

## Descriptive analytics

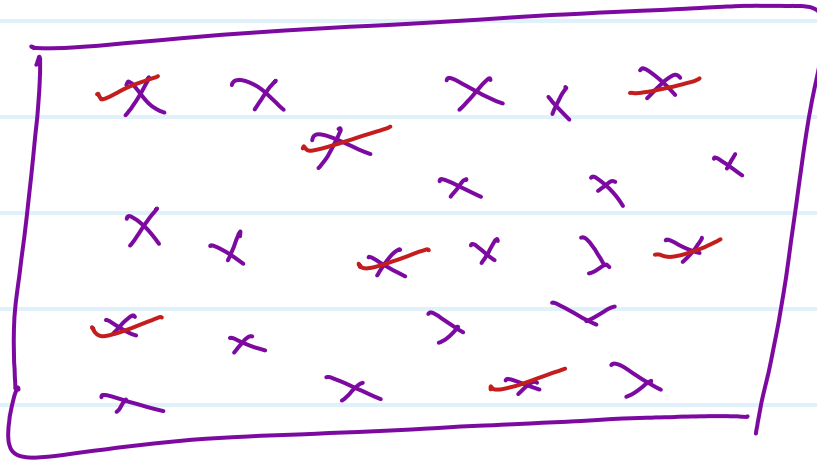
Population -  $N$ ,  $\mu$

Sampling -  $n$ ,  $\bar{X}$

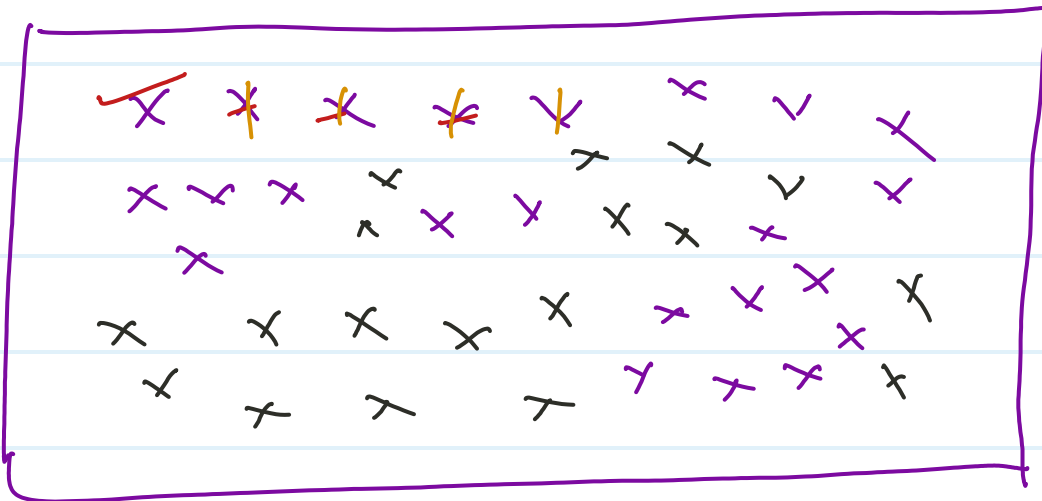
### \* Sampling Types

- ① Simple random sampling
- ② Stratified sampling
- ③ Systematic sampling
- ④ Convenience sampling

① simple random sampling



② stratified samp.



③ systematic samp.



④ Convi. Semp.

median

[1, 2, 3, 4, 5, 6, 7, 8]

$$\frac{4+5}{2} = 4.5$$

mode

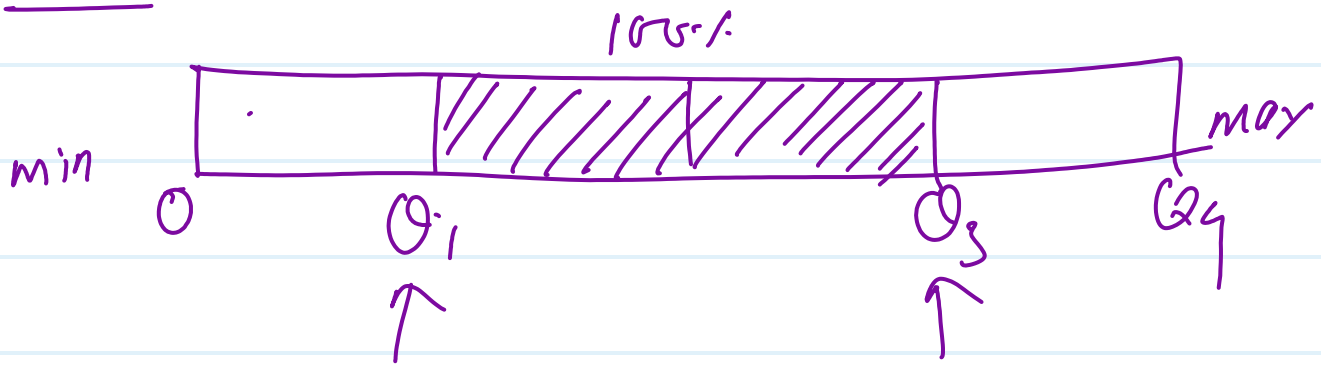
uni-modal

[1, 2, 3, 4, 4, 5, 6, 4, 6, 6]

Bi-modal

[2, 20, 15, 35, 40, 55, 52, 77]

10R



Variance

$$N \rightarrow \sigma^2 = \frac{\sum (x_i - \mu)^2}{N}$$

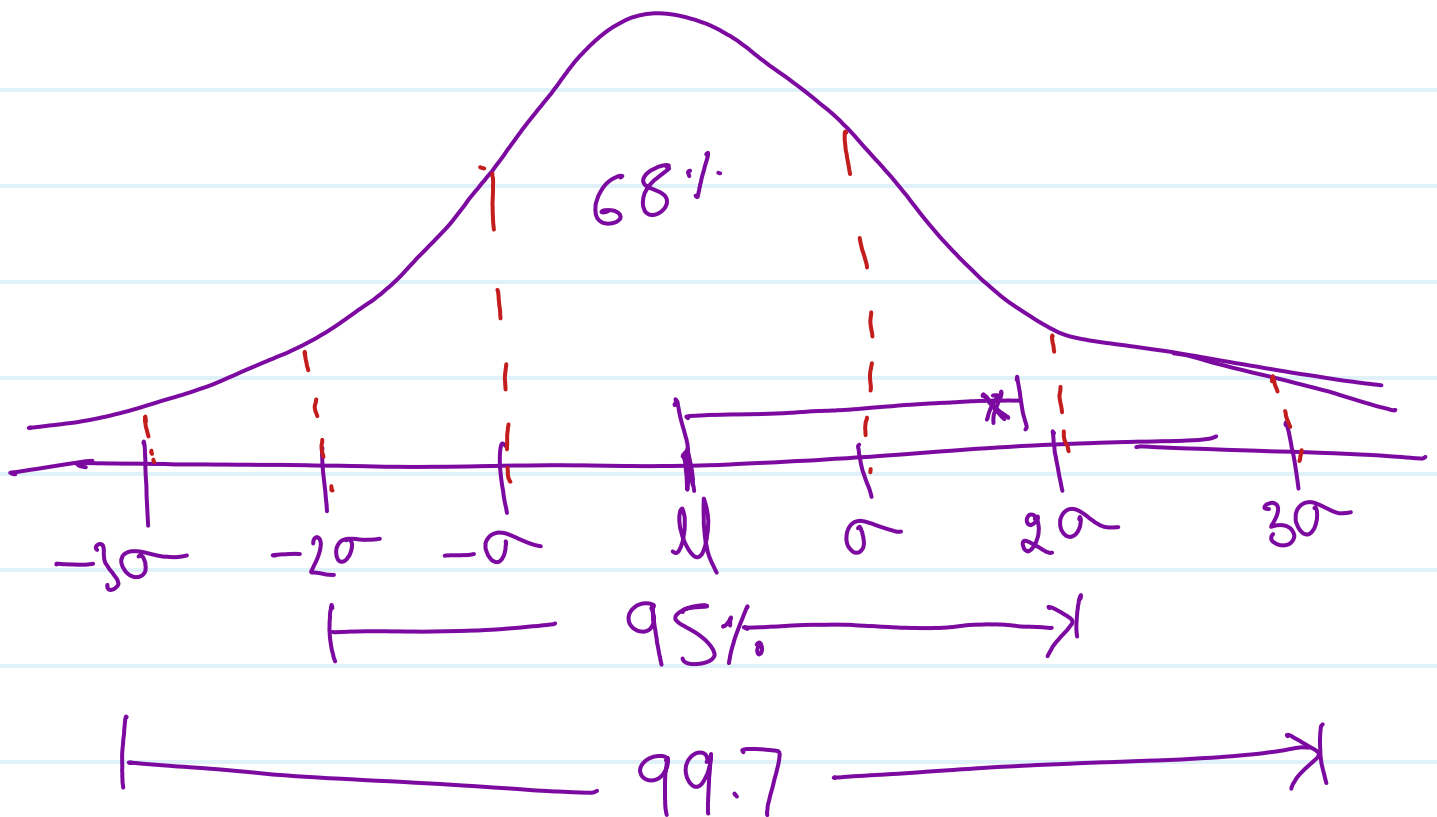
$$n \rightarrow s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}$$

OR <sup>(n-1)</sup> Degree of freedom  
Bessel's correction

SD

$$\sigma = \sqrt{\frac{\sum (x_i - \mu)^2}{n}}$$

$$s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$$

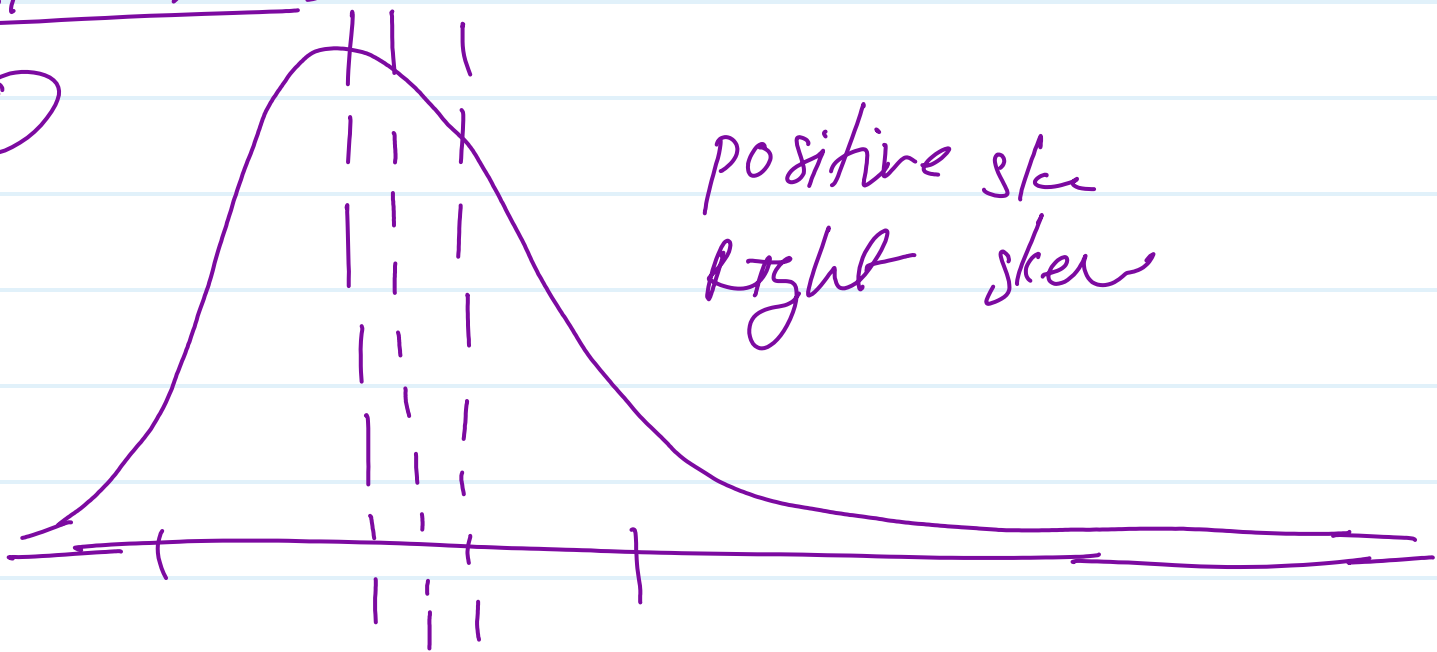


68 - 95 - 99.7

It called Empirical rule of n.D.

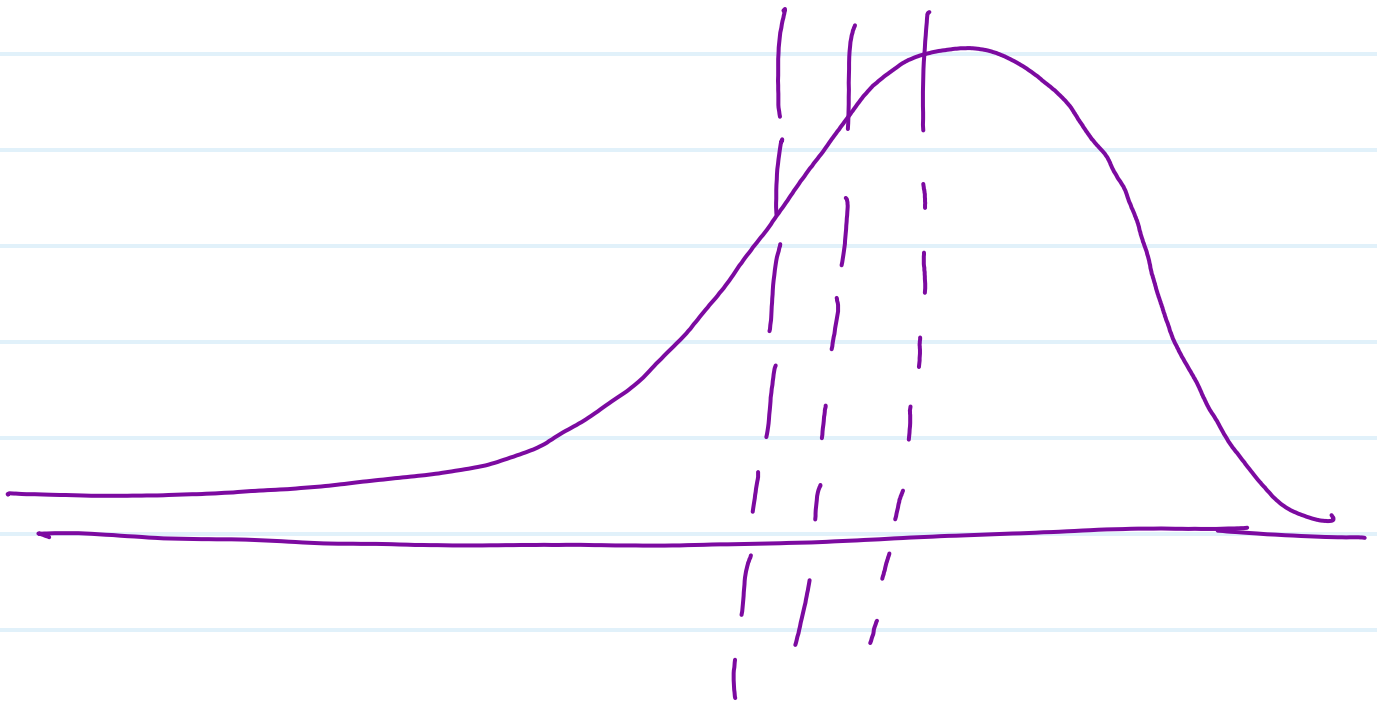
# Skewness

①



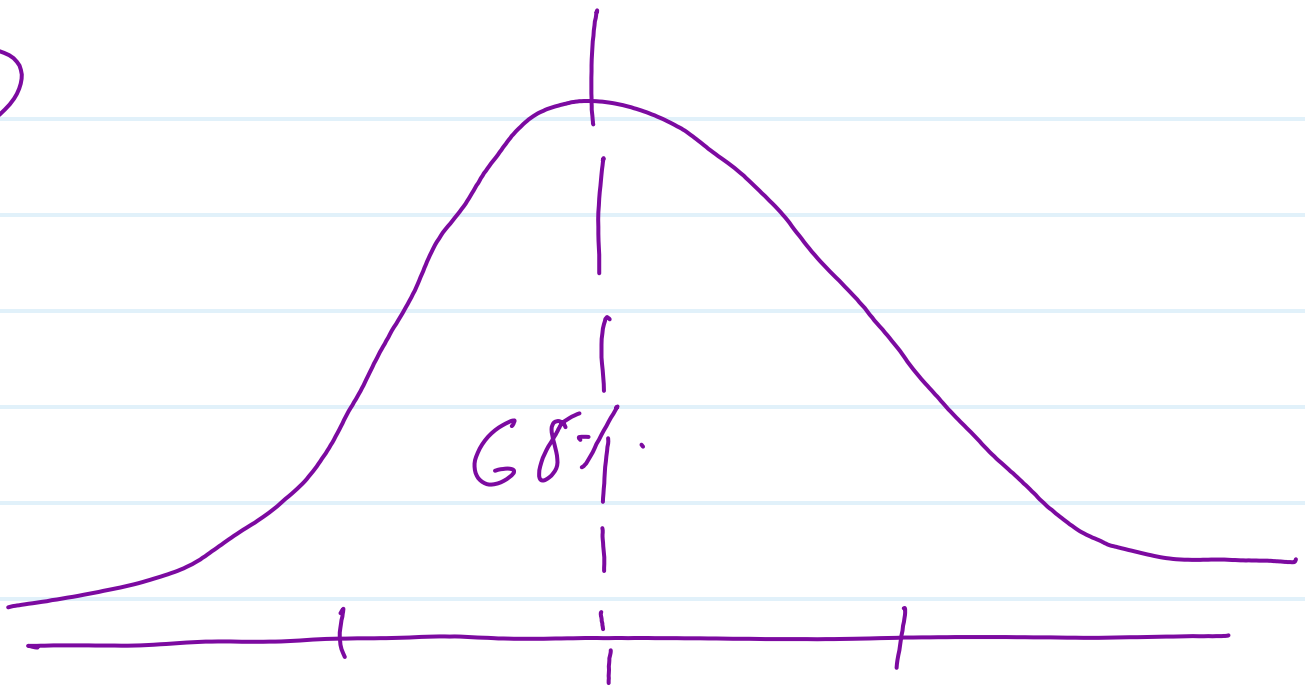
$$\text{mean} > \text{median} > \text{mode}$$

②



$$\text{mean} < \text{median} < \text{mode}$$

③

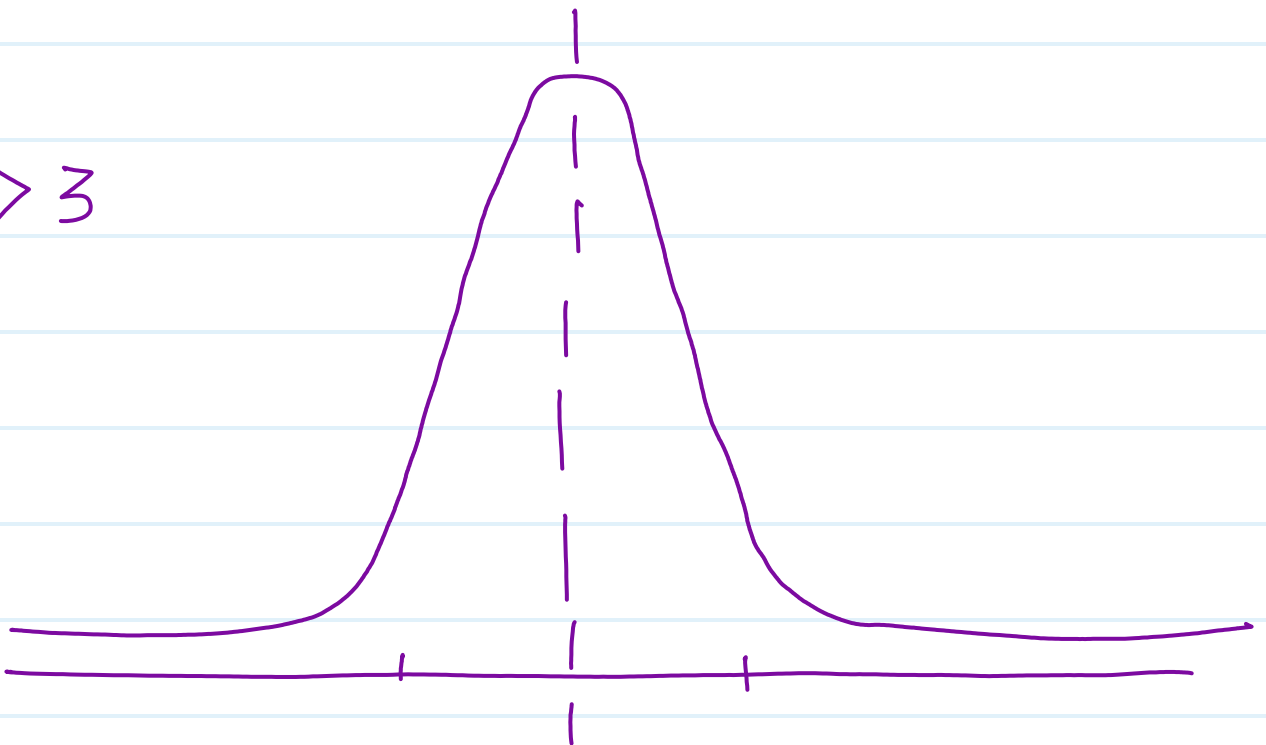


mean = median = mode

kurtosis —  $K = 3$

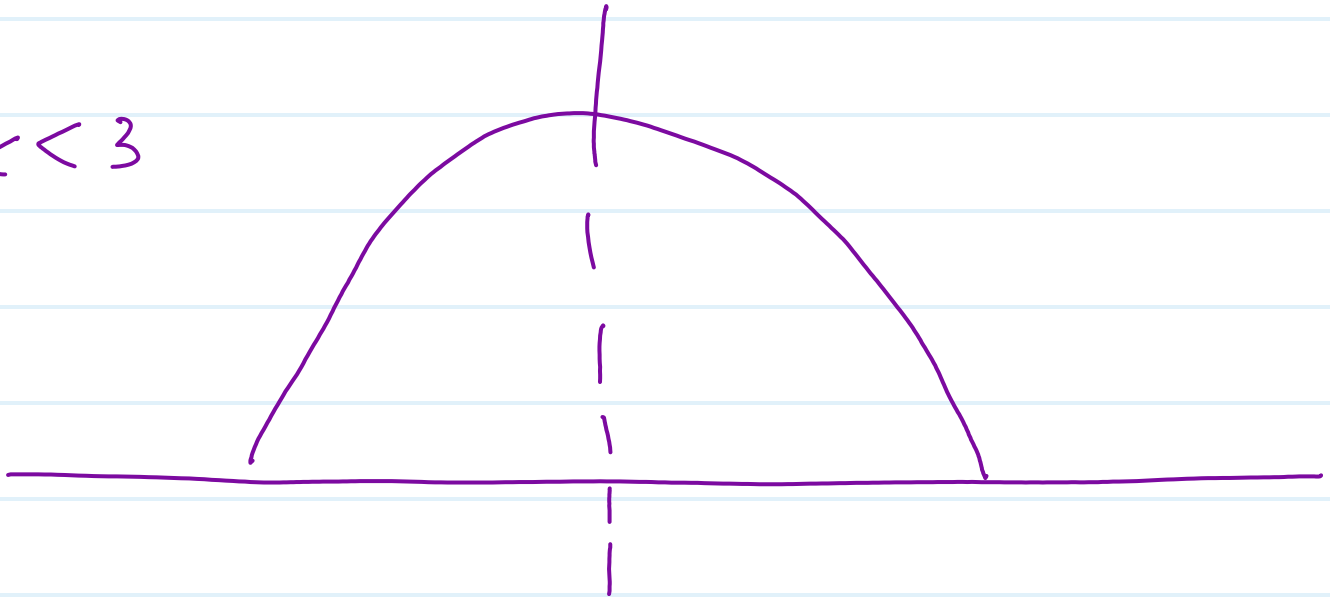
① Leptokurtosis —

$K > 3$



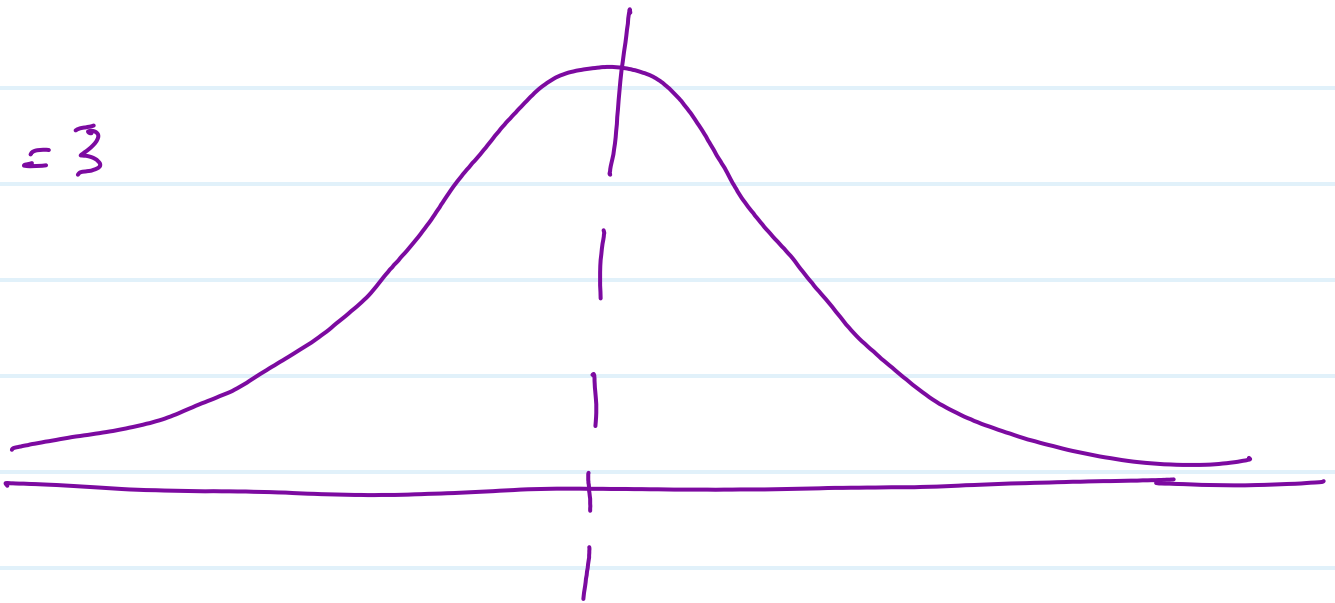
## ② platykurtosis

$$k < 3$$



## ③ mesokurtosis

$$k = 3$$





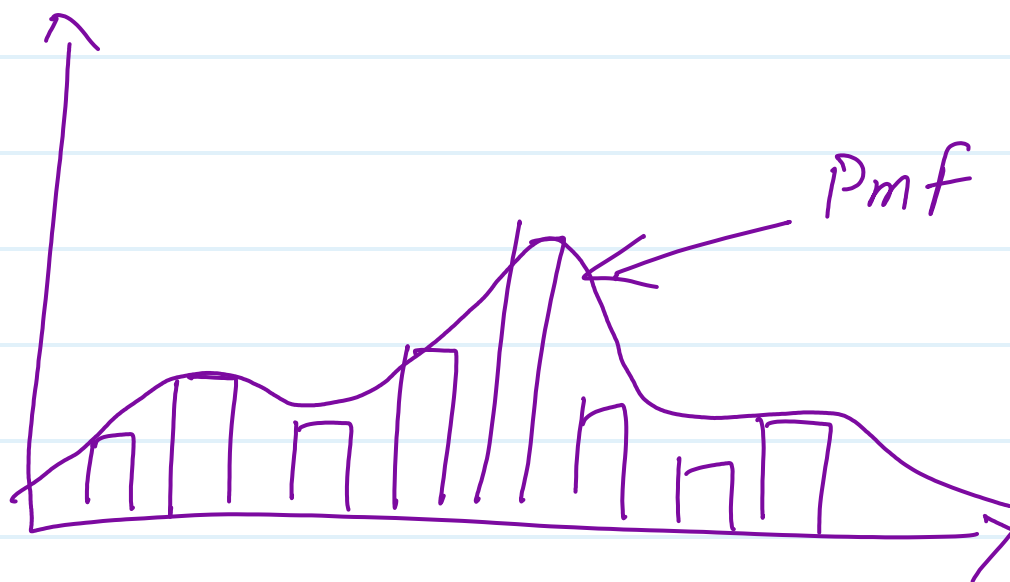


## ① Histogram



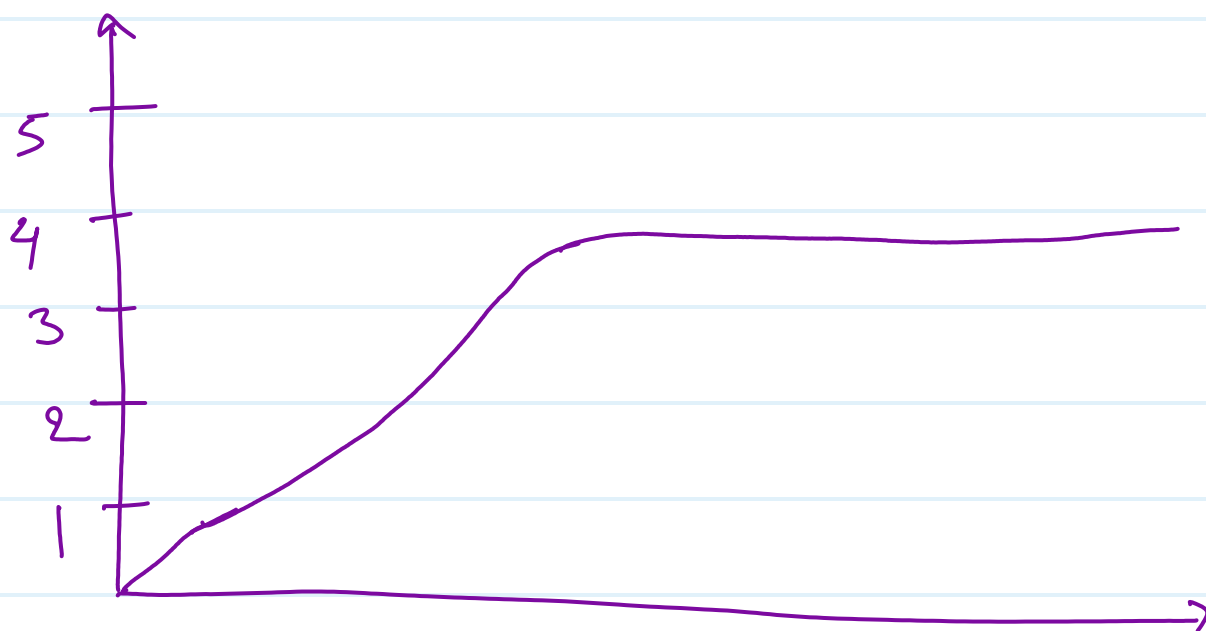
Probability density function

② Density histo



\* Prob. mass. function.

kde



$$1 = 1$$

$$2 = 1 + 2 = 3$$

$$3 = 3 + 3 = 6$$

$$4 = 6 + 5 = 11 + 0$$

# ★ correlation / covariance

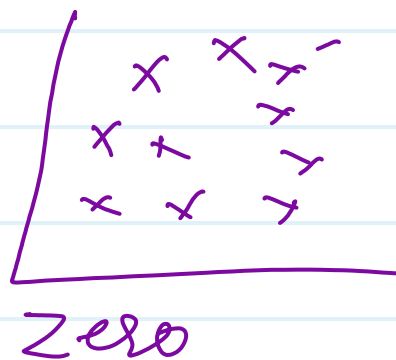
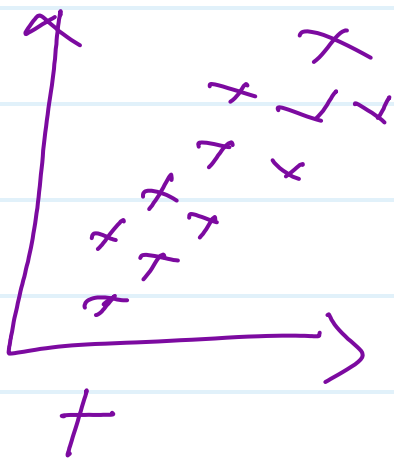
$x_1 \quad x_2 \quad x_3 \quad x_4 \quad y$

$x_1 \quad y$   
 $x_2 \quad y$   
 $x_3 \quad y$   
 $x_4 \quad y$

covariance :-

$-\infty$

$+\infty$



$$\begin{array}{cc} X \uparrow & Y \uparrow \\ X \downarrow & Y \downarrow \end{array} \left. \vphantom{\begin{array}{cc} X \uparrow & Y \uparrow \\ X \downarrow & Y \downarrow \end{array}} \right\} +$$

$$\begin{array}{cc} X \uparrow & Y \downarrow \\ X \downarrow & Y \uparrow \end{array} \left. \vphantom{\begin{array}{cc} X \uparrow & Y \downarrow \\ X \downarrow & Y \uparrow \end{array}} \right\} -$$

$$\begin{array}{cc} X \uparrow & Y \uparrow \downarrow \\ X \downarrow & Y \end{array} \left. \vphantom{\begin{array}{cc} X \uparrow & Y \uparrow \downarrow \\ X \downarrow & Y \end{array}} \right\} \text{zero}$$

## correlation

- ① Pearson corr. coeff.
- ② Spearman rank corr. coeff.

$$X \gamma = 0.85$$

$$X \gamma = -0.9$$

Assumption:

$X_1$	$X_2$	$X_3$	$X_4$	$\gamma$
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$$X_1 X_2 = 0.75$$

Pareto Dist. / Powerlaw Dist.

cricket - 11

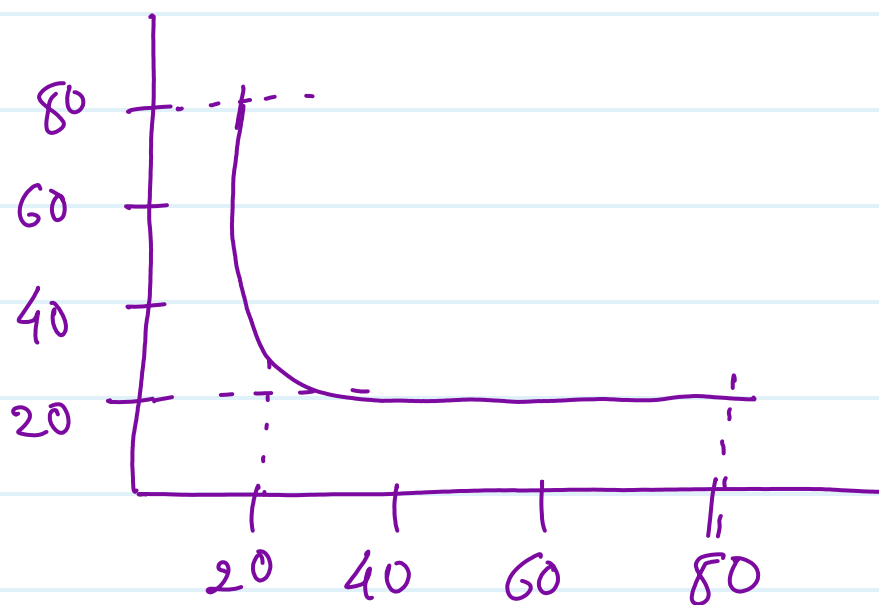
run - 80% — 20%

20% — 80%

work

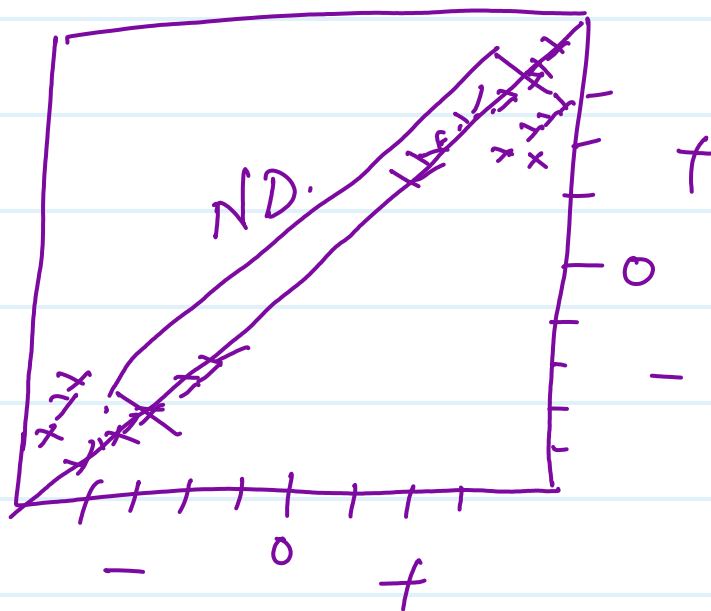
80% — 20%

20% — 80%



Box-Cox transformation

Q-Q



## Percentile

[2, 2, 3, 4, 5, 5, 5, 6, 7, 8, 8, 8, 8, 9, 9, 10, 11, 11, 12]

percentile of 10 position?

$$\begin{aligned} 10^{\text{th}} &= \frac{16}{19} \times 100 \\ &= 84\% \end{aligned}$$

$Q_1$

$Q_3$


$$IQR = Q_3 - Q_1$$

$$\underline{\text{upper fence}} = Q_3 + 1.5 IQR$$

$$\text{lower fence} = Q_1 - 1.5 IQR$$



-4 -3 -2 -1 0 +1 +2 +3 +4



## 5 number summary

- ① max
- ② min
- ③  $Q_1$
- ④  $Q_3$
- ⑤  $m/m$