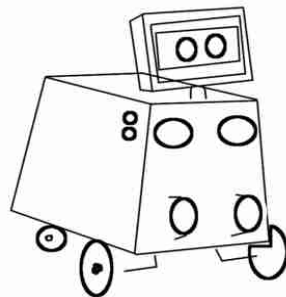ATHENS UNIVERSITY OF ECONOMICS AND BUSINESS
DEPARTMENT OF INFORMATICS

GuarddoG Project

DRAFT / WORK IN PROGRESS

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Acknowledgements

*GNU/Linux
*OpenCV
*Git / Github

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# Introduction and motivation

A few opening remarks

Humans increased their physical power during the industrial revolution using machines. They were able to create giant dams , factories , cars , airplanes and skyscrapers to make their everyday life easier . Technology has continued to improve exponentially and in the current age , labeled by some as the age of informatics or the internet , mental capabilities where multiplied. Merging the following two revolutions we can finally partly replace ourselves from dull and repetitive tasks of day to day life that will gradually stop to trouble the human kind leading to a more pleasant life. The GuarddoG project is about making machines that can see and act as a futuristic private guard .

The process of creating an autonomous robot that can perceive its environment and react and interact with it took nature millions of years. From the first bacteria to multi cell organisms , the wolf then the dog and the human , enormous evolutionary differences created beings of immense complexity and perfection. For someone to build something that took such a great amount of time in even a quarter of a lifetime is over-ambitious. An extra observation that is thought provoking is that while humans in complex decision making such as chess playing or tactic games with a limited set of rules have been surpassed by computers. In contrast in simple things for humans such as perceiving space , time , and "natural logic" every human has an innate superiority a result of the millions years of natural selection with these characteristics as a basis.

That being said GuarddoG does not attempt to create a dog (with everything a dog implies) , because this is practically impossible. Its goal is replacing a specific function of a dog as a guardian. I am very optimistic that with time robots will eventually be improved enough to be able to perform a multitude of tasks approaching something that will surely be different than a real dog , better at some things , and worse at some others.

Even though the future will offer even more tools , even now thanks to the marvelous technology and work of all the scientists , mathematicians , physicists , chemists , engineers and computer scientists (we are literally standing on the shoulders of giants) I was able to construct something very close to my original target , spending a fraction of the money and time that would be required before 15 or even 10 years.

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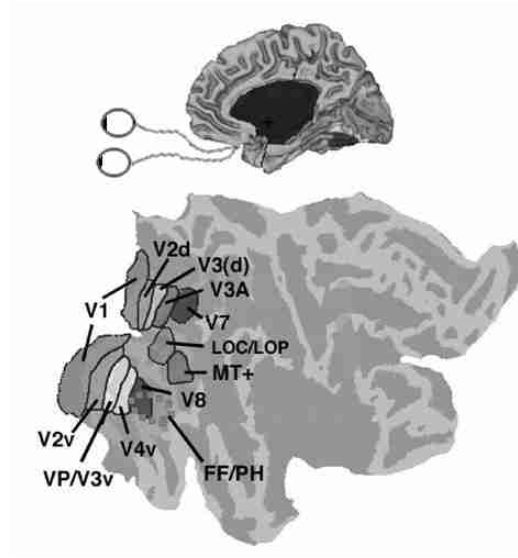
Illustration 1: A recent mapping on the first areas of the brain responsible for human vision

A better way for someone to visualize the small subset of functionality that is attempted by computer vision algorithms and in this case GuarddoG , is to compare it to the holy grail of cognition and intelligence , the human brain. Though computers for many years have managed to surpass human experts on tasks like playing chess , remembering sequences of numbers , performing arithmetic calculations on large data sets and recently even guessing questions to answers (IBM Watson on the Jeopardy TV Show) , things that everyone can do without even thinking about , like walking , identifying 3D objects and faces , and coordinating his head , eye and body movement are currently unachievable by machines at least to the extent of human performance .

This is a good indicator of the level of optimization that has taken place through the millions of years of evolution , because there is no doubt that if playing chess was a trait that leaded to natural selection the human brain would be totally different and have a much greater affinity towards these kind of activities. On the other hand , if breathing , beating the heart or walking and identifying objects wasn't crucial for the survival of the human species , to master these kind of activities could may well be as difficult and time consuming to be achieved as mastering chess .

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Project Goal

The goal of the "Guard Dog" Project

The goal of the Guard Dog Project is to build a robotics platform that can act as a guard , traverse a known path and fend off intruders. In case of a security breach it would signal the alarm and begin to follow the perpetrator and after a set distance would resume its previous path.

Robotics and computer vision are not a new domain of computer science and electrical engineering. It was especially shocking for me to see video footage of experiments in the AI Lab of Stanford (for example Les earnest and Lou paul and the Rancho Arm) circa 1971 that perform object detection , complex decision making and that actually use more or less the same algorithms as current robotics projects do. The major difference is not so much about the methods used , but the exponential improvement on computer hardware , popularly coined as Moore`s Law.

We are living in times where many high-end mobile phones actually have more complex processors than the satellites of the first mission to the moon and that experiments such as those that required equipment that cost millions of dollars in 1971 and could only be done in universities or government research centers can be reproduced with consumer electronics readily available everywhere. Unfortunately the consistent computation of the world around a robot is still a very difficult and expensive task with a generic CPU and no specialized hardware , but yet it seems almost feasible when you achieve even something that can work 10 times slower than a human.

Of course an additional goal of the project is to perform guard duties using only cheap building blocks but not passive sensors as modern security systems do. Instead building a semi-intelligent agent that can do this job the way humans would do it. It is an exploration of the possibilities and limits of current technologies along with software that can leverage the capabilities of computer hardware in an efficient way, to achieve an almost working result.

It is also interesting to note that the same computer vision libraries can , with adjustments , be fitted for tasks like driving cars in city streets to helping blind people find their way or any task that involves using optical information of ones surroundings to achieve a related goal.
The main difference would be the risk/cost and risk/performance ratio since a computer driving a car at full speed can have a much worse outcome than a small robot bumping on a wall.
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1 - Mathematical Model

1.1.0 Overview

The ease with which humans sense the world makes the problem of computer vision seem "easy" to solve. In fact the way we see is so natural and persistent that even scientists in the field made biased over-optimistic predictions about it. The fact is that despite the exponential growth in computational speed , and although there is a very big market that could certainly use vision algorithms to automate tasks , there is still no defacto algorithm that can compare to what human vision performs. Moreover from simple reflexes as maintaining focus and coordinating ones gaze , reading text , to tracking your position in an unknown city , vision seems to be "AI-Complete" , since understanding and combining what is seen is an altogether different task than the small building blocks which are presented here.
 A robot that can see and interact with the world , is basically a Turing machine on wheels. Therefore the whole model presented here is an adaptation of different mathematical concepts and a fusion of them together. The strip of tape in this Turing machine is constantly filled with symbols of light intensity as the light gets reflected and activates the camera sensor elements. When the control algorithm decides that the robot has to move it writes it to the according tape elements and the motors move , producing a new view of the world.
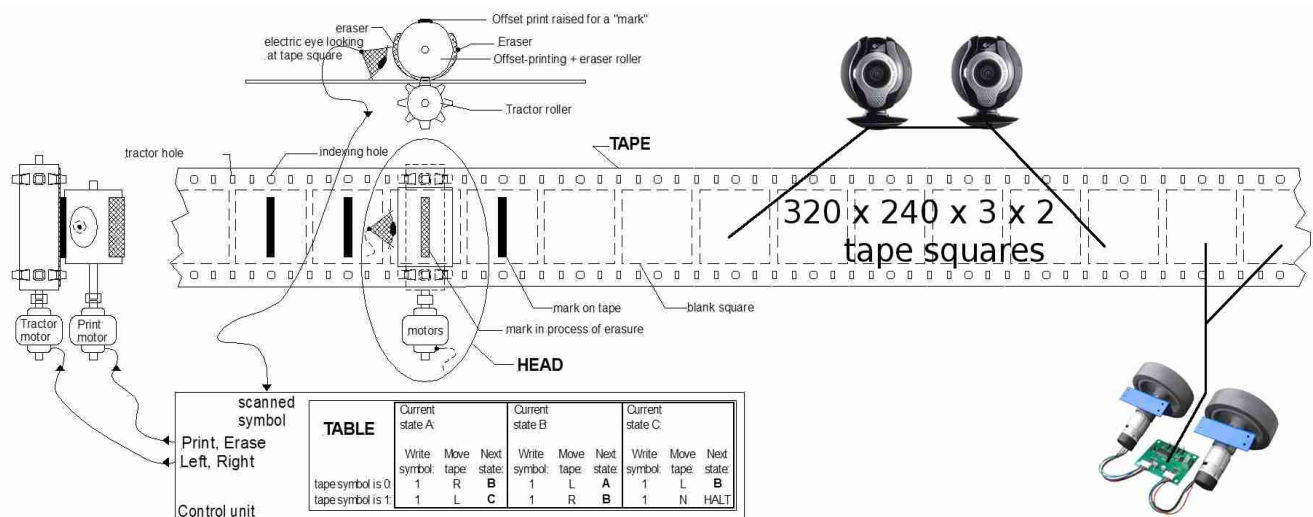
A fanciful mechanical Turing machine's TAPE and HEAD. The TABLE instructions might be on another "read only" tape, or perhaps on punch-cards. Usually a "finite state machine" is the model for the TABLE.

The first thing to take into consideration beginning to approach this problem , is how the physical world is being represented by the cameras. They are after all the means with which the GuarddoG/RoboVision algorithm collection , a "meta"physical entity can take a peek into reality. The data acquired must then be filtered to remove deformations and distortions that may corrupt the whole process. These steps are described in the Camera Model , Camera Calibration and Image Rectification parts of this document. Once two consistent images of the projection of the world on the camera sensors are aquired , they are examined for optical cues that reveal the details of the world in three dimensions and also the robots position. This is also discussed extensively , and the Disparity Mapping algorithm used by GuarddoG is a new implementation. When all these steps are finished , the next one is tracking the position of the robot (LK Optical Flow , RANSAC Homography) and the combination of the successive 3d Views together (SLAM , Obstacle Detection).

The final piece of the algorithm is a knowledge base that will set its goals and keep the state of the world , and steer the robot towards achieving them. For GuarddoG , its goal is the traversal of a standard path , and raising the alarm if a breach is found.
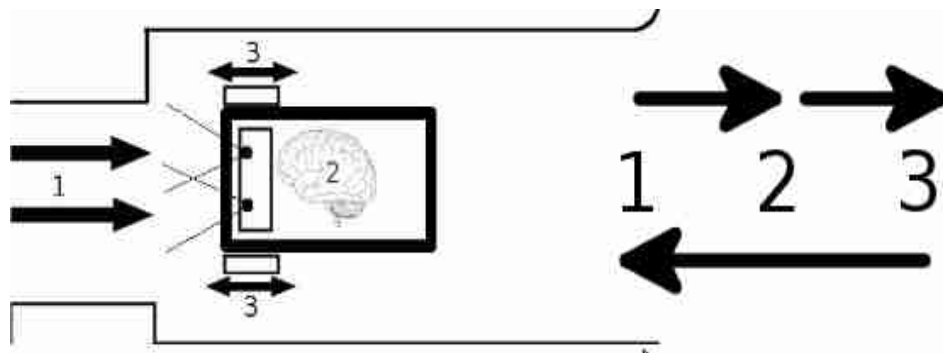
Illustration 2: The chicken and egg problem of an autonomous robot , that with its action changes its perception of the world , and with the changing perception of the world it changes its action..!

In beggining to make a system that sees , one can make many choices about the way with which to gather input. As nature teaches us , and by bringing to mind various insects and animals that have been optimized throught a process of millions of years to see one might use anything from ultrasonic sounds , to millions small eyes of insects up to human stereoscopy. With the world represented through the camera beeing so chaotic , and as this project does not deal with a fixed environment in which to be operated , while also having economic restrictions applied the best choice was a human like stereoscopic camera input. It is true that commercial RGB+depth cameras such as Microsoft Kinect can bypass a very big portion of the computational complexity of this project , but they still have their own short comings. The stereoscopic setup wasn`t chosen by accident by nature , and the nature of a robot that uses stereoscopic vision makes it closer to the human experience as a mode of viewing the world.

Illustration 3: What computers see
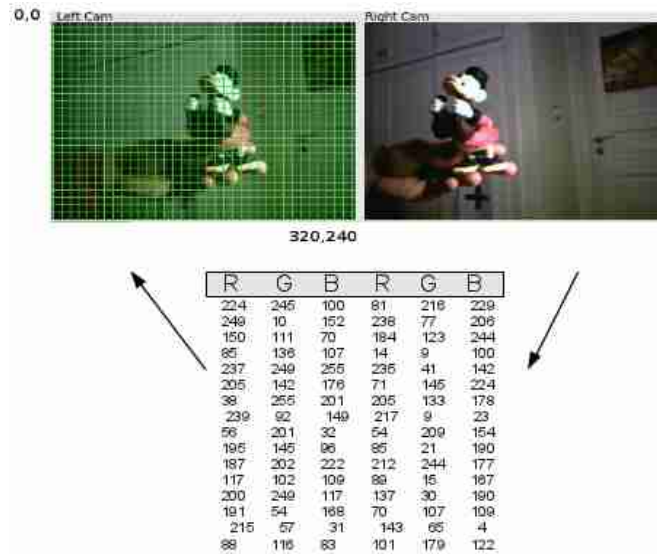
Trying to approach the computational limit of a dense stereoscopic method for two frames sized 320x240 pixels in order for a full search from an image patch sized 40x40 pixels on the left eye to all the possible matching patches along the epipolar line on the right eye , we have to make 320 x 320 x 240 / 40 = 24576000 /40 = 614400 operations in the worst case each time we get a depth map. In order to achieve a "human like" response time from the vision system this has to be done at a rate of 25 frames per second , or with a delay of 40 milliseconds per scan.. The number of operations per second increases exponentially as the image size becomes larger

SIZE	PIXEL AREA	OPERATIONS	OPERATIONS PER ms
QVGA	320 x 320 x 240 / 40	24576000	614,400 operations / ms
VGA	640 x 640 x 480 / 40	196608000	4,915,200 operations / ms
XGA	1024 x 1024 x 768 / 40	805306368	20,132,659 operations / ms
...	Other Configurations	...	...
WUXGA	1920 x 1920 x 1024 / 40	3774873600	94,371,840 operations / ms
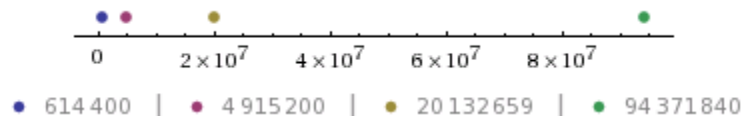
This exponential increase , of course , impacts all the algorithms used by the project , so the total number of operations is many times larger than the number on this table. The disparity mapping algorithm of guarddog is one of its "novelties" and is just showed here indicatively.

Manufacturing a physical stereo rig for the experiments which is perfectly aligned has a crucial effect on the calculations. Not only it increases computational efficiency and reduces errors but it also removes mathematical ambiguity about instances of the world that can be interpreted in many ways.. The relative position of the GuarddoG cameras is supposed to be constant and the two cameras always have a coplanar alignment with a fixed distance between the optical centers. The cameras are also never allowed to change their focus (nor could change it as they do not have an automatic focus control).
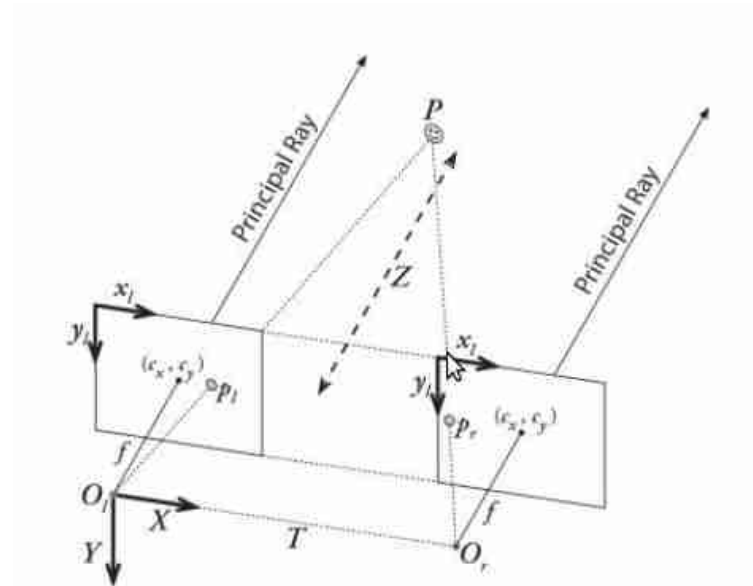

Illustration 4: Camera rig set-up

To avoid re calculation and use of the CPU for reasons avoidable by a better designed algorithm , the whole vision library uses a pipelined architecture , so that the same image will not have to pass a processing stage twice once it enters and according to the needs of the Robot Hypervisior the different stages try to be combined , or operations stay pending for the next frame.

The first , mathematical , part of the project analyzes all the mathematical background of the algorithms and discusses performance from a complexity viewpoint .

The second part focuses on software and technical details , along with performance statistics for different hardware setups and experimental results.

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1 - Mathematical Model

1.1.1 Camera Pinhole Model
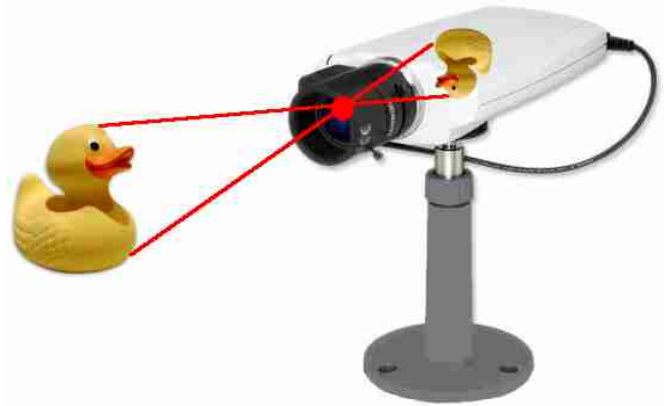
A **pinhole camera** is a simple [camera](#) without a [lens](#) and with a single small [aperture](#) – effectively a light-proof box with a small hole in one side. Light from a scene passes through this single point and projects an inverted image on the opposite side of the box. The human eye in bright light acts similarly, as do cameras using small apertures.

Up to a certain point, the smaller the hole, the sharper the image, but the dimmer the projected image. Optimally, the size of the aperture should be 1/100 or less of the distance between it and the projected image.

Because a pinhole camera requires a lengthy exposure, its [shutter](#) may be manually operated, as with a flap of light-proof material to cover and uncover the pinhole. Typical exposures range from 5 seconds to several hours.

The **pinhole camera model** describes the mathematical relationship between the coordinates of a 3D point and its [projection](#) onto the image plane of an *ideal* [pinhole camera](#), where the camera aperture is described as a point and no lenses are used to focus light. The model does not include, for example, geometric distortions or blurring of unfocused objects caused by lenses and finite sized apertures. It also does not take into account that most practical cameras have only discrete image coordinates. This means that the pinhole camera model can only be used as a first order approximation of the mapping from a 3D scene to a 2D image. Its validity depends on the quality of the camera and, in general, decreases from the center of the image to the edges as lens distortion effects increase.

Some of the effects that the pinhole camera model does not take into account can be compensated for, for example by applying suitable coordinate transformations on the image coordinates, and others effects are sufficiently small to be neglected if a high quality camera is used. This means that the pinhole camera model often can be used as a reasonable description of how a camera depicts a 3D scene, for example in [computer vision](#) and [computer graphics](#).

The [geometry](#) related to the mapping of a pinhole camera is illustrated in the figure. The figure contains the following basic objects

- A 3D orthogonal coordinate system with its origin at **O**. This is also where the *camera aperture* is located. The three axes of the coordinate system are referred to as X1, X2, X3. Axis X3 is pointing in the viewing direction of the camera and is referred to as the *optical axis*, *principal axis*, or *principal ray*. The 3D plane which intersects with axes X1 and X2 is the front side of the camera, or *principal plane*.

- An image plane where the 3D world is projected through the aperture of the camera. The image plane is parallel to axes X1 and X2 and is located at distance f from the origin **O** in the negative direction of the X3 axis. A practical implementation of a pinhole camera implies that the image plane is located such that it intersects the X3 axis at coordinate $-f$ where $f > 0$. f is also referred to as the *focal length*[[citation needed](#)] of the pinhole camera.

- A point **R** at the intersection of the optical axis and the image plane. This point is referred to as the *principal point* or *image center*.

- A point **P** somewhere in the world at coordinate (x_1, x_2, x_3) relative to the axes X1,X2,X3.

- The *projection line* of point **P** into the camera. This is the green line which passes through point **P** and the point **O**.

- The projection of point **P** onto the image plane, denoted **Q**. This point is given by the intersection of the projection line (green) and the image plane. In any practical situation we can assume that $x_3 > 0$ which means that the intersection point is well defined.

- There is also a 2D coordinate system in the image plane, with origin at **R** and with axes Y1 and Y2 which are parallel to X1 and X2, respectively. The coordinates of point **Q** relative to this coordinate system is (y_1, y_2).

The *pinhole* aperture of the camera, through which all projection lines must pass, is assumed to be infinitely small, a point. In the literature this point in 3D space is referred to as the *optical (or lens or camera) center*.[[citation needed](#)]

Next we want to understand how the coordinates (y_1, y_2) of point **Q** depend on the coordinates (x_1, x_2, x_3) of point **P**. This can be done with the help of the following figure which shows the same scene as the previous figure but now from above, looking down in the negative direction of the X2 axis.

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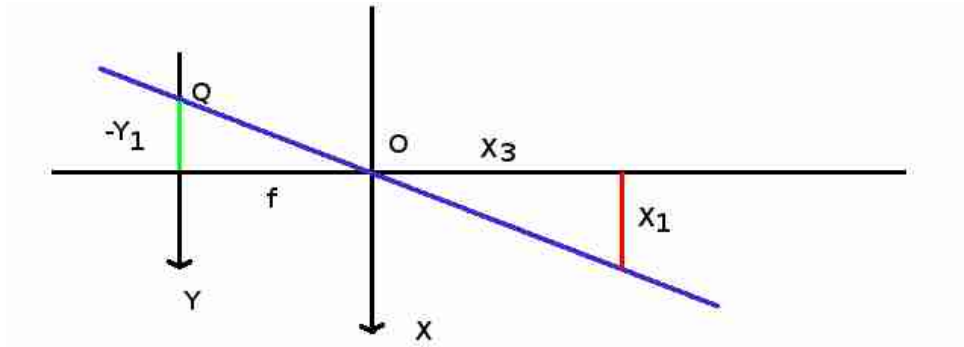
The geometry of a pinhole camera as seen from the X2 axis

In this figure we see two similar triangles, both having parts of the projection line (green) as their hypotenuses. The catheti of the left triangle are $-y_1$ and f and the catheti of the right triangle are x_1 and x_3. Since the two triangles are similar it follows that which is an expression that describes the relation between the 3D coordinates (x_1, x_2, x_3) of point **P** and its image coordinates (y_1, y_2) given by point **Q** in the image plane.[citation needed]

$$\frac{-y_1}{f} = \frac{x_1}{x_3} \vee y_1 = -f\frac{x_1}{x3}$$

$$\frac{-y_2}{f} = \frac{x_2}{x_3} \vee y_2 = -f\frac{x_2}{x3}$$

$$(y_1 y_2) = \frac{-f}{x_3}(x_1 x_2)$$

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1 - Mathematical Model

1.1.2 Camera Calibration

In mathematics, it is possible to define a lens set that will introduce no distortions in the image captured. In practice, however, and due to manufacturing process inefficiencies two types of distortion occur . Radial distortion , caused by the shape of lens not being parabolic , and tangential distortion due to the assembly process of the camera in the factory.

Radial distortion causes a characteristic twisting of straight lines as they get closer to the edges of the image and on systems that are heavily based on those images it can have a very detrimental effect on calculations that gets worse as the errors gradually accumulate in time. While disparity mapping algorithms can partly withstand this kind of distortion due to using a relatively large neighborhood of pixels that overall remains the same , point tracking and optical flow algorithms that estimate and track the camera position are very vulnerable to this kind of distortion.The reason this happens is because the relative positions of pixels change as they move to the edges and give wrong constraints for the system of equations to be solved later on.
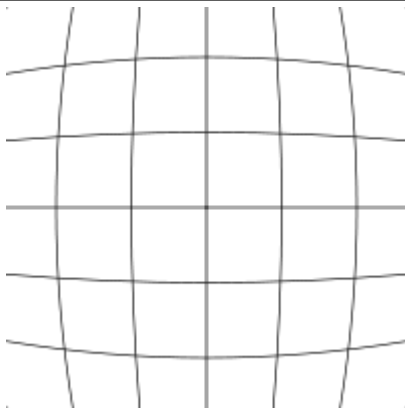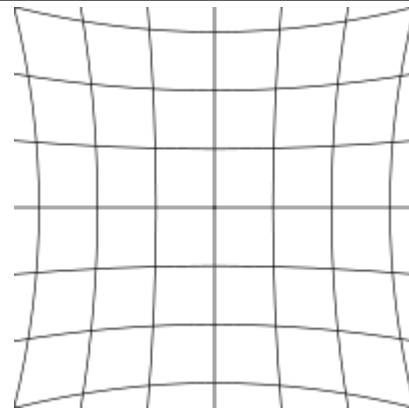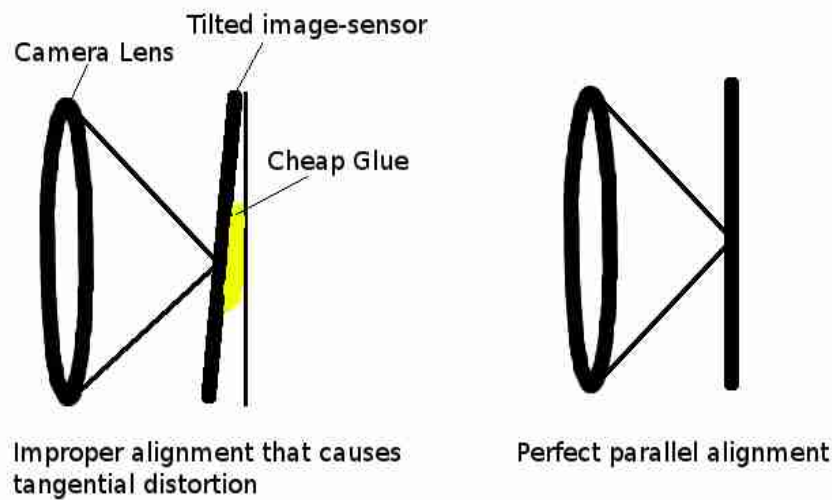
| Barrel distortion | Pincushion distortion |

Tangential Distortion on the other hand is a matter of misplacing the imaging sensor relatively to the lens (not a fully parallel placement) and therefore receiving a slightly skewed image.

 Figuring out the way with witch a camera distorts the projection of the world on to its image sensor is called camera calibration. There are numerous methods and considerations to be taken into account to achieve calibration , even methods that gradually "auto calibrate" the raw input images without special patterns and objects or prior training of the algorithm. [citations needed] . GuarddoG uses a much more common approach , acquiring the intrinsic camera parameters (explained in the next chapter) using a fixed chessboard pattern that on the calibration stage is expected to be moved across the visible image so that enough snapshots of data can be acquired that may lead to a precise calculation . The method used by OpenCV is [citation needed] and the pattern is for GuarddoG is a 10x7 chessboard. After OpenCV finds the calibration parameters , they are stored in a file and used by GuarddoG's pipelining as the first processing step after an image is acquired.
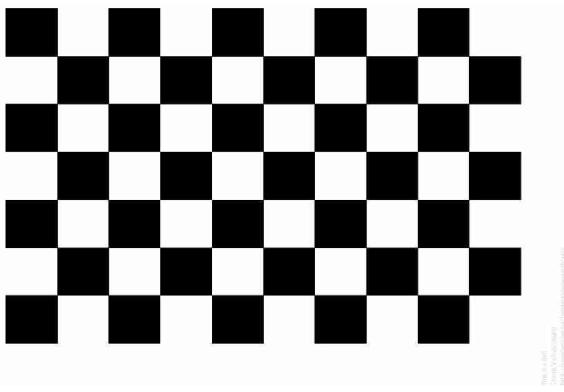
Illustration 5: OpenCV Chessboard 10x7 calibration pattern
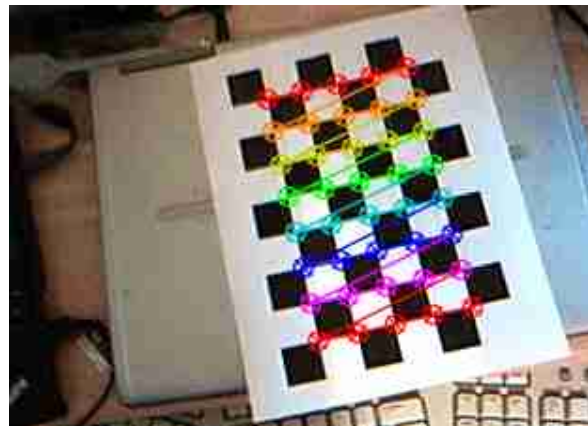
Illustration 6: Typical Detection Image Generated by OpenCV

The OpenCV implementation receives the corners between the chessboard blocks as inputs , which are extracted using a corner detector.   First, it computes the initial intrinsic parameters and sets the distortion coefficients to zero. Afterwards using the Levenberg-Marquardt optimization algorithm [citation needed] the reprojection error is minimized until a stable parameter set is found.

A thing that is worth to be mentioned is that the cameras used by GuarddoG are graded by the manufacturer to have a less than 5% distortion rate and the algorithms work sufficiently well even when input is uncalibrated.

The method was conceived by Zhang [Zhang99; Zhang00] and Sturm [Sturm99] , A Flexible New Technique for Camera Calibration (1998) by Zhengyou Zhang , Zhengyou Zhang
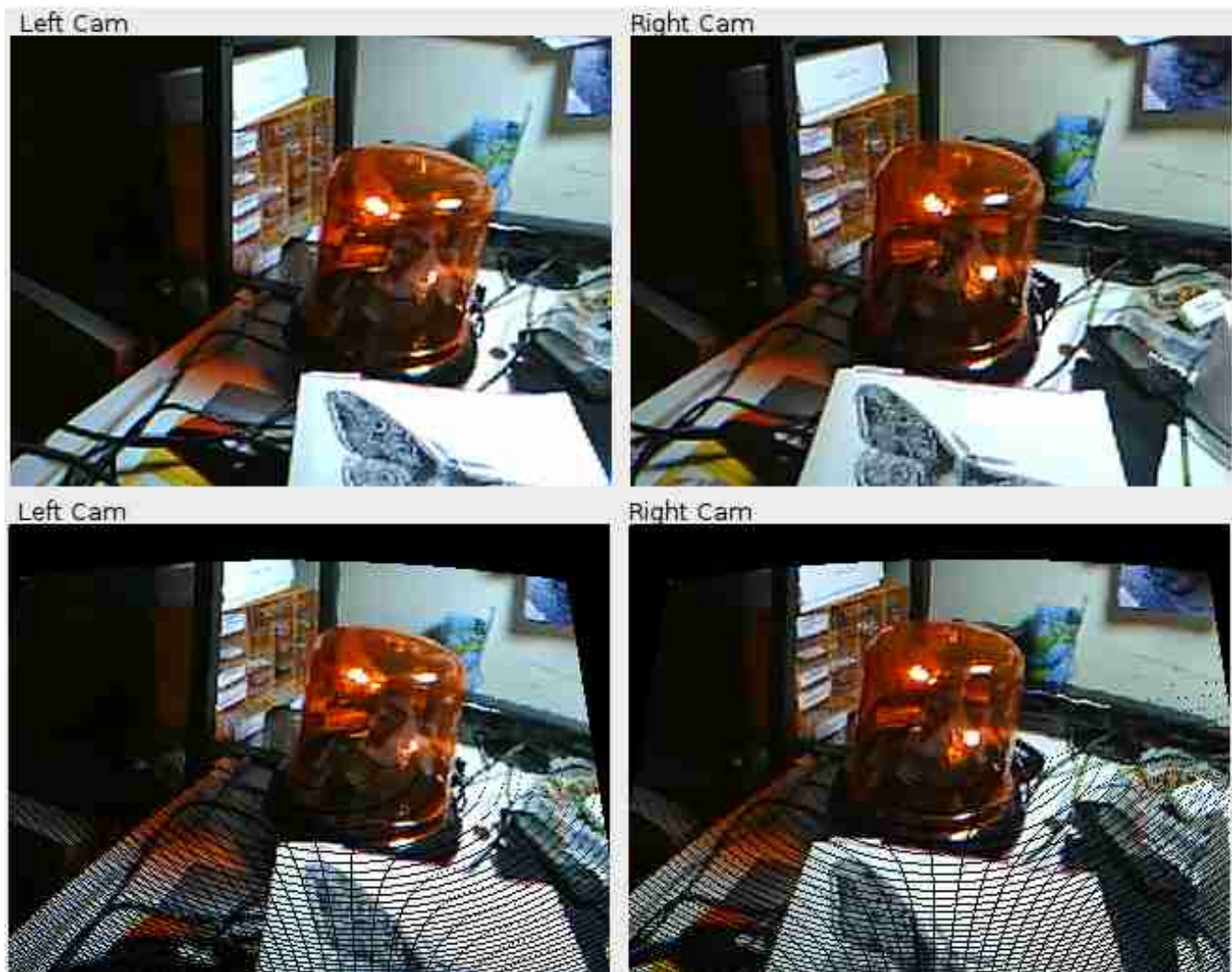
Illustration 7: Raw images received from the cameras and their calibrated equivalent (the distortion parameters are exaggerated to better show the way calibration alters the input images)

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1 - Mathematical Model

1.1.3 Image Rectification

Camera resectioning is the process of using the true parameters of the camera to produce a correct photograph or video stream of images. Usually, the camera parameters are represented in a 3 × 4 matrix called the camera matrix , and from the pinhole model we get the following equations for a perfect undistorted lens.

$$
s\begin{pmatrix} u \\ v \\ 1 \end{pmatrix} = \begin{pmatrix} f_x & \gamma & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_1 \\ r_{31} & r_{32} & r_{33} & t_1 \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix}
$$

$$
\begin{pmatrix} x \\ y \\ z \end{pmatrix} = R \begin{pmatrix} X \\ Y \\ Z \end{pmatrix} + t
$$
$$
x' = x/z
$$
$$
y' = y/z
$$
$$
u = f_x x' + c_x
$$
$$
v = f_y y' + c_y
$$

Where u , v are the undistorted pixels , fx and fy is focal length related to the pixel distance ratio [fx = mx * f , fy = my * f , (mx and my are determined by the physical dimensions of the pixel elements on the camera sensor)] , γ is a skew coefficient between axis x and y and for most contemporary imaging sensors is 0 and cx , cy are the coordinates of the principal point where the camera center (ideally at the center of the image) lies.

Radial and tangential distortion can be included to the model using the following equations

$$s\begin{pmatrix} u \\ v \\ 1 \end{pmatrix} = \begin{pmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} r_{11} & r_{11} & r_{11} & t_1 \\ r_{11} & r_{11} & r_{11} & t_1 \\ r_{11} & r_{11} & r_{11} & t_1 \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = R \begin{pmatrix} X \\ Y \\ Z \end{pmatrix} + t$$

$$x' = x/z$$
$$y' = y/z$$
$$r^2 = x'^2 + y'^2$$
$$x'' = x'(1 + k_1 r^2 + k_2 r^4 + k_3 r^6) + 2 p_1 x' y' + p_2(r^2 + 2x'^2)$$
$$y'' = y'(1 + k_1 r^2 + k_2 r^4 + k_3 r^6) + p_1(r^2 + 2y'^2) + 2p_2 x' y'$$
$$u = f_x x'' + c_x$$
$$v = f_y y'' + c_y$$

Radial distortion is modeled by the k_1 , k_2 and k_3 (which is usually zero) coefficients and tangential distortion is modeled by p_1 and p_2.

Since re sectioning the image must be done for every frame received from the usb cameras (which serve images @ 120 Hz) and since most camera chips don't offer a hardware interface for passing the distortion parameters to the local integrated circuit so it can perform this kind of image processing with out involving the main processor , a fast technique must be applied to avoid calculating all these numbers on every program loop.

Since the camera doesn't change its focus settings , the distortion parameters are always the same. We can use this knowledge to our advantage generating a precalculation frame that has pointers to the calibrated positions as its elements after acquiring the distortion parameters. That way , the expensive task of computing the formulas mentioned above happens only once and the least possible overhead is added to the pipeline process (around 500 microseconds per frame on the main development computer , hardware details are on the second part of this text).

This tactic is followed both by the OpenCV implementation , as well as the GuarddoG RoboVision stack.

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1 - Mathematical Model

1.2.0 Image Processing

Digital cameras are devices that capture the light that the universe reflects on their sensor. The general problem most vision algorithms try to solve is guessing what kind of a world reflects the light in that way. The algorithms presented here are building blocks that gradually transform the raw RGB input into more meaningful (for a computer) representations .

Convolution is a mathematical operation applied to sets of values that "redistributes" them according to weights. The carrier of the weights is called a convolution matrix and it is typically a 3x3 kernel with one of the values , usually the middle one , called an anchor point.

The values transformed by the convolution matrix are the red , green and blue light intensities of the pixels retrieved from the image sensor. In the following example we assume a 3x3 kernel and a monochrome image sensor that captured 9x6 pixels. The kernel is passed left to right and up to down until all of the elements are changed. GuarddoG uses Gaussian Blur , Sobel and Second Derivative Convolution kernels that follow with example images.

1	1	1
1	**1**	1
1	1	1

3X3 Convolution Kernel
Divisor 9

As the anchor of the kernel passes from each element of the image array the value (marked blue) gets replaced by the addition of the neighboring elements multiplied with the according kernel element.

$$H(x,y)=\sum_{i=0}^{Mi-1}\sum_{j=0}^{Mj-1} I(x+i-a_i,\, y+j-a_j)\,G(i,j)$$

The anchor element on the light intensities array will become
(1x90+1x80 +1x70+1x90+1*80+1*70+ 1x90 + 1x80 + 1x70) / 9 which is 80

9 x 6 Original Light Intensities Captured

90	80	70	90	80	70	90	80	70
90	**80**	70	90	80	70	90	80	70
90	80	70	90	80	70	90	80	70
90	80	70	90	80	70	90	80	70
90	80	70	90	80	70	90	80	70
90	80	70	90	80	70	90	80	70

 An important thing to be noted Is that values on the edges of the array (marked orange) can not be correctly calculated as not all neighboring elements exist , common solutions for this is "imagining" that there are zero elements when an element does not exist , using a different divisor to compensate for the missing elements or skipping the elements that can not be calculated correctlly .

- 🟡 The Frame pixel 0,0
- 🔵 The 3x3 Convolution Kernel
- 🟢 The anchor point
- 🔴 Areas Out of Frame
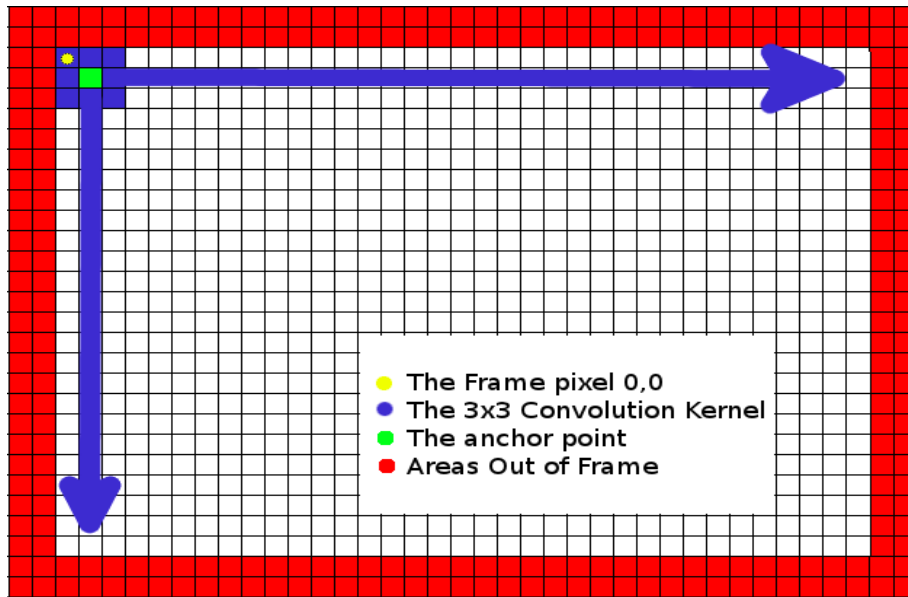
GAUSSIAN BLUR	
<table><tr><td>1</td><td>1</td><td>1</td></tr><tr><td>1</td><td>**1**</td><td>1</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table> Divisor 9	

SOBEL DERIVATIVE	
<table><tr><td>1</td><td>-2</td><td>1</td></tr><tr><td>2</td><td>**-4**</td><td>2</td></tr><tr><td>1</td><td>-2</td><td>1</td></tr></table> Divisor 1	

SECOND-ORDER DERIVATIVE	
<table><tr><td>-1</td><td>0</td><td>1</td></tr><tr><td>0</td><td>**0**</td><td>0</td></tr><tr><td>1</td><td>0</td><td>-1</td></tr></table> Divisor 3	

Gaussian blur evens out the colors on an input image using a Gaussian function. It is a common operation by vision software mainly used since due to the fact that image sensors retrieve pixels that suffer from noise , these noise spikes are reduced therefore leading to better edge and corner detection.

The Sobel operator acts as a differentiation operator , resulting in an output that only responds to "change" of colors and ignores similar colored areas. Thus it is very useful as it reduces the image to its more unique parts , its edges .

The second-order derivative operator acts also as a differentiation operator , resulting in an output that only responds to "change" of "change" of colors (second order) and ignores similar colored areas while also having a better reaction to sudden spikes on the color frequency. Its output also reveals the image edges but is much more stable than the sobel operator .

Palette reduction reduces the total number of possible tones that one pixel can take from 255 * 255 * 255 to an other given number. Reducing colors causes the similar colored pixels to fall into the same category.

Thresholding applies a high (or low) pass filter on an incoming signal and pixels that do not match the criteria are discarded . This is applied after sobel and second order edge operations to reduce false output caused by noise.

The miscellaneous image processing operations used by guarddog are mentioned in the table that follows

NAME	OPERATIONS	DESCRIPTION
Gaussian Blur	9 * Height*Width	Blurring input image to reduce noise
Sobel edge det.	9 * Height*Width	Edge Detection
Second-order de.	4 * Height*Width	Edge Detection
Palette Reduce	Height*Width	Group color frequencies together to reduce them
Threshold Image	Height*Width	Discard information that may be subject to noise
Histogram	Height*Width	Calculate total pixes that share each color value

*

1 - Mathematical Model

1.2.1 Corner Detection

Illustration 8: Left : An incoming image after passing through Sobel Edge detection , Right : The corners detected

After performing some of the various image processing steps mentioned above , it is almost time to move away from the image as an array of color frequencies and focus on specific points on it that stand out and are unique. These are called features and can be picked using a multitude of criteria. The features used by GuarddoG are corners which have been well documented and are typically detected casting a circle around a point

UNDER CONSTRUCTION

Fusing points and lines for high performance tracking.
Machine learning for high-speed corner detection.

*
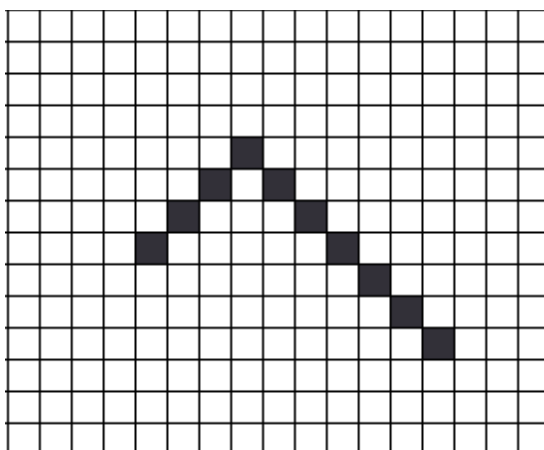
1 - Mathematical Model

1.2.2 Template Matching and Integral Images

After image processing is finished producing "versions" of the data that reveal different aspects of the input images , the next technique performed by guarddog is called Template Matching. There are numerous criteria that can be used to compare two image parts and decide if they match.

GuarddoG uses a combination of pyramid segmentation , feature and template based matching across different templates to achieve high performance without sacrificing result quality. To this end the use of integral images speeds up and greatly improves the algorithm (performance-wise) .

The most simple and computationally efficient method for comparing two blocks of pixels is named SAD (Sum of Absolute Differences) and is basically the following equation.

$$SAD = \sum_{x=0}^{width} \sum_{y=0}^{height} |(image1[x][y] - image2[x][y])|$$

This operation can be hardware accelerated on MMX and SSE2 instruction capable CPUs and thus is very lite weight. Although there are other metrics to find out if two image blocks match (and how similar they are) such as MSE (Mean Squared Error) , SATD (Sum of absolute transformed differences) , Normalized Cross Correlation (NCC) and other even more complex methods.

To make up for quality loss , while keeping the increased performance that SAD offers guarddog compares different "versions" of the patches that resulted mainly from convolution operations on the original data. That way the computational cost is moved from the block matching operation that can be performed millions of times (especially in large images) and does not take a guaranteed time to converting the image itself which has a fixed sized.

The different SAD results are then combined into a single value according to weights to compensate for the different range of values in each of the sub images. In order to further skip unneeded calculations a local histogram is used as a threshold that can completely avoid calculations if the 2 image blocks bear no resemblance at all (i.e. one is completely white and the other completely black)
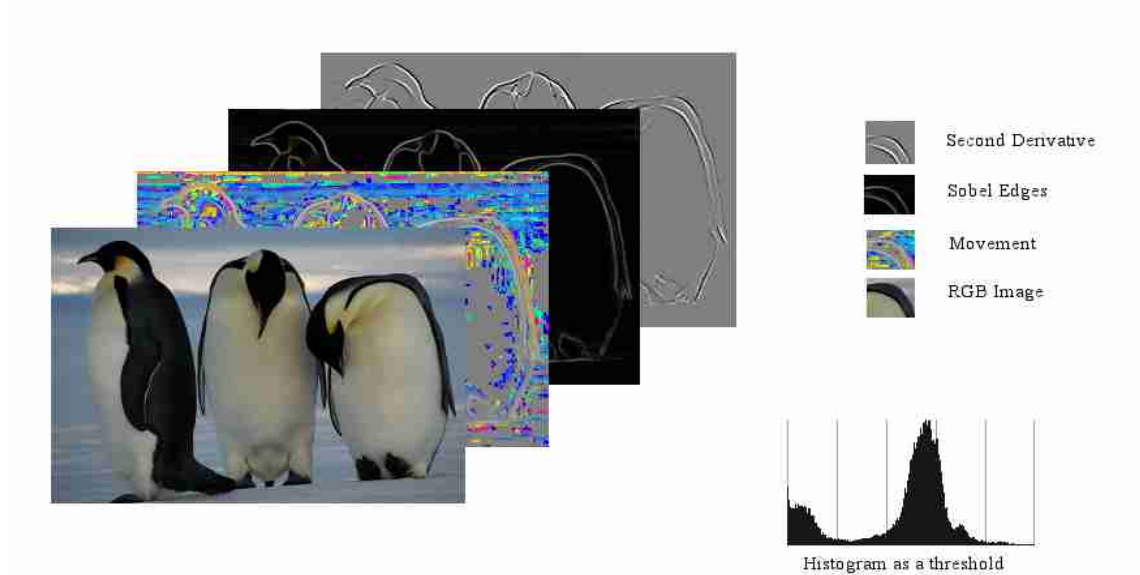
Illustration 9: The things taken into account when comparing patches

Before going into more detail about the template matching function , another useful representation for massive calculations on images is called integral images , or summed area tables.

$$I(x', y') = \sum_{x=0}^{x'} \sum_{y=0}^{y'} (image[x][y])$$

Once the table that every x,y has as an element the I(x,y) is created . We can skip a huge number of adding operations for an arbitrary area of the image (limited only by the maximum value of an integer on the machine). Any block addition operation is thus reduced to 4 operations.

$$\sum_{x=x1}^{x2} \sum_{y=y1}^{y2} image[x][y] = I(x1, y1) + I(x2, y2) - I(x2, y1) - I(x1, y2)$$

The resulting operation is not SAD because the subtraction does not produce an absolute difference on each pixel , the resulting operation is a plain Sum of Differences which is an even worse metric than SAD but it has such a big performance impact , that when used in conjunction with the sub images mentioned before it can make dense disparity mapping feasible , and when used in small enough areas provides good overall results.

Instead of
|image1[x1][y1] – image2[x1][y1]| + |image1[x2][y1] – image2[x2][y1]| + … + | image1[xN][yN] – image2[xN][yN]| we have

image1[x1][y1] + image1[x2][y1] + … + image1[xN][yN] - (image2[x1][y1] + image2[x2][y1] + … + image2[xN][yN]) which is the same with

image1[x1][y1] – image2[x1][y1] + image1[x2][y1] – image2[x2][y1] + ... +
image1[xN][yN] – image2[xN][yN]
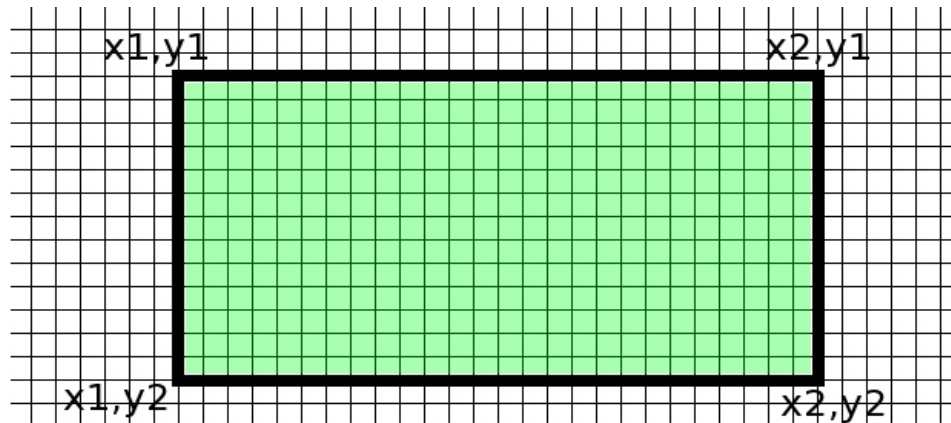
Illustration 10: We can find the sum of the green area by adding all the pixels in it performing (x2-x1)(y2-y1) operations*
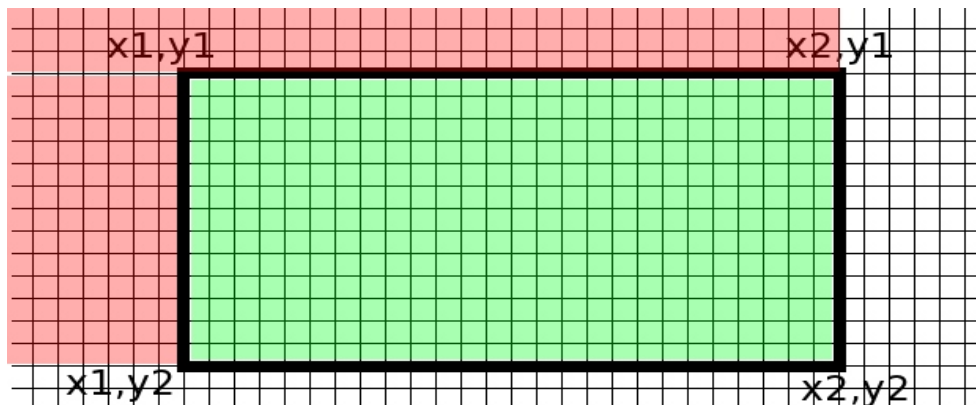
Illustration 11: We can find the sum of the green area by performing 4 operations , I(x1,y1)+I(x2,y2)-I(x1,y2)-I(x2,y1) provided we have first calculated the integral array I

Illustration 12: A SAD metric returns total mismatch of these two blocks. An addition of differences metric (not absolute) such as the integral imaging technique described before returns a total match of the two image blocks

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1 - Mathematical Model

1.2.2 HAAR Wavelet Face Detection

Haar-like features are digital image features used in object recognition. They owe their name to their intuitive similarity with Haar wavelets and were used in the first real-time face detector.

Historically, working with only image intensities (i.e., the RGB pixel values at each and every pixel of image) made the task of feature calculation computationally expensive. A publication by Papageorgiou et al.[1] discussed working with an alternate feature set based on Haar wavelets instead of the usual image intensities. Viola and Jones[2] adapted the idea of using Haar wavelets and developed the so called Haar-like features. A Haar-like feature considers adjacent rectangular regions at a specific location in a detection window, sums up the pixel intensities in these regions and calculates the difference between them. This difference is then used to categorize subsections of an image. For example, let us say we have an image database with human faces. It is a common observation that among all faces the region of the eyes is darker than the region of the cheeks. Therefore a common haar feature for face detection is a set of two adjacent rectangles that lie above the eye and the cheek region. The position of these rectangles is defined relative to a detection window that acts like a bounding box to the target object (the face in this case).

In the detection phase of the Viola–Jones object detection framework, a window of the target size is moved over the input image, and for each subsection of the image the Haar-like feature is calculated. This difference is then compared to a learned threshold that separates non-objects from objects. Because such a Haar-like feature is only a weak learner or classifier (its detection quality is slightly better than random guessing) a large number of Haar-like features are necessary to describe an object with sufficient accuracy. In the Viola–Jones object detection framework, the Haar-like features are therefore organized in something called a classifier cascade to form a strong learner or classifier.

The key advantage of a Haar-like feature over most other features is its calculation speed. Due to the use of integral images, a Haar-like feature of any size can be calculated in constant time (approximately 60 microprocessor instructions for a 2-rectangle feature).

Rectangular Haar-like features

A simple rectangular Haar-like feature can be defined as the difference of the sum of pixels of

areas inside the rectangle, which can be at any position and scale within the original image. This modified feature set is called 2-rectangle feature. Viola and Jones also defined 3-rectangle features and 4-rectangle features. The values indicate certain characteristics of a particular area of the image. Each feature type can indicate the existence (or absence) of certain characteristics in the image, such as edges or changes in texture. For example, a 2-rectangle feature can indicate where the border lies between a dark region and a light region.
[edit] Fast computation of Haar-like features

One of the contributions of Viola and Jones was to use summed area tables[3], which they called integral images. Integral images can be defined as two-dimensional lookup tables in the form of a matrix with the same size of the original image. Each element of the integral image contains the sum of all pixels located on the up-left region of the original image (in relation to the element's position). This allows to compute sum of rectangular areas in the image, at any position or scale, using only four lookups:

$$\text{sum} = pt_4 - pt_3 - pt_2 + pt_1. \,$$

where points ptn belong to the integral image (include a figure).

Each Haar-like feature may need more than four lookups, depending on how it was defined. Viola and Jones's 2-rectangle features need six lookups, 3-rectangle features need eight lookups, and 4-rectangle features need nine lookups.
[edit] Tilted Haar-like features

Lienhart and Maydt[4] introduced the concept of a tilted (45°) Haar-like feature. This was used to increase the dimensionality of the set of features in an attempt to improve the detection of objects in images. This was successful, as some of these features are able to describe the object in a better way. For example, a 2-rectangle tilted Haar-like feature can indicate the existence of an edge at 45°.

Messom and Barczak[5] extended the idea to a generic rotated Haar-like feature. Although the idea sounds mathematically sound, practical problems prevented the use of Haar-like features at any angle. In order to be fast, detection algorithms use low resolution images, causing rounding errors. For this reason, rotated Haar-like features are not commonly used.

The Viola–Jones object detection framework is the first object detection framework to provide competitive object detection rates in real-time proposed in 2001 by Paul Viola and Michael Jones[1][2]. Although it can be trained to detect a variety of object classes, it was motivated primarily by the problem of face detection. This algorithm is implemented in OpenCV as cvHaarDetectObjects().

The features employed by the detection framework universally involve the sums of image pixels within rectangular areas. As such, they bear some resemblance to Haar basis functions, which have been used previously in the realm of image-based object detection[3]. However, since the features used by Viola and Jones all rely on more than one rectangular area, they are

generally more complex. The figure at right illustrates the four different types of features used in the framework. The value of any given feature is always simply the sum of the pixels within clear rectangles subtracted from the sum of the pixels within shaded rectangles. As is to be expected, rectangular features of this sort are rather primitive when compared to alternatives such as steerable filters. Although they are sensitive to vertical and horizontal features, their feedback is considerably coarser. However, with the use of an image representation called the integral image, rectangular features can be evaluated in constant time, which gives them a considerable speed advantage over their more sophisticated relatives. Because each rectangular area in a feature is always adjacent to at least one other rectangle, it follows that any two-rectangle feature can be computed in six array references, any three-rectangle feature in eight, and any four-rectangle feature in just nine.

[edit] Learning algorithm

The speed with which features may be evaluated does not adequately compensate for their number, however. For example, in a standard 24x24 pixel sub-window, there are a total of 45,396 possible features, and it would be prohibitively expensive to evaluate them all. Thus, the object detection framework employs a variant of the learning algorithm AdaBoost to both select the best features and to train classifiers that use them.

Cascade Architecture

[edit] Cascade architecture

The evaluation of the strong classifiers generated by the learning process can be done quickly, but it isn't fast enough to run in real-time. For this reason, the strong classifiers are arranged in a cascade in order of complexity, where each successive classifier is trained only on those selected samples which pass through the preceding classifiers. If at any stage in the cascade a classifier rejects the sub-window under inspection, no further processing is performed and continue on searching the next sub-window (see figure at right). The cascade therefore has the form of a degenerate tree. In the case of faces, the first classifier in the cascade – called the attentional operator – uses only two features to achieve a false negative rate of approximately 0% and a false positive rate of 40%.[4] The effect of this single classifier is to reduce by roughly half the number of times the entire cascade is evaluated.

The cascade architecture has interesting implications for the performance of the individual classifiers. Because the activation of each classifier depends entirely on the behavior of its predecessor, the false positive rate for an entire cascade is:

Thus, to match the false positive rates typically achieved by other detectors, each classifier can get away with having surprisingly poor performance. For example, for a 32-stage cascade to achieve a false positive rate of $10 - 6$, each classifier need only achieve a false positive rate of about 65%. At the same time, however, each classifier needs to be exceptionally capable if it is to achieve adequate detection rates. For example, to achieve a detection rate of about 90%, each classifier in the aforementioned cascade needs to achieve a detection rate of approximately 99.7%.

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1 - Mathematical Model

1.3.0 World Coordinate System

EMPTY FOR NOW :P

*

1 - Mathematical Model

1.3.1 Epipolar Geometry

Assuming a rectified input of two pinhole cameras with a known alignment , viewing a 3D scene, there are some geometric relations about the projections of 3D points among them.

Both cameras see the world from a different viewpoint , and while the projected image is different there are some geometric constraints that can be leveraged to be used for disparity mapping , which will be analyzed later.

GuarddoG's cameras are positioned in parallel so the epipolar plane forms a parallel line from frame to frame. This configuration is used to reduce errors caused by incorrect calibration and reduce the overall complexity of the algorithms that are based on matching parts from one image to the other.
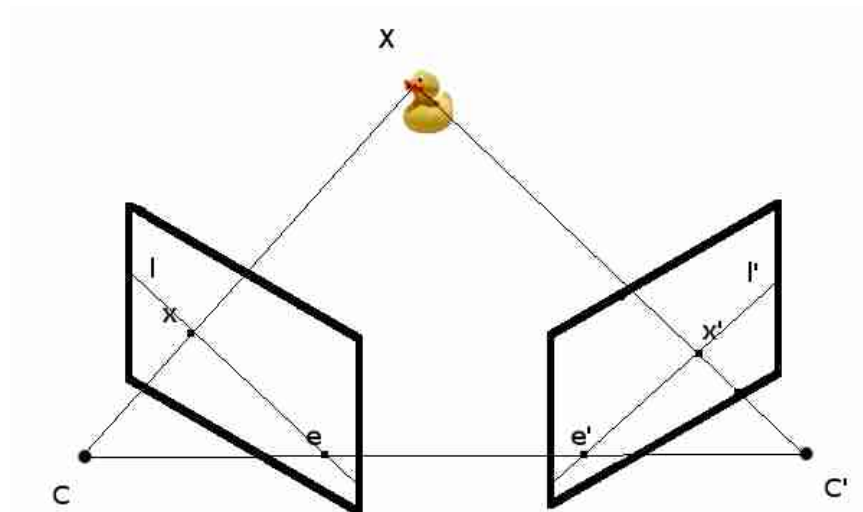
Illustration 13: A non parallel allignment where we can see highlighted the camera centers C and C' and the baseline that goes through them , the epipoles e and e' , the projection of the point X at x and x' and the epipolar lines l and l'

With the parallel setup the two projection images are essentially beeing produced by a translation of the camera center parallel to the image plane. This results in the points e and e' beeing in infinity , and the baseline never touching the image plane (since it is parallel to it)

Since the projection of all the points on the line from C to X lay on the l' epipolar line , to find out the projection of the ducks head on the right image we can search only the area having the same height coordinates from image to image and that makes disparity mapping practical for computation.

From frame to frame (in the axis of time and not space) since we have lots of different types of movements and combinations of rotations and translations epipolar geometry is once again useful for the calculation of the fundamental matrix since it provides the fundamental matrix equation constraint. GuarddoG though uses homographies and not the fundamental matrix for camera pose estimation since the 3d points typically have a higher error rate and lower coverage than the corners that are used for the homographies.

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1 - Mathematical Model

1.3.2 Disparity Mapping
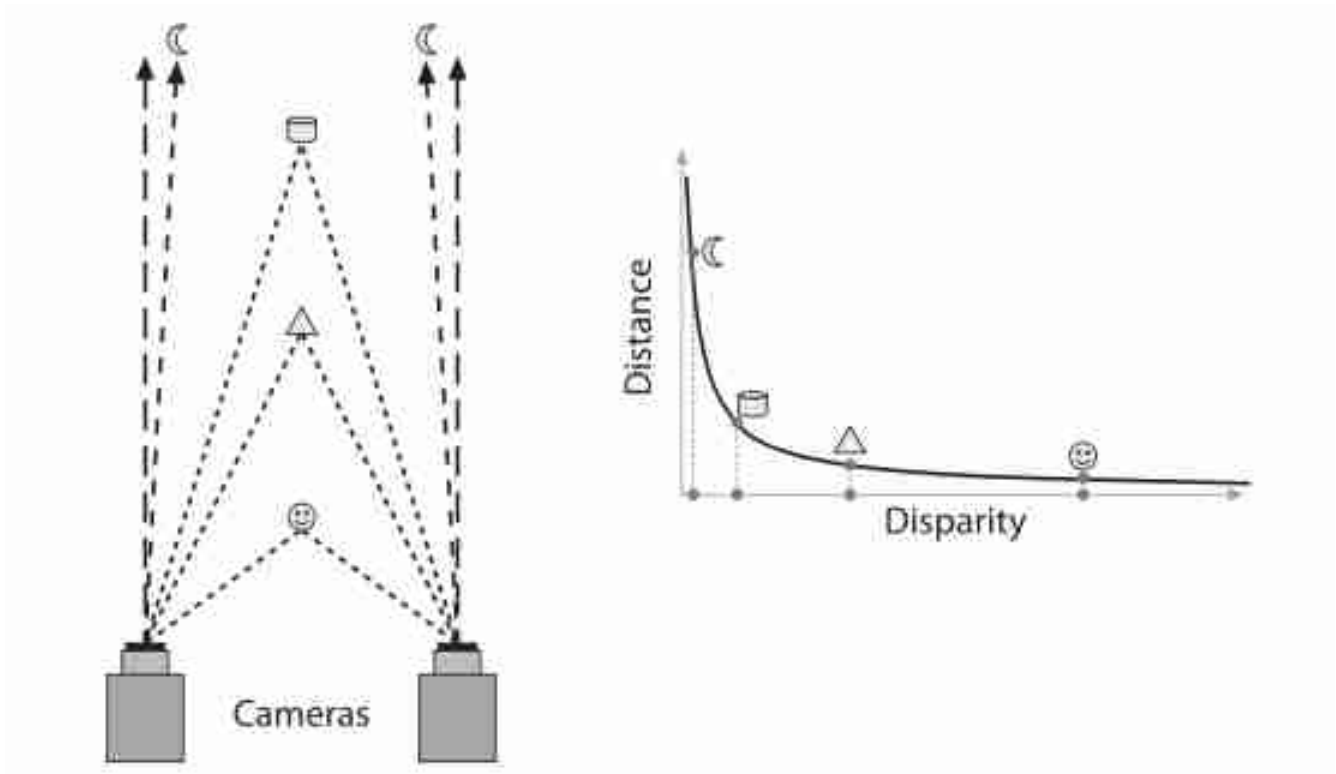
Binocular disparity refers to the difference in image location of an object seen by the left and right eyes, resulting from the eyes' horizontal separation. The brain uses binocular disparity to extract depth information from the two-dimensional retinal images in stereopsis. In computer vision, binocular disparity refers to the difference in coordinates of similar features within two stereo images.

A similar disparity can be used in rangefinding by a coincidence rangefinder to determine distance and/or altitude to a target. In astronomy, the disparity between different locations on the Earth can be used to determine various celestial parallax, and Earth's orbit can be used for stellar parallax.

Human eyes are horizontally separated by about 50–75 mm (interpupillary distance) depending on each individual. Thus, each eye has a slightly different view of the world. This can be easily seen when alternately closing one eye while looking at a vertical edge. The binocular disparity can be observed from apparent horizontal shift of the vertical edge between both views.

At any given moment, the line of sight of the two eyes meet at a point in space. This point in space projects to the same location (i.e. the center) on the retinae of the two eyes. Because of the different viewpoints observed by the left and right eye however, many other points in space do not fall on corresponding retinal locations. Visual binocular disparity is defined as the difference between the point of projection in the two eyes and is usually expressed in degrees as the visual angle.[1]

Figure 1: The full black circle is the point of fixation. The blue object lies nearer to the

observer. Therefore it has a "near" disparity dn. Objects lying more far away (green) correspondingly have a "far" disparity df. Binocular disparity is the angle between two lines of projection in one eye. One of which is the real projection from the object to the actual point of projection. The other one is the imaginary projection running through the focal point of the lens of the one eye to the point corresponding to the actual point of projection in the other eye. For simplicity reasons here both objects lie on the line of fixation for one eye such that the imaginary projection ends directly on the fovea of the other eye, but in general the fovea acts at most as a reference. Note that far disparities are smaller than near disparities for objects having the same distance from the fixation point.

In computer vision, binocular disparity is calculated from stereo images taken from a set of stereo cameras. The variable distance between these cameras, called the baseline, can affect the disparity of a specific point on their respective image plane. As the baseline increases, the disparity increases due to the greater angle needed to align the sight on the point. However, in computer vision, binocular disparity is referenced as coordinate differences of the point between the right and left images instead of a visual angle. The units are usually measured in pixels.
[edit] Tricking neurons with 2D images
Figure 2. Simulation of disparity from depth in the plane. (relates to Figure 1)

Brain cells (neurons) in a part of the brain responsible for processing visual information coming from the retinae (primary visual cortex) can detect the existence of disparity in their input from the eyes. Specifically, these neurons will be active, if an object with "their" special disparity lies within the part of the visual field to which they have access (receptive field).[2]

Researchers investigating precise properties of these neurons with respect to disparity present visual stimuli with different disparities to the cells and look whether they are active or not. One possibility to present stimuli with different disparities is to place objects in varying depth in front of the eyes. However, the drawback to this method may not be precise enough for objects placed further away as they possess smaller disparities while objects closer will have greater disparities. Instead, neuroscientists use an alternate method as schematised in Figure 2.

Figure 2: The disparity of an object with different depth than the fixation point can alternatively be produced by presenting an image of the object to one eye and a laterally shifted version of the same image to the other eye. The full black circle is the point of fixation. Objects in varying depths are placed along the line of fixation of the left eye. The same disparity produced from a shift in depth of an object (filled coloured circles) can also be produced by laterally shifting the object in constant depth in the picture one eye sees (black circles with coloured margin). Note that for near disparities the lateral shift has to be larger to correspond to the same depth compared with far disparities. This is what neuroscientists usually do with random dot stimuli to study disparity selectivity of neurons since the lateral distance required to test disparities is less than the distances required using depth tests. This principle has also been applied in autostereogram illusions.
[edit] Computing disparity usi

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1 - Mathematical Model

1.4.0 RANSAC

RANSAC is an abbreviation for "RANdom SAmple Consensus". It is an iterative method to estimate parameters of a mathematical model from a set of observed data which contains outliers. It is a non-deterministic algorithm in the sense that it produces a reasonable result only with a certain probability, with this probability increasing as more iterations are allowed. The algorithm was first published by Fischler and Bolles in 1981.

A basic assumption is that the data consists of "inliers", i.e., data whose distribution can be explained by some set of model parameters, and "outliers" which are data that do not fit the model. In addition to this, the data can be subject to noise. The outliers can come, e.g., from extreme values of the noise or from erroneous measurements or incorrect hypotheses about the interpretation of data. RANSAC also assumes that, given a (usually small) set of inliers, there exists a procedure which can estimate the parameters of a model that optimally explains or fits this data.

A simple example is fitting of a 2D line to a set of observations. Assuming that this set contains both inliers, i.e., points which approximately can be fitted to a line, and outliers, points which cannot be fitted to this line, a simple least squares method for line fitting will in general produce a line with a bad fit to the inliers. The reason is that it is optimally fitted to all points, including the outliers. RANSAC, on the other hand, can produce a model which is only computed from the inliers, provided that the probability of choosing only inliers in the selection of data is sufficiently high. There is no guarantee for this situation, however, and there are a number of algorithm parameters which must be carefully chosen to keep the level of probability reasonably high.

A data set with many outliers for which a line has to be fitted.

Fitted line with RANSAC, outliers have no influence on the result.

[edit] Overview

The input to the RANSAC algorithm is a set of observed data values, a parameterized model which can explain or be fitted to the observations, and some confidence parameters.

RANSAC achieves its goal by iteratively selecting a random subset of the original data. These data are hypothetical inliers and this hypothesis is then tested as follows:

A model is fitted to the hypothetical inliers, i.e. all free parameters of the model are reconstructed from the inliers.
All other data are then tested against the fitted model and, if a point fits well to the estimated model, also considered as a hypothetical inlier.
The estimated model is reasonably good if sufficiently many points have been classified as hypothetical inliers.
The model is reestimated from all hypothetical inliers, because it has only been estimated from the initial set of hypothetical inliers.

Finally, the model is evaluated by estimating the error of the inliers relative to the model.

This procedure is repeated a fixed number of times, each time producing either a model which is rejected because too few points are classified as inliers or a refined model together with a corresponding error measure. In the latter case, we keep the refined model if its error is lower than the last saved model.
[edit] The algorithm

The generic RANSAC algorithm, in pseudocode, works as follows:

```
input:
    data - a set of observations
    model - a model that can be fitted to data
    n - the minimum number of data required to fit the model
    k - the number of iterations performed by the algorithm
    t - a threshold value for determining when a datum fits a model
    d - the number of close data values required to assert that a model fits well to data
output:
    best_model - model parameters which best fit the data (or nil if no good model is found)
    best_consensus_set - data points from which this model has been estimated
    best_error - the error of this model relative to the data

iterations := 0
best_model := nil
best_consensus_set := nil
best_error := infinity
while iterations < k
    maybe_inliers := n randomly selected values from data
    maybe_model := model parameters fitted to maybe_inliers
    consensus_set := maybe_inliers

    for every point in data not in maybe_inliers
        if point fits maybe_model with an error smaller than t
            add point to consensus_set

    if the number of elements in consensus_set is > d
        (this implies that we may have found a good model,
        now test how good it is)
        this_model := model parameters fitted to all points in consensus_set
        this_error := a measure of how well this_model fits these points
        if this_error < best_error
            (we have found a model which is better than any of the previous ones,
            keep it until a better one is found)
            best_model := this_model
            best_consensus_set := consensus_set
```

best_error := this_error

    increment iterations

return best_model, best_consensus_set, best_error

Possible variants of the RANSAC algorithm includes

    Break the main loop if a sufficiently good model has been found, that is, one with sufficiently small error. May save some computation time at the expense of an additional parameter.
    Compute this_error directly from maybe_model without re-estimating a model from the consensus set. May save some time at the expense of comparing errors related to models which are estimated from a small number of points and therefore more sensitive to noise.

[edit] The parameters

The values of parameters t and d have to be determined from specific requirements related to the application and the data set, possibly based on experimental evaluation. The parameter k (the number of iterations), however, can be determined from a theoretical result. Let p be the probability that the RANSAC algorithm in some iteration selects only inliers from the input data set when it chooses the n points from which the model parameters are estimated. When this happens, the resulting model is likely to be useful so p gives the probability that the algorithm produces a useful result. Let w be the probability of choosing an inlier each time a single point is selected, that is,

w = number of inliers in data / number of points in data

A common case is that w is not well known beforehand, but some rough value can be given. Assuming that the n points needed for estimating a model are selected independently, wn is the probability that all n points are inliers and $1 - wn$ is the probability that at least one of the n points is an outlier, a case which implies that a bad model will be estimated from this point set. That probability to the power of k is the probability that the algorithm never selects a set of n points which all are inliers and this must be the same as $1 - p$. Consequently,

    $1 - p = (1 - wn)k$

which, after taking the logarithm of both sides, leads to

    k = \frac{\log(1 - p)}{\log(1 - w^n)}

This result assumes that the n data points are selected independently, that is, a point which has been selected once is replaced and can be selected again in the same iteration. This is often not a reasonable approach and the derived value for k should be taken as an upper limit in the case that the points are selected without replacement. For example, in the case of finding a line

which fits the data set illustrated in the above figure, the RANSAC algorithm typically chooses 2 points in each iteration and computes maybe_model as the line between the points and it is then critical that the two points are distinct.

To gain additional confidence, the standard deviation or multiples thereof can be added to k. The standard deviation of k is defined as

$$SD(k) = \frac{\sqrt{1 - w^n}}{w^n}$$

[edit] Advantages and disadvantages

An advantage of RANSAC is its ability to do robust estimation of the model parameters, i.e., it can estimate the parameters with a high degree of accuracy even when a significant number of outliers are present in the data set. A disadvantage of RANSAC is that there is no upper bound on the time it takes to compute these parameters. When the number of iterations computed is limited the solution obtained may not be optimal, and it may not even be one that fits the data in a good way. In this way RANSAC offers a trade-off; by computing a greater number of iterations the probability of a reasonable model being produced is increased. Another disadvantage of RANSAC is that it requires the setting of problem-specific thresholds.

RANSAC can only estimate one model for a particular data set. As for any one-model approach when two (or more) model instances exist, RANSAC may fail to find either one. The Hough transform is an alternative robust estimation technique that may be useful when more than one model instance is present.

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1 - Mathematical Model

1.4.1 Lucas Kanade Optical Flow

In computer vision, the Lucas–Kanade method is a widely used differential method for optical

flow estimation developed by Bruce D. Lucas and Takeo Kanade. It assumes that the flow is essentially constant in a local neighbourhood of the pixel under consideration, and solves the basic optical flow equations for all the pixels in that neighbourhood, by the least squares criterion.[1][2]

By combining information from several nearby pixels, the Lucas-Kanade method can often resolve the inherent ambiguity of the optical flow equation. It is also less sensitive to image noise than point-wise methods. On the other hand, since it is a purely local method, it cannot provide flow information in the interior of uniform regions of the image.

The Lucas-Kanade method assumes that the displacement of the image contents between two nearby instants (frames) is small and approximately constant within a neighborhood of the point p under consideration. Thus the optical flow equation can be assumed to hold for all pixels within a window centered at p. Namely, the local image flow (velocity) vector (Vx,Vy) must satisfy

$$Ix(q1)Vx + Iy(q1)Vy = - It(q1)$$

$$Ix(q2)Vx + Iy(q2)Vy = - It(q2)$$

$$\vdots$$

$$Ix(qn)Vx + Iy(qn)Vy = - It(qn)$$

where q_1,q_2,\dots,q_n are the pixels inside the window, and Ix(qi),Iy(qi),It(qi) are the partial derivatives of the image I with respect to position x, y and time t, evaluated at the point qi and at the current time.

These equations can be written in matrix form Av = b, where

$$A = \begin{bmatrix} I_x(q_1) & I_y(q_1) \\[10pt] I_x(q_2) & I_y(q_2) \\[10pt] \vdots & \vdots \\[10pt] I_x(q_n) & I_y(q_n) \end{bmatrix}, \quad\quad v = \begin{bmatrix} V_x\\[10pt] V_y \end{bmatrix}, \quad \mbox{and}\quad b = \begin{bmatrix} -I_t(q_1)\\[10pt] -I_t(q_2)\\[10pt] \vdots \\[10pt] -I_t(q_n) \end{bmatrix}$$

This system has more equations than unknowns and thus it is usually over-determined. The Lucas-Kanade method obtains a compromise solution by the least squares principle. Namely, it solves the 2×2 system

$$ATAv = ATb \text{ or}$$
$$v = (ATA) - 1ATb$$

where AT is the transpose of matrix A. That is, it computes

$$\begin{bmatrix} V_x\\[10pt] V_y \end{bmatrix} = \begin{bmatrix} \sum_i I_x(q_i)^2 & \sum_i I_x(q_i)I_y(q_i) \\[10pt] \sum_i I_x(q_i)I_y(q_i) & \sum_i I_y(q_i)^2 \end{bmatrix}^{-1} \begin{bmatrix} -\sum_i I_x(q_i)I_t(q_i) \\[10pt] -\sum_i I_y(q_i)I_t(q_i) \end{bmatrix}$$

with the sums running from i=1 to n.

The matrix ATA is often called the structure tensor of the image at the point p.
[edit] Weighted window

The plain least squares solution above gives the same importance to all n pixels qi in the window. In practice it is usually better to give more weight to the pixels that are closer to the central pixel p. For that, one uses the weighted version of the least squares equation,

ATWAv = ATWb

or

v = (ATWA) − 1ATWb

where W is an n×n diagonal matrix containing the weights Wii = wi to be assigned to the equation of pixel qi. That is, it computes

$$\begin{bmatrix} V_x\\[10pt] V_y \end{bmatrix} = \begin{bmatrix} \sum_i w_i I_x(q_i)^2 & \sum_i w_i I_x(q_i)I_y(q_i) \\[10pt] \sum_i w_i I_x(q_i)I_y(q_i) & \sum_i w_i I_y(q_i)^2 \end{bmatrix}^{-1} \begin{bmatrix} -\sum_i w_i I_x(q_i)I_t(q_i) \\[10pt] -\sum_i w_i I_y(q_i)I_t(q_i) \end{bmatrix}$$

The weight wi is usually set to a Gaussian function of the distance between qi and p.
[edit] Improvements and extensions

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1 - Mathematical Model

1.1.0 Homography

Homography is a concept in the mathematical science of geometry. A homography is an

invertible transformation from a projective space (for example, the real projective plane) to itself that maps straight lines to straight lines. Synonyms are collineation, projective transformation, and projectivity,[1] though "collineation" is also used more generally.

Formally, a projective transformation in a plane is a transformation used in projective geometry: it is the composition of a pair of perspective projections. It describes what happens to the perceived positions of observed objects when the point of view of the observer changes. Projective transformations do not preserve sizes or angles but do preserve incidence and cross-ratio: two properties which are important in projective geometry. Projectivities form a group.[1]

For more general projective spaces – of different dimensions or over different fields – "homography" means a projective linear transformation (an invertible transformation induced by a linear transformation of the associated vector space), while "collineation" (meaning "maps lines to lines") is more general, and includes both homographies and automorphic collineations (collineations induced by a field automorphism), as well as combinations of these.

Computer vision applications

In the field of computer vision, any two images of the same planar surface in space are related by a homography (assuming a pinhole camera model). This has many practical applications, such as image rectification, image registration, or computation of camera motion—rotation and translation—between two images. Once camera rotation and translation have been extracted from an estimated homography matrix, this information may be used for navigation, or to insert models of 3D objects into an image or video, so that they are rendered with the correct perspective and appear to have been part of the original scene (see Augmented Reality).
[edit] 3D plane to plane equation

We have two cameras a and b, looking at points Pi in a plane.

Passing the projections of Pi from bpi in b to a point api in a:

$${}^ap_i = K_a \cdot H_{ba} \cdot K_b^{-1} \cdot {}^bp_i$$

where Hba is

$$H_{ba} = R - \frac{t\, n^T}{d}$$

R is the rotation matrix by which b is rotated in relation to a; t is the translation vector from a to b; n and d are the normal vector of the plane and the distance to the plane respectively.

Ka and Kb are the cameras' intrinsic parameter matrices.

Homography-transl-bold.svg

The figure shows camera b looking at the plane at distance d.

Note: From above figure, nTPi is the projection of vector Pi into nT, and equal to d. So \frac{t n^T}{d} P_i = t. And we have HbaPi = RPi − t.
[edit] Mathematical definition

In the complex plane, a Mobius transformation is frequently called a homography. These linear-fractional transformations are expressions of projective transformations on the complex projective line, an extension of the complex plane.

In higher dimensions Homogeneous coordinates are used to represent projective transformations by means of matrix multiplications. With Cartesian coordinates matrix multiplication cannot perform the division required for perspective projection. In other words, with Cartesian coordinates a perspective projection is a non-linear transformation.
n{bmatrix} x_a\\y_a\\1\end{bmatrix}, p^\prime_b = \begin{bmatrix} w^{\prime}x_b\\w^{\prime}y_{b}\\w^{\prime}\end{bmatrix}, \mathbf{H}_{ab} = \begin{bmatrix}
h_{11}&h_{12}&h_{13}\\h_{21}&h_{22}&h_{23}\\h_{31}&h_{32}&h_{33}
\end{bmatrix}

Then:
Also:

   p_b = p^\prime_b/w^\prime = \begin{bmatrix} x_b\\y_b\\ 1\end{bmatrix}

[edit] Affine homography

When the image region in which the homography is computed is small or the image has been acquired with a large focal length, an affine homography is a more appropriate model of image displacements. An affine homography is a special type of a general homography whose last row is fixed to

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1 - Mathematical Model

1.1.0 Simultaneous localization and mapping

Simultaneous localization and mapping (SLAM) is a technique used by robots and

autonomous vehicles to build up a map within an unknown environment (without *a priori* knowledge), or to update a map within a known environment (with *a priori* knowledge from a given map), while at the same time keeping track of their current location.

Maps are used to determine a location within an environment and to depict an environment for planning and navigation; they support the assessment of actual location by recording information obtained from a form of perception and comparing it to a current set of perceptions. The benefit of a map in aiding the assessment of a location increases as the precision and quality of the current perceptions decrease. Maps generally represent the state at the time that the map is drawn; this is not necessarily consistent with the state of the environment at the time the map is used.

The complexity of the technical processes of locating and mapping under conditions of errors and noise do not allow for a coherent solution of both tasks. Simultaneous localization and mapping (SLAM) is a concept that binds these processes in a loop and therefore supports the continuity of both aspects in separated processes; iterative feedback from one process to the other enhances the results of both consecutive steps.

Mapping is the problem of integrating the information gathered by a set of sensors into a consistent model and depicting that information as a given representation. It can be described by the first characteristic question, What does the world look like? Central aspects in mapping are the representation of the environment and the interpretation of sensor data.

In contrast to this, localization is the problem of estimating the place (and pose) of the robot relative to a map; in other words, the robot has to answer the second characteristic question, Where am I? Typically, solutions comprise tracking, where the initial place of the robot is known, and global localization, in which no or just some a priori knowledge of the environmental characteristics of the starting position is given.

SLAM is therefore defined as the problem of building a model leading to a new map, or repetitively improving an existing map, while at the same time localizing the robot within that map. In practice, the answers to the two characteristic questions cannot be delivered independently of each other.

Before a robot can contribute to answering the question of what the environment looks like, given a set of observations, it needs to know e.g.:

   the robot's own kinematics,
   which qualities the autonomous acquisition of information has, and,
   from which sources additional supporting observations have been made.

It is a complex task to estimate the robot's current location without a map or without a directional reference.[1] Here, the location is just the position of the robot or might include, as well, its orientation.
[edit] Technical problems

SLAM can be thought of as a chicken or egg problem: An unbiased map is needed for localization while an accurate pose estimate is needed to build that map. This is the starting condition for iterative mathematical solution strategies. In comparison, the atomic orbital model may be seen as a classic approach of how to communicate sufficient results under conditions of imprecise observation.

Beyond, the answering of the two characteristic questions is not as straightforward as it might sound due to inherent uncertainties in discerning the robot's relative movement from its various sensors. Generally, due to the budget of noise in a technical environment, SLAM is not served with just compact solutions, but with a bunch of physical concepts contributing to results.

If at the next iteration of map building the measured distance and direction traveled has a budget of inaccuracies, driven by limited inherent precision of sensors and additional ambient noise, then any features being added to the map will contain corresponding errors. Over time and motion, locating and mapping errors build cumulatively, grossly distorting the map and therefore the robot's ability to determine (know) its actual location and heading with sufficient accuracy.

There are various techniques to compensate for errors, such as recognizing features that it has come across previously, and re-skewing recent parts of the map to make sure the two instances of that feature become one. Some of the statistical techniques used in SLAM include Kalman filters, particle filters (aka. Monte Carlo methods) and scan matching of range data.
[edit] Mapping

SLAM in the mobile robotics community generally refers to the process of creating geometrically consistent maps of the environment. Topological maps are a method of environment representation which capture the connectivity (i.e., topology) of the environment rather than creating a geometrically accurate map. As a result, algorithms that create topological maps are not referred to as SLAM.

SLAM is tailored to the available resources, hence not aimed at perfection, but at operational compliance. The published approaches are employed in unmanned aerial vehicles, autonomous underwater vehicles, planetary rovers, newly emerging domestic robots and even inside the human body.[2]

It is generally considered that "solving" the SLAM problem has been one of the notable achievements of the robotics research in the past decades.[3] The related problems of data association and computational complexity are amongst the problems yet to be fully resolved.

A significant recent advance in the feature based SLAM literature involved the re-examination the probabilistic foundation for Simultaneous Localisation and Mapping (SLAM) where it was posed in terms of multi-object Bayesian filtering with random finite sets that provide superior performance to leading feature-based SLAM algorithms in challenging measurement scenarios with high false alarm rates and high missed detection rates without the need for data

association[4]. Algorithms were developed based on Probability Hypothesis Density (PHD) filtering techniques[5].

SLAM will always use several different types of sensors to acquire data with statistically independent errors. Statistical independence is the mandatory requirement to cope with metric bias and with noise in measures.

Such optical sensors may be one dimensional (single beam) or 2D- (sweeping) laser rangefinders, 3D Flash LIDAR, 2D or 3D sonar sensors and one or more 2D cameras.

Recent approaches apply quasi-optical wireless ranging for multi-lateration (RTLS) or multi-angulation in conjunction with SLAM as a tribute to erratic wireless measures.

A special kind of SLAM for human pedestrians uses a shoe mounted inertial measurement unit as the main sensor and relies on the fact that pedestrians are able to avoid walls. This approach called FootSLAM can be used to automatically build floor plans of buildings that can then be used by an indoor positioning system.[6]

The results from sensing will feed the algorithms for locating. According to propositions of geometry, any sensing must include at least one lateration and (n+1) determining equations for an n-dimensional problem. In addition, there must be some additional a priori knowledge about orienting the results versus absolute or relative systems of coordinates with rotation and mirroring.

Contribution to mapping may work in 2D modeling and respective representation or in 3D modeling and 2D projective representation as well. As a part of the model, the kinematics of the robot is included, to improve estimates of sensing under conditions of inherent and ambient noise. The dynamic model balances the contributions from various sensors, various partial error models and finally comprises in a sharp virtual depiction as a map with the location and heading of the robot as some cloud of probability. Mapping is the final depicting of such model, the map is either such depiction or the abstract term for the model.

[edit] Literature

A seminal work in SLAM is the research of R.C. Smith and P. Cheeseman on the representation and estimation of spatial uncertainty in 1986.[7][8] Other pioneering work in this field was conducted by the research group of Hugh F. Durrant-Whyte in the early 1990s.[9]

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1 - Mathematical Model

1.1.0 A* Path Finding

Assuming a two dimensional map acquired by the operations above , and a stable track of the

position of the robot , there is a need for an algorithm to perform path finding , in order for the robot to be able to reach a target position and dynamically change its course when new obstacles are detected. The algorithm used by this project for this kind of functionality is A* , an extension of Dijkstra's graph search algorithm. Successful path finding is very critical because it means less battery drain due to unnecessary movements and better performance as a guard.

A* uses a heuristic that has to never over-estimate the route cost , and such a heuristic is the Manhattan distance that is commonly used by many implementations.
The complexity of the algorithm is $| h(x) - h * (x) | = O(\log h * (x))$ where h is the heuristic used.
The cost of the algorithm for each new node is calculated using $f(n) = g(n) + h(n)$ where g is the cost of the transition to the new node and h the heuristic for the transition to the goal node. A* is thus admissible since adding g which is an exact estimation of the distance from the source node to the optimistic heuristic since will always make the algorithm seek the solution with the lowest possible cost.
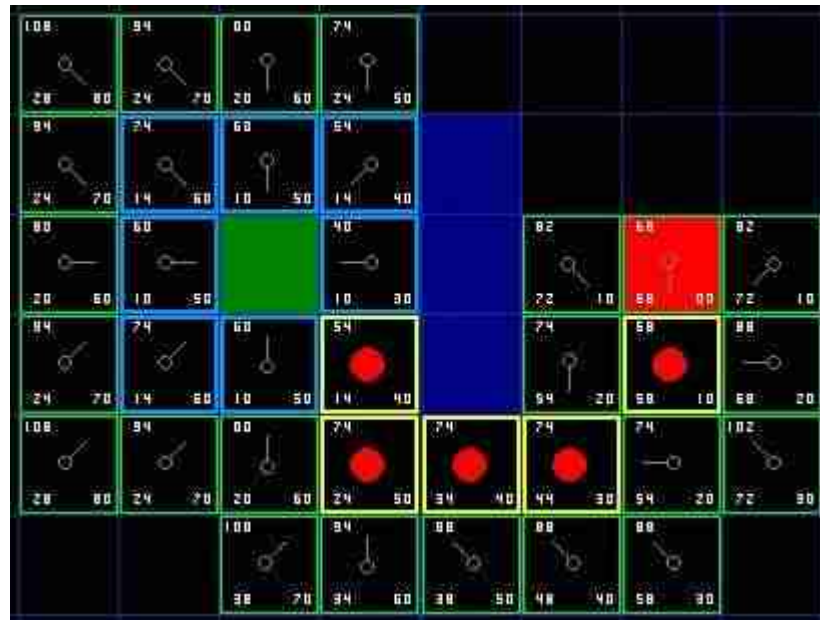
A* Algorithm
OPEN SET = START NODE
CLOSED SET = EMPTY
while the node with the lowest cost in OPEN SET is not the GOAL NODE:
  current = **remove** lowest rank item **from** OPEN SET
  add current **to** CLOSED SET
  for neighbors **of** current:
    cost = g(current) + movementcost(current, neighbor)
    if neighbor **in** OPEN **and** cost **less than** g(neighbor):
      remove neighbor **from** OPEN, /*new path is better*/
    if neighbor **in** CLOSED SET **and** cost **less than** g(neighbor):
      remove neighbor **from** CLOSED SET

```
    if neighbor not in OPEN SET and neighbor not in CLOSED SET:
        set g(neighbor) to cost
        add neighbor to OPEN SET
        set priority queue rank to g(neighbor) + h(neighbor)
        set neighbor's parent to current

Reconstruct path following parent pointers from goal to start
```

One of the shortcomings of a raw implementation of an uncustomized A* algorithm is that in the real world diagonal movement is a little further away than than horizontal (pythagorean theorem) . The result is that returned paths can be "non optimal" for a real world moving robot. Added to this problem comes the fact that in physical movement one tends to hold a course turning as little as it is possible. A* can provide an optimal solution that has many turns , but this will take more time for the robot to be traversed. The solution to this problem is keeping the heading of the robot as an information vector on every opened node and adding an extra weight when turns are made , while also adding an extra weight when performing diagonal movement to balance them.

The final element needed is a way to represent uncertainty about the mapped obstacles since there may be errors in the input , not only caused by "mis-detection of obstacles" but also by the the lack of detail of the map since an area of 200 m^2 quantized at a scale of 10 cm^2 per block results in an array sized 2000x1000 that cannot reflect the full complexity of the scene.

Using these modifications , the output becomes better but there is a further improvement that can be achieved by using the largest possible straight paths to connect sub regions of the A* paths. Doing that the turning maneuvers of the robot are reduced to the fewest possible. To achieve that , after a path has been extracted ,instead of reconstructing the path following the parnet pointers we use a second pass algorithm runs which casts a line (using Bresenham's line algorithm) from the last step of the path to all the previous ones until an obstacle is detected. The previous point before the obstacle is then marked as connected to the first one and the algorithm continues until the source node is connected. This improves the operation of the robot . This could also be improved in the future to use odometer based curves instead of point to point turning , something that would also make the movement of GuarddoG seem more life like.
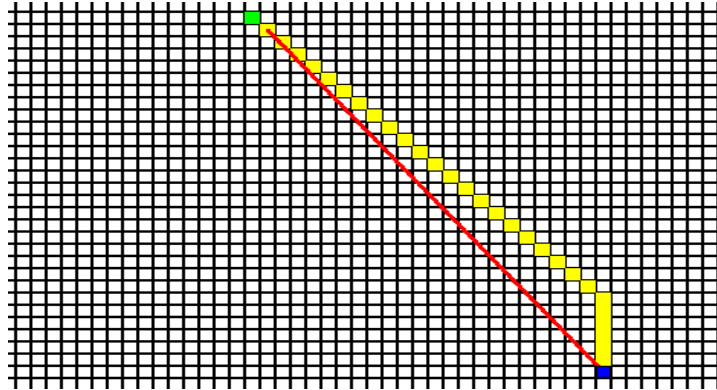
Illustration 14: The problems that may occur using an uncustomized A Algorithm , and how they are corrected*
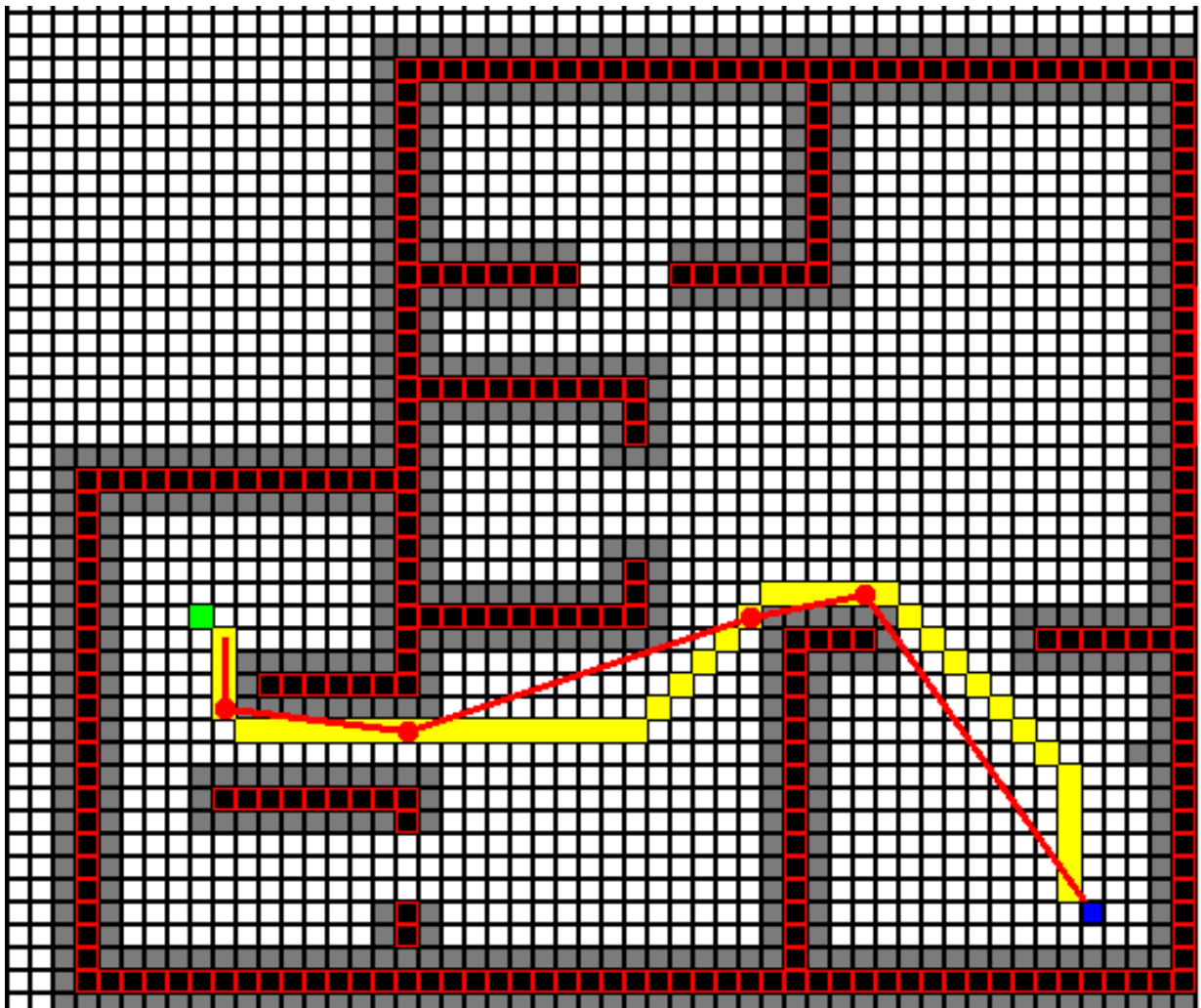
Illustration 15: The green block is the source , the blue the target , red/black blocks are obstacles and gray areas , areas of uncertainty. The yellow path is the one that A returns and the red line the compressed path for as little turning as possible.*

*

1 - Mathematical Model

1.1.0 First-order logic and a Wumpus like world

Or a Shakey one also taken from Russel & Norvig

First-order logic is a formal logical system used in mathematics, philosophy, linguistics, and computer science. It goes by many names, including: first-order predicate calculus, the lower predicate calculus, quantification theory, and predicate logic (a less precise term). First-order logic is distinguished from propositional logic by its use of quantifiers; each interpretation of first-order logic includes a domain of discourse over which the quantifiers range. The adjective "first-order" is used to distinguish first-order theories from higher-order theories in which there are predicates having other predicates or functions as arguments or in which predicate quantifiers or function quantifiers are permitted or both.[1] In interpretations of first-order theories, predicates are associated with sets. In interpretations of higher order theories, they may be also associated with sets of sets.

There are many deductive systems for first-order logic that are sound (only deriving correct results) and complete (able to derive any logically valid implication). Although the logical consequence relation is only semidecidable, much progress has been made in automated theorem proving in first-order logic. First-order logic also satisfies several metalogical theorems that make it amenable to analysis in proof theory, such as the Löwenheim–Skolem theorem and the compactness theorem.

First-order logic is of great importance to the foundations of mathematics, where it has become the standard formal logic for axiomatic systems. It has sufficient expressive power to formalize two important mathematical theories: Zermelo–Fraenkel set theory (ZF) and first-order Peano arithmetic. However, no axiom system in first order logic is strong enough to fully (categorically) describe infinite structures such as the natural numbers or the real line. Categorical axiom systems for these structures can be obtained in stronger logics such as second-order logic.

While propositional logic deals with simple declarative propositions, first-order logic additionally covers predicates and quantification.

A predicate resembles a function that returns either True or False. Consider the following sentences: "Socrates is a philosopher", "Plato is a philosopher". In propositional logic these are

treated as two unrelated propositions, denoted for example by p and q. In first-order logic, however, the sentences can be expressed in a more parallel manner using the predicate Phil(a), which asserts that the object represented by a is a philosopher. Thus if a represents Socrates then Phil(a) asserts the first proposition, p; if a instead represents Plato then Phil(a) asserts the second proposition, q. A key aspect of first-order logic is visible here: the string "Phil" is a syntactic entity which is given semantic meaning by declaring that Phil(a) holds exactly when a is a philosopher. An assignment of semantic meaning is called an interpretation.

First-order logic allows reasoning about properties that are shared by many objects, through the use of variables. For example, let Phil(a) assert that a is a philosopher and let Schol(a) assert that a is a scholar. Then the formula

   \text{Phil}(a)\to \text{Schol}(a) \,,

asserts that if a is a philosopher then a is a scholar. The symbol \to is used to denote a conditional (if/then) statement. The hypothesis lies to the left of the arrow and the conclusion to the right. The truth of this formula depends on which object is denoted by a, and on the interpretations of "Phil" and "Schol".

Assertions of the form "for every a, if a is a philosopher then a is a scholar" require both the use of variables and the use of a quantifier. Again, let Phil(a) assert a is a philosopher and let Schol(a) assert that a is a scholar. Then the first-order sentence

   \forall a (\text{Phil}(a) \to \text{Schol}(a))

asserts that no matter what a represents, if a is a philosopher then a is scholar. Here \forall, the universal quantifier, expresses the idea that the claim in parentheses holds for all choices of a.

To show that the claim "If a is a philosopher then a is a scholar" is false, one would show there is some philosopher who is not a scholar. This counterclaim can be expressed with the existential quantifier \exists:

   \exists a (\text{Phil}(a) \land \lnot \text{Schol}(a)).

Here:

   \lnot is the negation operator: \lnot \text{Schol}(a) is true if and only if \text{Schol}(a) \, is false, in other words if and only if a is not a scholar.
   \land is the conjunction operator: \text{Phil}(a) \land \lnot \text{Schol}(a) asserts that a is a philosopher and also not a scholar.

The predicates Phil(a) and Schol(a) take only one parameter each. First-order logic can also express predicates with more than one parameter. For example, "there is someone who can be fooled every time" can be expressed as:

$\exists x (\mbox{Person}(x) \and \forall y (\mbox{Time}(y) \rightarrow \mbox{Canfool}(x,y)))$.

Here Person(x) is interpreted to mean x is a person, Time(y) to mean that y is a moment of time, and Canfool(x,y) to mean that (person) x can be fooled at (time) y. For clarity, this statement asserts that there is at least one person who can be fooled at all times, which is stronger than asserting that at all times at least one person exists who can be fooled. Asserting the latter (that there is always at least one foolable person) does not signify whether this foolable person is always the same for all moments of time.

The range of the quantifiers is the set of objects that can be used to satisfy them. (In the informal examples in this section, the range of the quantifiers was left unspecified.) In addition to specifying the meaning of predicate symbols such as Person and Time, an interpretation must specify a nonempty set, known as the domain of discourse or universe, as a range for the quantifiers. Thus a statement of the form $\exists a \text{Phil}(a)$ is said to be true, under a particular interpretation, if there is some object in the domain of discourse of that interpretation that satisfies the predicate that the interpretation uses to assign meaning to the symbol Phil.

[edit] Syntax

There are two key parts of first order logic. The syntax determines which collections of symbols are legal expressions in first-order logic, while the semantics determine the meanings behind these expressions.

[edit] Alphabet

Unlike natural languages, such as English, the language of first-order logic is completely formal, so that it can be mechanically determined whether a given expression is legal. There are two key types of legal expressions: terms, which intuitively represent objects, and formulas, which intuitively express predicates that can be true or false. The terms and formulas of first-order logic are strings of symbols which together form the alphabet of the language. As with all formal languages, the nature of the symbols themselves is outside the scope of formal logic; they are often regarded simply as letters and punctuation symbols.

It is common to divide the symbols of the alphabet into logical symbols, which always have the same meaning, and non-logical symbols, whose meaning varies by interpretation. For example, the logical symbol $\land$ always represents "and"; it is never interpreted as "or". On the other hand, a non-logical predicate symbol such as Phil(x) could be interpreted to mean "x is a philosopher", "x is a man named Philip", or any other unary predicate, depending on the interpretation at hand.

[edit] Logical symbols

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2 - Hardware

2.1.0 Camera Sensors

An active-pixel sensor (APS) is an image sensor consisting of an integrated circuit containing an array of pixel sensors, each pixel containing a photodetector and an active amplifier. There are many types of active pixel sensors including the CMOS APS used most commonly in cell phone cameras, web cameras and in some DSLRs. Such an image sensor is produced by a CMOS process (and is hence also known as a CMOS sensor), and has emerged as an alternative to charge-coupled device (CCD) imager sensors.

 The term active pixel sensor was coined by Tsutomu Nakamura who worked on the Charge Modulation Device active pixel sensor at Olympus,[4] and more broadly defined by Eric Fossum in a 1993 paper.[5]

 Image sensor elements with in-pixel amplifiers were described by Noble in 1968,[6] by Chamberlain in 1969,[7] and by Weimer et al. in 1969,[8] at a time when passive-pixel sensors – that is, pixel sensors without their own amplifiers – were being investigated as a solid-state alternative to vacuum-tube imaging devices. The MOS passive-pixel sensor used just a simple switch in the pixel to read out the photodiode integrated charge.[9] Pixels were arrayed in a two-dimensional structure, with access enable wire shared by pixels in the same row, and output wire shared by column. At the end of each column was an amplifier. Passive-pixel sensors suffered from many limitations, such as high noise, slow readout, and lack of scalability. The addition of an amplifier to each pixel addressed these problems, and resulted in the creation of the active-pixel sensor. Noble in 1968 and Chamberlain in 1969 created sensor arrays with active MOS readout amplifiers per pixel, in essentially the modern three-transistor configuration. The CCD was invented in 1970 at Bell Labs. Because the MOS process was so variable and MOS transistors had characteristics that changed over time (Vt instability), the CCD's charge-domain operation was more manufacturable and quickly eclipsed MOS passive and active pixel sensors. A low-resolution "mostly digital" N-channel MOSFET imager with intra-pixel amplification, for an optical mouse application, was demonstrated in 1981.[10]

Another type of active pixel sensor is the hybrid infrared focal plane array (IRFPA) designed to operate at cryogenic temperatures in the infrared spectrum. The devices are two chips that are put together like a sandwich: one chip contains detector elements made in InGaAs or HgCdTe, and the other chip is typically made of silicon and is used to readout the photodetectors. The exact date of origin of these devices is classified, but by the mid-1980s they were in widespread use. By the late 1980s and early 1990s, the CMOS process was well established as a well controlled stable process and was the baseline process for almost all logic and microprocessors. There was a resurgence in the use of passive-pixel sensors for low-end imaging applications,

[11] and active-pixel sensors for low-resolution high-function applications such as retina simulation[12] and high energy particle detector.[13] However, CCDs continued to have much lower temporal noise and fixed-pattern noise and were the dominant technology for consumer applications such as camcorders as well as for broadcast cameras, where they were displacing video camera tubes.

In 1995, personnel from JPL founded Photobit Corp., who continued to develop and commercialize APS technology for a number of applications, such as web cams, high speed and motion capture cameras, digital radiography, endoscopy (pill) cameras, DSLRs and of course, camera-phones. Many other small image sensor companies also sprang to life shortly thereafter due to the accessibility of the CMOS process and all quickly adopted the active pixel sensor approach.

The cameras used by GuarddoG are based on the OV7720/OV7221 CMOS VGA (640x480) CAMERACHIP Sensor , and are cheap and easy to find as they are the camera system used by the Playstation 3 Gaming Console

Camera Sensor Key Specifications

Array Size	640 x 480
Power Supply Digital Core Voltage	1.8VDC + 10%
Power Supply Analog Voltage	3.0V to 3.3V
Power Supply I/O Voltage	1.7V to 3.3V
Power Requirements - Active	120 mW typical (60 fps VGA, YUV)
Power Requirements - Standby	< 20 µA
Temperature Range	-20°C to +70°C
Output Format (8-bit)	• YUV/YCbCr 4:2:2 • RGB565/555/444 • GRB 4:2:2 • Raw RGB Data
Lens Size	1/4"
Max Image Transfer Rate	60 fps for VGA
Scan Mode	Progressive
Electronic Exposure	Up to 510:1 (for selected fps)
Pixel Size	6.0 µm x 6.0 µm
Fixed Pattern Noise	< 0.03% of VPEAK-TO-PEAK
Image Area	3984 µm x 2952 µm
Package Dimensions	5345 µm x 5265 µm

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2 - Hardware

2.1.0 Camera Synchronization

Stereo vision on a mobile robot is a non-trivial problem that traditionally requires expensive hardware-synchronized cameras. Because standard stereo reconstruction assumes that the images from the left and right cameras are captured from a common scene , any motion that occurs between the left and right cameras capturing frames is equivalent to a change in the stereo camera`s baseline. This change in baseline invalidates the system`s extrinsic calibration , causing the quality of the rectification to decrease and the distances to be distorted by the robot`s velocity.

Hardware synchronization , the process of forcing two or more cameras to share a common hardware clock , has been traditionally limited to the professional stereo vision systems such as Point Grey`s Bumblebee product line . Thankfully , the inexpensive Playstation Eye camera is built on the same high-end OmniVision OV7720 chipset that is comparable to those found in many machine vision cameras. These cameras can be hardware-synchronized using the exposed frame clock input (FSIN) and output (VSYNC) pins . By shorting one camera`s VSYNC pin to the others cameras FSIN pins the cameras are forced to share a common clock . To reduce the risk of a difference in ground potentials damaging the OV7720 delicate circuitry , each camera was also modified to share a common ground .

This hardware synchronization guarantees that all three cameras capture images simultaneously , but does not guarantee that the frames will travel retaining their synchronization on the USB .

Each camera has its own hardware clock and that means that in addition to the small distortion in space (due to optics) we have a small distortion in the fourth dimension , the axis of time. To tackle this problem guarddog uses cameras that have a very fast refresh rate of 120fps @ 320x240 pixels with a rewired shutter (FSIN , VSYNC pins) in order for synchronization on the hardware side of the camera snapshots. A secondary problem is that there is non uniform latency over the USB cable and the USB host controller . This is problem is combated using direct frame grabbing via V4L2 and zero-copy passing by pointer to the beginning of the image pipelining and static linkage of the libraries consisting of the project to reduce delays and overheads.

*

2 - Hardware

2.1.0 USB Host

A USB system has an asymmetric design, consisting of a host, a multitude of downstream USB ports, and multiple peripheral devices connected in a tiered-star topology. Additional USB hubs may be included in the tiers, allowing branching into a tree structure with up to five tier levels. A USB host may have multiple host controllers and each host controller may provide one or more USB ports. Up to 127 devices, including hub devices if present, may be connected to a single host controller.

USB devices are linked in series through hubs. There always exists one hub known as the root hub, which is built into the host controller.

A physical USB device may consist of several logical sub-devices that are referred to as device functions. A single device may provide several functions, for example, a webcam (video device function) with a built-in microphone (audio device function). Such a device is called a compound device in which each logical device is assigned a distinctive address by the host and all logical devices are connected to a built-in hub to which the physical USB wire is connected. A host assigns one and only one device address to a function.
Diagram: inside a device are several endpoints, each of which is connected by a logical pipes to a host controller. Data in each pipe flows in one direction, although there are a mixture going to and from the host controller.
USB endpoints actually reside on the connected device: the channels to the host are referred to as pipes

USB device communication is based on pipes (logical channels). A pipe is a connection from the host controller to a logical entity, found on a device, and named an endpoint. Because pipes correspond 1-to-1 to endpoints, the terms are sometimes used interchangeably. A USB device can have up to 32 endpoints: 16 into the host controller and 16 out of the host controller. The USB standard reserves one endpoint of each type, leaving a theoretical maximum of 30 for normal use. USB devices seldom have this many endpoints.

There are two types of pipes: stream and message pipes depending on the type of data transfer.

   isochronous transfers: at some guaranteed data rate (often, but not necessarily, as fast as possible) but with possible data loss (e.g., realtime audio or video).
   interrupt transfers: devices that need guaranteed quick responses (bounded latency) (e.g.,

pointing devices and keyboards).

    bulk transfers: large sporadic transfers using all remaining available bandwidth, but with no guarantees on bandwidth or latency (e.g., file transfers).

    control transfers: typically used for short, simple commands to the device, and a status response, used, for example, by the bus control pipe number 0.

A stream pipe is a uni-directional pipe connected to a uni-directional endpoint that transfers data using an isochronous, interrupt, or bulk transfer. A message pipe is a bi-directional pipe connected to a bi-directional endpoint that is exclusively used for control data flow. An endpoint is built into the USB device by the manufacturer and therefore exists permanently. An endpoint of a pipe is addressable with a tuple (device_address, endpoint_number) as specified in a TOKEN packet that the host sends when it wants to start a data transfer session. If the direction of the data transfer is from the host to the endpoint, an OUT packet (a specialization of a TOKEN packet) having the desired device address and endpoint number is sent by the host. If the direction of the data transfer is from the device to the host, the host sends an IN packet instead. If the destination endpoint is a uni-directional endpoint whose manufacturer's designated direction does not match the TOKEN packet (e.g., the manufacturer's designated direction is IN while the TOKEN packet is an OUT packet), the TOKEN packet will be ignored. Otherwise, it will be accepted and the data transaction can start. A bi-directional endpoint, on the other hand, accepts both IN and OUT packets.

*

2 - Hardware

2.1.0 Embedded System

V4L2 mmap()
Name
v4l2-mmap -- Map device memory into application address space
Synopsis

#include <unistd.h>
#include <sys/mman.h>

void *mmap(void *start, size_t length, int prot, int flags, int fd, off_t offset);

Arguments

start

   Map the buffer to this address in the application's address space. When the MAP_FIXED
flag is specified, start must be a multiple of the pagesize and mmap will fail when the specified
address cannot be used. Use of this option is discouraged; applications should just specify a
NULL pointer here.

uATX (6.75 inches by 6.75 inches [171.45 millimeters by 171.45
millimeters]) (ITX compatible)
Integrated Intel® Celeron® 220 processor (1.2 Ghz) with a 533
MHz system bus
One 240-pin DDR2 SDRAM Dual Inline Memory Module (DIMM)
sockets
Support for DDR2 677/533/400 MHz DIMMs
Support for up to 1 GB of system memory
SiS* SiS662 Northbridge
SiS* SiS964L Southbridge
ADI* AD1888 audio codec
Integrated SiS Mirage* 1 graphic engine
Winbond* W83627DHG-B based Legacy I/O controller for
hardware management, serial, parallel, and PS/2* ports

Booting from a USB STICK

Most current PC firmware permits [booting](#) from a USB drive, allowing the launch of an operating system from a [bootable](#) flash drive. Such a configuration is known as a [Live USB](#).

Original flash memory designs had very limited estimated lifetimes. The failure mechanism for flash memory cells is analogous to a [metal fatigue](#) mode; the device fails by refusing to write new data to specific cells that have been subject to many read-write cycles over the device's lifetime. Originally, this potential failure mode limited the use of "live USB" system to special purpose applications or temporary tasks, such as:

- Loading a minimal, hardened kernel for embedded applications (e.g. network router, firewall).
- Bootstrapping an operating system install or [disk cloning](#) operation, often across a network.
- Maintenance tasks, such as virus scanning or low-level data repair, without the primary host operating system loaded.

As of 2011, newer flash memory designs have much higher estimated lifetimes. Several manufacturers are now offering warranties of 5 years, or more. That should make the device more attractive for more applications. By reducing the probability of the device's premature failure, flash memory devices can now be considered for use where a magnetic disk would normally have been required. Flash drives have also experienced an exponential growth in their storage capacity over time (following the [Moore's Law](#) growth curve). As of 2011, single packaged devices with capacities of 64[GB](#) are readily available, and devices with 8GB capacity are very economical. Storage capacities in this range have traditionally been considered to offer adequate space, because they allow enough space for both the operating system software and some free space for the user's data.

Advantages

Data stored on flash drives is impervious to scratches and dust, and flash drives are mechanically very robust making them suitable for transporting data from place to place and keeping it readily at hand. Most personal computers support USB as of 2010.

Flash drives also store data densely compared to many removable media. In mid-2009, 256 GB drives became available, with the ability to hold many times more data than a DVD or even a Blu-ray disc.

Compared to hard drives, flash drives use little power, have no fragile moving parts, and for most capacities are small and light.

Flash drives implement the USB mass storage device class so that most modern operating systems can read and write to them without installing device drivers. The flash drives present a simple block-structured logical unit to the host operating system, hiding the individual complex implementation details of the various underlying flash memory devices. The operating system can use any file system or block addressing scheme. Some computers can boot up from flash drives.

Specially manufactured flash drives are available that have a tough rubber or metal casing designed to be waterproof and virtually "unbreakable". These flash drives retain their memory after being submerged in water, and even through a machine wash. Leaving such a flash drive out to dry completely before allowing current to run through it has been known to result in a working drive with no future problems. Channel Five's Gadget Show cooked one of these flash drives with propane, froze it with dry ice, submerged it in various acidic liquids, ran over it with a jeep and fired it against a wall with a mortar. A company specializing in recovering lost data from computer drives managed to recover all the data on the drive.[38] All data on the other removable storage devices tested, using optical or magnetic technologies, were destroyed.
[edit] Disadvantages
Main article: Flash memory#Limitations

Like all flash memory devices, flash drives can sustain only a limited number of write and erase cycles before the drive fails.[39][40] This should be a consideration when using a flash drive to run application software or an operating system. To address this, as well as space limitations, some developers have produced special versions of operating systems (such as Linux in Live USB)[41] or commonplace applications (such as Mozilla Firefox) designed to run from flash drives. These are typically optimized for size and configured to place temporary or intermediate files in the computer's main RAM rather than store them temporarily on the flash drive.

Most USB flash drives do not include a write-protect mechanism, although some have a switch on the housing of the drive itself to keep the host computer from writing or modifying data on the drive. Write-protection makes a device suitable for repairing virus-contaminated host computers without risk of infecting the USB flash drive itself.

A drawback to the small size is that they are easily misplaced, left behind, or otherwise lost. This is a particular problem if the data they contain are sensitive (see data security). As a consequence, some manufacturers have added encryption hardware to their drives—although software encryption systems which can be used in conjunction with any mass storage medium achieve the same thing.[citation needed] Most drives can be attached to keychains, necklaces and lanyards. The USB plug is usually fitted with a removable and easily lost protective cap, or is retractable.

USB flash drives are more expensive per unit of storage than large hard drives, but are less expensive in capacities of a few tens of gigabytes as of 2011.[42][43] Maximum available capacity is increasing with time, but is less than larger hard drives. This balance is changing, but the rate of change is slowing.

Hardware

The Energy – Weight – Heat – Cost Problem

Hardware

GuarddoG Part List / Specifications

Embedded Electronics
1x Arduino = 25 euro (Uno)
3x Infrared Led = 3 euro
1x RD-01 (or RD-02 Devantech motors) = 130 euro
2x Buttons (power -on) = 2 euro
2x Switches (power supply) = 2 euro
2x LED HeadLights = 10 euro
2x Ultrasonic Devantech SRF-05 with mounting = 40 euro
1x Dual Axis Accelerometer (memsic 2125) = 30 euro
Total : 252 euro

Computer Hardware

1x Fan = 5 euro
1x Mini-Itx Motherboard = 65-75 euro (Currently on guarddog Intel D201GLY2)
1x PicoPSU 90W = 45 euro
1x AC-DC 12 V Converter = 30 euro
2x Webcams (On guarddog MS VX-6000) = 92 euro , LOGITECH C510 HD , PS3 Eyes
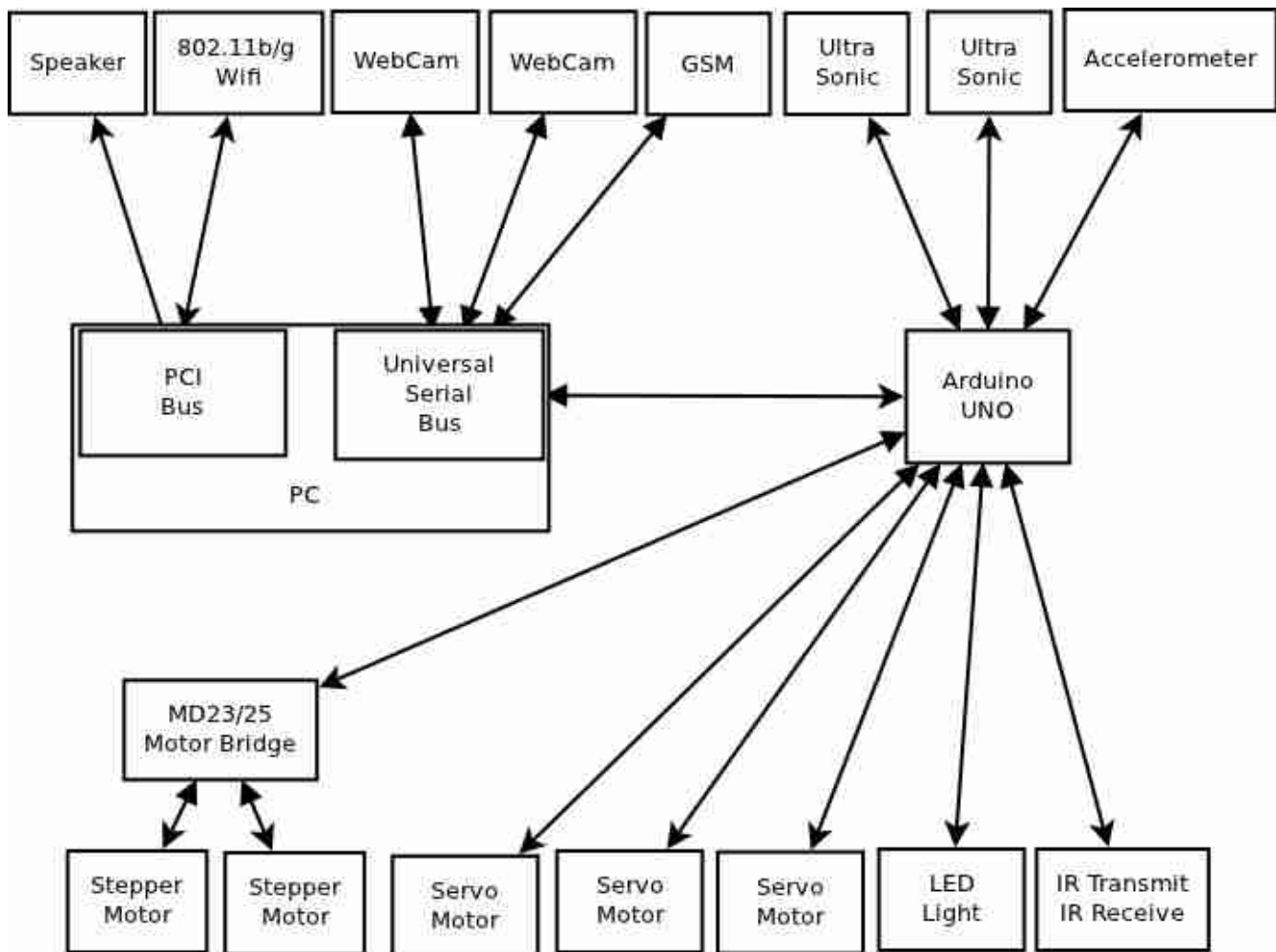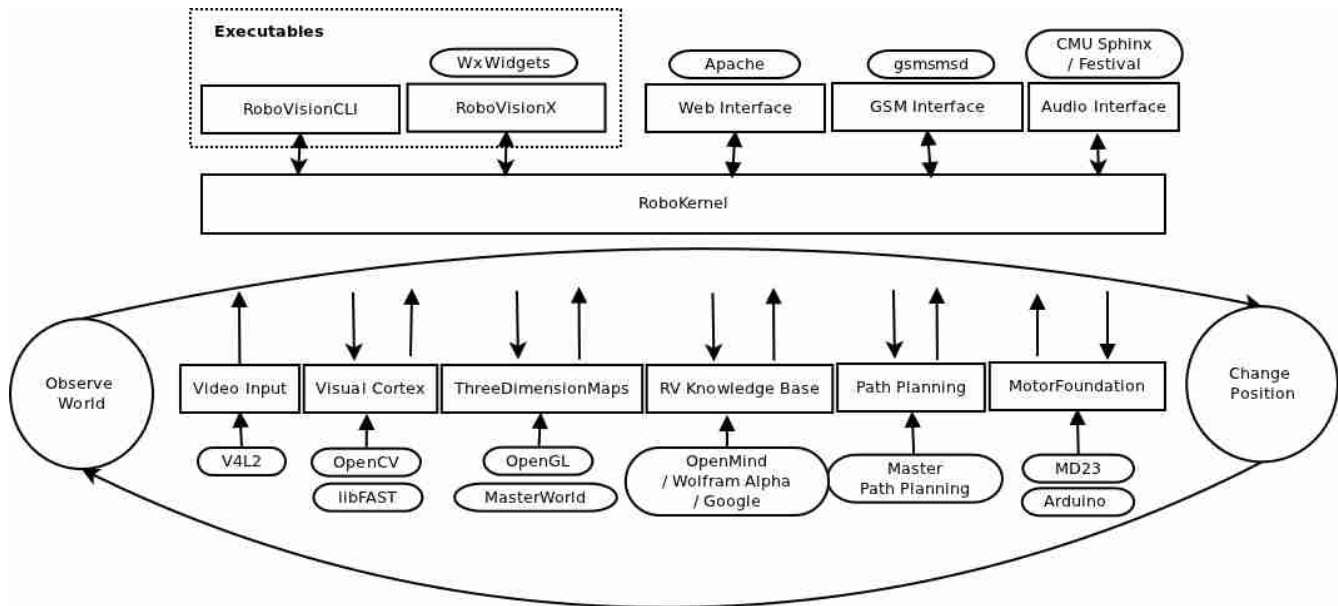1x WIFI PCI card (WG311T) = 30 euro
1x USB Flash Drive 8GB + = 20 euro
1x 512-2048MB RAM DIMM (on guarddog 512MB DDR2) = 30 euro
Total : 327 euro

Software Stack

Pipeline Outline

Executables

WxWidgets

RoboVisionCLI RoboVisionX

Apache gsmsmsd CMU Sphinx / Festival

Web Interface GSM Interface Audio Interface

RoboKernel

Observe World

Video Input Visual Cortex ThreeDimensionMaps RV Knowledge Base Path Planning MotorFoundation

V4L2 OpenCV OpenGL OpenMind / Wolfram Alpha / Google Master Path Planning MD23

libFAST MasterWorld Arduino

Change Position

Speaker 802.11b/g Wifi WebCam WebCam GSM Ultra Sonic Ultra Sonic Accelerometer

PCI Bus Universal Serial Bus

PC

Arduino UNO

MD23/25 Motor Bridge

Stepper Motor Stepper Motor Servo Motor Servo Motor Servo Motor LED Light IR Transmit IR Receive

BIOS → MBR → GRUB → Kernel /sbin/init → Runlevel Initialization

GuarddoG Service Start

RAM Runtime
Filesystem Preperation and
File Copying

gsmsmsd

Apache
Web Server

RoboVision CLI
or
RoboVisionX

SMS Interface
Thread

WebInterface
Thread

RoboKernel
Thread

VideoInput
Thread

MD23
Thread

Motor HAL
Thread

VisualCortex
Thread

Arduino
Thread

ScriptRunner
Thread

Activity
Thread

Software Stack
Performance Hypervisor

Software Stack
Implementation Framework

Software Stack
Statistics

The System in Practice
Installation

The System in Practice
Data Sets and Test Results

The System in Practice
Commercial Value

The System in Practice
Weaknesses

Future Work
Network Connectivity
NLP – AI Knowledge Base
Speech Recognition
Commercial Robots
CUDA / VLSI acceleration

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