

Decision Tree using GINI Index

Main Dataset

Weekend	Weather	Parents	Money	Decision
1 W1	Sunny	Yes	Rich	Cinema
2 W2	Sunny	No	Rich	Tennis
3 W3	Windy	Yes	Rich	Cinema
4 W4	Rainy	Yes	Poor	Cinema
5 W5	Rainy	No	Rich	Stay In
6 W6	Rainy	Yes	Poor	Cinema
7 W7	Windy	No	Poor	Cinema
8 W8	Windy	No	Rich	Shopping
9 W9	Windy	Yes	Rich	Cinema
10 W10	Sunny	No	Rich	Tennis

Excluded
Feature

Finding GINI Index of the System

$$\begin{aligned} \text{Gini(System)} &= 1 - \text{Gini(Decision=Cinema)} - \text{Gini(Decision=Tennis)} - \text{Gini(Decision=Stay In)} - \text{Gini(Decision=Shopping)} \\ \text{Gini(System)} &= 1 - 16/10^2 - 2/10^2 - 1/10^2 - 1/10^2 \\ &= 0.58 \end{aligned}$$

Finding GINI index of the Feature = Money

$$\text{Gini(Feature=Money)} = \text{weight average of (Gini(Money,Rich) , Gini(Money,Poor))}$$

$$\text{Gini(Money, Rich)} = 1 - (3/7)^2 - (2/7)^2 - (1/7)^2 - (1/7)^2 = 0.6938776$$

Gini(Money,Rich)

Weekend	Weather	Parents	Money	Decision
1 W1	Sunny	Yes	Rich	Cinema
2 W2	Sunny	No	Rich	Tennis
3 W3	Windy	Yes	Rich	Cinema
4 W5	Rainy	No	Rich	Stay In
6 W9	Windy	Yes	Rich	Cinema
7 W10	Sunny	No	Rich	Tennis

$$\text{Gini(Money, Poor)} = 1 - (3/3)^2 = 0$$

Weekend	Weather	Parents	Money	Decision
1 W4	Rainy	Yes	Poor	Cinema
2 W6	Rainy	Yes	Poor	Cinema
3 W7	Windy	No	Poor	Cinema

$$\text{Gini(Feature=Money)} = \text{Gini(Money,Rich)} * \text{Ratio of Rich} + \text{Gini(Money,Poor)} * \text{Ratio} = 0.4857143$$

Finding GINI index of the Feature = Weather

$$\text{Gini (Feature=Weather)} = \text{average weighted[Gini(Weather=Sunny) , Gini(Weather=Windy) , Gini(Weather=Rainy)]}$$

$$\text{Gini (Weather=Sunny)} = 1 - (1/3)^2 - (2/3)^2 = 0.4444444$$

Weekend	Weather	Parents	Money	Decision
1 W1	Sunny	Yes	Rich	Cinema
2 W2	Sunny	No	Rich	Tennis
3 W10	Sunny	No	Rich	Tennis

$$\text{Gini(Weather=Windy)} = 1 - (3/4)^2 - (1/4)^2 = 0.375$$

Weekend	Weather	Parents	Money	Decision
1 W3	Windy	Yes	Rich	Cinema
2 W7	Windy	No	Poor	Cinema
4 W8	Windy	No	Rich	Shopping
5 W9	Windy	Yes	Rich	Cinema

$$\text{Gini(Weather=rainy)} = 1 - (2/3)^2 - (1/3)^2 = 0.4444444$$

Weekend	Weather	Parents	Money	Decision
1 W4	Rainy	Yes	Poor	Cinema
2 W5	Rainy	No	Rich	Stay In
3 W6	Rainy	Yes	Poor	Cinema

$$\begin{aligned} \text{Gini(Feature=Weather)} &= (\text{ratio of sunny in dataset} * \text{Gini(Weather=Sunny)}) + (\text{ratio of windy in dataset} * \text{Gini(Weather=Windy)}) + (\text{ratio of rainy in dataset} * \text{Gini(Weather=Rainy)}) \\ &= 0.13333 + 0.15 + 0.13333 = 0.4166667 \end{aligned}$$

Finding GINI index of the Feature = Parents

$$\text{Gini(Feature=parents)} = \text{Weight Average [Gini(Parents=Yes) , Gini(Parents=NO)]}$$

$$\text{Gini(Parents=Yes)} = 1 - (5/5)^2 = 0$$

Weekend	Weather	Parents	Money	Decision
1 W1	Sunny	Yes	Rich	Cinema
2 W3	Windy	Yes	Rich	Cinema
3 W4	Rainy	Yes	Poor	Cinema
4 W6	Rainy	Yes	Poor	Cinema
5 W9	Windy	Yes	Rich	Cinema

$$\text{Gini (parents=No)} = 1 - (2/5)^2 - (1/5)^2 - (1/5)^2 - (1/5)^2 = 0.72$$

Weekend	Weather	Parents	Money	Decision
1 W2	Sunny	No	Rich	Tennis
2 W5	Rainy	No	Rich	Stay In
3 W7	Windy	No	Poor	Cinema
4 W8	Windy	No	Rich	Shopping
5 W10	Sunny	No	Rich	Tennis

$$\text{Gini(Feature=Parents)} = \text{ratio of "YES" in dataset} * \text{Gini(Parent=yes)} + \text{Ratio of "NO" in dataset} * \text{Gini(Parents=NO)} = 0.36$$

Assesment of Root Node

	Weather	Parent	Money	Result	Remarks
Gini Index	0.4166667	0.36	0.48571	Parent	Feature with minimum GINI Index has the max info gain

