

Binary Search Tree (BST)

Introduction

Data structures are essential in computer science for efficient data management and retrieval. One such data structure is the Binary Search Tree (BST). A BST is a node-based binary tree where each node has up to two children, with the left child containing a value less than its parent node and the right child containing a value greater than its parent node. This property makes BSTs highly efficient for search, insert, and delete operations.

Importance of BST

BSTs are crucial due to their efficient operations:

- **Search:** Average time complexity of $O(\log n)$.
- **Insertion:** Average time complexity of $O(\log n)$.
- **Deletion:** Average time complexity of $O(\log n)$.

These operations are fundamental in various applications such as databases, file systems, and many real-time systems.

Implementation Details

```
#include <iostream>
using namespace std;

struct Node {
    int data;
    Node* left;
    Node* right;

    Node(int val) : data(val), left(nullptr), right(nullptr) {}
};

class BST {
public:
    Node* root;

    BST() : root(nullptr) {}
};
```

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```
void insert(int data) {  
    root = insert(root, data);  
}  
  
bool search(int data) {  
    return search(root, data) != nullptr;  
}  
  
void remove(int data) {  
    root = remove(root, data);  
}  
  
void inorder() {  
    inorder(root);  
    cout << endl;  
}  
  
void preorder() {  
    preorder(root);  
    cout << endl;  
}  
  
void postorder() {  
    postorder(root);  
    cout << endl;  
}  
  
private:  
Node* insert(Node* node, int data) {
```

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```
if (node == nullptr) {  
    return new Node(data);  
}  
  
if (data < node->data) {  
    node->left = insert(node->left, data);  
} else {  
    node->right = insert(node->right, data);  
}  
  
return node;  
}  
  
Node* search(Node* node, int data) {  
    if (node == nullptr || node->data == data) {  
        return node;  
    }  
  
    if (data < node->data) {  
        return search(node->left, data);  
    } else {  
        return search(node->right, data);  
    }  
}  
  
Node* remove(Node* node, int data) {  
    if (node == nullptr) return node;  
  
    if (data < node->data) {  
        node->left = remove(node->left, data);  
    }
```

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```
    } else if (data > node->data) {
        node->right = remove(node->right, data);
    } else {
        if (node->left == nullptr) {
            Node* temp = node->right;
            delete node;
            return temp;
        } else if (node->right == nullptr) {
            Node* temp = node->left;
            delete node;
            return temp;
        }
    }

    Node* temp = minValueNode(node->right);
    node->data = temp->data;
    node->right = remove(node->right, temp->data);
}

return node;
}

Node* minValueNode(Node* node) {
    Node* current = node;
    while (current && current->left != nullptr) {
        current = current->left;
    }
    return current;
}

void inorder(Node* node) {
    if (node != nullptr) {
```

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```
        inorder(node->left);
        cout << node->data << " ";
        inorder(node->right);
    }
}

void preorder(Node* node) {
    if (node != nullptr) {
        cout << node->data << " ";
        preorder(node->left);
        preorder(node->right);
    }
}

void postorder(Node* node) {
    if (node != nullptr) {
        postorder(node->left);
        postorder(node->right);
        cout << node->data << " ";
    }
}

};

int main() {
    BST bst;
    bst.insert(50);
    bst.insert(30);
    bst.insert(20);
    bst.insert(40);
    bst.insert(70);
```

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```
bst.insert(60);
bst.insert(80);

cout << "Inorder traversal: ";
bst.inorder();

cout << "Preorder traversal: ";
bst.preorder();

cout << "Postorder traversal: ";
bst.postorder();

cout << "Search 40: " << (bst.search(40) ? "Found" : "Not Found") << endl;
cout << "Search 100: " << (bst.search(100) ? "Found" : "Not Found") << endl;

cout << "Deleting 20\n";
bst.remove(20);
cout << "Inorder traversal after deleting 20: ";
bst.inorder();

cout << "Deleting 30\n";
bst.remove(30);
cout << "Inorder traversal after deleting 30: ";
bst.inorder();

cout << "Deleting 50\n";
bst.remove(50);
cout << "Inorder traversal after deleting 50: ";
bst.inorder();

return 0; }
```

Binary Search Tree (BST)

How the Code Works

1. Node Structure:

- o A structure Node to represent each node in the tree.
- o Each node contains an integer data and pointers to its left and right children.

2. BST Class:

- o Contains a root pointer and functions to perform various operations.

3. Insertion:

- o The insert function inserts a new value in the correct position based on BST properties.
- o If the tree is empty, the new node becomes the root. Otherwise, it traverses the tree to find the correct spot for the new node.

4. Search:

- o The search function traverses the tree to check if a value exists.
- o Returns true if found, false otherwise.

5. Deletion:

- o The remove function handles three cases:
 - Node to be deleted has no children (leaf node).
 - Node to be deleted has one child.
 - Node to be deleted has two children: Find the in-order successor (smallest value in the right subtree), replace the node's value with the successor's value, and delete the successor.

6. Traversals:

- o inorder: Traverses left subtree, visits root, traverses right subtree.
- o preorder: Visits root, traverses left subtree, traverses right subtree.
- o postorder: Traverses left subtree, traverses right subtree, visits root.

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Input/Output

Sample Input/Output:

1. Insertion and Traversal:

```
BST bst;  
bst.insert(50);  
bst.insert(30);  
bst.insert(20);  
bst.insert(40);  
bst.insert(70);  
bst.insert(60);  
bst.insert(80);  
  
// Output Inorder: 20 30 40 50 60 70 80  
// Output Preorder: 50 30 20 40 70 60 80  
// Output Postorder: 20 40 30 60 80 70 50
```

2. Search:

```
cout << "Search 40: " << (bst.search(40) ? "Found" : "Not Found") << endl; //  
Output: Found  
  
cout << "Search 100: " << (bst.search(100) ? "Found" : "Not Found") << endl;  
// Output: Not Found
```

3. Deletion and InOrder Traversal:

```
bst.remove(20);  
// Output Inorder after deleting 20: 30 40 50 60 70 80  
bst.remove(30);  
// Output Inorder after deleting 30: 40 50 60 70 80  
bst.remove(50);  
// Output Inorder after deleting 50: 40 60 70 80
```


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Test Cases and Results

Test Case 1: Insertion

- **Input:** Insert values [50, 30, 20, 40, 70, 60, 80].
- **Expected Output:** Inorder traversal: 20 30 40 50 60 70 80.

Test Case 2: Search

- **Input:** Search for 40.
- **Expected Output:** Found.
- **Input:** Search for 100.
- **Expected Output:** Not Found.

Test Case 3: Deletion

- **Input:** Delete 20.
- **Expected Output:** Inorder traversal: 30 40 50 60 70 80.
- **Input:** Delete 30.
- **Expected Output:** Inorder traversal: 40 50 60 70 80.
- **Input:** Delete 50.
- **Expected Output:** Inorder traversal: 40 60 70 80.

Conclusion

This report demonstrates the implementation of a Binary Search Tree (BST) in C++ with search, insert, and delete functions. The BST provides efficient data management and retrieval, making it a crucial data structure in computer science. The implementation is tested with sample test cases to verify its correctness and efficiency. The provided code and explanations offer a comprehensive understanding of how BST operations work, making it a valuable resource for students and developers.

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```
PROBLEMS  OUTPUT  DEBUG CONSOLE  TERMINAL  PORTS  COMMENTS

PS C:\Users\Susha\Downloads\DSA CPP Assignment> cd "c:\Users\Susha\Downloads\DSA CPP Assignment"

*****

*                               *
**Welcome to Cipher Schools Assignment **
*               of DSA CPP Summer Training               *
*                               *
*****

Enter the number of elements to insert into the BST: 7
Enter value 1: 50
Enter value 2: 30
Enter value 3: 20
Enter value 4: 40
Enter value 5: 70
Enter value 6: 60
Enter value 7: 80

1. Inorder traversal: 20 30 40 50 60 70 80

2. Preorder traversal: 50 30 20 40 70 60 80

3. Postorder traversal: 20 40 30 60 80 70 50

Enter a value to search: 20
4. Search 20: Found

Enter a value to delete: 20
5. Deleting 20
   Inorder traversal after deleting 20: 30 40 50 60 70 80
PS C:\Users\Susha\Downloads\DSA CPP Assignment> 
```











