

Assignment

EE23010: Probability and Random Processes

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Question: For the following probability distribution determine standard deviation of the random variable X .

X	2	3	4
p_X	0.2	0.5	0.3

Solution: Given, X be the random variable and p_X is the probability distribution. Standard deviation is given by

$$\sigma_X = \sqrt{E(X^2) - E(X)^2} \quad (1)$$

$$= \sqrt{\sum_{i=1}^n X_i^2 p_{Xi} - [\sum_{i=1}^n X_i p_{Xi}]^2} \quad (2)$$

Now,

$$E(X^2) = \sum_{i=1}^n X_i^2 p_{Xi} \quad (3)$$

$$= (2)^2(0.2) + (3)^2(0.5) + (4)^2(0.3) \quad (4)$$

$$= 10.1 \quad (5)$$

Similarly,

$$E(X)^2 = [\sum_{i=1}^n X_i p_{Xi}]^2 \quad (6)$$

$$= [(2)(0.2) + (3)(0.5) + (4)(0.3)]^2 \quad (7)$$

$$= 9.61 \quad (8)$$

Now putting the values in eqn (2):

$$\sigma_X = \sqrt{10.1 - 9.61} \quad (9)$$

$$= 0.7 \quad (10)$$