

**ME 533 Nonlinear Dynamics Analysis**  
**Spring 2014**

**Homework 3**

All problems are from the textbook from the textbook “Applied Nonlinear Control” by Slotine and Li, Prentice Hall, 1991.

**Problem 1**

(Problem 7.7 from textbook)

Design a sliding controller for the system:

$$\ddot{x} + \alpha_1(t) |x| \dot{x}^2 + \alpha_2(t) x^3 \cos 2x = 5 \dot{u} + u,$$

where  $\alpha_1(t)$  and  $\alpha_2(t)$  are unknown time-varying functions verifying the known bounds

$$|\alpha_1(t)| \leq 1$$

$$-1 \leq \alpha_2(t) \leq 5$$

[Hint: Let  $v = 5 \dot{u} + u$  and do the problem. Discuss the effect of chatter in  $v$ ]

**Problem 2**

(Problem 7.10 from textbook)

Design a sliding controller for the system:

$$\dddot{x} + \alpha_1(t) \ddot{x}^2 + \alpha_2(t) \dot{x}^5 \sin 4x = b(t) u,$$

where  $\alpha_i(t)$  are unknown time-varying functions verifying the known bounds:

$$|\alpha_1(t)| \leq 1$$

$$|\alpha_2(t)| \leq 2$$

$$1 \leq |b(t)| \leq 4$$

Assume that the state is measured and that the slowest unmodeled dynamics is the actuator dynamics with a time-constant of about  $1/50$ . Simulate the system's performance on various trajectories (which you may want to generate using a reference model).

**Problem 3**

(Problem 8.3 from textbook)

Simulate the adaptive control system for the second-order plant

$$y = (p + b_p) / (p^2 + a_{p1} p + a_{p2})$$

with  $a_{p1} = 0.1$  and  $a_{p2} = -4$ , and  $b_p = 2$

**Problem 4**

(Problem 8.10 from textbook)

Discuss intuitively why parameter estimation can be easier on unstable systems than on stable systems