Assignment

1

EE23010: Probability and Random Processes Indian Institute of Technology, Hyderabad

Aman Kumar EE22BTECH11006

Question: For the following probability distribution determine standard deviation of the random variable X.

X	2	3	4
p_X	0.2	0.5	0.3

Solution: Given, X be the random variable and $p_X(k)$ is the probability distribution.

Variance of X is given by

$$\sigma_X^2 = E[X - E(X)]^2 \tag{1}$$

$$= E(X^{2}) - [E(X)]^{2}$$
 (2)

Now,

$$E(X^{2}) = \sum_{k=1}^{n} X_{k}^{2} p_{X}(k)$$
 (3)

$$= 10.1$$
 (4)

Similarly,

$$[E(X)]^2 = \left[\sum_{k=1}^n X_k p_X(k)\right]^2 \tag{5}$$

$$= 9.61$$
 (6)

Now putting the values in eqn (2):

$$\sigma_X^2 = 10.1 - 9.61 \tag{7}$$

$$\sigma_X = 0.7 \tag{8}$$