

$$P(X \geq a) \leq \frac{E(X)}{a}$$

Markov's inequality

$$P(|X - E(X)| \geq a) \leq \frac{\text{Var}(X)}{a^2}$$

Chebyshev's inequality

$$P(|X - E(X)| \geq a) \leq \frac{E[|X - E(X)|^k]}{a^k}$$

↙ Generalized Chebyshev's inequality

$$P(X \geq a) \leq M_X(t) e^{-ta}$$

Moment generating function

$$E(e^{tx}) \cdot e^{-ta}$$

$$|X_i| \stackrel{\text{d.s.}}{\leq} 1$$

$$E(X_i) = 0, \quad \sum_{i=1}^n X_i$$

Central Limit Theorem

where $a > 0$ and

$$P\left(\sum_{i=1}^n X_i \geq a\right) \leq \exp\left(-\frac{a^2}{2n}\right)$$