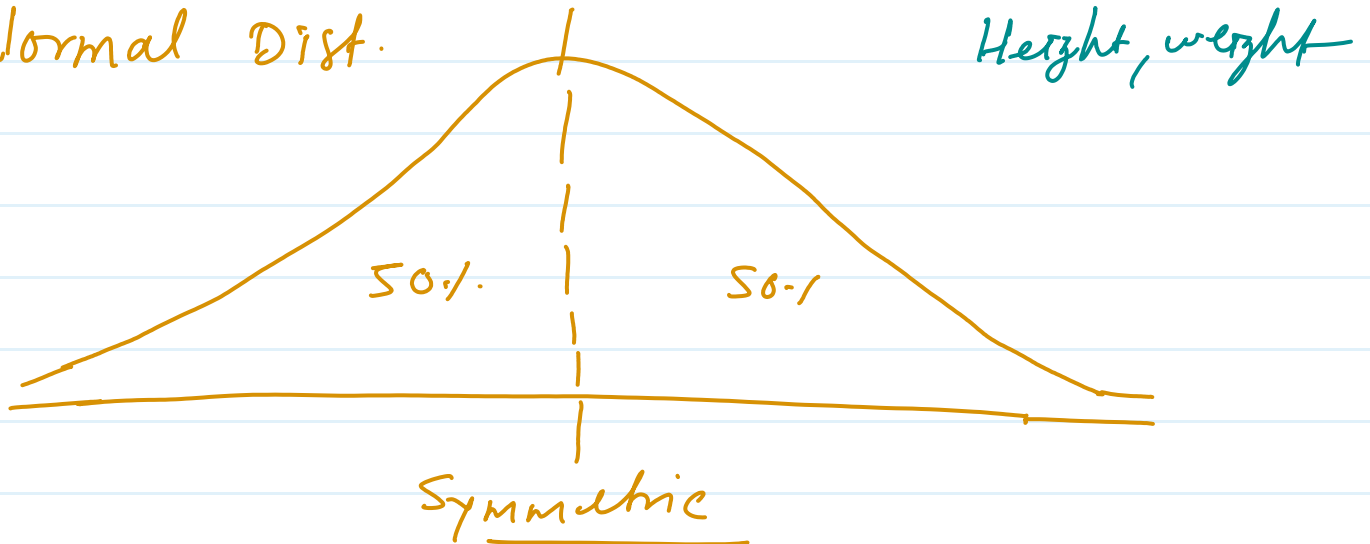
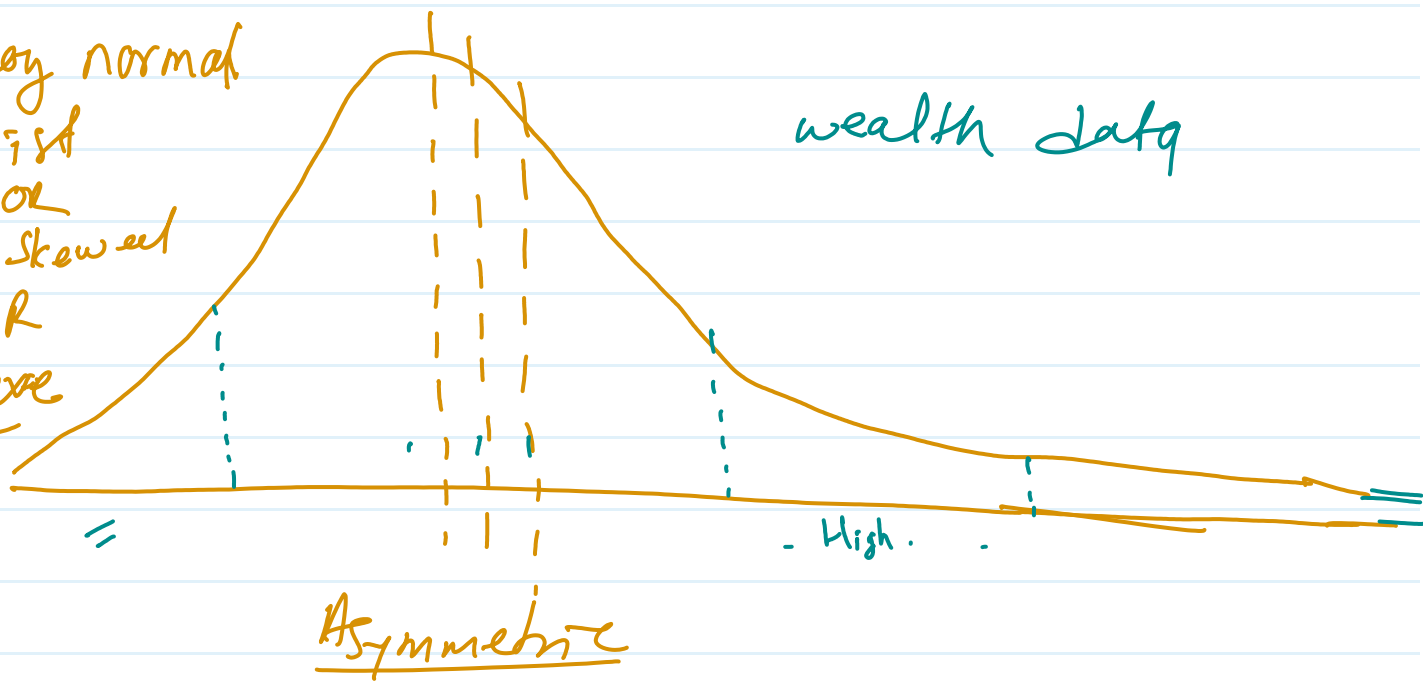


# \* Measure of shape

① Normal Dist.

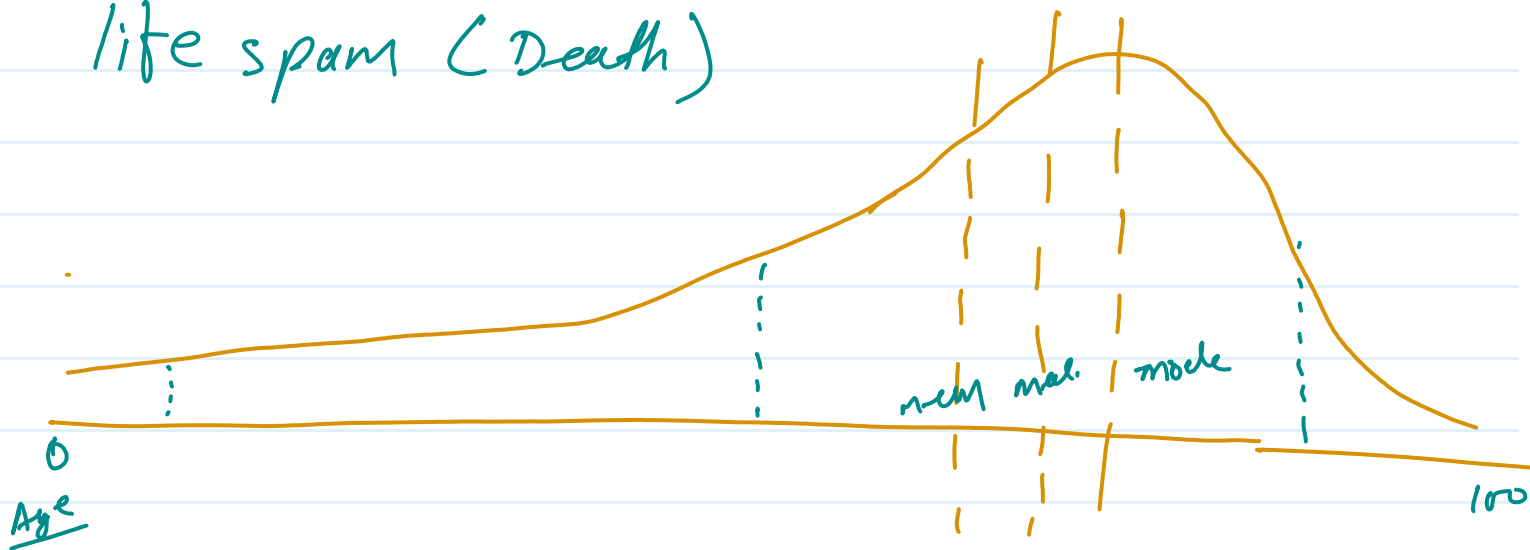


② Log normal  
Dist  
or  
Right skewed  
or  
Positive  
Dist



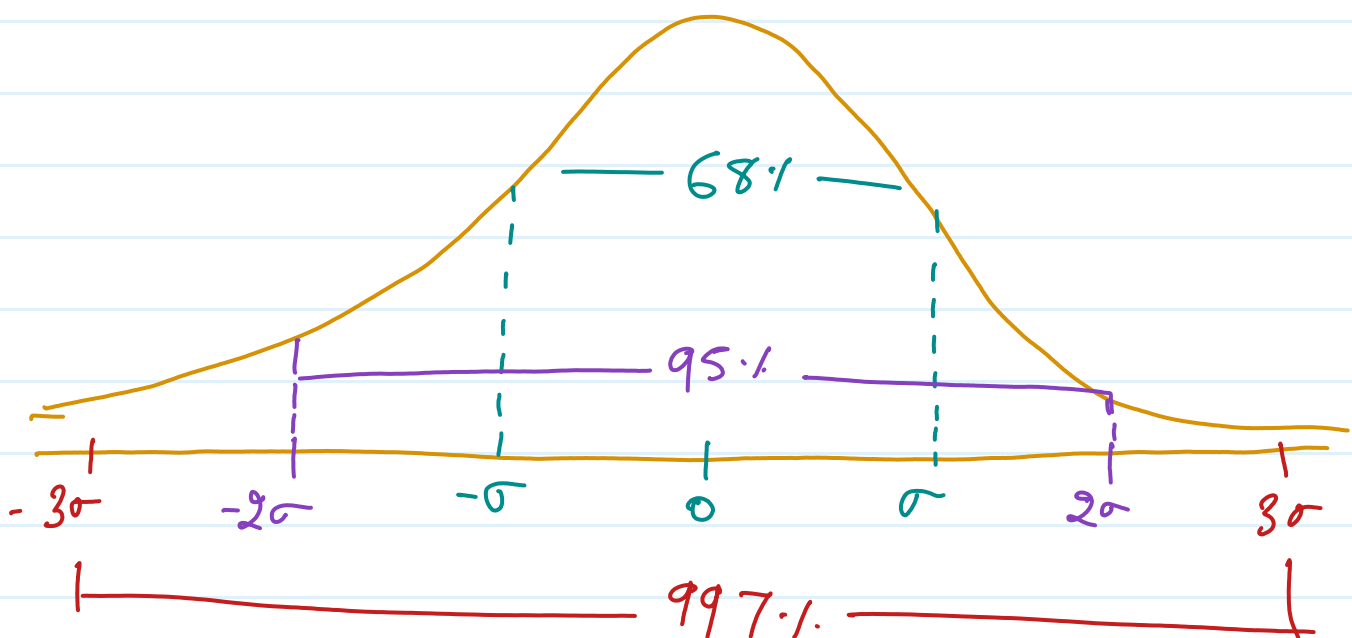
$$\text{mean} > \text{median} > \text{mode}$$

③ Left skewed Dist or Negative Dist  
life span (Death)



mean < median < mode

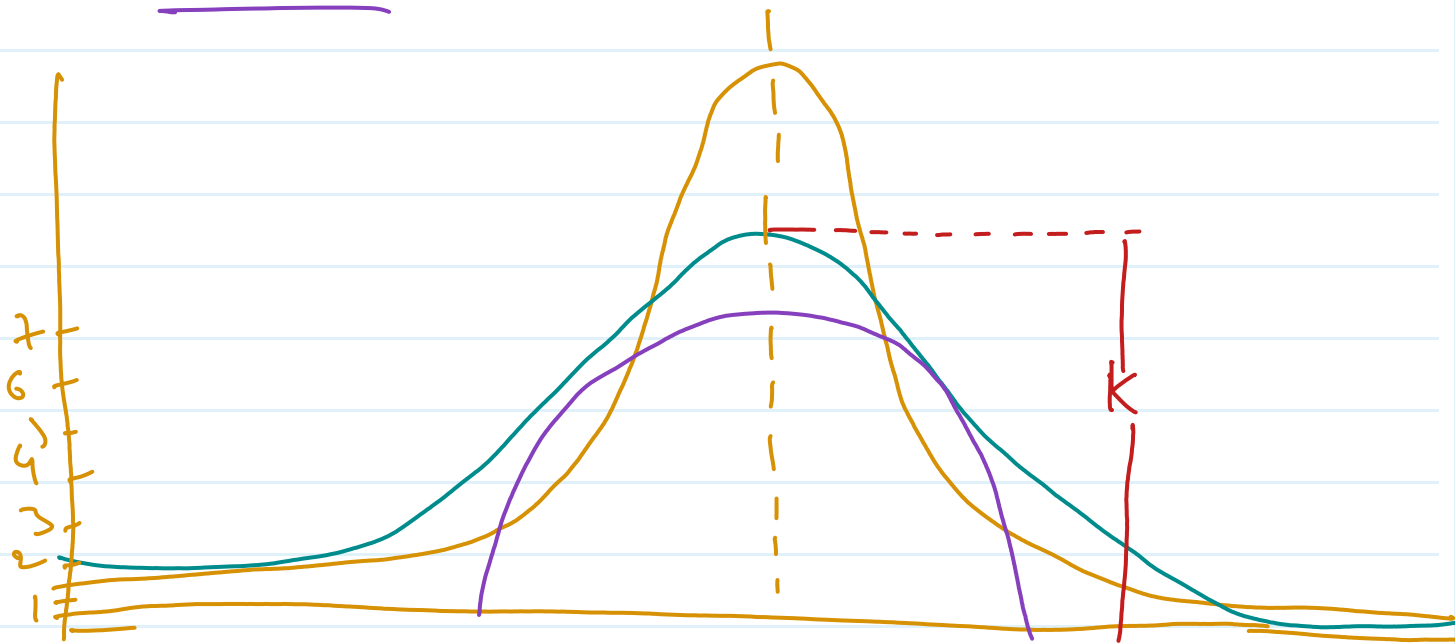
\* Empirical Rule of Distribution



68 - 95 - 99.7

\* kurtosis

$k = 3$



If  $k = 3$

① Mesokurtosis

If  $k > 3$

② Leptokurtosis

If  $k < 3$

③ Platykurtosis

# \* Chebyshev's Inequality

$X \approx$  Gaussian Dist

$$P_{r_1}(\mu - \sigma \leq X \leq \mu + \sigma) = 68.1\%$$

$$P_{r_2}(\mu - 2\sigma \leq X \leq \mu + 2\sigma) = 95.4\%$$

$$P_{r_3}(\mu - 3\sigma \leq X \leq \mu + 3\sigma) = 99.7\%$$

$Y \not\approx$  Gaussian Dist.

$$P_r(\mu - k\sigma \leq Y \leq \mu + k\sigma) \geq 1 - \frac{1}{k^2}$$

$k$  is SD., value of  $k$  will be 2 or more than two.

If  $k = 2$

$$P_r(\mu - 2\sigma \leq Y \leq \mu + 2\sigma) \geq 1 - \frac{1}{2^2}$$

$$\geq 1 - \frac{1}{4}$$

$$\geq \frac{3}{4} \Rightarrow 0.75$$

$$\Rightarrow 75\%$$

If  $k = 3$

$$P_r(\mu - 3\sigma \leq Y \leq \mu + 3\sigma) \geq 1 - \frac{1}{8}$$

$$\geq \frac{7}{8} = 87.5\%$$

If  $k = 4$

$$P_r(\mu - 4\sigma \leq Y \leq \mu + 4\sigma) \geq 1 - \frac{1}{16}$$

$$\geq \frac{15}{16} = 93.75\%$$