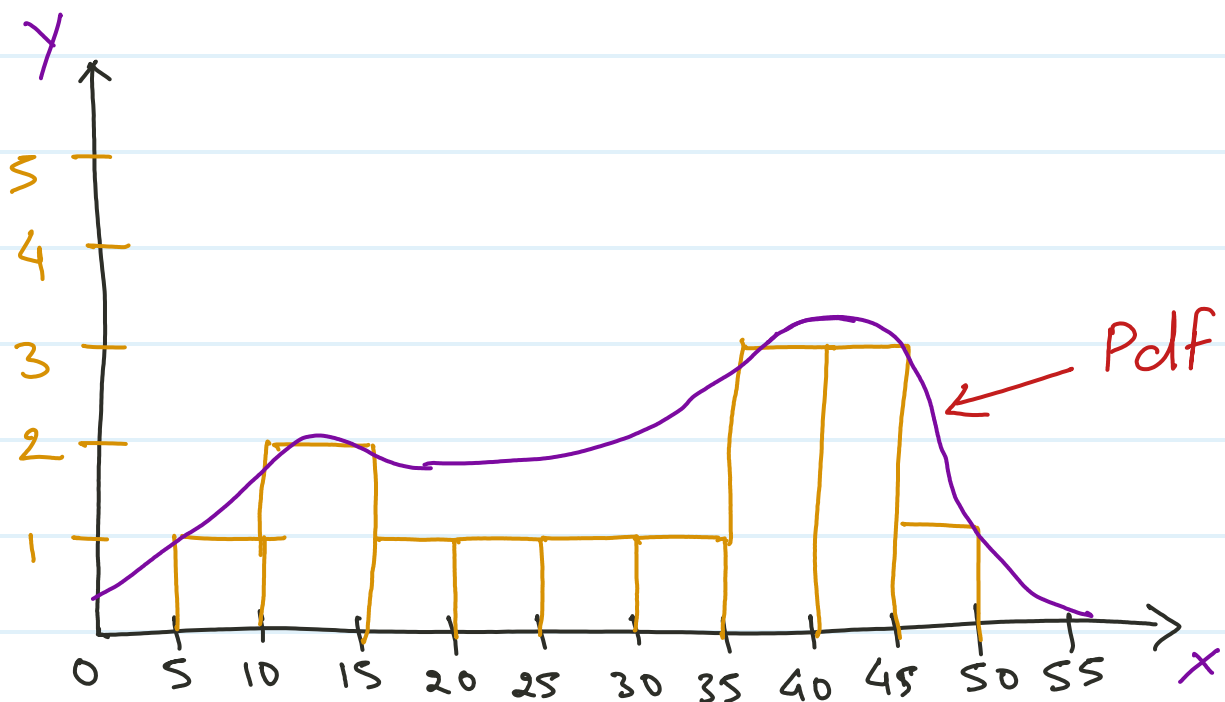


* Histogram

Dataset = [10, 12, 14, 18, 24, 30, 35, 36, 37, 40, 41, 42, 43, 50, 51]

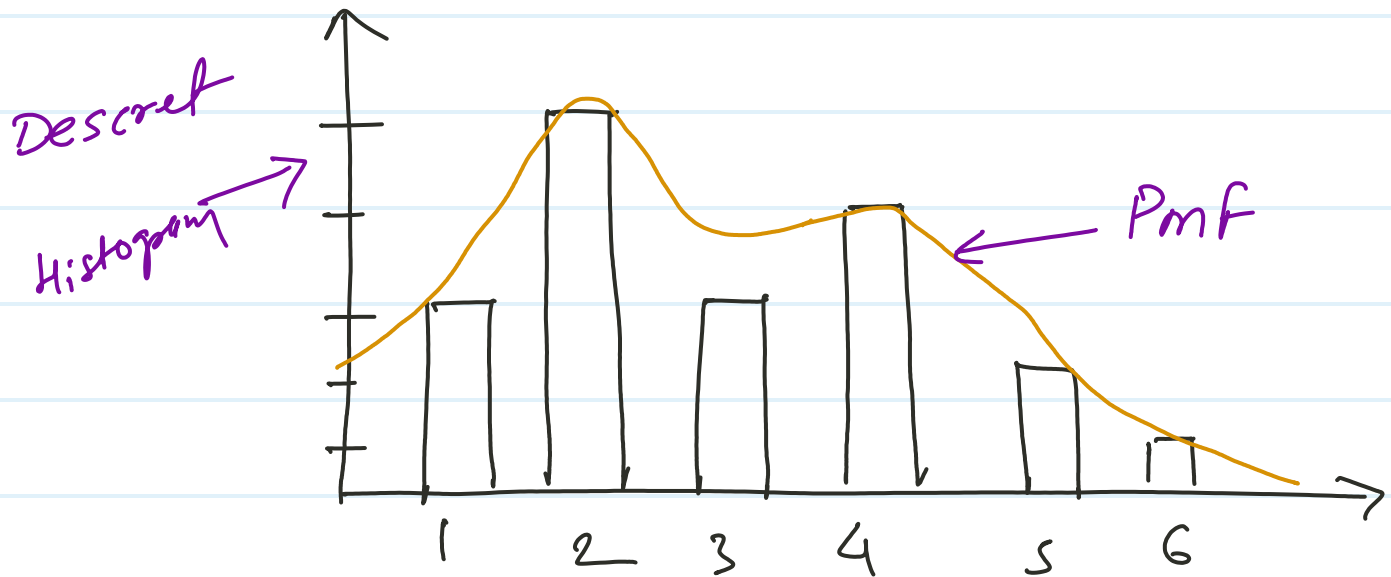
Bin / Bin size Assume bin size = 5

$$\Rightarrow \text{No of Bin} = \frac{50}{5} = 10$$



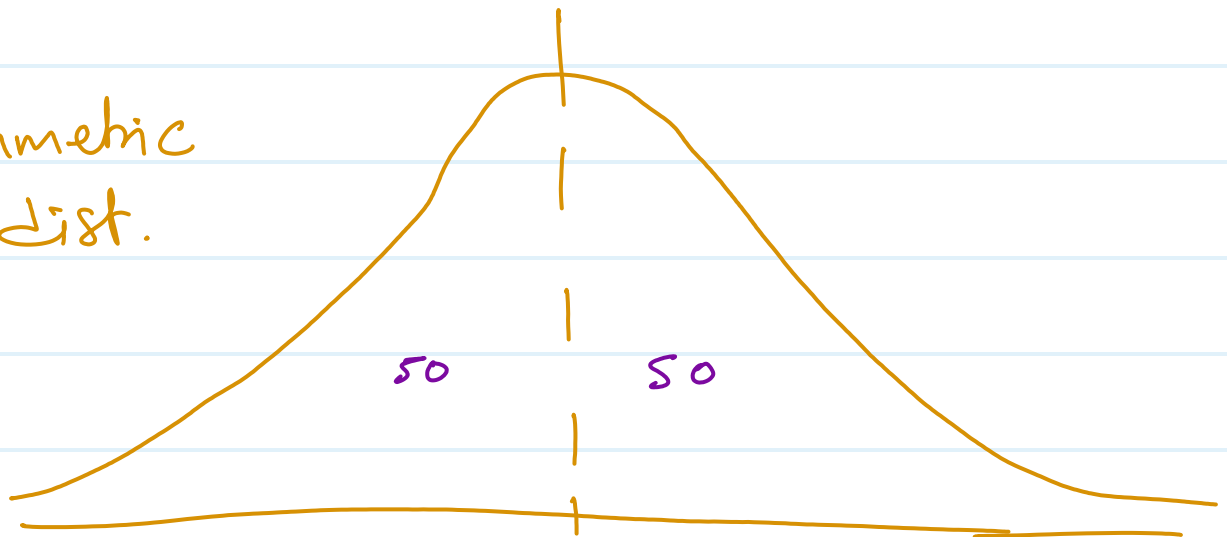
Pdf = Probability density function.

continuous histogram



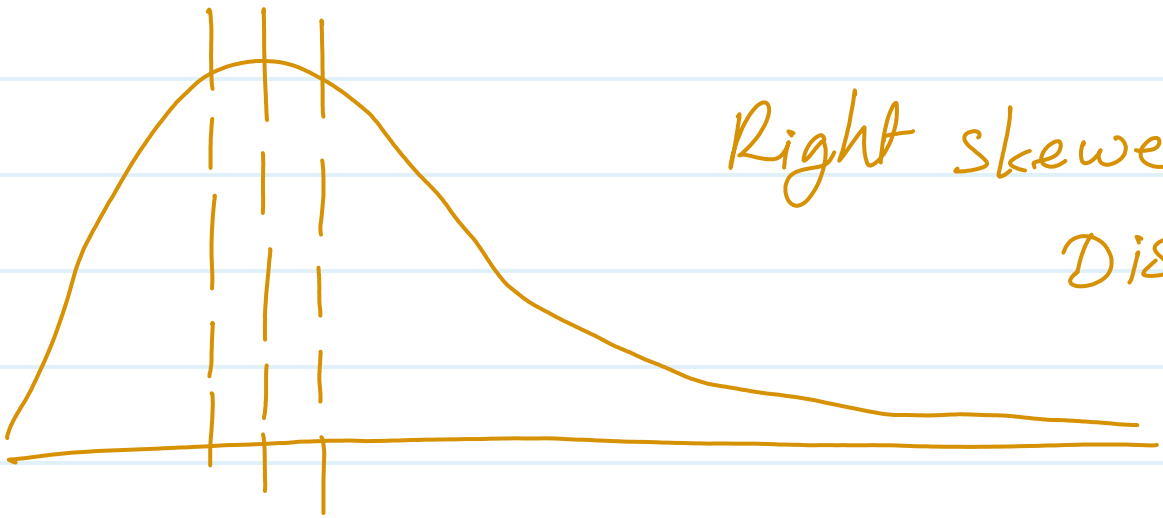
Pmf = Probability mass function

① Symmetric
dist.



mean = median = mode

(9)



Right skewed
Dist.

$$\text{mean} > \text{median} > \text{mode}$$

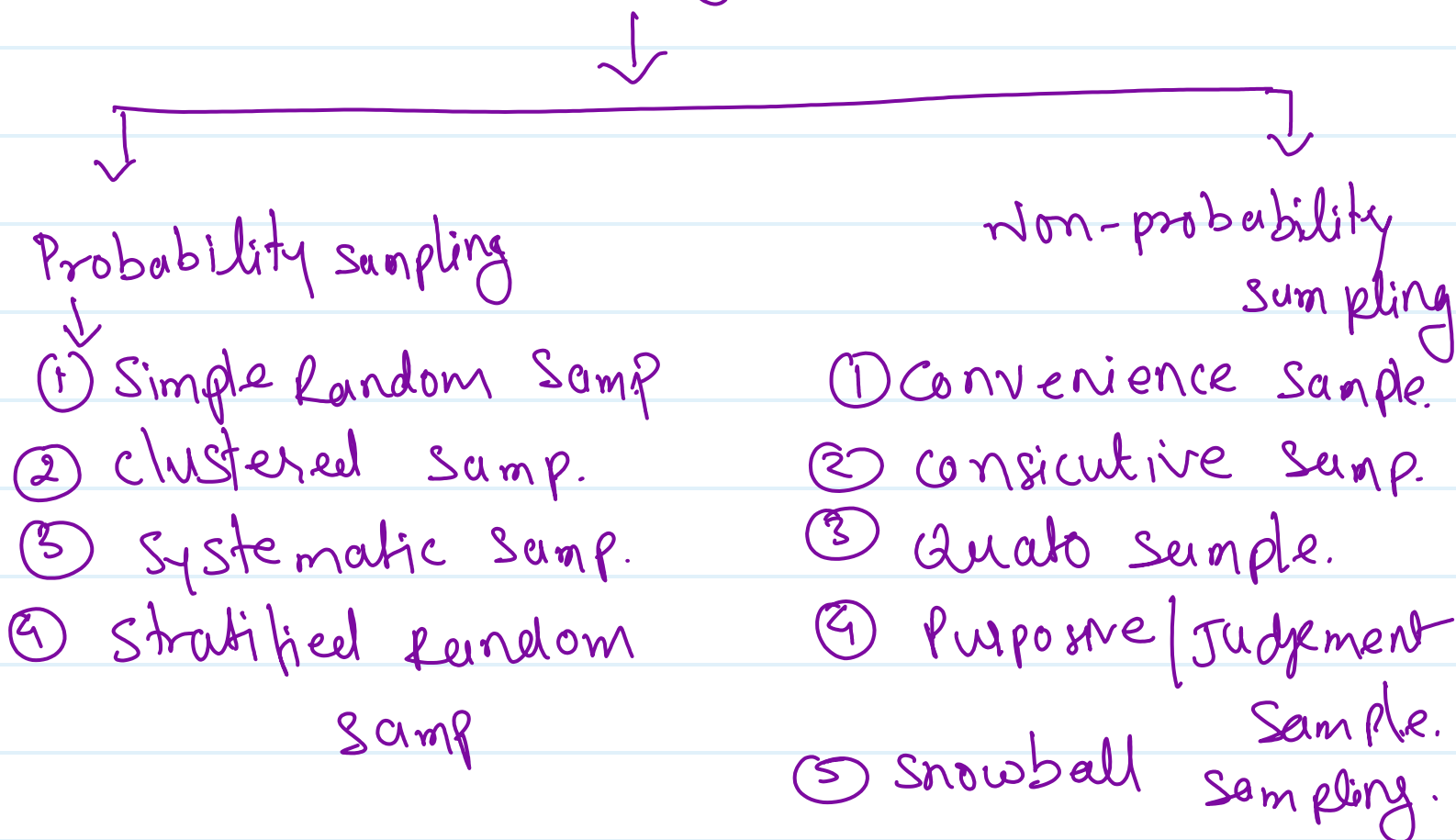
(5)

Left skewed Dist.



$$\text{mean} < \text{median} < \text{mode}$$

Sampling methods



Quartiles

* Percentile and Quartile

100 %

25% percentile = Q_1

50% percentile = Q_2 / median

75% —||— = Q_3

100 % —||— = Q_4

Score	Rank
30	1
33	2
43	3
53	4
56	5
67	6
68	7
72	8

find out where is the 25th percentile is in the above list.

Rank at 25th percentile

$$\begin{aligned}\# \text{ Rank} &= \frac{\text{Percentile}}{100} \times (\overline{n+1}) \\ &= \frac{25}{100} \times 9\end{aligned}$$

$$= 0.25 \times 9$$

$$= 2.25$$

when rounding up/down the closest value will be Rank.

$$\text{So Rank is } = 2$$

$$\underline{\text{Rank } 75\%}$$

$$= \frac{75}{100} \times (n+1)$$

$$= 0.75 \times 9$$

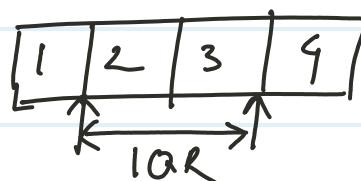
$$= 6.75$$

$$\text{Rank} = 7$$

$$\begin{aligned}
 25\% &= Q_1 \\
 50\% &= Q_2 / \text{median} \\
 75\% &= Q_3 \\
 100\% &= Q_4
 \end{aligned}$$

IQR (Inter Quartile Range)

$$IQR = Q_3 - Q_1$$



★ 5-Number Summary

- ① min
 - ② Q_1
 - ③ median.
 - ④ Q_3
 - ⑤ max.
- IQR

$$= [1, 2, 3, 4, 6, 8, 11, 14, 18, 19, 5, 21, 82, 95, 7]$$

$$1, 2, 3, 4, 5, 6, 8, 11, 14, 18, 19, 21, 82, 95, 140$$

↑
11
11
11

To find outliers we use 5 number summary to display values in Box-whisker plot

Formula upper limit = $Q_3 + 1.5(IQR)$
 lower limit = $Q_1 - 1.5(IQR)$

$$Q_1 = \frac{Q_1}{100} \times (n+1)$$

$$= \frac{25}{100} \times (15+1)$$

$$= \frac{25}{100} \times 16 =$$

$$Q_1 = 4$$

$$Q_3 = \frac{\overset{3}{\cancel{78}}}{\underset{\cancel{28}}{+100}} \times 16$$

$$Q_3 = 12$$

$$IQR = Q_3 - Q_1$$

$$= 12 - 4$$

$$= 8$$

$$\begin{aligned} \text{lower limit} &= 4 - 1.5 \times 8 \\ &= -8 \end{aligned}$$

$$\begin{aligned} \text{upper limit} &= 12 + 1.5 \times 8 \\ &= 24 \end{aligned}$$

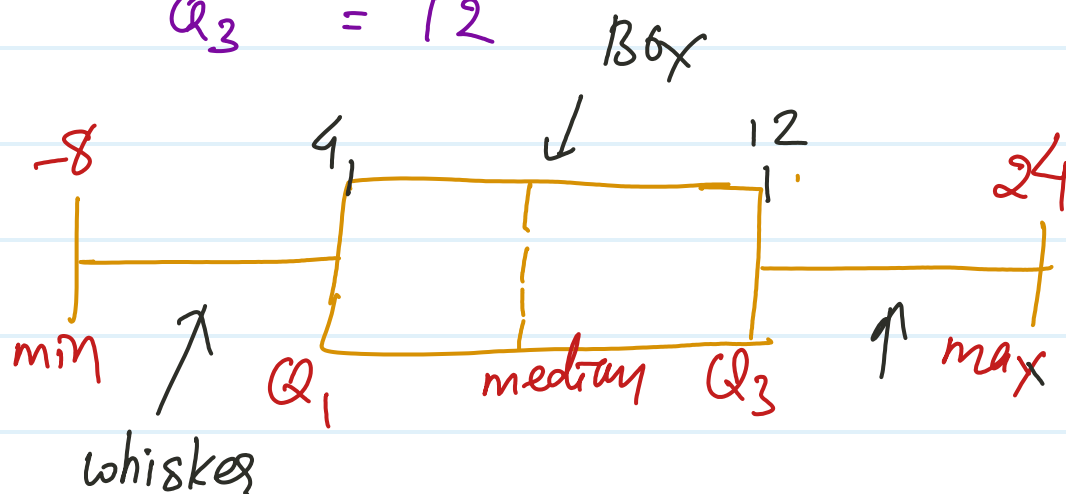
$$\text{min} = -8$$

$$\text{max} = 24$$

$$Q_1 = 4$$

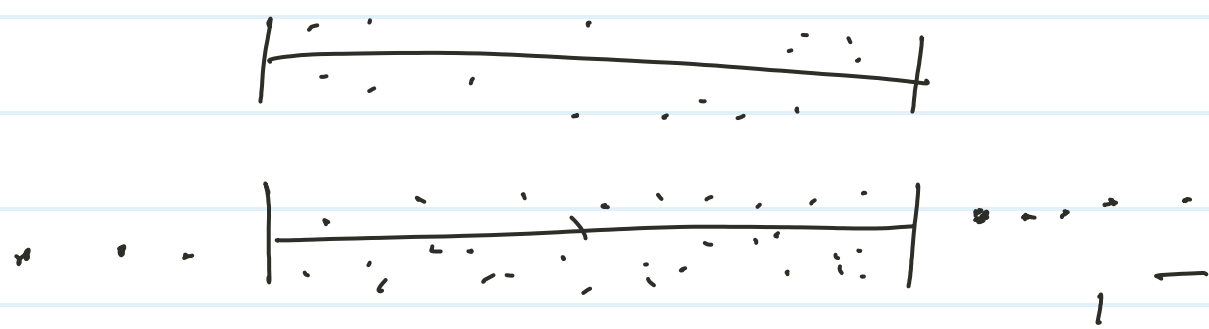
$$Q_3 = 12$$

Box and whisker plot



82, 95,
140

To treat outliers, we can use median



- i) mean
- ii) median
- iii) mode

- 1
- 2
- 3
- 4
- 5
- 6 → 6.5
- 7
- 8
- 9

Outlier $\frac{45 + 75 + 86 + 89}{12} = \frac{289}{12} \Rightarrow \underline{\underline{24}}$

24	75	-	6.5
24	80	-	6.5
24	89	-	6.5

7
1
2
7.5 ~~NAN~~ 15.2
5 →
6
9
7.5 ~~NAN~~ 15.2
11
7.5 ~~NAN~~ 15.2
12

1
2
5
6 → 7.5
9
11
12
77

15.2
 $\frac{122}{8}$
 $\frac{54}{8} \Rightarrow \underline{\underline{8.8}}$

missing → mean
 → median
 → mode

numeric
 data

P
 F
 P
 F
 NA - P
 F
 NA - P
 P
 NA - P
 P

mode
 =

