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A Novel Approach to Time Series Forecasting using Liquid Time-constant Networks

A Project Specification Design & Prototype by

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ABSTRACT

Time Series (TS) forecasting advancements have been stagnant lately due to limitations of the existing algorithms; therefore, systems built using these algorithms are also limited in performance. Although recent advancements in Deep Learning (DL) have produced significant contributions in the domain of Natural Language Processing (NLP), Computer Vision and Reinforcement Learning (RL), the field of TS still needs to be improved.

Multiple approaches have been taken to solve this problem, the more promising being Neural Ordinary Differential Equations (ODEs) that introduce the concept of continuous-time and depth models. Although the idea seems promising, the results are underwhelming compared to traditional neural networks such as Long Short-Term Memory (LSTM). Considering these limitations, MIT researchers introduced Liquid Time-Constant (LTC) networks that surpassed performance expectations. However, these networks carry problems of their own: the obsolete architecture used behind the scenes. This research project proposes a novel implementation of the LTC algorithm with a more modern architecture that uses Stochastic Differential Equations (SDEs). Furthermore, its application is demonstrated on a TS forecasting problem that has piqued the interest of many audiences worldwide – forecasting the price of Bitcoin (BTC).

The LTC with SDEs, dubbed "Liquid Time-Stochasticity" by the author, produced a more stable and robust implementation of continuous-time and depth models due to its ability to handle small noises. The solution utilized traditional Backpropagation Through Time (BPTT) to produce more accurate results with the trade-off of consuming more memory, which created a promising result in its application in the chosen domain - a percentage error of $2.5\% \pm 0.1$. It is worth noting that, utilizing adjoint sensitivities instead must be researched in the future as it is recommended.

Keywords: Time Series (TS) forecasting, Neural Ordinary Differential Equations (ODEs), Liquid Time-Constant (LTC) networks, Stochastic Differential Equations (SDEs).

Subject Descriptors:

- Theory of computation → Design and analysis of algorithms → Approximation algorithms analysis → Stochastic approximation.
- Mathematics of computing → Probability and statistics → Stochastic processes.

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Acronyms

AI Artificial Intelligence.

API Application Programming Interface.

AD Automatic Differentiation.

ARIMA Autoregressive Integrated Moving Average.

BPTT Back-Propagation Through Time.

BTC Bitcoin.

CT-GRU / RNN Continuous-time Gated Recurrent Unit / Recurrent Neural Network.

DL Deep Learning.

GPU Graphics Processing Unit.LSTM Long Short-Term Memory.

LTC Liquid Time-constant.

ML Machine Learning.

(s)MAPE Symmetric Mean Absolute Product Error.

MASE Mean Absolute Scaled Error.

MSE Mean Squared Error.

MVP Minimal Viable Product.

N-BEATS Neural Basis Expansion Analysis for interpretable Time Series.

NLP Natural Language Processing.ODE Ordinary Differential Equations.

POC Proof-Of-Concept.

REST Representational State Transfer.

RMSE Root Mean Squared Error.

RNN Recurrent Neural Network.

SOTA State Of the Art.

SDE Stochastic Differential Equations.

SGD Stochastic Gradient Descent.

TS Time Series.

UI User Interface.

XAI Explainable Artificial Intelligence.

CHAPTER 01. INTRODUCTION

1.1. Chapter overview

In this chapter, the author aims to identify and provide the reader with an overview of the current issues in time series forecasting and highlight what a liquid time-constant network is and what it aims to solve. In detail, the author will define the problem and evaluate the necessary literature to arrive at a justifiable research gap, respective research objectives, and challenges that would arise. The novelty within the chosen problem and the proposed solution are also stated.

1.2. Problem domain

1.2.1 Time series forecasting

TS forecasting is a significant business issue and an area where ML could create an impact. It is the foundation for contemporary business practices, including pivotal domains like customer management, inventory control, marketing, and finance. As a result, it has a comprehensive financial impact, with millions of dollars for subtle improvements in forecasting accuracy (Jain, 2017).

Having said that, although ML and DL have outperformed classical approaches for NLP and computer vision, the domain of TS still seems to be a struggle compared to classical statistical methodologies (Makridakis et al., 2018a;b). Most of the top-ranking methods in the M4 competition were ensembles of traditional statistical techniques (Makridakis et al., 2018b), while regular ML methods were nowhere near.

Therefore, this competition's winner was a hybrid model of LSTM and classical statistics (Smyl, 2020). Furthermore, they claimed that the only way to improve the accuracy of TS forecasting was by creating such hybrid models, which the author aspires to challenge in this research project.

1.2.2 Liquid Time-Constant (LTC) networks

LTCs are neural ODEs: hidden layers are not specified; instead, the derivative of hidden states is parameterized by neural networks (Chen et al., 2019). RNNs are successful algorithms for TS data modelling, if there exist continuous time-hidden states determined by ODEs (Chen et al., 2019).

Studies show that existing algorithms such as the CT-RNN (Funahashi and Nakamura, 1993; Rubanova, Chen and Duvenaud, 2019) and CT-GRU (Mozer, Kazakov and Lindsey, 2017) produce such performance. However, they have issues with expressivity and fixed behaviour once trained (Hasani et al., 2020). Therefore, the question arises: what would happen if there were unexpected changes to the characteristic of the inputs during inference? Additionally, these algorithms lose in generalization compared to even a simple LSTM network (Hasani et al., 2021), which raises another question, what is the point of defining a different and 'fancy' approach if they cannot work well in real-world applications?

Hasani et al. state that LTCs can "identify specialized dynamical systems for input features arriving at each time point" (2020, p1). The ability to exhibit stable and bounded behaviour demonstrates that the proposed approach yields better expressivity than traditional implementations.

The LTC state and their respective time constant "exhibit bounded dynamics and ensure the stability of the output dynamics", which is a prominent factor when inputs increase relentlessly (Hasani et al., 2020).

1.2.3 Cryptocurrencies

The word 'crypto' has been an enormous buzzword recently, especially BTC. It has even come to the point where crypto and BTC are used interchangeably.

Cryptocurrencies are a fully decentralized digital currency form; it is a form of a peer-to-peer system without the need for a third party, thus enabling safer online transactions (S. Nakamoto, 2008). BTC is the first and the most popular digital currency to date, piquing many academic researchers' interest (Rahouti et al., 2018).

However, being at the forefront of the digital currency world, it has developed high volatility, making it difficult to predict future rates and a disadvantage for multiple investors (Kervanci and Akay, 2020). Despite that, recent advances in ML and statistics have shown acceptable results in the analysis and prediction of cryptocurrencies, yet the root cause of these algorithms persists: they are static.

1.3. Problem definition

As of writing this report, there is no application of LTC networks in any domain since this novel neural ODE has only recently been announced (Hasani et al., 2020). Existing intelligent systems utilize more traditional approaches of neural nets developed some time ago.

Having mentioned that, most applications of ML available do perform quite well (ex: image classification, transfer learning, NLP), yet, as mentioned, the field of TS forecasting is subpar (Makridakis et al., 2018a;b). Existing TS forecasting algorithms cannot adapt to unforeseen changes in data streams; consequently, they could perform relatively poorly when used in areas of high volatility (in this case: the forecasting of BTC).

Building an algorithm inspired by the LTC architecture and its application on an ML domain that still can struggle could be the stepping stone for future intelligent systems by aiding further research. Additionally, as a supplement, it could provide hope to crypto investors for more straightforward predictions.

1.3.1 Problem statement

Existing TS forecasting systems cannot adapt to incoming data streams with unexpected changes and characteristics that are different from the data on which they were trained; implementing an algorithm capable of having the 'liquid' adaptability mentioned could be an advancement for more capable, accurate, and interpretable TS forecasting systems.

1.4. Research questions

RQ1: What are the recent advancements in TS algorithms that can be considered when building the algorithm?

RQ2: How can the algorithm be used to implement a TS forecasting system, and how will the challenges faced be overcome?

RQ3: What contributions can be made to the chosen domain?

1.5. Research aim & objectives

1.5.1 Research aim

The aim of this research is to design, develop & evaluate a novel algorithm inspired by the LTC so that it can build intelligent systems by developing a novel architecture for TS forecasting, which could be the stepping stone to be further expanded to other domains as well.

Specifically, this research project will produce a TS forecasting system utilizing the said algorithm, focused on the forecasting of BTC.

1.5.2 Research objectives

Research objectives are milestones that the author must achieve for the research to succeed.

Table 1: Research objectives (Self-Composed)

Objective	Description	Learning	Research
		Outcomes	Questions
Literature Review	Collate relevant information by reading, understanding, and evaluating previous work. RO1: Conduct preliminary studies and investigations on existing TS forecasting systems. RO2: Analyze the requirement for specialized TS algorithms. RO3: Conduct research on neural ODEs, LTCs & SDEs. RO4: Obtain deep insights into the architecture behind the LTC.	LO1, LO2, LO4, LO5	RQ1
Requirement Elicitation	Collect and analyze project requirements using appropriate tools and techniques. RO5: Gather the requirements and architectures of LTCs and SDEs. RO6: Collate the most up-to-date details of BTC. RO7: Design a schedule, associated deliverables, and the Gantt chart.		RQ1

Design	Design the architecture and a corresponding system		
	capable of effectively solving the identified		
	problems.		
	RO8: Design an efficient and novel LTC		
	implementation.	LO1	RQ2
	R O9: Design an automated flow to update the built		
	network with the latest data.		
	RO10: Design an ML pipeline for easy		
	deployments.		
Implementation	Implement a system that is capable of addressing the		
	research gaps.		
	RO11: Implement a novel LTC architecture.		
	R O12: Integrate the algorithm developed into a TS	LO1,	PO2
	forecasting application.	LO5,	RQ2
	RO13: Integrate the intelligent system into the	LO6, LO7	
	prototype to display forecasts.		
	RO14: Consider any legal, social, ethical &		
	professional issues upon implementation.		
Evaluation	Effectively test the algorithm implemented, the		
	system, and the respective data science model using		
	recommended techniques.		
	RO15: Create a test plan & test cases and perform	LO4	RQ2,
			R Q3
	RO16: Evaluate the developed algorithm and the		
	respective model against the mentioned evaluation		
	metrics.		
Documentation	Document the progression of the research project		-
	and inform about any challenges faced.		
	RO17: Document any legal, social, ethical &	LO6, LO8	
	professional issues faced and how the author solved		
	them.		

RO18: Create a coherent report of new skills	
obtained throughout the project plan and critical	
evaluations.	

1.6. Novelty of the research

1.6.1 Problem novelty

The core novelty of this research is that TS algorithms and respective systems built utilizing them are static and lack adaptability (Hasani et al., 2021).

1.6.2 Solution novelty

A solution for this problem is a dynamic algorithmic architecture that can adapt and change its underlying mathematical expressions and evaluation strategies based on changes in the incoming data streams. Additionally, further enhancements are required to avoid sudden and tiny changes that are common in TS data.

1.7. Research gap

The literature defines only a single paper for the proposed algorithmic solution (Hasani et al., 2020). Where every other work is not directly related to the algorithm but is to the family of neural ODEs (CT-RNN (Rubanova, Chen and Duvenaud, 2019) and CT-GRU (Mozer, Kazakov and Lindsey, 2017)) and the secondary problem domain of cryptocurrencies and TS. Furthermore, no algorithmic solution exists for the proposed LTC architecture for model implementation.

Gap in existing forecasting algorithms

It is also worth noting that, because of this, existing forecasting solutions are all implemented using traditional deep neural net approaches (ex: LSTM (Hochreiter and Schmidhuber, 1997)) that are static and hence have the limitation of not being able to learn and adapt during inference (Hasani et al., 2020), which results in the model's accuracy degrading overtime – a 'data drift' (Poulopoulos, 2021).

Gap in chosen algorithm

The proposed LTC architecture uses a sequence of linear ODEs, which are now considered obsolete and lack rapid adaptability. Recent advancements in this field suggest the usage of SDEs

instead, as they are more flexible (Duvenaud, 2021). An additional issue is that ODEs model 'deterministic dynamics' – uncertainty, or any unobserved interactions cannot be modelled, which is inevitable in TS data.

1.8. Contribution to the body of knowledge

In a nutshell, the author desires to answer the following question:

• Would a novel architecture built by a novel algorithm utilizing an LTC architecture with SDEs instead of ODEs be an advancement for TS forecasting?

1.8.1 Contribution to the research domain

An implementation of the LTC algorithm with the above-mentioned change will be developed, following the proposed architecture, to facilitate the model creation. Additionally, the algorithm built will be generalized without being problem-specific so that researchers can apply it elsewhere to evaluate its performance and identify whether the architecture would also be an advancement to other domains.

1.8.2 Contribution to the problem domain

Having understood the issues in the current literature, a solution capable of solving the mentioned issues could advance future research. Adapting to unforeseen changes and being highly expressive could be the stepping stone within the TS forecasting community.

Moreover, based on the above critique, creating a more robust forecasting solution considering the mentioned factors (Twitter, Google Trends) could mean that the highly volatile market of cryptocurrencies could be predicted much more efficiently and be the way forward for investors.

1.9. Research challenge

Existing architectures scale up, and the LTC scales down - with more expressive nodes (Hasani et al., 2020). Having adapted to the "deeper is usually better" mindset of deep neural nets, a challenge opens up in identifying the requirement of scaling down and what a neural ODE aims to solve.

LTCs are a new approach with only a single research paper regarding its proposed solution. Currently, it is only in the experimental stage and utilizes a novel formulation compared to other existing neural ODEs (Hasani et al., 2020). The broader domain of neural ODEs (Chen et al., 2019) is also relatively new; hence the scarcity of references could create more challenges for further research or implementation of systems.

SDEs are an advanced topic in mathematics, and modelling them as neural SDEs have had a couple of research conducted; however, they were primarily for specific purposes. Therefore, no generic papers exist for neural SDEs, unlike neural ODEs, which makes modelling difficult.

Currently, existing TS forecasting systems are built using statistical ensemble methods (Makridakis et al., 2018b) or traditional neural net architectures (Hasani et al., 2021), which creates a new challenge where there is no reference implementation.

The chosen domain of application is an open system. Open system forecasting is usually poor and generally difficult to beat the naïve forecast (A naïve forecast is not necessarily bad, 2014) since it can depend on any external factor. Therefore, there is the possibility of discouragement from continuing the research if the results are not as expected.

1.10. Chapter summary

In this chapter, the author provided an overview of the research project carried out, respective reasons for the research and problem to be a novelty, and the challenges they can face upon solving it. Furthermore, the necessary goals that must be aimed to consider the research successful were proposed and mapped to the learning outcomes that must be attained by the chosen degree.

CHAPTER 02. SOFTWARE REQUIREMENTS SPECIFICATION

2.1. Chapter overview

In this chapter, the author focuses on identifying the requirements and the steps followed to gather these requirements. In detail, possible stakeholders, alongside their interaction points and roles, are documented using a rich picture diagram and a stakeholder onion model. Furthermore, the requirement-gathering techniques followed and the insights obtained to analyze and produce functional and non-functional requirements, use case diagrams, and prototype descriptions are defined.

2.2. Rich picture

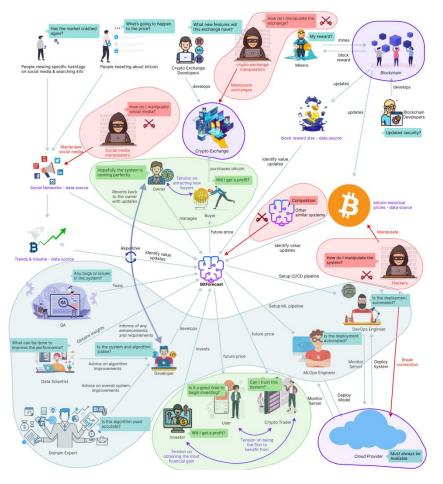


Figure 1: Rich picture diagram (Self-Composed)

A clearer version can be found Here

The above diagram illustrates a helicopter view of the wider environment, how specific stakeholders would interact with the system, and how they would benefit. Furthermore, the possibilities of negative impact on the design and possible critical analysis are identified, alongside the knowledge the researcher could receive to improve the system.

2.3. Stakeholder analysis

The following section recognizes key stakeholders associated with the system, their relationships, and their respective roles. The stakeholder onion model depicts this information, and the stakeholder viewpoints further detail it.

2.3.1 Stakeholder onion model

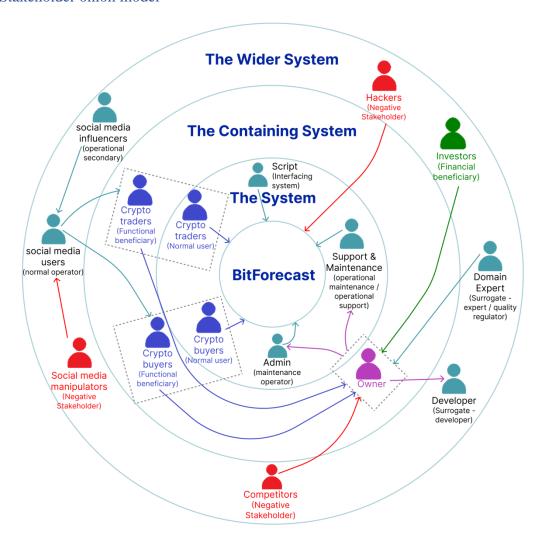


Figure 2: Stakeholder onion model (*self-Composed*)

2.3.2 Stakeholder viewpoints

Table 2: Stakeholder viewpoints (self-Composed)

Stakeholder	Role	Benefits/Description
Support &	Operational – support &	Maintains the health of the system and attends to
Maintenance	Operational - maintenance	user inquiries.
Admin	Maintenance operator	Monitors and updates the system when
		necessary.
Script	Interfacing system	Fetches data and makes sure system is updated.
Owner	Owner &	Manages other operators, listens to feedback,
	Operational - administration	and communicates with other stakeholders.
Crypto trader	Functional beneficiary	More convenient for deciding whether to
Crypto buyer		purchase or sell currently held assets.
Investor	Financial beneficiary	Makes profit by investing in the system, upon
		marketing, or user subscriptions.
Domain	Surrogate – expert &	Provides advice on overall system
expert	Quality regulator	improvements.
Developer	Surrogate – developer	Develops the system.
Social media	Operational - secondary	Influence users, drive trends, and provide
influencers		thoughts.
Social media	Normal operator	Get influenced to invest or sell currently held
users		assets.
Competitors	Negative stakeholder	Build competing products that outperform or
		have better value.
Social media		Manipulate set trends and influencer thoughts.
manipulators		
Hackers		Disrupt the system and corrupt data.

2.4. Selection of requirement elicitation methodologies

Researchers can carry out requirement elicitation methodologies to gather requirements. The following table discusses the selected ones and their purpose.

Table 3: Requirement elicitation methodologies (Self-Composed)

Method 01: Literature review

An exhaustive literature review has been conducted to identify a respectable research gap in a cutting-edge research field and a domain of interest. The author studied existing systems to determine limitations and future research. A brief understanding of the implementation methods was also identified, alongside necessary best practices.

Method 02: Observations

Upon conducting the literature review, analysis of similar systems is an added advantage. Validating and evaluating its viability is paramount as the chosen research domain is relatively new. Existing algorithmic POCs must be studied and thoroughly assessed, as this will provide the author with the necessary insights and techniques to implement.

Method 03: Interview

Interviews can help gather knowledge and insights into more theoretical concepts that will be helpful behind the scenes for implementing the research component and associating with and answering the proposed research questions. The author can interview specific niche experts with knowledge of neural ODEs and SDEs to obtain said intuition, which they cannot acquire by conducting a survey.

Method 04: Survey

Obtaining insights and expectations from end users can be gathered by conducting a survey, specifically, the questionnaire. Upon receiving this prominent information, the author can decide whether the proposed system is helpful for the target audience and understand how the target audience intends to benefit from it. As they are large in sample size, the survey is a powerful choice for data collection.

Method 05: Prototyping

Prototyping will allow the developer to iterate between implementations and improvements. As the architecture is more novel, this procedure will be used abundantly as a straightforward approach to obtaining the optimal performance is unlikely and will take time.

2.5. Discussion of findings

The essential stakeholders were separated into groups, and each group was analyzed in the most suited methodology. The table breakdown of these stakeholders is available in **APPENDIX A.1**.

2.5.1 Literature review

Table 4: Literature review findings (Self-Composed)

Citation	Discussion of findings	
Research domain		
Hasani et al., 2021	Existing solutions in TS forecasting use traditional neural nets or statistics.	
Hasani et al., 2020	Traditional neural ODEs were underwhelming in performance compared	
	to existing neural nets.	
Duvenaud, 2021	The proposed architecture by Hasani et al. (2020) uses the obsolete ODE,	
	which lacks rapid adaptability - using an SDE instead can improve	
	flexibility further. Therefore, combining both would produce the optimal	
	architecture.	
Problem domain		
Abraham et al.,	Based on the reviewed literature, work that included multiple exogenous	
2018; Valencia et	features had not utilized a non-linear model.	
al., 2019		
Fleischer et al.,	Work that used a non-linear model had not included the additional features	
2022; Serafini et	et the author aims to include. As implied, a non-linear model with multiple	
al., 2020	features would produce the optimal solution.	

2.5.2 Observations

Table 5: Observations findings (Self-Composed)

Criteria	Discussion of findings
To find approaches to	The author noticed that POCs of neural SDEs are available sparingly
creating a neural SDE	and had yet to be utilized in an ML system like the proposed solution.
to implement the core	It is also safe to assume that building the research component could
research component	be later used as a baseline for future neural SDE implementations.
To find approaches	Although POCs of BTC forecasting systems that use LSTMs and
taken to implement the	statistical algorithms are available in abundance, what was noticed is
additional component	that they all naively utilize only the closing price as a feature or the
of BTC forecasting.	closing price with the Twitter sentiment. Considering this, the author

decided to build the primary research component first so that the
algorithm could be used to build ML systems and create the additional
BTC forecasting system utilizing as many exogenous features as
possible that can be of effect. Therefore, insights into implementing
the supplementary system and effective evaluation techniques were
acquired.

2.5.3 Interviews

Interviews were conducted to obtain domain expertise and any information that the author may have missed and could be significant. The author interviewed only a few candidates as the research domain is new and unknown; fortunately, they were the most knowledgeable. The author also interviewed a candidate experienced in the problem domain area. The findings were analyzed using thematic analysis and presented below. The participants' affiliations expertise areas are available in **APPENDIX A.3** with necessary evidence for the respective finding.

Table 6: Interview thematic analysis codes, themes & conclusions (Self-Composed)

Code	Theme	Conclusion	
Research compo	Research component		
Algorithm	Research	The interviewees validated the research gap and the defined	
architecture	Problem &	problem. They were also happy that the author had been	
	Gap	conducting this research, as few papers were published in this	
		domain.	
Resource	Requirements	The interviewees were concerned that ODEs and SDEs could	
intensive		be expensive to compute and hence could take some time,	
		which can be an issue given that the forecasts must be produced	
		quickly. Therefore, the author must optimize the model as	
		much as possible to avoid user-unfriendliness.	
Obsolete,	Advice	The author had initially planned on only creating an	
Inflexible		implementation of the LTC architecture proposed by Hasani et	
		al. (2020). However, the author could further improve the	
		architecture by using SDEs instead (the base LTC uses ODEs),	

		which could manifest into a novel algorithm, which is the
		author's current aim as it carries more significance and a
		potentially more outstanding contribution.
Visualizations,	Other	What was concluded here was that XAI is primarily present for
Explainability	suggestions	image classification, and there needs to be more literature on
		the TS domain. However, XAI integration into TS modelling
		could be confusing and complicated due to the temporal
		component. Additionally, XAI for SDEs needs to be
		researched, which the author could look into if time permits.
Problem domain	n	
External	Robustness	The interview was an additional validation for the data
features		collected in the survey. Most suggestions were to use as many
and trends		extra features as possible to make the model robust. Therefore,
		the author will ensure that they utilize the mentioned
		exogenous features.

2.5.4 Survey

A survey was conducted to gather requirements from the target audience to infer functionalities to implement for the supplementary product developed.

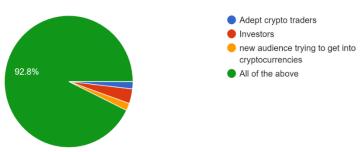
Table 7: Survey analysis (Self-Composed)

Question	How much would a system capable of assuming tomorrow's price benefit
	you?
Aim of question	To identify whether the system is beneficial in the first place
Findings & concl	usions
	 I do not trust the market graphs to convince me on tomorrow's price; hence, it will definitely be useful It will be useful I doubt it will be useful I do not think it will be useful: I trust my instincts more
All the participants believed that the proposed system would be beneficial – where the majority	
had a greater bel	lief than others. Having obtained this information, it is evident that the

supplementary proposed system will be helpful. As identified, not a single participant thought that the system would not be beneficial. Notably, this validates the problem domain and gives the author the 'green light' to go ahead.

Question	Who do you think would benefit from this system?
Aim of question	To identify beneficiaries and target audience

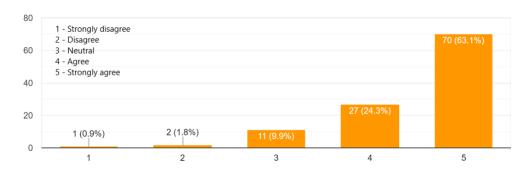
Findings & conclusions



The majority of the participants believed that the system would be beneficial for expert traders, investors as well as a new audience. However, what can be identified, is that a minute portion of participants assumed that the system would be helpful primarily for people who are already involved in the market – this is some evidence that the system must be made as simple as possible to attract a newer audience. It is also identified to help only a new audience – this is evidence that the system must not be immature.

Question	This system will also benefit people who are not experts in cryptocurrencies
Aim of question	To identify whether non-technical crypto traders would benefit

Findings & conclusions

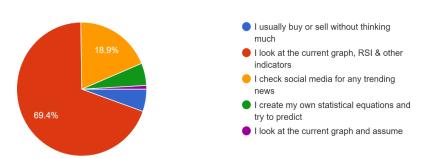


The responses to the above question show that the system will also apply to audiences who are not cryptocurrency experts. This question goes hand in hand with the previous question to

confirm whether the system can target a newer audience of people to get into cryptocurrencies rather than just focusing on a niche audience who are experts or current investors/traders.

Question	How do you decide whether to buy or sell assets?
Aim of question	To understand how a buyer/seller proceeds with their decision

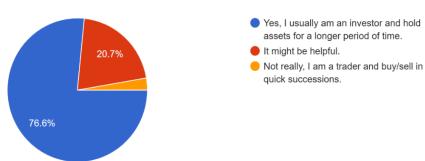
Findings & conclusions



The responses to the above question are more of a 'Know Your Customer' question with no specific project-related purpose. Nevertheless, what can be identified is that most of the respondents have some knowledge of cryptocurrencies, where almost 70% are experienced in trading/investing cryptocurrencies – a great insight as nearly all the respondents have specific knowledge. Therefore, the author could use this to reach out to the respondents (whom they gathered requirements from) during the evaluation phase.

Question	Do you think predicting a more future date (ex: a week from now) is as
	important as tomorrow's price?
Aim of question	To identify whether a greater future date prediction is also necessary

Findings & conclusions

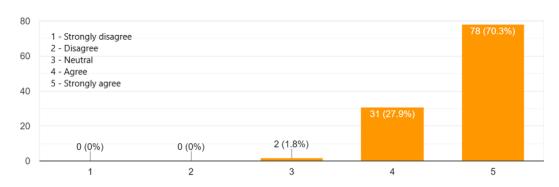


The author initially considered only having a single horizon forecast, considering the limited time. However, based on the above responses, it is evident that the audience would also expect

forecasts for multi horizons. Therefore, the author will additionally aim to implement the ability of multi-horizon forecasting.

Question	Social media trends can impact the price
Aim of question	To identify whether the community believes that social media trends impact
	the price

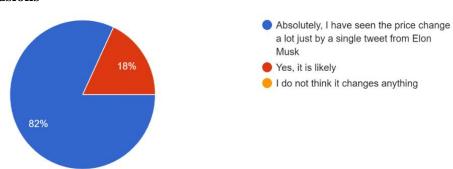
Findings & conclusions



The majority of the respondents believe that social trends impact the price. Therefore, it is necessary to consider as many trends as possible. Considering the project's limited time and scope, the author has decided to use Twitter volume and Google Trends; however, Reddit, Facebook, and others would also provide insights and could be considered future work.

Question	If a highly influential person tweets about Bitcoin, do you expect the price
	to tip to the side in favor of their tweets meaning?
Aim of question	To identify whether including Twitter sentiment is beneficial and to confirm
	the problem domain contribution.

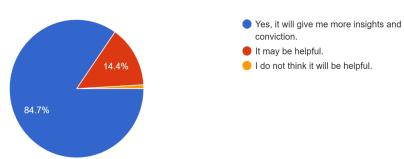
Findings & conclusions



All participants believe that the current thoughts on social media affect the price in one way or another. Most participants further thought that the tweeter's influence adds additional significance. Considering this and the previous question, it is apparent that the mentioned social factors contribute to price changes, which validates the problem domain contribution. Additionally, based on the responses, the requirement for NER and weighted search is more apparent to give more weightage to specific tweeter's sentiments.

Question	Would it be helpful to obtain a range of prices rather than a point price? (Ex:
	10,000 - 15,000 instead of 12,500)
Aim of question	To identify whether including uncertainty estimates is beneficial

Findings & conclusions



The author initially decided on only providing a point forecast for the system, as this research aims to develop a novel architecture for TS forecasting. However, based on the responses and while conducting prototyping, it became evident that a single-point prediction is likely to be less valuable than a range of prices. A point prediction is implausible to be accurate, which makes the requirement of uncertainty estimates more vital.

Question	What functionalities would you expect to have in a bitcoin forecasting
	system?
Aim of question	To identify any additional requirements

Findings & conclusions

To analyze opened ended questions, the author can perform thematic analysis. The analysis, including the theme and related codes, is available in **APPENDIX A.2**.

Based on the analysis conducted, it is evident that the participants would appreciate some Explainability. Including XAI is an addition that the author could look into if time permits. The participants also mentioned that the system would be better performant and robust if it utilized as many exogenous factors while making it as simple as possible. Based on these findings, the author will aim to include as much Explainability as possible and make it mandatory to use the mentioned exogenous features.

Question	Any extra feedback you would like to provide?		
Aim of question	No specific reason – is mainly used to obtain any additional feedback		
Findings & conclusions			
The respondents submitted a few motivational sentences to inspire and motivate the author to			
perform their best.			

2.5.5 Prototyping

Table 8: Prototyping findings (Self-Composed)

Criteria

To explore the feasibility of creating the primary research component.

Discussion of findings

Upon iterative prototyping, challenges that the developer did not expect to arise emerged. Challenges ranged from finding a suitable dataset to implementing the algorithm itself. Building the algorithm is intimidating, as no proper reference exists. They realized that, alongside traditional DL theories, implementing the algorithm required more profound knowledge and understanding of SDEs and differential solvers. Furthermore, they had depended on the Twitter API to get tweet sentiment of specific days; however, this was impossible as Twitter had updated the API only to provide tweets of the past seven days. Fortunately, there were public datasets available up to a certain point in time; therefore, they had to use a third-party library to scrape tweets of dates ahead of that point in time. Moreover, upon experimentation, they gained an epiphany that solely the point price prediction would be useless; instead, a range of uncertainty estimations that provide a range of values would be more helpful. Furthermore, any explainable insights from the networks can be valuable to provide intuition into the forecast generation.

2.5.6 Summary of findings

ID	Finding	Li	0	Su	In	Pr
		Literature Review	Observations	Survey	Interview	Prototyping
		ture	vatic	7	iew	ypin
		Rev	ns			0,cd
		iew				
Res	earch component					
1	Validate research domain and gap.	✓	✓		✓	
2	The novelty of the research hypothesis (an architecture	✓	✓		✓	
	inspired by the LTC).					
3	Neural ODEs are an advancement for TS forecasting.	✓			✓	
4	Try to integrate latent SDEs into an LTC architecture for				✓	✓
	a novel algorithm implementation instead of using the					
	same obsolete latent ODE.					
Pro	blem domain					
5	The system will be of use to experts and new audiences.			✓		
6	Social trends can be a source of impact.	✓		✓		✓
7	Well-known influencers' opinions cause a more drastic	✓		✓		
	impact.					
8	A system combining all exogenous features in a non-	✓				
	linear model has yet to be explored.					
9	Including a range of prices than a point price is an added			✓		✓
	advantage and can produce more credibility.					
10	Implementing an Explainability component will			✓		√
	drastically make the system more credible.					
11	A system capable of changing its hyperparameters would			✓		
	make it worthwhile for experts.					

2.6. Context diagram

The following diagram depicts the system's boundaries and interactions. Determining them before the development will provide the author insight into how the information should flow.

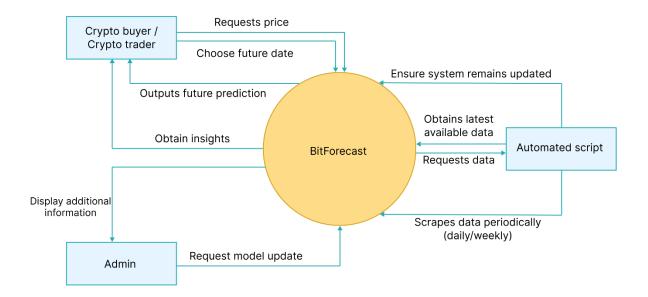


Figure 3: Context diagram (Self-Composed)

2.7. Use case diagram

The below diagram demonstrates the "sea level" use cases of the proposed system, describing the functionalities at a high level the system will provide end users with.

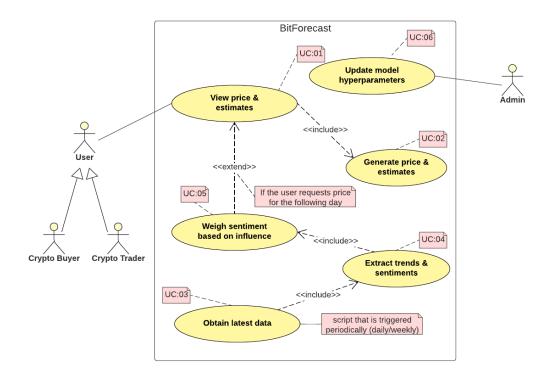


Figure 4: Use case diagram (Self-Composed)

2.8. Use case descriptions

The core use case description is presented below; any sub-descriptions are available in **APPENDIX A.4**.

Table 9: Use case description UC:01; UC:02 (Self-Composed)

Use case	Display price & estimates
Id	UC:01; UC:02
Description	Display future prices and their respective uncertainty estimations based on
	the user's choice of date, alongside any Explainability insights.
Actor	User
Supporting	None
actor (if any)	
Stakeholders (if	Crypto buyer, crypto trader
any)	

Pre-conditions	All the data must be scraped and preprocessed, and the forecast should have
	been generated.
Main flow	MF1. User requests tomorrow's price.
	MF2. The system recognizes the need to utilize available exogenous
	features.
	MF3. The system ensures data available is up-to-date (must be in this case,
	as the script will run periodically automatically). If not:
	1. Obtains the latest available data.
	2. Performs sentiment analysis and self-retrains.
	MF4. The system generates price and upper and lower estimations.
	MF5. Display output to the user along with any insights.
Alternative	AF1. The user requests the price for a date ahead of tomorrow.
flows	AF2. The system recognizes the inability to utilize other features.
	AF3. The system generates price and upper and lower estimations.
	AF4. Display output to the user along with any insights.
Exceptional	EF1. The system could not generate a prediction – display a user-friendly
flows	error message.
Post-conditions	The user is displayed with a forecast and necessary insights.

2.9. Requirements

2.9.1 Functional requirements

The functional requirements were determined based on priority using the 'MoSCoW' technique, which is detailed in **APPENDIX A.5**.

Table 10: Functional requirements (Self-Composed)

ID	Description	Priority	Use
			Case
Research level			
FR1	A robust and scalable implementation of the novel algorithm must	M	-
	follow recommended standards.		

FR2	The developed algorithm must be able to be used as existing layers	M	-
	and algorithms (ex: LSTM, CNN).		
System	level		I
FR3	Users must be able to choose a future date.	M	UC:01
FR4	Users must be able to view the point prediction price.	M	UC:03
FR5	The system must generate the point prediction price based on the	M	UC:02
	user's choice of date.		
FR6	The script must obtain the latest data available periodically.	M	UC:04
FR7	The script must extract trends and sentiments from obtained data.	M	UC:05
FR8	Users should be able to view a range of prices along with the	S	UC:03
	single-point price.		
FR9	The system should generate higher and lower bound uncertainty	S	UC:02
	estimations.		
FR10	The GUI should plot the forecast with the current prices in a single	S	UC:03
	graph to show the growth/decline.		
FR11	The script should weigh sentiment based on any influential	С	UC:06
	personnel's tweet.		
FR12	The system could display some insights to the user, such as a	С	UC:03
	highly influential tweet that made it predict the price.		
FR13	Admins could authenticate and update the model with different	С	N/A
	parameters.		
FR14	Admins could get additional information about a prediction, such	С	N/A
	as the evaluation metric and accuracy.		
FR15	The system will not produce forecasts for other cryptocurrencies.	W	N/A
FR16	The system will not produce real-time forecasts (ex: hourly).	W	N/A

2.9.2 Non-functional requirements

The author prioritized the non-functional requirements based on the following two levels:

- Important best to have them.
- Desirable better to have them.

Table 11: Non-functional requirements (Self-Composed)

ID	Requirement	Description	Priority
NFR1	Performance	The system must take little time to generate a forecast,	Important
		given that a couple of extra features are in use.	
NFR2	Performance	The system must not unnecessarily keep updating its data.	Important
NFR3	Usability	The user interface must be simple and effective and	Important
		provide user-friendly errors if any occur.	
NFR4	Maintainability	The author must document the codebase well in case of	Important
		future reference, mainly the algorithm development	
		repository.	
NFR5	Quality	The output must be of good quality so that it provides	Desirable
		vital insights.	
NFR6	Scalability	The system must be deployed to a cloud with no scaling	Desirable
		issues and good resources for efficient and optimal	
		performance, especially as there could be multiple	
		concurrent active user requests.	
NFR7	Security	The system must be resilient to attackers, specifically to	Desirable
		prevent data manipulation.	
NFR8	Compatibility	To ensure compatibility, the developer must test the	Desirable
		system on most browsers and mobile phones.	
NFR9	Availability	In critical failures, the primary operator must be available	Desirable
		and solve issues as soon as possible.	

2.10. Chapter summary

In this chapter, the author defined necessary stakeholders interacting with the system and described how the interaction would occur, visualizing this using a rich picture diagram and Saunder's Onion model. Additionally, requirement elicitation techniques, their reasoning, and their respective findings were discussed and presented. Finally, they specified the use cases, associated descriptions, and system requirements.

CHAPTER 03. DESIGN

3.1. Chapter overview

In this chapter, the author focuses on selecting suitable architectural structures for implementation, considering the gathered requirements. Specifically, high-level, low-level, and associated design diagrams are presented alongside necessary UI wireframes and the reasoning behind each choice. Moreover, the novel algorithm architecture is also proposed.

3.2. Design goals

Table 12: Design goals of the proposed system (Self-Composed)

Goal	Justification
Performance	A typical flow in TS forecasting requires retraining the model whenever a
	prediction is made, as the data the model had been trained on could be
	outdated. However, as multiple features are being used in the proposed system,
	this can severely hinder performance. The author can avoid this by storing past
	data and only fetching needed data when necessary; as a further step, the data
	can be fetched periodically. The model can automatically be retrained
	beginning each day (which would deem the retraining step on each inference
	unnecessary) as the solution proposed.
Usability	Based on the analysis obtained during the requirement-gathering phase, there
	were mixed thoughts on whether the application would benefit people who are
	not experts in cryptocurrencies. Therefore, this requirement is mandatory as it
	is crucial to create a system that is as user-friendly as possible to be used by
	users across all levels of expertise.
Quality	The output must be of the highest possible quality. Also, as identified in the
	gathered requirements, the system must display a range of prices to provide
	more conviction. Additionally, providing insights into how the model made
	the inference is an added benefit if time permits.

Maintainability	As implied by the author, the research must yield two products for the project
	to be successful. The goal of maintainability is solely for the research product
	proposed. The architecture of the algorithm must be optimal and independent
	to be able to be used as a reference for future research.

3.3. High level design

3.3.1. Architecture diagram

The system's high-level architecture design is depicted below. The author chose a three-tiered architecture because of the distinct separation of concerns of the presentation, logic, and data layers.

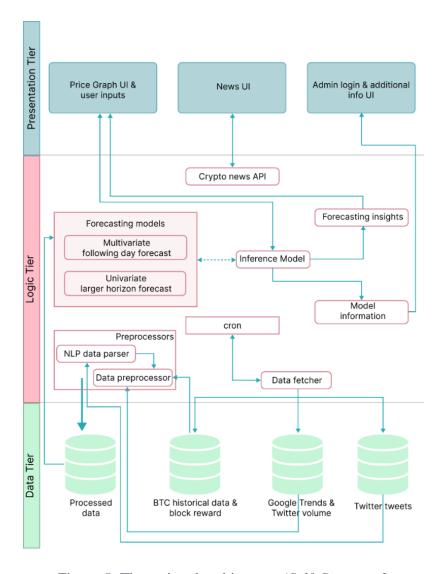


Figure 5: Three-tiered architecture (Self-Composed)

3.3.2. Discussion of tiers of the architecture

Data Tier

All data in this layer are fetched from an API and stored in individual documents to ensure updated data is available whenever necessary.

- BTC historical data & block reward historical data of BTC closing prices of the past several years and the associated block reward obtained for mining BTC.
- Google Trends historical data of the number of searches made each day that are BTC-related.
- Twitter volume historical data of the number of tweets posted each day that are BTC-related.
- Twitter tweets historical data of the tweets posted that are BTC-related.

Logic Tier

The logic tier consists of the base logic performed on the data in the data tier to provide an output in the presentation tier.

- Preprocessors consist of code required to process the raw data fetched from the API's so that the forecasting model can use it.
 - Data preprocessor required for general preprocessing steps such as normalization and cleaning.
 - NLP data parser required to perform sentiment analysis on the tweet data and named entity recognition to give more weightage to specific tweeter's sentiment.
- Data fetcher & cron the automated scheduler that the script will run periodically to ensure that the data and model are up-to-date.
- Forecasting models models that will be used to provide forecasts.
 - o Multivariate following-day forecast utilized for the following-day forecasts.
 - Univariate greater horizon forecast utilized for forecasts requested days ahead of the following day.
- Model information extra information of the model that the admin could view (ex: accuracy, no. of epochs).

- Forecasting insights additional information presented to the user to demonstrate forecasting-related Explainability.
- Crypto news API an additional third-party API to provide users with daily cryptocurrency news.

Presentation Tier

The point of interaction where the user interacts with the system.

- Price graph UI & user inputs main UI of the MVP that is presented to the user. It would display the current pricing graph, provide the user options to choose a future date, and generate a new chart with the inference.
- News UI a minor sub-feature that will display news about the cryptocurrency world.
- Admin login & additional info UI a 'could have' feature that will provide an authorized user to obtain information about the current model in use and, further, provide the ability to retrain the model by adjusting hyperparameters in use.

3.4. System design

3.4.1. Choice of design paradigm

As identified in previous chapters, the choice of design paradigm is SSADM. To re-elaborate, as this research is primarily focused on developing a novel architecture with a novel algorithm, extensive experimentation is paramount. Furthermore, the selected programming languages do not promote OOP; instead, they encourage using function-based modules and components.

3.5. Design diagrams

3.5.1. Data flow diagrams

The data flow diagrams are depicted using level 0, level 1, and level 2, where level 0 is the context diagram presented in the SRS chapter.

3.5.1.1. Level 01 data flow diagram

The level 01 diagram is an extensive breakdown of the core components proposed in the context diagram.

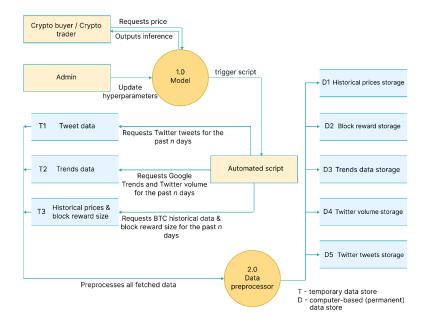


Figure 6: Data flow diagram - level 01 (Self-Composed)

3.5.1.2. Level 02 data flow diagram

The level 02 diagram is a more extensive breakdown of the core data preprocessor component proposed in level 01.

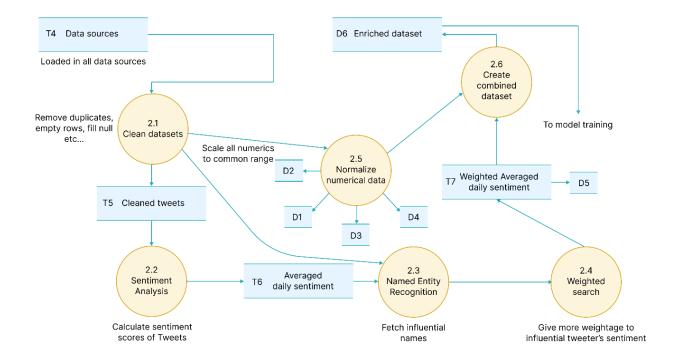


Figure 7: Data flow diagram - level 02 (Self-Composed)

3.5.2. Algorithmic design

Upon gathering requirements to implement the research component, the author realized they could further enhance the existing LTC architecture by integrating flexible latent SDEs instead of the current ODEs. The author will therefore attempt to design and evaluate a novel algorithmic implementation inspired by the original LTC proposed by Hasani et al. (2020), which can be considered their primary contribution to the body of knowledge. A simple illustration is available in **APPENDIX B.1** to gather intuition alongside an in-depth derivation and explanation of the proposed formula.

3.5.2.2. Algorithm proposed by the author

Upon studying the architecture proposed by Hasani et al. (2020), the author could utilize a linear system of SDEs to declare the flow to manifest a potentially novel algorithm with more flexibility for instantaneous adaptation of tiny changes. Moreover, this is an excellent enhancement as the additional component being developed belongs to the open market, which can have small instant price changes. The below formula is what the author proposes:

$$\frac{dx(t)}{dt} = -\left[\frac{1}{\tau} + f(x(t), I(t), t, \theta) - \sigma B\right] x(t) + f(x(t), I(t), t, \theta) A$$

Where;

τ Time-constant

x(t) Hidden state

I(t) Input

t Time

f Neural network

 θ , A Parameters

B Noise (Brownian motion)

o Intensity of noise (parameter)

Algorithm forward propagation by SDE solvers

Hasani et al. (2020) determined that their LTC architecture that uses a linear system of ODEs was 'stiff equations'. They also found that regular Runge-Kutta was not suitable for solving LTCs; therefore, they designed a custom ODE solver by combining both implicit and explicit Euler methods.

As this system uses SDEs, SDE solvers must be used. As Hasani et al. (2020) determined, the architecture is a system of stiff equations. Therefore, as Press et al. (2007) decided, researchers must use an implicit solver to ensure stability. Additionally, researchers can combine an explicit solver to achieve further stability. Therefore, the author will use an SDE solver, which is implicit, and if time permits, create a further enhanced custom SDE solver by fusing an explicit solver within.

Based on the author's research, the SDE equivalent for ODE Euler methods is the Euler-Maruyama method; this is the recommended solver as it can handle all forms of noise (Li et al., 2020). Combining the explicit Euler-Maruyama solver within to create a custom solver is something researchers should explore in the future.

How to train the network?

Training these networks has a trade-off between accuracy and memory. Chen et al. (2019) promoted the use of the adjoint sensitivity method to perform reverse-mode AD, which is more memory efficient. Hasani et al. (2020) mentioned that this method introduced more numerical errors and opted to use the traditional BPTT approach, which is more accurate but consumes more memory. Although there exists a technique of adjoints specifically for SDEs, they cannot be used, as determined by Tzen and Raginsky (2019), and hence requires a custom-built backpropagation rule.

For this research, the author will opt for the approach by Hasani et al. (2020) to give more precision and as the author is time constrained to implement a custom backpropagation algorithm. Researchers must investigate reverse-mode AD in the future as it is the recommended approach when memory efficiency is more important. It is also worth noting that using the BPTT approach carries added benefits, such as being able to be used as an RNN layer alongside the popular optimization algorithms that are very familiar (ex: Adam, SGD) (Hasani et al., 2020).

3.5.3. Algorithmic analysis

The notable difference between the proposed architecture and traditional neural ODEs proposed by Chen et al. (2019) is the traditional BPTT approach instead of the recommended adjoint sensitivity. The below table demonstrates the difference in the complexities of these approaches.

Table 13: Complexities of BPTT and adjoint sensitivity

Note: L = number of steps

	BPTT	Adjoint sensitivity
Time	O(L)	O(LlogL)
Memory	O(L)	O(1)
Forward accuracy	High	High
Backward accuracy	High	Low

What can be noticed from the above table is that the traditional BPTT approach yields more accurate results, with the trade-off of consuming more memory. Therefore, to obtain the best result possible, the author chose the approach of the traditional BPTT.

3.5.4. System process activity diagram

A summarized system flow activity diagram that end-users will follow is presented below.

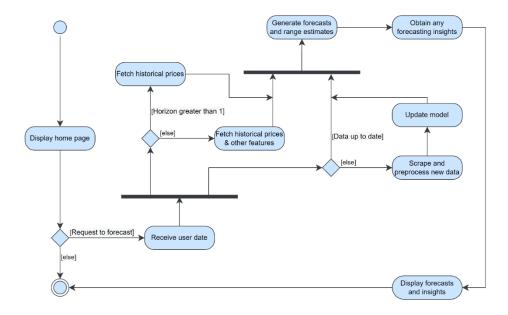


Figure 8: System process activity diagram (Self-Composed)

3.5.5. UI design

The author had decided to implement a web application for the supplementary application being built due to convenience. The low-fidelity wireframes designed to be of use are available in **APPENDIX B.2**.

3.6. Chapter summary

This chapter presented the design of the core novel algorithmic architecture, the necessary intuition behind it, and the reasons for taking specific directions over others. Additionally, it illustrated the system's design, architecture, and data and system flow alongside the wireframes that would demonstrate them in the end application.

CHAPTER 04. INITIAL IMPLEMENTATION

4.1. Chapter overview

In this chapter, the author describes the core implementation of the system and the necessary decisions taken to approach that implementation. Moreover, the chosen tools, languages, and technologies are presented alongside their reasoning.

4.2. Technology selection

4,2.1. Technology stack

The chosen technologies are depicted in the diagram below.

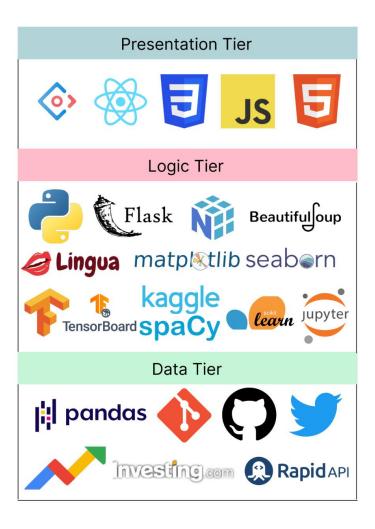


Figure 9: Tech stack (Self-Composed)

4.2.2. Selection of data

Table 14: Dataset sources (Self-Composed)

Dataset	Source
BTC historical data	From a third-party investing.com API.
BTC block reward size,	From a public dashboard that provides multiple different information
BTC Twitter volume	about a specific cryptocurrency.
BTC tweets	Tweets from 2014-2019 were downloaded from Kaggle – the remaining dates were extracted from a Twitter tweet scraper.
BTC Google Trends	From the PyTrends library that provides Google Trends data.

The multivariate single-horizon forecasting model combined the above data, while the univariate multi-horizon forecasting model solely used the historical data. Gathering the data was long and arduous as it was not as simple as downloading available datasets, and specific APIs being rate-limited. Dedicated python scripts were written to extract the data and to streamline updating data. The author will publicize these scripts to facilitate future research.

4.2.3. Selection of programming language

Programming languages were analyzed before development. Specifically for three main aspects: the client, the data science component, and the API communicating between the model and the client. Based on the analysis conducted in **APPENDIX C.1**, the author decided to use **Python**.

To develop the user interface, not much competition is present to analyze. **JavaScript** is the stand-alone leader and is the author's choice, as it is dynamic and can handle user interactions seamlessly. Although recent technology has presented the usage of C# for frontend development, high latency issues and lack of community knowledge are a downfall.

APIs are required to set up the communication between the model and the user interface. Multiple technologies are available for API development. The author chose **Python** as their core data science component is also built using Python; therefore, utilizing the same language would reduce the time taken to learn new languages for insignificant reasons.

4.2.4. Selection of development framework

4.2.4.1 Deep Learning (DL) framework

The author chose Python for developing the core data science component. As the core algorithm and model will be DL-based, DL frameworks must be meticulously analyzed to select the most relevant framework. The two most popular frameworks, TensorFlow and PyTorch, were analyzed in **APPENDIX C.2**, where the author opted to use **TensorFlow**.

4.2.4.2. User Interface (UI) framework

As JavaScript was chosen for developing the UI, respective JavaScript frontend frameworks and libraries must be analyzed. There is an ocean of JavaScript libraries - the top four were selected for evaluation: Angular, Vue, Svelte, and React. The author decided to use **React**; the evaluation can be found in **APPENDIX C.3**.

4.2.4.3. Application Programming Interface (API) web framework

As python was chosen for the API development, respective Python web frameworks must be analyzed to select the more relevant one. Analysis was conducted between Django and Flask, as they are the two most popular frameworks. **APPENDIX C.4** demonstrates the comparison where the author decided to use **Flask**.

4.2.5. Other libraries & tools

Table 15: Chosen libraries (Self-Composed)

Library	Justification
NumPy	Facilitates mathematical functions and calculations that are immensely
	required when building the algorithm.
Pandas	To create dataframes to perform analysis, cleaning, transformations,
	filtration, etc., on the datasets.
Scikit-learn	To create data splits and feature scaling.
Lingua	To detect the language of the tweets. As this project is limited to using
	only English tweets, they must first be identified.
SpacCy	To perform NER to extract entities that could be within the pre-defined
	impactful index.
Matplotlib + Seaborn	For analysis, visualizations, and dashboarding.

Beautiful Soup	For scraping the block reward size and the Twitter volume from the
	public dashboard.
VADER	Perform sentiment analysis on the tweets.
TensorBoard	Visualize and obtain insights of the model training process associated
	evaluation metrics and additional dashboarding.
Redux	For API requests from the client.
Ant design	Makes creating appealing user interfaces hassle-free.

4.2.6. Integrated Development Environment (IDE)

Table 16: Chosen IDEs (Self-Composed)

IDE	Justification
Kaggle	Consists of 32GB of RAM; therefore, all datasets can be loaded and processed at
	once without needing to process sections of data at a time. Additionally, it provides
	easy integration with existing Kaggle datasets and user-uploaded datasets.
Jupyter	For local trials, testing, and model training.
VSCode	Lightweight and extremely powerful. It consists of multiple shortcuts, extensions,
	and snippets that can significantly boost development productivity.

4.2.7. Summary of chosen tools & technologies

Table 17: Chosen tools & technologies (Self-Composed)

Component	Tools
Programming languages	Python, JavaScript
Development framework	Flask, TensorFlow
UI development framework	React
Libraries	Ant design, NumPy, Pandas, Scikit-learn, Beautiful Soup,
	Lingua, Matplotlib, Seaborn, VADER sentiment analyzer.
IDEs	Kaggle and Jupyter notebooks; VSCode.
Version control	Git + GitHub

4.3. Implementation of core functionalities

The novel algorithm, the scripts to fetch the required data, and the preprocessing performed can be considered the core functionalities of the project.

4.3.1. Algorithm implementation

The author initially implemented the LTC architecture since there is no modern reference utilizing recommended best practices and approaches. The author then built on this architecture, replacing the underlying ODEs with SDEs.

Figure 10: Initialize algorithm (Self-Composed)

The above code snippet initializes the algorithm cell with the necessary variable maximum and minimum values. In the above method, the built model can perform input-independent initializations. By inheriting from the base Keras Layer class, the ability to be used in the higher level of the model's layer definition is obtained (as existing LSTM and RNN cells).

```
def build(self, input_shape):
...
Automatically triggered the first time __call__ is run
...
self.input_size = int(input_shape[-1])
self.get_variables()
self.built = True
. . .
```

Figure 11: Build algorithm (Self-Composed)

The above snippet defines what occurs upon initialization; in other words, it "builds" the algorithm cell. A helper function is utilized here that defines the variables (sigma, mu, weights, and leakage conductance variables (Hasani et al., 2020)). The input shape is available within the above function; therefore, the model can initialize the variables used here. The below snippet demonstrates how some of these variables are initialized.

```
# Define base stochastic differential equation variables
# Define sensory variables
                                             self.mu = tf.Variable(
self.sensorv mu = tf.Variable(
                                              tf.random.uniform(
 tf.random.uniform(
                                                 [self.units, self.units],
   [self.input_size, self.units],
                                                 minval = 0.3.
   minval = 0.3,
   maxval = 0.8,
                                                 maxval = 0.8,
  dtype = tf.float32
                                                dtype = tf.float32
 name = 'sensory_mu',
                                               name = 'mu',
 trainable = True,
                                               trainable = True.
            # Synaptic leakage conductance variables of the neural dynamics of small species
            if self._fix_vleak is None:
              self.vleak = tf.Variable(
   tf.random.uniform(
                  [self.units],
                  minval = -0.2,
                  maxval = 0.2
                  dtype = tf.float32
                name = 'vleak'
                trainable = True
            else:
              self.vleak = tf.Variable(
               tf.constant(self._fix_vleak, dtype = tf.float32),
                name = 'vleak',
trainable = False,
                shape = [self.units]
```

Figure 12: Algorithm – sensory, stochastic and leakage variables (*Self-Composed*)

The final step is the forward computation process that will occur on each epoch, in other words, the forward propagation process.

```
@tf.function
def call(self, inputs, states):
    ...
Automatically calls build() the first time.
Runs the LTS cell for one step using the previous RNN cell output & state
by calculating the SDE solver to generate the next output and state
    ...

inputs = self._map_inputs(inputs)
    next_state = self._sde_solver_euler_maruyama(inputs, states)
    output = next_state
    return output, next_state
```

Figure 13: Algorithm – forward propagation (*Self-Composed*)

The above function is run automatically on each epoch. Initially, a helper function defines the weights and biases of the network, as demonstrated below.

```
def map_inputs(self, inputs):
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```

Figure 14: Algorithm – define weights and biases (Self-Composed)

As determined in previous chapters, the optimal way of performing the forward computation of SDEs is to use the Euler-Maruyama method. The below code snippet is an implementation of the Euler-Maruyama SDE solver used by the author utilizing Brownian motion as the noise, as demonstrated by Duvenaud (2021).

Figure 15: Algorithm – Euler-Maruyama SDE solver (Self-Composed)

4.3.2. Data fetchers

The scripts that are used to extract the data. The scripts are placed under **APPENDIX C.5**.

4.3.3. Preprocessing

Preprocessing steps are required to prepare the data fetched from the data fetchers before being used by the model. The preprocessing scripts are placed under **APPENDIX C.6**.

4.4. Chapter summary

This chapter focused on defining the technologies and tools that facilitate the software development that would demonstrate the research. Additionally, the implementation of the core features is shown with accompanying code snippets.

CHAPTER 05. CONCLUSION

5.1. Chapter overview

This chapter provides an initial conclusion to the research project focused on implementing the core components required to consider it a functional prototype. In detail, any deviations taken from the proposed scope and the schedule in the project proposal are mentioned. Moreover, any additional improvements required to produce an MVP alongside the current evaluation results are specified.

5.2. Deviations

5.2.1. Scope related deviations

The features in scope proposed in the project proposal are stated in **APPENDIX D.1**. Based on the proposed scope, no deviations have been taken in the category of "in-scope". Unfortunately, due to time constraints, none of the "desirables" category had been implemented.

5.2.2. Schedule related deviations

The schedule proposed by the author is available in **APPENDIX D.2**. Based on the proposed Gantt chart, the author's journey so far has not had any significant deviations. The progress of the Gantt chart with the updated dates provided is available in **APPENDIX D.3**. However, minor deviations from the proposed schedule had been taken, The below table demonstrates these deviations, their current status and status descriptions.

Table 18: Schedule related deviations (Self-Composed)

Task	Task	Status	Status description
No.	description		
45	Implement	IN	The author had planned to complete their supplementary
	supplementary	PROGRESS	components by Jan 23 rd , however ran into issues while
	components		implementing the core component. Therefore, the
			author had to prioritize developing the core research
			component first. Nevertheless, the client application has

			been implemented, and only the API to communicate
			between the model and client is left to integrate.
62	Writing /	IN	The author planned to publish a research paper before
	publishing a	PROGRESS	the PSDP submission, however could not due to limited
	research paper		conferences available during the winter season, and the
			time taken to review. It is however worth mentioning
			that the author did register and was accepted to a
			conference that will be held within March 2023. The
			acceptance notification can be found in APPENDIX
			D.5.

5.3. Initial test results

Two different models were created for the prototype implementation. A univariate and multivariate model for forecasts greater than a horizon of 1 and forecasts for a horizon of 1, respectively.

It is notoriously challenging to surpass the "naïve" forecast in open market forecasting, which fortunately was the case for the models implemented. The two snippets below demonstrate the comparison of these models against the naïve forecast via evaluation metrics that are specified in **APPENDIX D.4** for the test dataset.

5.3.1. Univariate model

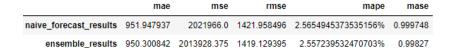


Figure 16: Univariate model evaluation (Self-Composed)

5.3.2. Multivariate model

	mae	mse	rmse	mape	mase
naive_forecast_results	858.99939	1631689.25	1277.375977	2.41947078704834%	0.998859
ensemble_results_2	918.780212	1788472.375	1337.337769	2.618018627166748%	1.069594

Figure 17: Multivariate model evaluation (*Self-Composed*)

5.4. Required improvements

To consider this research successful, a couple of improvements are required.

- Enhance the system's performance to the best possible accuracy attempt more optimization procedures, and compare the system's performance with existing solutions
- Integrate the model in use to a GUI GUI has been prepared; the author should create a simple Flask API to establish communication.
- Perform testing for each section of the application conduct unit, performance, and integration testing.

5.6. Demo of the prototype

A prototype demo was recorded and uploaded as an unlisted video on YouTube; the video can be found at https://youtu.be/HMUa9J0KcJQ. The slides demonstrated can be found Here.

5.7. Implementation code

The code written for the prototype and associated research work conducted is in GitHub for convenience, in the below links:

- Algorithm trials and testing repository http://bit.ly/3HYOqBB.
- Application implementation repository http://bit.ly/3HXDtQu.
- Research documentation chapters and diagrams repository http://bit.ly/3ixjf6V.

5.8. Chapter summary

This chapter provided the reader with an overview of the current status of the ongoing research project, including, but not limited to - deviations taken from the proposed features and schedule, the evaluation results, and any further improvements required.

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APPENDIX A – SRS

A.1. Requirement elicitation methodologies

Table 19: Stakeholder groups (Self-Composed)

Group	Stakeholders	Reason	Instrument
G1	Domain experts	Gather any insights and knowledge	Interview
	(neural ODE/SDE	specifically in the research domain to answer	
	and	research questions and anything the author	
	blockchain/crypto)	may have missed.	
G2	End users (trader &	Gather requirements for supplementary	Survey
	buyer)	application implementation.	
G3	Competitors	Analyze any existing systems and literature	LR/Observations
G4	Developers	Ensure completion and feasibility of the	Prototyping
		project.	

A.2. Survey analysis

Table 20: Survey thematic analysis codes, themes & conclusions (Self-Composed)

Code	Theme
Exogenous factors	Robustness
Explainability, Insights	Reliability
Simplicity, Convenience	User-friendly
Tuning	Editability
On-demand	Future consideration

Theme	Conclusion Evidence				
Robustness	Participants believed that prediction	"Use previous trends in the past."			
	needed more than just including	"Consider all possible external			
	historical prices and that social media	factors."			

	Trends and other factors (ex:		
	sentiment) are required to make the		
	system as robust and performant as		
	possible.		
Reliability	Almost all respondents requested that	"Insights about the forecast will be	
	the system provide an Explainability	beneficial."	
	component so that the insights obtained	"Provide as much Explainability to	
	can be reliable as the inference	make the prediction as credible as	
	becomes as transparent as possible.	possible."	
		"The rate of success of the prediction	
		would be useful."	
User-friendly	A couple of participants requested that	"Show some news about the current	
	the system provide some	cryptocurrency world in the platform,	
	cryptocurrency news to make it	so it's convenient for the users."	
	convenient and make the inference	"Make the steps from choosing a date	
	procedure as straightforward as	to forecasting as simple as possible."	
	possible, so there is no hindrance.		
Editability	An ML-knowledgeable participant	"Coming from machine learning	
	mentioned that it would be an ideal	point of view, I think it'll be a good	
	scenario if the system could tune the	idea if there's a functionality to	
	hyperparameters of the model in use,	change the hyperparameters used."	
	which could be an excellent		
	enhancement to the system as the		
	model anyways retrains periodically.		
Future	A couple of participants mentioned	"Predict the market for any given	
considerations	some additional features the author	time duration."	
	believes they will not be able to cover,	"Ability to identify a pump and dump	
	given the time allotted.	scenario compared to an actual	
		increase in the price of stock/crypto."	

A.3. Interview analysis

Table 21: Interview participant details (Self-Composed)

Participant	Affiliation	Expertise related to the research
ID		
P1	Google Brain visiting researcher and	Neural ODEs and SDEs.
	Associate Professor at University of	
	Toronto.	
P2	Research scientist at Deepmind.	Neural ODEs and SDEs.
P3	Research scientist at Meta AI.	Probabilistic DL and differential
		equations.
P4	PhD candidate at University of	XAI
	Nottingham.	
P5	Chief Product Officer at Niftron.	Blockchain and cryptocurrencies.

Table 22: Interview thematic analysis themes, conclusions & evidence (Self-Composed)

Theme	Conclusion	Evidence		
Research comp	Research component			
Research	The interviewees validated the research	"Yes, there are many TS forecasting		
Problem &	gap and the defined problem. They	algorithms; however, many are		
Gap	were also happy that the author had	obsolete."		
	been conducting this research, as few	"Yes, the chosen field of		
	papers were published in this domain.	architectures can be considered an		
		advancement."		
		"As per my knowledge, I have not		
		seen a system using the basic LTC		
		architecture itself, so this new		
		architecture will be novel."		
Requirements	The interviewees were concerned that	"They are expensive to compute."		
	ODEs and SDEs could be expensive to	"It can be resource-intensive."		
	compute and hence could take some			

	time, which can be an issue given that		
	the forecasts must be produced quickly.		
	Therefore, the author must optimize the		
	model as much as possible to avoid		
	user-unfriendliness.		
Advice	The author had initially planned on	"I think latent ODEs are obsolete."	
	only creating an implementation of the	"You should look into latent SDEs	
	LTC architecture proposed by Hasani	instead."	
	et al. (2020). However, the author	"Latent SDEs are more flexible, you	
	could further improve the architecture	could try applying LTC architectures	
	by using SDEs instead (the base LTC	to those more flexible models	
	uses ODEs), which could manifest into	instead."	
	a novel algorithm, which is the author's		
	current aim as it carries more		
	significance and a potentially more		
	outstanding contribution.		
Other	What was concluded here was that XAI	"Yea, in the domain of TS I have not	
suggestions	is primarily present for image	seen many explainable AI research	
	classification, and there needs to be	conducted."	
	more literature on the TS domain.	"Explainable AI is flourishing in	
	However, XAI integration into TS	image classification but I have not	
	modelling could be confusing and	seen it in TS."	
	complicated due to the temporal	"Integrating explainable AI might	
	component. Additionally, XAI for	not be straightforward as other	
	SDEs needs to be researched, which the	domains."	
	author could look into if time permits.		
Problem doma	in		
Robustness	The interview was an additional	"It is best if you try to include as	
	validation for the data collected in the	many features as possible."	
	survey. Most suggestions were to use	"It is not practical to forecast with	
	as many extra features as possible to	only historical prices."	

make the model robust. Therefore, the	
author will ensure that they utilize the	
mentioned exogenous features.	

A.4. Use case descriptions

Table 23: Use case description UC:03; UC:04; UC:05 (Self-Composed)

Use case	Manage exogenous features
Id	UC:03; UC:04, UC:05
Description	Manage and process new data without the need for manual interaction.
Actor	None
Supporting	None
actor (if any)	
Stakeholders (if	None
any)	
Pre-conditions	The latest available data must be scraped and available.
Main flow	MF1. A Cron job triggered fetches the latest historical prices, tweets,
	Twitter volume, trends, and block reward size data.
	MF2. Twitter volume, Google trends, and block reward size are scaled and
	cleaned.
	MF3. Tweets undergo sentiment analysis to determine current speculation.
	MF4. The sentiment is further weighted based on the Tweeter's importance
	(ex: Elon Musk)
	MF5. Features are combined with historical closing prices to create an
	enriched dataset and retrain the model.
Alternative	None
flows	
Exceptional	EF1. The script could not fetch recent data – retry a few days later or alert
flows	Admin for manual overhaul.
Post-conditions	A new enriched dataset with the features is generated.

Table 24: Use case description UC:07 (Self-Composed)

Use case	Update model hyperparameters
Id	UC:07
Description	Manually change the hyperparameters used by the model.
Actor	Admin
Supporting	None
actor (if any)	
Stakeholders (if	None
any)	
Pre-conditions	All the data must be scraped and preprocessed (as the model would ideally
	need to be retrained upon hyperparameter tuning).
Main flow	MF1. Admin authorizes themselves.
	MF2. Admin can change the hyperparameters in use to a set of predefined
	values.
	MF3. The system ensures data available is up-to-date (must be in this case,
	as the script will run periodically automatically). If not:
	1. Obtains the latest available data.
	2. Performs sentiment analysis and self-retrains.
	MF4. The system retrains itself with the data and new hyperparameters.
Alternative	None
flows	
Exceptional	None
flows	
Post-conditions	The model is updated with the chosen hyperparameters.

A.5. Functional requirements

Table 25: 'MoSCoW' technique of requirement prioritization (Self-Composed)

Priority level	Description
M (Must have)	The author must implement requirements with this priority for the project
	to succeed.
S (Should have)	Requirements that would be of value but are not necessary.
C (could have)	Features that are optional and have no significant impact. It is desirable to
	implement them if time permits.
W (Will not have)	Requirements that will not be a part of the implementation at this point.

APPENDIX B - DESIGN

B.1. Algorithm intuition

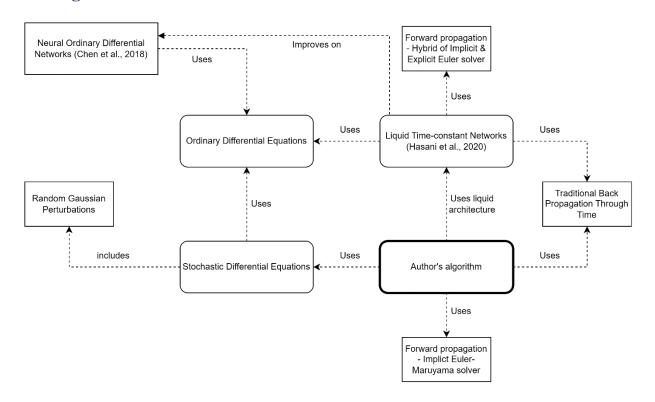


Figure 18: Algorithm intuition (Self-Composed)

Existing LTC architecture

$$\frac{dx(t)}{dt} = -\left[\frac{1}{\tau} + f(x(t), I(t), t, \theta)\right] x(t) + f(x(t), I(t), t, \theta)A$$

- τ Time-constant
- x(t) Hidden state
- *I(t) Input*
 - t Time
- f Neural network
- θ , A Parameters

The above formulation was proposed by Hasani et al. (2020), where a system of linear ODEs is used to declare the flow of the hidden state; the ODEs are of the following form.

$$\frac{dx(t)}{dt} = \frac{-x(t)}{\tau} + S(t)$$

Where S(t) represents the following nonlinearity

$$S(t) = f(x(t), I(t), t, \theta)(A - x(t))$$

The equation manifests by plugging the above equation into the system of linear ODEs.

Formulation

Step 01 – transitioning from an ODE to an SDE

In simple terms, an SDE is an ODE with additional noise added at each step, which the model can use to model uncertainty.

Assume an ODE is:
$$\frac{dx}{dt} = f(x)$$
; which obtains the expected slope of $x(t)$

The above ODE can be used to calculate the 'expected' slope, whereas the 'realized' slope differs from the 'expected' due to random noise, also called random Gaussian perturbations or Gaussian white noise. With that in consideration, the following can be derived:

An SDE is:
$$\frac{dx}{dt} = f(x) + \mathcal{E}_{t+dt}$$
; where \mathcal{E}_{t+dt} is $\sim N(0,1)$

Where
$$N(0,1)$$
 is a Gaussian 0,1 random variable

However, noise can be of varying intensities (some could be high, some could be low). Considering this varying intensity, the SDE can be further expressed as follows:

$$\frac{dx}{dt} = f(x) + g(x) * \mathcal{E}_{t+dt}; where g(x) is the intensity$$

As implied, the missing factor in the existing architecture that consists of ODEs is the absent stochastic transition dynamics (i.e., a noise for each timestep – which is vital to model the tiny unobserved interactions). The above equation considers the small unobserved interactions and uncertainties that could occur; this is further important in the context of TS data, as the initial state of data is unlikely to be certain.

Step 02 – adding neural networks into SDE dynamics

Based on the findings of Duvenaud (2021), the noise mentioned in the previous step can be considered as Brownian motion, a generalized form of the Gaussian noise. Researchers can produce the following by plugging Brownian motion into the equation determined in the previous step.

$$dx = f(x(t))dt + o(x(t))dB(t)$$

A neural network can be integrated into the above equation to solve the system, resulting in the following equation:

$$dx = f_{\theta}(x(t))dt + \sigma_{\theta}(x(t))dB(t)$$

where f is usually a tiny neural network and θ are its parameters

Step 03 – Integrating the above equation into the LTC architecture

Moving back to the main problem at hand, the author can now construct a new formula by using the equation determined in the previous step.

$$\frac{dx(t)}{dt} = \frac{-x(t)}{\tau} + S(t)$$

As the above equation is a linear system of ODEs initially proposed by Lapicque (1907), the author could add the uncertainty noise to the equation to produce the following:

$$\frac{dx(t)}{dt} = \frac{-x(t)}{\tau} + S(t) + \sigma(x(t))B$$

The above equation now defines a stochastic process instead of deterministic evolution. Therefore, researchers can model any tiny unobserved interactions.

Finally, the following could be derived by applying this to the LTC formula:

$$\frac{dx(t)}{dt} = \frac{-x(t)}{\tau} + S(t) + o(x(t))B$$

Replace S(t) with the nonlinearity proposed,

$$\frac{dx(t)}{dt} = \frac{-x(t)}{\tau} + f(x(t), I(t), t, \theta)(A - x(t)) + \sigma(x(t))B$$

Expand out the equation,

$$\frac{dx(t)}{dt} = \frac{-x(t)}{\tau} - f(x(t), I(t), t, \theta)x(t) + \sigma(x(t))B + f(x(t), I(t), t, \theta)A$$

Lastly, refactor the equation into the format of the original LTC

$$\frac{dx(t)}{dt} = -\left[\frac{1}{\tau} + f(x(t), I(t), t, \theta) - \sigma B\right] x(t) + f(x(t), I(t), t, \theta) A$$

B.2. UI wireframes

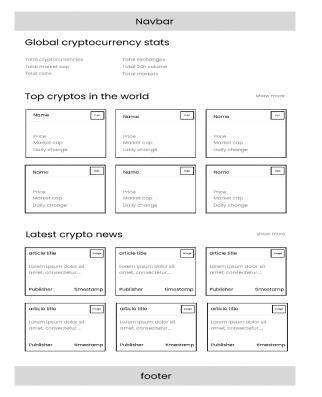


Figure 19: UI wireframes – Home (*Self-Composed*)

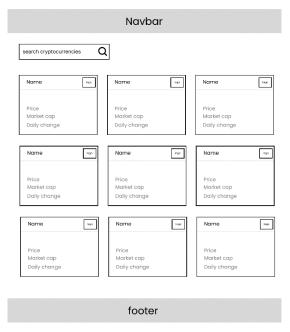


Figure 21: UI wireframes – Cryptocurrencies (*Self-Composed*)



Figure 20: UI wireframes – News (*Self-Composed*)

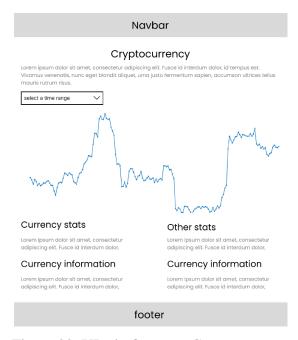


Figure 22: UI wireframes – Cryptocurrency (*Self-Composed*)

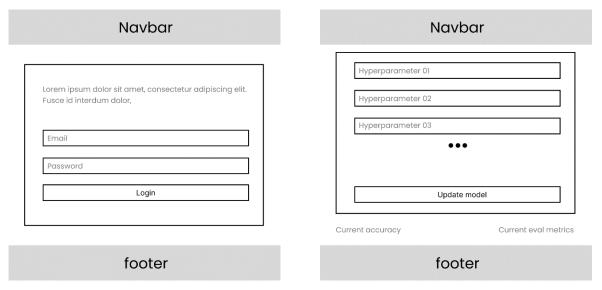


Figure 23: UI wireframes – Admin login (Self-Composed)

Figure 24: UI wireframes – Admin model configuration (*Self-Composed*)

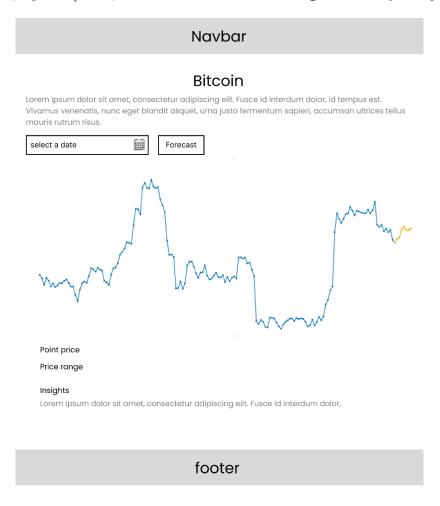


Figure 25: UI wireframes – Forecast (Self-Composed)

APPENDIX C - IMPLEMENTATION

C.1. Selection of programming language

The below table summarizes the analysis of the language chosen for the data science component, where each option was given a score within H - High, M - Medium, and L - Low.

Table 26: Selection of data science language (Self-Composed)

Data science

Two of the most popular languages used widely for data science were analyzed to implement the core data science components.

Aspect Relevance		_	
Aspect	Recevance	Python	R
Availability of	A language supporting multiple libraries is paramount, as the	Н	M
libraries.	author would require numerous techniques to gather the		
	necessary data and streamline the model and algorithm		
	development.		
Author	Implementing the algorithm, the mathematical intricacies, and	Н	M
familiarity and	the respective model should be as simple as possible. It is an		
ease of	additional benefit if the author has hands-on experience with		
implementation.	the chosen language,		
Learning curve	The difficulty of the chosen language must not be a hindrance,	L	M
	as the goal is to utilize the tool to implement a system rather		
	than spending time learning the language.		
Community and	Community support and well-written documentation are	Н	M
documentation.	important, as the author will not have time to debug trivial		
	issues.		

Conclusion

Based on the analysis, the author decided to use **Python**, as it was more relevant.

C.2. Selection of Deep Learning (DL) framework

Table 27: Selection of DL framework (Self-Composed)

Framework	Description			
TensorFlow	Used for production-level applications, has detailed documentation ar			
	community support, and handles large datasets. It also provides better			
	visualization options, making it easy to debug and monitor training, which is			
	vital as a novel algorithm is being built, and no comparison is present.			
PyTorch	It is more lightweight and developer-friendly, as it provides a higher-level			
	development. Therefore, it has a much smaller learning curve, easier to get			
	started, and feels more intuitive as it is simpler to build models.			
G 1 1				

Conclusion

The author opted to use **TensorFlow**. Although it is more complicated, the higher-level API: Keras, is now officially a part of TensorFlow. Therefore, model development has become much more straightforward. Additionally, building the algorithm requires more low-level details. (PyTorch vs. TensorFlow: 2022 Deep Learning Comparison | Built In, 2022)

C.3. Selection of User Interface (UI) framework

Table 28: Selection of UI framework (Self-Composed)

Framework	Description
Angular	Suitable for large-scale applications with dedicated submodules for particular
	functionalities. However, it can be less performant in comparison and
	unnecessarily heavy.
Vue	A tiny framework that takes little to no time to startup and is much more
	intuitive as the code is simple. Additionally, based on simulations, it has been
	identified to perform better than Angular and React. However, it has much
	fewer resources.
Svelte	The most lightweight and genuinely reactive. Much more performant than the
	rest; however, it has a small community of developers and is relatively new.

React	Customizable and promotes code reusability via functions as components. It		
	carries a large community and is open-source while being SEO-friendly.		
	Additionally, the React developer tools is very handy.		

Conclusion

Based on the analysis, the author chose **React** as the GUI built will be simple, and there is no requirement for large-scale applications, as it is not the primary focus.

(Angular vs React | Angular vs Vue | React vs Vue – Know the Difference, 2021)

C.4. Selection of Application Programming Interface (API) framework

Table 29: Selection of web framework (Self-Composed)

Framework	Description		
Flask	A very lightweight framework that provides only the simplest of		
	functionalities. However, it is the preferred choice for ML API development because it is light.		
Django	Suitable for more larger scaled applications that provide a vast range of functionalities, it is stricter and less flexible. Therefore, is much more		
	demanding and heavier.		

Conclusion

The author chose **Flask** as it provides only the necessities in exposing an ML model and since the luxury features provided by Django (ex: authentication) were not required.

(Flask Vs Django: Which Python Framework to Choose?, 2021)

C.5. Fetch data

Fetch historical prices

Figure 26: Fetch historical prices (Self-Composed)

The above script describes a couple of functions that can be used to fetch the latest BTC historical prices data and create a new updated CSV file that can be later read from by the model. A third-party API was used to fetch the data, as existing APIs are all discontinued.

Fetch Twitter volume & block reward size

Figure 27: Fetch Twitter volume (*Self-Composed*)

```
UBL. * 'https://bitinfocharts.com/comparison/size-btc.html#alltime'
FILE_PAIN = "./../m/data/Bic_Block_Reward.cay'
response = requests.get(UBL)
sopp = SeautifulSoup(response.text, 'html.parser')
scripts = soup(rime_lit'script')

de parse(string_list):

parse list of strings within the script tag
    [date, volume]

    ...

clean = re.sub(r[\\\]\s\]', ', string_list)
splitted = re.sub(r[\\\]\s\]', ', ', string_list)
script und values_only = [s for a in splitted if s \( \pm '' \)]
return values_only = [s for a in splitted if s \( \pm '' \)]
script UBL script tag and extract block reward \( \phi \) respective date

if 'da = new Upgraph(coument_getLementById("container")' in script.text:
    if 'd = new Upgraph(coument_getLementById("container")' in script.text:
    if 'd = new Upgraph(coument_getLementById("container")' in script.text:
    if 'id = new Upgraph(coument_getLementById("container")' in script.
```

Figure 28: Fetch block reward size (*Self-Composed*)

The above scripts fetch the Twitter volume and block reward from a website that publicly exposes this data. Therefore, a simple website scraping tool can be used without authentication or authorization.

Fetch tweet data

Figure 29: Scrape tweets (Self-Composed)

Obtaining the tweet data required a more tedious process as the Twitter API had been updated only to provide tweets for the past week. However, third-party libraries offer this functionality. Tweets fetched were limited to 500 for a single day due to time, performance, and storage constraints, and the application is not the core contribution. Initially, tweets were fetched up to a specific time point; in the future, the above script could be run to scrape tweets of particular dates that are described to be from the days currently existing in the data folder up to the day at which the script is run. There is a further limitation as only '#bitcoin' is searched.

```
def clean_tweets(dates):
    ""
    Clean tweets that have empty records and non-english tweets
    ""

    tweets_list = scrape_tweets(dates)
    df_days = process_tweets(tweets_list)

for df in df_days:
    df.dropna(subset=['user', 'timestamp', 'text'], inplace=True)

L = []
    for row in df['text']:
    # Use WTL to remove any non-english observations
    if len(row) ≠ 0:
        | L.append(detector.detect_language_of(row))
        else:
        | L.append(None)

df['lang'] = L
    df_filtered = df[df['lang'] = Language.ENGLISH]
    df_filtered.drop(['lang'], axis=1, inplace=True)
    filename = str(df.iloc[0]['date'])
    df_filtered.to_csv(f'{FOLDER_PATH}/{filename}.csv')

return df_days
```

Figure 30: Clean tweets (Self-Composed)

As this research is currently limited to only English, the tweets are filtered, and non-English tweets are removed.

Fetch Google Trends

```
def get_new_trends_data():
    Fetch latest Trends data
   pytrends = TrendReq()
kw_list = ['bitcoin']
    pytrends.build_payload(
       kw_list,
cat=0,
timeframe='now 7-d',
        gprop='
   curr_data = pytrends.interest_over_time()
   return curr_data
def format_new_data(df):
    Converts the obtained data into the format of the available data
  df.rename(columns={ 'bitcoin': 'bitcoin_unscaled' }, inplace=True)
   # Create stringified dates
   df.index = [str(i) for i in pd.to_datetime(df.index).date]
df.index.rename('date', inplace=True)
    # As the data obtained is for every hour, get an average of it all for each day
    grouped_df = df.groupby(level=0)
avg_df = grouped_df.agg({ 'bitcoin_unscaled': 'mean' })
    return avg_df
```

Figure 31: Fetch Google Trends (Self-Composed)

Fetching Google Trends data was a relatively straightforward procedure, as Python specifically exposes a library for this purpose. However, rate limitations had to be overcome by running the script multiple times for specific data ranges at a time rather than the entire history.

C.6. Preprocessing

Tweet sentiment analysis

The main step of preprocessing is to perform sentiment analysis on the obtained tweet data. In this research, the VADER sentiment analyzer is used as determined in previous chapters.

Figure 32: Analyze sentiments (Self-Composed)

The above script is used to perform sentiment analysis on the tweets and concatenates the negative, positive, neutral, and compound scores into the existing tweet dataset, which can then be condensed down to create an average score for a single day.

Tweet dataset condensation

```
Load all tweet csvs in folder into a list of dfs which can then be condensed
     dfs = [pd.read_csv(f'{FOLDER_PATH}/{i}', engine='python') for i in ALL_FILES]
def condense tweets(dfs):
     Condense tweet dfs into a single df of averaged sentiment values
     for each date
   condensed df = None
     for i, df in tqdm(enumerate(dfs)):
          # Certain files have timestamp column, certain have date if df.iloc[0].get('timestamp'):

| df_filename = str(df.iloc[0]['timestamp'])
         else:
       df_filename = str(df.iloc[0]['date'])
print(f'Currently at df: {i+1} | {df_filename}')
        # Get the average values for each date
averages = list(df[['negative_score', 'neutral_score', 'positive_score', 'compound_score']].mean())
data = {
                'date': [df_filename],
                'negative_score': averages[0],
'neutral_score': averages[1],
'positive_score': averages[2],
'compound_score': averages[3],
       tweet_df = pd.DataFrame(data, index=None)
         if condensed_df is not None:
    condensed_df = pd.concat([condensed_df, tweet_df])
        else:
condensed_df = pd.DataFrame(data, index=None)
 return condensed df
def export_data(df):
     Save data
    df.to_csv(OUTPUT_PATH)
```

Figure 33: Combine and condense tweets (Self-Composed)

As the other data being used directly creates a single CSV file with a row for each date, the condensation process is unnecessary. However, as the tweet data fetched consists of a separate CSV file for each date, this data must be compressed to the same format as other datasets.

The above script condenses the tweet dataset into a single CSV file by averaging the sentiment scores for each day.

Final dataset creation

```
def create_combined_dataset():
   Create and clean the final combined dataset
   exogenous_features = get_exogenous_datasets()
   filtered_prices = get_prices()
 combined df = filtered prices.copy(deep=True)
   # Combine datasets together and add NaN to empty date rows
    for i in exogenous_features:
        combined_df = pd.merge(
           combined_df,
           on=['date'],
           how='left'
   # Impute missing values with the respective columns mean
   combined_df.fillna(combined_df.mean(numeric_only=True), inplace=True)
   return combined_df
def export_data(df):
   Save data
   df.to_csv(OUTPUT_PATH)
def create_final_dataset():
   Main runner
   print('\nRunning final dataset creation ...', end='\n')
   combined_df = create_combined_dataset()
    export_data(combined_df)
   print('\nFinal dataset created', end='\n')
```

Figure 34: Combine all datasets (*Self-Composed*)

The above script is used to create the final dataset that the model uses. It fetches all the datasets and combines them into a single data frame. Initially, a helper function removes unneeded columns from the data files, which were decided upon conducting correlation tests. The mean of their respective columns imputes missing values of each feature of specific dates. This combined dataset can be saved so the model can finally utilize it.

APPENDIX D - CONCLUSION

D.1. Project scope

In scope

- Implementing a novel LTC architecture capable of being used as currently existing solutions and the corresponding creation of a system.
- Periodic updates of the model with the latest available data.
- Evaluate and compare the implemented system against existing solutions.
- Ability to display a range of predictions for the chosen horizon.
- By combining them with the BTC historical data, consider Twitter sentiment, volume, and the 'block reward size' as external factors.

Desirables

- Benchmark implementation against the M4 competition to further justify the future of TS forecasting algorithms.
- Evaluate other neural ODEs (CT-RNN, CT-GRU, Latent ODE) and SDEs (Latent SDE).
- Explainable AI for neural SDEs and neural ODEs.

D.2. Project schedule

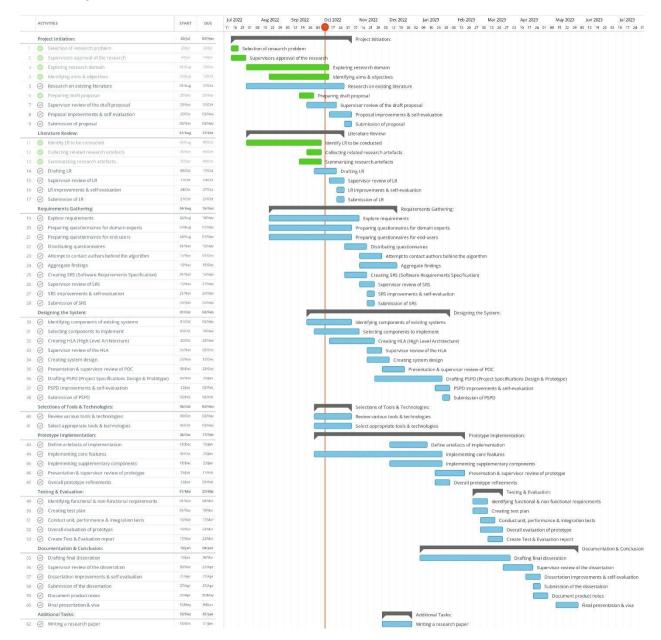


Figure 35: Initial Gantt chart (Self-Composed)

A clearer version can be found Here

D.3. Project progress

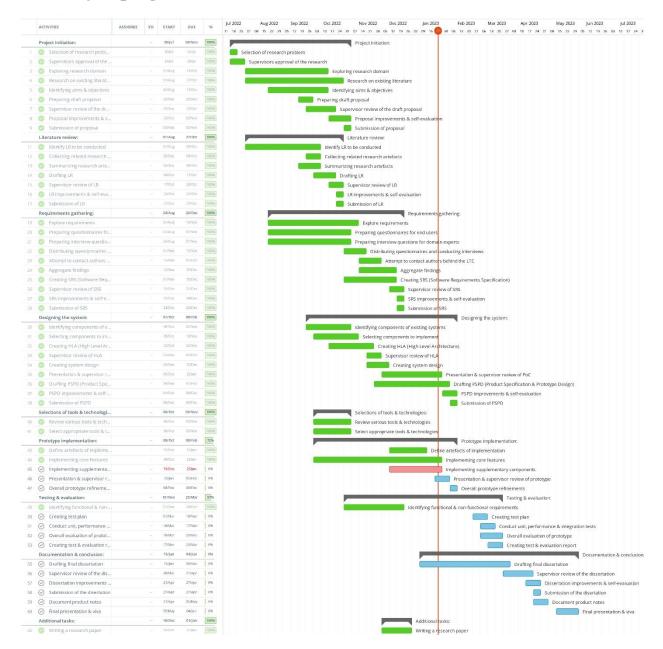


Figure 36: Current Gantt chart (Self-Composed)

A clearer version can be found <u>Here</u>

D.4. Evaluation metrics

Table 30: Evaluation metrics for TS forecasting systems

Metric	Description	Formulae
MAE	The absolute difference between the generated forecast and the ground truths. Since it is simple to understand, it will give the author an idea of how inaccurate the forecast is.	$\frac{\sum_{i=1}^{n} y_i - \widehat{y}_i }{n}$
MSE	Similar to MAE, but computes the squared differences. This metric gives more emphasis to more significant errors and also considers outliers.	$\frac{\sum_{i=1}^{n} (y_i - \widehat{y}_i)^2}{n}$
RMSE	The square root of MSE.	$\sqrt{\frac{\sum_{i=1}^{n}(y_i-\widehat{y}_i)^2}{n}}$
MAPE	The ratio of the forecast to the average absolute difference between the forecast and ground truths. Helpful if the algorithm is evaluated in the M4 competition, as this metric is used widely in competitions since it does not have any units. Therefore, it can be compared across other datasets.	$\frac{100}{n} \sum_{i=1}^{n} \frac{y_i - \hat{y_i}}{y_i} $

D.5. Extended review paper acceptance notification

