The intcalc package

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Abstract

This package provides expandable arithmetic operations with integers.

Contents

1	Doo	cumentation 2
	1.1	Introduction
	1.2	Conditions
		1.2.1 Preconditions
		1.2.2 Postconditions
	1.3	Error handling
	1.4	Operations
		1.4.1 Num
		1.4.2 Inv, Abs, Sgn
		1.4.3 Min, Max, Cmp
		1.4.4 Inc, Dec, Add, Sub
		1.4.5 Shl, Shr
		1.4.6 Mul, Sqr, Fac, Pow
		1.4.7 Div, Mod
	1.5	Interface for programmer
2	Imp	plementation 7
	2.1	Reload check and package identification
	2.2	Catcodes
	2.3	Macros independent of ε -T _E X 9
		2.3.1 Abs, Sgn
		2.3.2 Min, Max, Cmp
		2.3.3 Fac
	2.4	Implementation based on ε -TeX
		2.4.1 Num
		2.4.2 Inv, Abs, Sgn
		2.4.3 Min, Max, Cmp
		2.4.4 Inc, Dec
		2.4.5 Add, Sub
		2.4.6 Shl, Shr
		2.4.7 Mul, Sqr, Fac
		2.4.8 Pow
		2.4.9 Div, Mod
	2.5	Implementation without ε -TFX
		2.5.1 Num
		2.5.2 Inv, Abs, Sgn
		2.5.3 Min, Max, Cmp
		2.5.4 Inc, Dec
		2.5.5 Add, Sub

		2.5.6	Shl, Shr	27
		2.5.7	\InCa@Tim	29
		2.5.8	Mul	32
		2.5.9	Sqr, Fac	34
		2.5.10	Pow	34
		2.5.11	Div	36
		2.5.12	Mod	39
		2.5.13	Help macros	41
3	Tes	t		41
	3.1	Catcoo	de checks for loading	41
	3.2	Macro	tests	43
		3.2.1	Preamble with test macro definitions	43
		3.2.2	Time	46
		3.2.3	Test 4: additional mod/div operations	47
		3.2.4	Test sets	48
4	Inst	allatio	n	56
	4.1	Downl	oad	56
	4.2	Bundle	e installation	57
	4.3	Packag	ge installation	57
	4.4		h file name databases	57
	4.5	Some	details for the interested	57
5	Cat	alogue		5 8
6	His	tory		58
			9 v1.0]	58
			7 v1.1	58
7	Ind	ov		50

1 Documentation

1.1 Introduction

Package intcalc defines arithmetic operations that deal with integers. Integers mean numbers in T_EX. The same restrictions apply, the range is limited to [-2147483647, 2147483647].

The operations have the form of macros that take one or two integers as parameter and return the integer result. The macro name is a three letter operation name prefixed by the package name, e.g. \intcalcAdd{10}{43} returns 53.

The macros are fully expandable, exactly two expansion steps generate the result. Therefore the operations may be used nearly everywhere in TeX, even inside \number, \csname, file names, or other expandable contexts.

The package contains two implementations of the operations. If ε -TeX is detected then the macros are implemented using its features (\numexpr). Otherwise the slower implementation without ε -TeX's help is choosen.

1.2 Conditions

1.2.1 Preconditions

- Arguments can be anything that TEX interprets as "number". Examples: plain numbers, count or length register, macros that expands to a number.
- The arguments are limited to the range -2147483647 until 2147483647. These numbers belong to the range. Note that some operations have additionals restrictions to the range.

- The argument may be expressions that \numexpr understands if ε -TEX is available.
- The resulting number must fit in the allowed range.

1.2.2 Postconditions

Additional properties of the macros apart from calculating a correct result (of course ©):

- The macros are fully expandable. Thus they can be used inside \edef, \csname, after \number, for example.
- Furthermore exactly two expansion steps calculate the result.
- The number consists of one optional minus sign and one to ten digits. The first digit is larger than zero for numbers that consists of more than one digit.

In short, the number format is exactly the same as \number generates. And the tokens (minus sign, digits) have catcode 12 (other).

• Call by value is simulated. First the arguments are converted to numbers. Then these numbers are used in the calculations.

Remember that arguments may contain expensive macros or ε -TeX expressions. This strategy avoids multiple evaluations of such arguments.

1.3 Error handling

There are two kinds of errors if a precondition is violated: Some errors are detected by the macros, example: division by zero. In this cases an undefined control sequence is called and causes a TeX error message, example: \IntCalcError:DivisionByZero. The name of the control sequence contains the reason for the error. The TEX error may be ignored. Then the operation returns zero as result. Because the macros are supposed to work in expandible contexts. An traditional error message, however, is not expandable and would break these contexts.

If a number exceeds the range of -2147483647 until 2147483647, then T_EX throws an error "Number too big" and recovers by using biggest allowed value. Example for the negative number -30000000000 is replaced by -2147483647.

1.4 Operations

Some definition equations below use the function Int that converts a real number to an integer. The number is truncated that means rounding to zero:

$$\operatorname{Int}(x) := \begin{cases} \lfloor x \rfloor & \text{if } x \ge 0 \\ \lceil x \rceil & \text{otherwise} \end{cases}$$

1.4.1 Num

\intcalcNum $\{\langle x \rangle\}$

Macro \intcalcNum converts its argument to a normalized integer number without unnecessary leading zeros or signs. The result matches the regular expression:

1.4.2 Inv, Abs, Sgn

\intcalcInv $\{\langle x \rangle\}$

Macro \intcalcInv switches the sign.

$$Inv(x) := -x$$

\intcalcAbs $\{\langle x \rangle\}$

Macro \intcalcAbs returns the absolute value of integer $\langle x \rangle$.

$$Abs(x) := |x|$$

\intcalcSgn $\{\langle x \rangle\}$

Macro \intcalcSgn encodes the sign of $\langle x \rangle$ as number.

$$Sgn(x) := \begin{cases} -1 & \text{if } x < 0 \\ 0 & \text{if } x = 0 \\ 1 & \text{if } x > 0 \end{cases}$$

These return values can easily be distinguished by \ifcase:

1.4.3 Min, Max, Cmp

\intcalcMin $\{\langle x \rangle\}$ $\{\langle y \rangle\}$

Macro \intcalcMin returns the smaller of the two integers.

$$Min(x, y) := \begin{cases} x & \text{if } x < y \\ y & \text{otherwise} \end{cases}$$

\intcalcMax $\{\langle x \rangle\}$ $\{\langle y \rangle\}$

Macro \intcalcMax returns the larger of the two integers.

$$Max(x,y) := \begin{cases} x & \text{if } x > y \\ y & \text{otherwise} \end{cases}$$

\intcalcCmp $\{\langle x \rangle\}$ $\{\langle y \rangle\}$

Macro \intcalcCmp encodes the comparison result as number:

$$Cmp(x,y) := \begin{cases} -1 & \text{if } x < y \\ 0 & \text{if } x = y \\ 1 & \text{if } x > y \end{cases}$$

These values can be distinguished by \ifcase:

1.4.4 Inc, Dec, Add, Sub

\intcalcInc $\{\langle x \rangle\}$

Macro \intcalcInc increments $\langle x \rangle$ by one.

$$Inc(x) := x + 1$$

\intcalcDec $\{\langle x \rangle\}$

Macro \intcalcDec decrements $\langle x \rangle$ by one.

$$Dec(x) := x - 1$$

\intcalcAdd $\{\langle x \rangle\}$ $\{\langle y \rangle\}$

Macro \intcalcAdd adds the two numbers.

$$Add(x, y) := x + y$$

\intcalcSub $\{\langle x \rangle\}$ $\{\langle y \rangle\}$

Macro \intcalcSub calculates the difference.

$$Sub(x, y) := x - y$$

1.4.5 Shl, Shr

\intcalcShl $\{\langle x \rangle\}$

Macro \intcalcShl implements shifting to the left that means the number is multiplied by two. Overflow is possible. The sign is preserved.

$$Shl(x) := x * 2$$

\intcalcShr $\{\langle x \rangle\}$

Macro \intcalcShr implements shifting to the right. That is equivalent to an integer division by two. The sign is preserved.

$$Shr(x) := Int(x/2)$$

1.4.6 Mul, Sqr, Fac, Pow

\intcalcMul $\{\langle x \rangle\}$ $\{\langle y \rangle\}$

Macro \intcalcMul calculates the product of $\langle x \rangle$ and $\langle y \rangle$.

$$Mul(x, y) := x * y$$

\intcalcSqr $\{\langle x \rangle\}$

Macro \intcalcSqr returns the square product.

$$Sqr(x) := x^2$$

\intcalcFac $\{\langle x \rangle\}$

Macro \intcalcFac returns the factorial of $\langle x \rangle$. Negative numbers are not permitted.

$$\operatorname{Fac}(x) := x! \qquad \text{ for } x \ge 0$$

$$(0! = 1)$$

\intcalcPow $\{\langle x \rangle\}$ $\{\langle y \rangle\}$

Macro \intcalcPow calculates the value of $\langle x \rangle$ to the power of $\langle y \rangle$. The error "division by zero" is thrown if $\langle x \rangle$ is zero and $\langle y \rangle$ is negative. permitted:

$$\operatorname{Pow}(x,y) := \operatorname{Int}(x^y) \qquad \text{for } x \neq 0 \text{ or } y \geq 0$$

$$(0^0 = 1)$$

1.4.7 Div, Mod

\intcalcDiv $\{\langle x \rangle\}$ $\{\langle y \rangle\}$

Macro \intcalcDiv performs an integer division. Argument $\langle y \rangle$ must not be zero.

$$\operatorname{Div}(x,y) := \operatorname{Int}(x/y)$$
 for $y \neq 0$

\intcalcMod $\{\langle x \rangle\}$ $\{\langle y \rangle\}$

Macro \intcalcMod gets the remainder of the integer division. The sign follows the divisor $\langle y \rangle$. Argument $\langle y \rangle$ must not be zero.

$$Mod(x, y) := x \% y$$
 for $y \neq 0$

The result ranges:

$$\begin{aligned} -|y| &< \operatorname{Mod}(x,y) \leq 0 & \text{for } y < 0 \\ 0 &\leq \operatorname{Mod}(x,y) < y & \text{for } y \geq 0 \end{aligned}$$

1.5 Interface for programmer

If the programmer can ensure some more properties about the arguments of the operations, then the following macros are a little more efficient.

In general numbers must obey the following constraints:

- Plain number: digit tokens only, no command tokens.
- Non-negative. Signs are forbidden.
- \bullet Arguments and the result must fit in range $0\ldots2147483647.$
- Delimited by exclamation mark. Curly braces around the number are not allowed and will break the code.

```
\label{eq:localcond} $$ \operatorname{IntCalcInc} \langle number \rangle \ !$$ Incrementation, range: 0...2147483646. $$ \operatorname{IntCalcDec} \langle number \rangle \ !$$ Decrementation, range: 1...2147483647. $$ \operatorname{IntCalcAdd} \langle number A \rangle \ ! \langle number B \rangle \ !$$ Addition, $A \geq B$. $$ \operatorname{IntCalcSub} \langle number A \rangle \ ! \langle number B \rangle \ !$$ Subtraction, $A \geq B$. $$ \operatorname{IntCalcShl} \langle number \rangle \ !$$ $$ \operatorname{IntCalcShl} \langle number \rangle \ !$$ $$ }
```

 $\IntCalcShr\ \langle number \rangle$!

Right shift (integer division by two).

Multiplication, $A \geq B$.

\IntCalcDiv $\langle number A \rangle$! $\langle number B \rangle$!

Division operation.

Modulo operation.

2 Implementation

 $_1$ $\langle *package \rangle$

2.1 Reload check and package identification

Left shift (multiplication with two), range: 0..1073741823.

Reload check, especially if the package is not used with LATEX.

```
2 \begingroup\catcode61\catcode48\catcode32=10\relax%
```

- $3 \ \catcode13=5 \% ^M$
- 4 \endlinechar=13 %
- $_{5}$ \catcode35=6 % #
- 6 \catcode39=12 % '
- $7 \cdot \text{catcode44=12 \%},$
- 8 \catcode45=12 % 9 \catcode46=12 % .
- 10 \catcode58=12 % :
- 11 \catcode64=11 % @
- 12 \catcode123=1 % {
- 13 \catcode125=2 % }

```
\expandafter\let\expandafter\x\csname ver@intcalc.sty\endcsname
 14
      \ifx\x\relax % plain-TeX, first loading
 15
 16
      \else
        \def\empty{}%
 17
        \ifx\x\empty % LaTeX, first loading,
  18
 19
          \mbox{\ensuremath{\%}} variable is initialized, but \ProvidesPackage not yet seen
 20
 21
          \expandafter\ifx\csname PackageInfo\endcsname\relax
            \def\x#1#2{%}
 22
               \immediate\write-1{Package #1 Info: #2.}%
 23
            }%
 24
          \else
 25
            \def\x#1#2{\PackageInfo{#1}{#2, stopped}}%
 26
 27
          \x{intcalc}{The package is already loaded}%
 28
 29
          \aftergroup\endinput
 30
        \fi
      \fi
 31
 32 \endgroup%
Package identification:
 33 \begingroup\catcode61\catcode48\catcode32=10\relax%
      \catcode13=5 % ^^M
      \endlinechar=13 %
 35
      \catcode35=6 % #
 36
      \catcode39=12 % '
 37
      \catcode40=12 % (
 38
      \catcode41=12 % )
 39
      \catcode44=12 % ,
 40
 41
      \catcode45=12 % -
 42
      \catcode46=12 % .
 43
      \catcode47=12 % /
  44
      \catcode58=12 % :
      \catcode64=11 % @
 45
      \catcode91=12 % [
 46
      \catcode93=12 % ]
 47
      \catcode123=1 % {
 48
      \catcode125=2 % }
 49
      \expandafter\ifx\csname ProvidesPackage\endcsname\relax
 50
        \def\x#1#2#3[#4]{\endgroup
 51
          \immediate\write-1{Package: #3 #4}%
 52
          \xdef#1{#4}%
 53
        }%
 54
 55
      \else
 56
        \def \x#1#2[#3]{\endgroup}
 57
          #2[{#3}]%
          \ifx#1\@undefined
 58
            \xdef#1{#3}%
 59
          \fi
 60
 61
          \int x#1\relax
            \xdef#1{#3}%
 62
 63
          \fi
 64
        }%
 66 \expandafter\x\csname ver@intcalc.sty\endcsname
 67 \ProvidesPackage{intcalc}%
      [2007/09/27 v1.1 Expandable calculations with integers (HO)]%
2.2
      Catcodes
 69 \begingroup\catcode61\catcode48\catcode32=10\relax%
     \catcode13=5 % ^^M
 70
      \endlinechar=13 %
 71
```

```
\catcode123=1 % {
 72
     \catcode125=2 % }
     \catcode64=11 % @
 74
     \def\x{\endgroup
 75
 76
       \expandafter\edef\csname InCa@AtEnd\endcsname{%
 77
         \endlinechar=\the\endlinechar\relax
 78
         \catcode13=\the\catcode13\relax
 79
         \catcode32=\the\catcode32\relax
         \catcode35=\the\catcode35\relax
 80
         \catcode61=\the\catcode61\relax
 81
         \catcode64=\the\catcode64\relax
 82
         \catcode123=\the\catcode123\relax
 83
         \catcode125=\the\catcode125\relax
 84
       }%
 85
    }%
 87 \x\catcode61\catcode48\catcode32=10\relax%
 88 \catcode13=5 % ^^M
 89 \endlinechar=13 %
 90 \catcode35=6 % #
 91 \catcode64=11 % @
 92 \catcode123=1 % {
 93 \catcode125=2 % }
 94 \def\TMP@EnsureCode#1#2{%
     \edef\InCa@AtEnd{%
 95
       \InCa@AtEnd
 97
       \catcode#1=\the\catcode#1\relax
 98
     }%
 99
     \catcode#1=#2\relax
100 }
101 \TMP@EnsureCode{33}{12}% !
102 \TMP@EnsureCode{40}{12}% (
103 \TMP@EnsureCode{41}{12}% )
104 \TMP@EnsureCode{42}{12}% *
105 \TMP@EnsureCode{43}{12}% +
106 \TMP@EnsureCode{45}{12}% -
107 \TMP@EnsureCode{47}{12}% /
108 \TMP@EnsureCode{58}{11}% : (letter!)
109 \TMP@EnsureCode{60}{12}% <
110 \TMP@EnsureCode{62}{12}% >
111 \TMP@EnsureCode{63}{14}% ? (comment!)
113 \begingroup\expandafter\expandafter\expandafter\endgroup
114 \expandafter\ifx\csname InCa@TestMode\endcsname\relax
115 \else
116
    \catcode63=9 % ? (ignore)
117 \fi
118 ? \let\InCa@@TestMode\InCa@TestMode
     Macros independent of -TEX
2.3.1 Abs, Sgn
119 \def\InCa@Abs#1#2!{%
120 \ifx#1-%
       #2%
121
122 \else
123
       #1#2%
124
     \fi
125 }
```

\InCa@Abs

\InCa@Sgn

126 \def\InCa@Sgn#1#2!{%

```
\ifx#1-%
127
128
        -1%
129
      \else
130
        \ifx#10%
131
          0%
        \else
132
133
          1%
        \fi
134
      \fi
135
136 }
```

2.3.2 Min, Max, Cmp

\InCa@Min

```
137 \def\InCa@Min#1!#2!{%

138 \ifnum#1<#2 %

139 #1%

140 \else

141 #2%

142 \fi

143 }
```

 $\InCa@Max$

```
144 \def\InCa@Max#1!#2!{%

145 \ifnum#1>#2 %

146 #1%

147 \else

148 #2%

149 \fi

150}
```

\InCa@Cmp

```
151 \def\InCa@Cmp#1!#2!{%
     \ifnum#1=#2 %
152
        0%
153
     \else
154
        \ifnum#1<#2 %
155
156
          -%
157
        \fi
158
        1%
159
     \fi
160 }
```

2.3.3 Fac

\InCa@Fac It does not make much sense to calculate the faculty by an general algorithm. The allowed range of arguments is too low because of the limited integer domain.

```
161 \def\InCa@Fac#1!{%
     \ifcase#1 1% 0!
162
     \or 1% 1!
163
     \or 2% 2!
164
     \or 6% 3!
165
     \or 24% 4!
166
     \or 120% 5!
167
168
     \or 720% 6!
169
     \or 5040% 7!
170
     \or 40320% 8!
171
     \or 362880% 9!
     \or 3628800% 10!
172
     \or 39916800% 11!
173
     \or 479001600% 12!
174
175
     \else
```

```
\int 1 \sqrt{z}
              176
                        0\IntCalcError:FacNegative%
              177
              178
                      \else
                        0\IntCalcError:FacOverflow%
              179
              180
                      \fi
              181
                    \fi
              182 }
                   Implementation based on -TeX
             2.4
             Only \numexpr is used from \varepsilon-T<sub>E</sub>X.
              183 \begingroup\expandafter\expandafter\expandafter\endgroup
              184 \expandafter\ifx\csname numexpr\endcsname\relax
             2.4.1 Num
\intcalcNum
                   \def\intcalcNum#1{%
              186
                      \the\numexpr#1\relax
              187
                   }%
              188
             2.4.2 Inv, Abs, Sgn
\intcalcInv
              189
                   \def\intcalcInv#1{%
              190
                      \number-\intcalcNum{#1} %
              191
\intcalcAbs
              192
                   \def\intcalcAbs#1{%
                     \number\expandafter\InCa@Abs\the\numexpr#1! %
              193
              194
\intcalcSgn
              195
                   \def\intcalcSgn#1{%
                      \number\expandafter\InCa@Sgn\the\numexpr#1! %
              196
              197
                   }%
             2.4.3 Min, Max, Cmp
\intcalcMin
                   \def\intcalcMin#1#2{%
              198
              199
                      \number\expandafter\InCa@Min
                      \the\numexpr#1\expandafter!%
              200
                      \the\numexpr#2! %
              201
              202
\intcalcMax
                   \def\intcalcMax#1#2{%
              203
              204
                      \number\expandafter\InCa@Max
                      \the\numexpr#1\expandafter!%
              205
                      \the\numexpr#2! %
              206
              207
\intcalcCmp
                   \def\intcalcCmp#1#2{%
              208
              209
                      \number\expandafter\InCa@Cmp
              210
                      \the\numexpr#1\expandafter!\the\numexpr#2! %
```

211

}%

2.4.4 Inc, Dec

		,
\intcalcInc		
(111000101110)
	212	
	213	\the\numexpr#1+1\relax
	214	}%
\intcalcDec		
	215	\def\intcalcDec#1{%
	216	\the\numexpr#1-1\relax
	217	}%
	217	1/6
\ T+C-1 -T		
\IntCalcInc		
	218	\def\IntCalcInc#1!{%
	219	\the\numexpr#1+1\relax
	220	}%
\IntCalcDec		
	221	\def\IntCalcDec#1!{%
	222	\the\numexpr#1-1\relax
	223	}%
	2.4.5	Add, Sub
		•
\intcalcAdd		
	224	\def\intcalcAdd#1#2{%
	225	\the\numexpr#1+(#2)\relax
	226	}%
	220	9) (
\intcalcSub		
\IIICCAICDUD		
	227	
	228	$\theta = \frac{42}{relax}$
	229	}%
\IntCalcAdd		
	230	\def\IntCalcAdd#1!#2!{%
	231	\the\numexpr#1+#2\relax
	232	}%
	202	, n
\IntCalcSub		
(IIICOAICDUD		
	233	\def\IntCalcSub#1!#2!{%
	234	\the\numexpr#1-#2\relax
	235	}%
	2.4.6	Shl, Shr
	4.1. 0	····, ····
\intcalcShl		
	226	\dof\intcalcGhl#159
	236	\def\intcalcShl#1{%
	237	\the\numexpr(#1)*2\relax
	238	}%
\ · · ·		
\intcalcShr		
	239	\def\intcalcShr#1{%
	240	\number\expandafter\InCa@Shr\the\numexpr#1! %
	241	}%
	-	
\IntCalcShl		
		\\
	0.40	
	242	\def\IntCalcShl#1!{%
	242 243 244	\def\IntCalcShl#1!{% \the\numexpr#1*2\relax }%

```
\IntCalcShr
                   \def\IntCalcShr#1!{%
              245
                     \theta = 1-1 \leq 1-1
              246
              247
 \InCa@Shr
              248
                   \def\InCa@Shr#1#2!{%
                     \ifx#1-%
              249
                       -\InCa@Shr#2!%
              250
              251
                     \else
                       \ifodd#1#2 %
              252
              253
                         \theta = \frac{1#2-1}{2}
              254
                       \else
                         \theta = 1#2/2 relax
              255
                       \fi
              256
                     \fi
              257
              258 }%
             2.4.7 Mul, Sqr, Fac
\intcalcMul
                   \def\intcalcMul#1#2{%
              259
                     \t \sum_{\#2} \pi(\#2) \
              260
              261
\IntCalcMul
                  \def\IntCalcMul#1!#2!{%
              262
              263
                   \t \sum_{x=0}^{the\numexpr#1*#2\relax}
              264
                   }%
\intcalcSqr
                   \def\intcalcSqr#1{\%}
              265
                    \number\expandafter\InCa@Sqr\the\numexpr#1! %
              266
              267
                   }%
 \InCa@Sqr
                   \def\InCa@Sqr#1!{%
              268
              269
                    \the\numexpr#1*#1\relax
                   }%
              270
\intcalcFac
                   \def\intcalcFac#1{%
              271
              272
                     \number\expandafter\InCa@Fac\the\numexpr#1! %
              273
             2.4.8 Pow
\intcalcPow
              274
                  \def\intcalcPow#1#2{%
              275
                     \number\expandafter\InCa@Pow
              276
                     \the\numexpr#1\expandafter!%
                     \the\numexpr#2! %
              277
              278
                  }%
 \InCa@Pow
              279
                   \def\InCa@Pow#1#2!#3#4!{%
              280
                     \ightharpoonup \ifcase#3#4 % power = 0
              281
                       1%
              282
                     \or \% power = 1
                      #1#2%
              283
              284
                     \or \% power = 2
```

```
\theta = 1#2*#1#2\
               285
               286
                       \else
                         \footnote{1} \iftit{ifcase#1#2 % basis = 0, power <> 0
               287
               288
                           ifx#3-% power < 0
               290
                             0\IntCalcError:DivisionByZero%
               291
                           \fi
               292
                         \or
                           1% basis = 1
               293
                         \else
               294
                           295
                             \ifodd#3#4 %
               296
                               -%
               297
                             \fi
               298
                             1%
               299
                           \else % |basis| > 1
               301
                             \int x#3-\% power < 0
               302
                               0%
                             \else % power > 2
               303
                               \InCa@PowRec#1#2!#3#4!1!%
               304
               305
                             \fi
                           \fi
               306
               307
                         \fi
               308
                       \fi
                    }%
\InCa@PowRec
                    Pow(b, p) {
                      PowRec(b, p, 1)
                    PowRec(b, p, r) {
                      if p == 1 then
                        return r*b
                      else
                        ifodd p then
                          return PowRec(b*b, (p-1)/2, r*b) % p div 2 = (p-1)/2
                        else
                          return PowRec(b*b, (p-1)/2, r)
                      fi
                    }
                     \def\InCa@PowRec#1!#2!#3!{%
               310
               311
                       \int 12 = 0 
                         \the\numexpr#1*#3\relax
               312
                       \else
               313
                         \ifodd#2 %
               314
                           \expandafter\InCa@PowRec
               315
                           \the\numexpr#1*#1\expandafter!%
               316
                           \the\numexpr(#2-1)/2\expandafter!%
               317
                           \the\numexpr#1*#3\expandafter\expandafter\expandafter!%
               318
                         \else
               319
               320
                           \expandafter\InCa@PowRec
               321
                           \the\numexpr#1*#1\expandafter!%
               322
                           \the\numexpr(#2-1)/2\expandafter!%
               323
                           \number#3\expandafter\expandafter\expandafter!%
               324
                         \fi
               325
                       \fi
                    }%
               326
```

2.4.9 Div, Mod

TeX's \divide truncates, ε -TeX's \numexpr rounds the result of a division. The rounding method is called "Symmetric Arithmetic Rounding" or "Round-Half-Up" ("Kaufmännisches Runden" in German):

```
1 = 3 divide 2 = 1.5 = numexpr 3/2 = 2
-1 = -3 divide 2 = -1.5 = numexpr -3/2 = -2
```

Macro $\$ intcalcDiv follows TeX and truncates. The calculation is done by the following formula:

$$Div(X, Y) = (X - (Y - 1)/2)/Y \quad \text{for } X, Y > 0$$
 (1)

The operator '/' is \numexpr's division.

```
\intcalcDiv
```

```
327 \def\intcalcDiv#1#2{%
328 \number\expandafter\InCa@Div
329 \the\numexpr#1\expandafter!%
330 \the\numexpr#2! %
331 }%
```

\InCa@Div

```
\def\InCa@Div#1!#2!{%
332
        \ifcase#2 %
333
          0\IntCalcError:DivisionByZero%
334
335
        \else
336
          \ifcase#1 %
337
            0%
338
          \else
            \expandafter\InCa@@Div
339
            \romannumeral 0%
340
            \int \frac{1}{z} dx
341
               \expandafter-\number-#1%
342
343
            \else
               \expandafter+\number#1%
344
345
346
            \expandafter!%
            \romannumeral 0%
347
            \lim 2<\z0
348
               \verb|\expandafter-\number-#2%| \\
349
            \else
350
               \expandafter+\number#2%
351
            \fi
352
            !%
353
          \fi
354
        \fi
355
     }%
356
```

\IntCalcDiv

```
\def\InCa@Temp#1{%
357
       \def\IntCalcDiv##1!##2!{%
358
         \number
359
         \ifcase##2 %
360
361
            0\IntCalcError:DivisionByZero%
362
          \else
363
            \ifcase##1 %
364
              0%
            \else
365
              \theta = \frac{\#1-(\#2-1)/2}{\#2}
366
            \fi
367
368
         \fi
369
         #1%
370
       }%
371
372
     \InCa@Temp{ }%
```

```
\InCa@@Div
              373
                    \def\InCa@@Div#1#2!#3#4!{%
              374
                      #1#3%
               375
                      \theta = \frac{4-1}{2} / 4 relax
               376
                    }%
\intcalcMod
                    \def\intcalcMod#1#2{%
               377
                      \number\expandafter\InCa@Mod
               378
                      \the\numexpr#1\expandafter!%
               379
               380
                      \the\numexpr#2! %
               381
                    }%
  \InCa@Mod
                    \def\InCa@Mod#1!#2!{%
               382
                      \ifcase#2 %
               383
                        0\IntCalcError:DivisionByZero%
               384
               385
                      \else
               386
                        \ifcase#1 %
               387
                          0%
                        \else
               388
                          \expandafter\InCa@@Mod
               389
                          \romannumeral 0%
               390
                          \lim 1<\z0
               391
                             \expandafter-\number-#1%
               392
                          \else
               393
                             \expandafter+\number#1%
               394
               395
                           \fi
               396
                           \expandafter!%
               397
                           \romannumeral 0%
               398
                          \lim 2<\z0
                             \expandafter-\number-#2%
               399
                          \else
               400
                             \expandafter+\number#2%
               401
                          \fi
               402
                          ! %
               403
                        \fi
               404
               405
                      \fi
               406
                    }%
\IntCalcMod
                    \def\InCa@Temp#1{%
               407
                      \def\IntCalcMod##1!##2!{%
               408
               409
                        \number
                        \ifcase##2 %
               410
                          0\IntCalcError:DivisionByZero%
               411
                        \else
               412
               413
                          \ifcase##1 %
               414
                            0%
               415
                          \else
                             \theta = \frac{\#1-(\#4-1)/2}{\#2*\#2}
               416
               417
                          \fi
                        \fi
               418
                        #1%
               419
                      }%
               420
               421
                    }%
               422
                    \InCa@Temp{ }%
 \InCa@@Mod
                    \def\InCa@@Mod#1#2!#3#4!{%
               423
                      \if#3+%
               424
                        \if#1+%
               425
```

```
\the\numexpr#2-\InCa@@Div+#2!+#4!*#4\relax
                    426
                    427
                             \else
                               \expandafter\InCa@ModX
                    428
                               \the\numexpr-#2+\InCa@@Div+#2!+#4!*#4!#4!%
                    430
                             \fi
                    431
                           \else
                    432
                             -%
                             \if#1+%
                    433
                               \expandafter\InCa@ModX
                    434
                               \the\numexpr-#2+\InCa@@Div+#2!+#4!*#4!#4!%
                    435
                    436
                               \theta^2-\ln Ca@@Div+#2!+#4!*#4\
                    437
                             \fi
                    438
                    439
                           \fi
                    440
                        }%
      \InCa@ModX
                         \def\InCa@ModX#1!#2!{%
                    441
                   442
                           \ifcase#1 %
                             0%
                    443
                    444
                           \else
                    445
                             \theta = 1+#2\
                    446
                           \fi
                    447
                        }%
                    448
                         \expandafter\InCa@AtEnd
                   449 \fi%
                         Implementation without -TEX
                   2.5
                   2.5.1 Num
     \intcalcNum
                   450 \ensuremath{\mbox{\sc Num#1}}\
                         \number\expandafter\InCa@FirstOfOne\number#1! %
                   451
                   452 }
                   2.5.2 Inv, Abs, Sgn
     \intcalcInv
                   453 \ensuremath{\mbox{def}\mbox{intcalcInv#1}}\%
                        \number\expandafter\InCa@FirstOfOne\number-#1! %
                   455 }
\InCa@FirstOfOne
                    456 \def\InCa@FirstOfOne#1!{#1}
     \intcalcAbs
                    457 \def\intcalcAbs#1{%
                        \number\expandafter\InCa@Abs\number#1! %
                   459 }
     \intcalcSgn
                    460 \def\intcalcSgn#1{%
                         \number\expandafter\InCa@Sgn\number#1! %
                   462 }
```

2.5.3 Min, Max, Cmp

```
\intcalcMin
                   463 \def\intcalcMin#1#2{%
                   464 \number\expandafter\InCa@Min
                   465 \number*1\expandafter!\number#2! \%
                   466 }
    \intcalcMax
                   467 \left( \frac{467}{m} \right)
                   468 \number\expandafter\InCa@Max
                   469 \number\number#1\expandafter!\number#2! \%
                   470 }
    \intcalcCmp
                   471 \def\intcalcCmp#1#2{%}
                   472 \number\expandafter\InCa@Cmp
473 \number\number#1\expandafter!\number#2! %
                   474 }%
                  2.5.4 Inc, Dec
    \intcalcInc
                   475 \def\intcalcInc#1{%
                   476 \number\expandafter\InCa@IncSwitch\number#1! \%
                   477 }
\InCa@IncSwitch
                   478 \def\InCa@IncSwitch#1#2!{%
                   479 \ifx#1-%
                   480
                          \csname InCa@Empty%
                   481
                          \InCa@Dec#2!%
                   482
                   483 \else
                   484
                          \csname InCa@Empty%
                   485
                          \InCa@Inc#1#2!%
                   486 \fi
                   487 }
    \intcalcDec
                   488 \def\intcalcDec#1{%}
                   489 \number\expandafter\InCa@DecSwitch\number#1! \%
                   490 }
\InCa@DecSwitch
                   491 \ensuremath{ \mbox{\sc def}\mbox{\sc Switch#1#2!}}\
                   492 \ifx#1-%
                   493
                           \csname InCa@Empty%
                   494
                          \expandafter\InCa@Inc#2!%
                   495
                   496 \else
                   497
                          \ifx#10%
                   498
                            -1%
                           \else
                   499
                            \csname InCa@Empty%
                   500
                             \InCa@Dec#1#2!%
                   501
                         \fi
                   502
                   503 \fi
                   504 }
```

```
\IntCalcInc
                                                                   505 \def\IntCalcInc#1!{%
                                                                                 \number\csname InCa@Empty\InCa@Inc#1! %
                                                                   506
                                                                   507 }
                         \IntCalcDec
                                                                   508 \def\IntCalcDec#1!{%
                                                                   509 \number\csname InCa@Empty\InCa@Dec#1! %
                                                                   510 }
                              \InCa@Inc
                                                                   512 \ifx#2!%
                                                                                     \csname InCa@IncDigit#1\endcsname1%
                                                                   513
                                                                  514 \else
                                                                                         \csname InCa@IncDigit#1%
                                                                   515
                                                                   516
                                                                                        \expandafter\InCa@Inc\expandafter#2%
                                                                   517 \fi
                                                                   518 }
\InCa@IncDigit[0-8]
                                                                   519 \ensuremath{\mbox{\sc S}}19\ensuremath{\mbox{\sc S}}19\ensuremath{\mbox{\sc S}}19\%
                                                                   520 \expandafter\def\csname InCa@IncDigit#1\endcsname##1{%
                                                                   521
                                                                                         \endcsname
                                                                   522
                                                                                        \ifcase##1 %
                                                                   523
                                                                   524
                                                                                              #1%
                                                                   525
                                                                                        \else
                                                                   526
                                                                                              #2%
                                                                                         \fi
                                                                   527
                                                                   528 }%
                                                                  529 }
                                                                  530 \InCa@Temp 01
                                                                   531 \InCa@Temp 12
                                                                  532 \InCa@Temp 23
                                                                  533 \InCa@Temp 34
                                                                   534 \InCa@Temp 45
                                                                  535 \InCa@Temp 56
                                                                   536 \InCa@Temp 67
                                                                   537 \InCa@Temp 78
                                                                   538 \InCa@Temp 89
            \InCa@IncDigit9
                                                                   539 \expandafter\def\csname InCa@IncDigit9\endcsname#1{%
                                                                                 \expandafter\endcsname
                                                                   541
                                                                                  \ifcase#1 %
                                                                   542
                                                                                        09%
                                                                   543 \else
                                                                   544
                                                                                       10%
                                                                  545 \fi
                                                                  546 }
                              \InCa@Dec
                                                                   547 \ensuremath{\mbox{\sc 147}}\ensuremath{\mbox{\sc 147}}\ensuremath{\mb
                                                                   548 \ifx#2!%
                                                                                        \csname InCa@DecDigit#1\endcsname1%
                                                                   549
                                                                   550 \else
                                                                                         \csname InCa@DecDigit#1%
                                                                   551
                                                                                         \expandafter\InCa@Dec\expandafter#2%
                                                                   552
                                                                   553 \fi
                                                                   554 }
```

```
\InCa@DecDigit[1-9]
                       555 \def\InCa@Temp#1#2{%
                             \expandafter\def\csname InCa@DecDigit#1\endcsname##1{%
                               \endcsname
                       557
                       558
                               \ifcase##1 %
                       559
                       560
                                 #1%
                       561
                               \else
                                 #2%
                       562
                               \fi
                       563
                       564
                            }%
                       565 }
                       566 \InCa@Temp 98
                       567 \InCa@Temp 87
                       568 \InCa@Temp 76
                       569 \InCa@Temp 65
                       570 \InCa@Temp 54
                       571 \InCa@Temp 43
                       572 \label{lnCa@Temp} 32
                       573 \InCa@Temp 21
                       574 \InCa@Temp 10
    \InCa@DecDigit0
                       575 \expandafter\def\csname InCa@DecDigit0\endcsname#1{%
                             \expandafter\endcsname
                       576
                             \ifcase#1 %
                       577
                               00%
                       578
                             \else
                       579
                       580
                               19%
                       581
                             \fi
                       582 }
                      2.5.5 Add, Sub
        \intcalcAdd
                       583 \def\intcalcAdd#1#2{%
                       584
                            \number
                               \expandafter\InCa@AddSwitch
                       585
                               \number\number#1\expandafter!%
                       586
                               \number#2! %
                       587
                       588 }
        \intcalcSub
                       589 \def\intcalcSub#1#2{%}
                       590
                            \number
                               \expandafter\InCa@AddSwitch
                       591
                               \number\number#1\expandafter!%
                       592
                               \number-\number#2! %
                       593
                       594 }
```

\InCa@AddSwitch Decision table for \InCa@AddSwitch. The sign of negative numbers can be removed by a simple \@gobble instead of the more expensive \number-.

x < 0	y < 0	x < y	_	Add(-x, -y)
		else		Add(-y, -x)
	else	-x > y	_	Sub(-x,y)
		else	+	Sub(y, -x)
else	y < 0	x > -y	+	Sub(x, -y)
		else	_	Sub(-y,x)
	else	x > y	+	Add(x,y)
		else		Add(y,x)

```
595 \def\InCa@AddSwitch#1!#2!{%
                    \lim 1<\z0
               596
                       \lim 2<\z0
               597
               598
                         -%
                         \ifnum#1<#2 %
               599
                            \expandafter\InCa@Add\number-#1\expandafter!%
               600
               601
                           \@gobble#2!%
               602
                         \else
                           \expandafter\InCa@Add\number-#2\expandafter!%
               603
               604
                           \@gobble#1!%
                         \fi
               605
               606
                       \else
               607
                         \ifnum-#1>#2 %
               608
               609
                           \expandafter\InCa@Sub\@gobble#1!#2!%
               610
                           \expandafter\InCa@Sub\number#2\expandafter!%
               611
                           \@gobble#1!%
               612
               613
                         \fi
                       \fi
               614
                    \else
               615
                       \lim 2<\z0
               616
                         \ifnum#1>-#2 %
               617
                           \expandafter\InCa@Sub\number#1\expandafter!%
               618
               619
                           \@gobble#2!%
               620
                         \else
                           -%
               621
                           \expandafter\InCa@Sub\@gobble#2!#1!%
               622
                         \fi
               623
                       \else
               624
               625
                         \ifnum#1>#2 %
               626
                           \InCa@Add#1!#2!%
               627
                         \else
                           \InCa@Add#2!#1!%
               628
               629
                         \fi
               630
                       \fi
               631
                    \fi
               632 }
\IntCalcAdd
               633 \def\IntCalcAdd#1!#2!{%
                    \number\InCa@Add#1!#2! %
               635 }
\IntCalcSub
               636 \def\IntCalcSub#1!#2!{%
                    \number\InCa@Sub#1!#2! %
               637
               638 }
\InCa@Space
               639 \begingroup
               640
                    \def\x#1{\endgroup
               641
                       \verb|\label{lnCa@Space}| #1% \\
               642 }%
               643 \x{ }
  \InCa@Add
               644 \def\InCa@Add#1!#2!{%
                    \ifcase#2 %
               645
                       #1%
               646
               647
                    \else
                       \label{localize} $$\prod_a@Add#1!#2!00000000\InCa@Space $$
               648
```

```
\fi
              649
              650 }
  \InCa@Sub
              651 \def\InCa@Sub#1!#2!{%
              652 \ifnum#1=#2 %
              653
                     0%
              654
                   \else
              655
                     \InCa@@Sub#1!#2!00000000\InCa@Space
              656
                   \fi
              657 }
\InCa@@Add
              658 \def\InCa@@Add#1!#2#3!{%
              659 \ifx\InCa@Empty#3\InCa@Empty
              660
                     \@ReturnAfterElseFi{%
              661
                        \InCa@@@Add!!#1!#2%
              662
                     }%
              663
                   \else
                     \@ReturnAfterFi{%
              664
                       \InCa@@Add#1!#3!#2%
              665
                     }%
              666
                   \fi
              667
              668 }
\InCa@@Sub
              669 \def\InCa@@Sub#1!#2#3!{%
              670 \ifx\InCa@Empty#3\InCa@Empty
                     \@ReturnAfterElseFi{%
              671
                       \InCa@@@Sub!!#1!#2%
              672
                     }%
              673
                  \else
              674
                     \@ReturnAfterFi{%
              675
                       \InCa@@Sub#1!#3!#2%
              676
              677
              678
                   \fi
              679 }
\InCa@@@Add
              680 \def\InCa@@@Add#1!#2!#3#4!#5{%
                   \ifx\InCa@Empty#4\InCa@Empty
              681
                     \csname InCa@Empty%
              682
              683
                      \@ReturnAfterElseFi{%
              684
                        \InCa@ProcessAdd#1#3!#5#2%
              685
                     }%
              686
                   \else
              687
                      \@ReturnAfterFi{%
                       \InCa@@@Add#1#3!#5#2!#4!%
              688
                     }%
              689
                   \fi
              690
              691 }
\InCa@@@Sub
              692 \def\InCa@@@Sub#1!#2!#3#4!#5{%
              693
                   \ifx\InCa@Empty#4\InCa@Empty
                      \csname @gobble%
              694
                      \@ReturnAfterElseFi{%
              695
                        \InCa@ProcessSub#1#3!#5#2%
              696
                     }%
              697
              698
                   \else
                     \@ReturnAfterFi{%
              699
                        \InCa@@@Sub#1#3!#5#2!#4!%
```

```
}%
                         701
                              \fi
                         702
                         703 }
     \InCa@ProcessAdd
                         704 \def\InCa@ProcessAdd#1#2!#3#4{%
                         705 \ifx\InCa@Empty#2\InCa@Empty
                         706
                                \csname InCa@AddDigit#1\endcsname#3%
                         707
                                \romannumeral0#4%
                         708
                              \else
                         709
                                 \csname InCa@AddDigit#1\csname InCa@DigitCarry#3%
                         710
                                \@ReturnAfterFi{%
                                  \InCa@ProcessAdd#2!#4%
                         711
                         712
                                }%
                              \fi
                         713
                         714 }
     \InCa@ProcessSub
                         715 \def\InCa@ProcessSub#1#2!#3#4{%
                              \ifx\InCa@Empty#2\InCa@Empty
                                 \csname InCa@SubDigit#1\endcsname#3%
                         717
                                 \romannumeral0#4%
                         718
                              \else
                         719
                                \csname InCa@SubDigit#1\csname InCa@DigitCarry#3%
                         720
                                 \@ReturnAfterFi{%
                         721
                                   \InCa@ProcessSub#2!#4%
                         722
                                }%
                         723
                              \fi
                         724
                         725 }
\InCa@DigitCarry[0-9]
                         726 \def\InCa@Temp#1#2{%
                              \expandafter\def\csname InCa@DigitCarry#1\endcsname##1{%
                         727
                                 \ifcase##1 %
                         728
                                   \endcsname#1%
                         729
                                 \else
                         730
                         731
                                   \endcsname#2%
                         732
                                \fi
                         733 }%
                         734 }
                         735 \InCa@Temp 01
                         736 \InCa@Temp 12
                         737 \InCa@Temp 23
                         738 \InCa@Temp 34
                         739 \InCa@Temp 45
                         740 \InCa@Temp 56
                         741 \InCa@Temp 67
                         742 \InCa@Temp 78
                         743 \InCa@Temp 89
                         744 \InCa@Temp 9{{10}}
      \InCa@AddDigit0
                         745 \expandafter\def\csname InCa@AddDigit0\endcsname#1{%
                              \ifnum#1>9 %
                         746
                         747
                                 \endcsname10%
                         748
                               \else
                                \endcsname0#1%
                         749
                              \fi
                         750
                         751 }
  \InCa@AddDigit[1-9]
                         752 \def\InCa@Temp#1#2#3{%
```

```
\expandafter\def\csname InCa@AddDigit#1\endcsname##1{%
753
754
        \ifnum##1>#2 %
755
          \endcsname 1%
756
        \else
757
         \endcsname 0%
758
        \fi
       \ifcase##1 #1% 0
759
       #3%
760
       \else #1% 10
761
762
       \fi
763
     }%
764 }
765 \InCa@Temp 18{\%}
766
     \or 2% 1
767
     \or 3% 2
     \or 4% 3
768
     \or 5% 4
769
     \or 6% 5
770
     \or 7% 6
771
     \or 8% 7
772
     \or 9% 8
773
     \or 0% 9
774
775 }%
776 \InCa@Temp 27{\%}
777
     \or 3% 1
     \or 4% 2
778
     \or 5% 3
779
     \or 6% 4
780
     \or 7% 5
781
     \or 8% 6
782
     \or 9% 7
783
     \or 0% 8
784
     \or 1% 9
785
786 }%
787 \InCa@Temp 36{%
    \or 4% 1
788
     \or 5% 2
789
     \or 6% 3
790
     \or 7% 4
791
     \or 8% 5
792
     \or 9% 6
793
794
     \or 0% 7
795
     \or 1% 8
796
     \or 2% 9
797 }%
798 \InCa@Temp 45{%
799
     \or 5% 1
     \or 6% 2
800
     \or 7% 3
801
     \or 8% 4
802
     \or 9% 5
803
     \or 0% 6
804
     \or 1% 7
805
     \or 2% 8
806
807
    \or 3% 9
808 }%
809 \InCa@Temp 54{%
810
     \or 6% 1
     \or 7% 2
811
812
     \or 8% 3
     \or 9% 4
813
```

\or 0% 5

814

```
\or 1% 6
815
816
     \or 2% 7
817
     \or 3% 8
818
     \or 4% 9
819 }%
820 \InCa@Temp 63{%
821
     \or 7% 1
     \or 8% 2
822
     \or 9% 3
823
     \or 0% 4
824
     \or 1% 5
825
     \or 2% 6
826
827
     \or 3% 7
     \or 4% 8
829
     \or 5% 9
830 }%
831 \InCa@Temp 72{%
     \or 8% 1
832
     \or 9% 2
833
     \or 0% 3
834
     \or 1% 4
835
     \or 2% 5
836
837
     \or 3% 6
838
     \or 4% 7
839
     \or 5% 8
     \or 6% 9
840
841 }%
842\ \ \ B1{\%}
     \or 9% 1
843
     \or 0% 2
844
845
     \or 1% 3
     \or 2% 4
846
     \or 3% 5
847
     \or 4% 6
848
849
     \or 5% 7
850
     \or 6% 8
     \or 7% 9
851
852 }%
853 \InCa@Temp 90{%
     \or 0% 1
854
     \or 1% 2
855
     \or 2% 3
856
857
     \or 3% 4
858
     \or 4% 5
859
     \or 5% 6
     \or 6% 7
     \or 7% 8
861
862
     \or 8% 9
863 }%
864 \def\InCa@Temp#1#2{%
     \expandafter\def\csname InCa@SubDigit#1\endcsname##1{%
865
        \ifnum##1>#1 %
866
867
          \endcsname 1%
868
        \else
869
          \endcsname 0%
870
        \fi
       \ifcase##1 #1% 0
871
       #2%
872
       \else #1% 10
873
       \fi
874
     }%
```

\InCa@SubDigit[0-9]

875

```
876 }
877 \InCa@Temp 0{%
878
    \or 9% 1
879
     \or 8% 2
     \or 7% 3
880
     \or 6% 4
881
    \or 5% 5
882
883 \or 4% 6
884 \or 3% 7
885 \or 2% 8
886 \or 1% 9
887 }
888 \InCa@Temp 1{%
    \or 0% 1
    \or 9% 2
890
    \or 8% 3
891
    \or 7% 4
892
     \or 6% 5
893
     \or 5% 6
894
     \or 4% 7
895
     \or 3% 8
896
897
    \or 2% 9
898 }
899 \InCa@Temp 2{%
900
    \or 1% 1
     \or 0% 2
901
    \or 9% 3
902
903 \or 8% 4
904 \or 7% 5
905 \or 6% 6
906 \or 5% 7
907 \or 4% 8
908 \or 3% 9
909 }
910 \InCa@Temp 3{%
911 \or 2% 1
    \or 1% 2
912
    \or 0% 3
913
    \or 9% 4
914
915
     \or 8% 5
916
     \or 7% 6
917
     \or 6% 7
918
     \or 5% 8
919
     \or 4% 9
920 }
921 \InCa@Temp 4{%
922 \or 3% 1
    \or 2% 2
923
924 \or 1% 3
    \or 0% 4
925
926 \or 9% 5
927 \or 8% 6
928 \or 7% 7
929 \or 6% 8
930 \or 5% 9
931 }
932 \InCa@Temp 5{\%}
933
   \or 4% 1
    \or 3% 2
934
    \or 2% 3
935
936 \or 1% 4
```

937 \or 0% 5

```
938
     \or 9% 6
939
     \or 8% 7
940
     \or 7% 8
941
     \or 6% 9
942 }
943 \InCa@Temp 6{%
944 \or 5% 1
945 \or 4% 2
946 \or 3% 3
947 \or 2% 4
948 \or 1% 5
949 \or 0% 6
950 \or 9% 7
951 \or 8% 8
952 \or 7% 9
953 }
954 \InCa@Temp 7\%
955 \or 6% 1
     \or 5% 2
956
    \or 4% 3
957
     \or 3% 4
958
     \or 2% 5
959
960
     \or 1% 6
961
     \or 0% 7
962
     \or 9% 8
963 \or 8% 9
964 }
965 \InCa@Temp 8{%
966 \or 7% 1
967 \or 6% 2
968 \or 5% 3
969 \or 4% 4
970 \or 3% 5
971 \or 2% 6
972 \or 1% 7
973 \or 0% 8
974 \or 9% 9
975 }
976 \InCa@Temp 9{%
977 \or 8% 1
    \or 7% 2
978
     \or 6% 3
979
980
     \or 5% 4
981
     \or 4% 5
982
     \or 3% 6
983
     \or 2% 7
     \or 1% 8
984
985
     \or 0% 9
986 }
2.5.6 Shl, Shr
987 \def\intcalcShl#1{%
988 \number\expandafter\InCa@ShlSwitch\number#1! %
989 }
990 \def\InCa@ShlSwitch#1#2!{%
991 \ifx#1-%
992
       -\csname InCa@Empty%
       \InCa@Sh1#2!%
993
```

\intcalcShl

\InCa@ShlSwitch

```
994
                             \else
                               \csname InCa@Empty%
                        995
                                \InCa@Shl#1#2!%
                        996
                        997
                        998 }
         \IntCalcShl
                        999 \def\IntCalcShl#1!{%
                       1000 \number
                              \csname InCa@Empty%
                             \InCa@Shl#1! %
                       1002
                       1003 }
   \IntCal@ShlDigit
                       1004 \left\lceil \ln Ca@Shl#1#2 \right\rceil
                       1005 \ifx#2!%
                       1006
                                \csname InCa@ShlDigit#1\endcsname0%
                       1007
                              \else
                                \csname InCa@ShlDigit#1%
                       1008
                       1009
                                \@ReturnAfterFi{%
                                  \InCa@Sh1#2%
                       1010
                                }%
                       1011
                       1012 \fi
                       1013 }
    \InCa@ShlDigit0
                       1014 \expandafter\def\csname InCa@ShlDigit0\endcsname{\%}
                       1015 \endcsname0%
                       1016 }
\InCa@ShlDigit[1-9]
                       1017 \ensuremath{\mbox{lnCa@Temp#1#2#3#4#5{\mathcal{\mathcal{\mathcal{\mathcal{\model}}}}}
                             \expandafter\def\csname InCa@ShlDigit#1\endcsname##1{%
                                \expandafter\endcsname
                       1019
                                \ifcase##1 %
                       1020
                                  #2#3%
                       1021
                                \else
                       1022
                       1023
                                  #4#5%
                       1024
                                \fi
                       1025 }%
                       1026 }
                       1027 \InCa@Temp 10203
                       1028 \InCa@Temp 20405
                       1029 \InCa@Temp 30607
                       1030 \InCa@Temp 40809
                       1031 \InCa@Temp 51011
                       1032 \InCa@Temp 61213
                       1033 \InCa@Temp 71415
                       1034 \InCa@Temp 81617
                       1035 \InCa@Temp 91819
        \intcalcShr
                       1036 \def\intcalcShr#1{%
                             \number\expandafter\InCa@ShrSwitch\number#1! %
                       1037
                       1038 }
    \InCa@ShrSwitch
                       1039 \def\InCa@ShrSwitch#1#2!{%
                       1040 \ifx#1-%
                       1041
                                -\InCa@Shr#2!%
                       1042
                             \else
                       1043
                                \InCa@Shr#1#2!%
```

```
1044 \fi
                                                                        1045 }
\IntCalcShr
                                                                       1046 \def\IntCalcShr#1!{%
                                                                       1047 \number\InCa@Shr#1! %
                                                                       1048 }
         \InCa@Shr
                                                                       1049 \ensuremath{\mbox{lnCa@Shr}\#1\#2\{\%\ensuremath{\mbox{\mbox{\mbox{$\sim$}}}}\xspace 1049 \ensuremath{\mbox{\mbox{$\sim$}}}\xspace 1049 \ensuremath{\mbox{\mbox{$\sim$}}}\xspace 1049 \ensuremath{\mbox{$\sim$}}\xspace 104
                                                                       1050 \InCa@ShrDigit#1!%
                                                                       1051
                                                                                                  \ifx#2!%
                                                                       1052 \else
                                                                       1053
                                                                                                                   \@ReturnAfterFi{%
                                                                       1054
                                                                                                                             \ifodd#1 %
                                                                       1055
                                                                                                                                         \@ReturnAfterElseFi{%
                                                                       1056
                                                                                                                                                   \InCa@Shr{1#2}%
                                                                                                                                         }%
                                                                       1057
                                                                       1058
                                                                                                                              \else
                                                                                                                                         \expandafter\InCa@Shr\expandafter#2%
                                                                       1059
                                                                       1060
                                                                                                                              \fi
                                                                                                                  }%
                                                                       1061
                                                                                                    \fi
                                                                       1062
                                                                       1063 }
                                                                       1064 \ensuremath{\mbox{\sc loss}} 1064 \ensuremath{\mbox{\sc loss}} 11064 \ensuremat
                                                                       1065 \ifcase#1 0% 0
                                                                       1066
                                                                                                        \or 0% 1
                                                                                                        \or 1% 2
                                                                       1067
                                                                       1068
                                                                                                        \or 1% 3
                                                                       1069
                                                                                                        \or 2% 4
                                                                       1070
                                                                                                        \or 2% 5
                                                                                                        \or 3% 6
                                                                       1071
                                                                                                    \or 3% 7
                                                                       1072
                                                                       1073 \or 4% 8
                                                                       1074 \or 4% 9
                                                                       1075 \or 5% 10
                                                                       1076 \or 5% 11
                                                                       1077 \or 6% 12
                                                                       1078 \or 6% 13
                                                                       1079 \or 7% 14
                                                                       1080 \or 7% 15
                                                                       1081 \or 8% 16
                                                                       1082 \or 8% 17
                                                                       1083 \or 9% 18
                                                                       1084 \or 9% 19
                                                                       1085
                                                                                                       \fi
                                                                       1086 }
                                                                       2.5.7 \ \InCa@Tim
          \InCa@Tim Macro \InCa@Tim implements "Number times digit".
                                                                       1087 \def\InCa@Temp#1{%
                                                                       1088
                                                                                                      \def\InCa@Tim##1##2{%
                                                                       1089
                                                                                                                   \number
                                                                                                                              \ifcase##2 % 0
                                                                       1090
                                                                       1091
                                                                                                                                        0%
                                                                                                                             \or % 1
                                                                       1092
                                                                                                                                         ##1%
                                                                       1093
                                                                                                                              \else % 2-9
                                                                       1094
                                                                       1095
                                                                                                                                        \csname InCa@Empty%
                                                                                                                                         \InCa@ProcessTim##2##1!%
                                                                       1096
```

```
1097
                                \fi
                      1098
                              #1%
                      1099
                           }%
                      1100 }
                      1101 \InCa@Temp{ }
   \InCa@ProcessTim
                      1102 \def\InCa@ProcessTim#1#2#3{%
                      1103 \ifx#3!%
                      1104
                              \csname InCa@TimDigit#2\endcsname#10%
                      1105
                            \else
                      1106
                              \csname InCa@TimDigit#2\csname InCa@Param#1%
                      1107
                              \@ReturnAfterFi{%
                      1108
                                \InCa@ProcessTim#1#3%
                              }%
                      1109
                      1110 \fi
                      1111 }
   \InCa@Param[0-9]
                      1112 \def\InCa@Temp#1{%}
                      1113 \expandafter\def\csname InCa@Param#1\endcsname{%
                      1114
                              \endcsname#1%
                      1115
                            }%
                      1116 }
                      1117 \InCa@Temp 0%
                      1118 \InCa@Temp 1%
                      1119 \InCa@Temp 2%
                      1120 \InCa@Temp 3%
                      1121 \InCa@Temp 4%
                      1122 \InCa@Temp 5%
                      1123 \InCa@Temp 6\%
                      1124 \InCa@Temp 7%
                      1125 \InCa@Temp 8%
                      1126 \InCa@Temp 9%
    \InCa@TimDigitO
                      1127 \expandafter\def\csname InCa@TimDigitO\endcsname#1#2{%
                           \endcsname
                      1129
                            0#2%
                      1130 }
    \InCa@TimDigit1
                      1131 \expandafter\def\csname InCa@TimDigit1\endcsname#1#2{%
                            \ifcase#2 %
                      1133
                              \endcsname 0#1%
                      1134
                            \else
                              \csname InCa@AddDigit#1\endcsname #2%
                      1135
                      1136
                           \fi
                      1137 }
\InCa@TimDigit[2-9]
                      1138 \def\InCa@Temp#1#2{%
                            \expandafter\def\csname InCa@TimDigit#1\endcsname##1{%
                      1140
                              \expandafter\InCa@TimDigitCarry
                      1141
                              \number
                                \ifcase##1 0% 0
                      1142
                                #2%
                      1143
                                \fi
                      1144
                      1145
                              ! %
                      1146
                           }%
                      1147 }
                      1148 \InCa@Temp 2{%
```

```
1149 \or 2% 1
1150 \or 4% 2
1151 \or 6% 3
1152 \or 8% 4
     \or 10% 5
1153
1154 \or 12% 6
1155 \or 14% 7
1156 \or 16% 8
1157 \or 18% 9
1158 }
1159 \InCa@Temp 3{%
     \or 3% 1
1160
1161
     \or 6% 2
1162 \or 9% 3
1163 \or 12% 4
1164 \or 15% 5
1165 \or 18% 6
1166 \or 21% 7
1167 \or 24% 8
1168 \or 27% 9
1169 }
1170 \InCa@Temp 4{%
     \or 4% 1
\or 8% 2
1171
1172
     \or 12% 3
1173
1174 \or 16% 4
1175 \or 20% 5
1176 \or 24% 6
1177 \or 28% 7
1178 \or 32% 8
1179 \or 36% 9
1180 }
1181 \InCa@Temp 5{%
1182 \or 5% 1
     \or 10% 2
1183
1184 \or 15% 3
1185 \or 20% 4
1186 \or 25% 5
1187 \or 30% 6
1188 \or 35% 7
1189 \or 40% 8
      \or 45% 9
1190
1191 }
1192 \InCa@Temp 6{%
1193 \or 6% 1
1194
      \or 12% 2
     \or 18% 3
1195
1196 \or 24% 4
1197 \or 30% 5
1198 \or 36% 6
1199 \or 42% 7
1200 \or 48% 8
1201 \or 54% 9
1202 }
1203 \InCa@Temp 7{%
1204 \or 7% 1
1205
     \or 14% 2
1206 \or 21% 3
1207 \or 28% 4
1208 \or 35% 5
1209 \or 42% 6
1210 \or 49% 7
```

```
\or 56% 8
                                                                       1211
                                                                       1212 \or 63% 9
                                                                       1213 }
                                                                       1214 \InCa@Temp 8{%
                                                                       1215 \or 8% 1
                                                                                       \or 16% 2
                                                                      1216
                                                                       1217 \or 24% 3
                                                                       1218 \or 32% 4
                                                                      1219 \or 40% 5
                                                                      1220 \or 48% 6
                                                                      1221 \or 56% 7
                                                                      1222 \or 64% 8
                                                                      1223 \or 72% 9
                                                                      1224 }
                                                                      1225 \InCa@Temp 9{%
                                                                      1226 \or 9% 1
                                                                      1227 \or 18% 2
                                                                      1228 \or 27% 3
                                                                      1229 \or 36% 4
                                                                       1230 \or 45% 5
                                                                                     \or 54% 6
                                                                       1231
                                                                       1232
                                                                                        \or 63% 7
                                                                       1233
                                                                                        \or 72% 8
                                                                       1234 \or 81% 9
                                                                       1235 }
   \InCa@TimDigitCarry
                                                                       1236 \ensuremath{\mbox{\mbox{$1$}}\mbox{$2$}} 1236 \ensuremath{\mbox{\mbox{$1$}}\mbox{$2$}} 1236 \ensuremath{\mbox{\mbox{$1$}}\mbox{$2$}} 1236 \ensuremath{\mbox{\mbox{$1$}}\mbox{$2$}} 1236 \ensuremath{\mbox{$1$}}\mbox{$2$} 1236 \ensuremath{\mbox{$1$}}\mbox{$2$} 1236 \ensuremath{\mbox{$1$}}\mbox{$2$} 1236 \ensuremath{\mbox{$1$}}\mbox{$2$} 1236 \ensuremath{\mbox{$1$}}\mbox{$2$} 1236 \ensuremath{\mbox{$1$}}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$2$}\mbox{$
                                                                       1237 \ifnum#1<10 %
                                                                                               \csname InCa@AddDigit#1\expandafter\endcsname
                                                                       1238
                                                                       1239
                                                                                         \else
                                                                       1240
                                                                                               \@ReturnAfterFi{%
                                                                       1241
                                                                                                      \InCa@@TimDigitCarry#1!%
                                                                                           }%
                                                                       1242
                                                                      1243 \fi
                                                                       1244 }
\InCa@@TimDigitCarry
                                                                       1245 \def\InCa@@TimDigitCarry#1#2!#3{%
                                                                       1246 \csname InCa@DigitCarry#1%
                                                                                         \csname InCa@AddDigit#2\endcsname #3%
                                                                      1247
                                                                       1248 }
                                                                       2.5.8 Mul
                             \intcalcMul
                                                                       1249 \def\intcalcMul#1#2{%
                                                                       1250 \number
                                                                       1251
                                                                                                \expandafter\InCa@MulSwitch
                                                                                                \number\number#1\expandafter!%
                                                                       1252
                                                                       1253
                                                                                                \number#2! %
                                                                       1254 }
                \InCa@MulSwitch Decision table for \InCa@MulSwitch.
```

32

x < 0	y < 0	x < y	+	Mul(-x, -y)
		else		Mul(-y, -x)
	else	-x > y	_	Mul(-x,y)
		else		Mul(y, -x)
else	y < 0	x > -y	_	Mul(x, -y)
		else		Mul(-y,x)
	else	x > y	+	Mul(x, y)
		else		Mul(y, x)

```
1255 \ensuremath{\mbox{\sc local}}\ensuremath{\mbox{\sc local}}\ensurema
1256
                  \int \frac{1}{z} dx
                            \lim 2<\z0
1257
                                  \ifnum#1<#2 %
1258
                                          \verb|\expandafter\InCa@Mul\number-#1\expandafter!%| \\
1259
                                          \@gobble#2!%
1260
1261
                                   \else
1262
                                          \verb|\expandafter\InCa@Mul\number-#2\expandafter!||%
1263
                                          \@gobble#1!%
1264
                                  \fi
1265
                            \else
1266
                                  -%
1267
                                   \ifnum-#1>#2 %
1268
                                          \expandafter\InCa@Mul\@gobble#1!#2!%
1269
                                          \expandafter\InCa@Mul\number#2\expandafter!%
1270
                                          \@gobble#1!%
1271
1272
                                  \fi
                            \fi
1273
1274
                     \else
1275
                           \lim 2<\z0
1276
                                  -%
                                   \ifnum#1>-#2 %
1277
                                          \expandafter\InCa@Mul\number#1\expandafter!%
1278
                                          \@gobble#2!%
1279
                                  \else
1280
                                          \expandafter\InCa@Mul\@gobble#2!#1!%
1281
                                  \fi
1282
1283
                            \else
                                  \ifnum#1>#2 %
1284
1285
                                         \InCa@Mul#1!#2!%
1286
1287
                                          \InCa@Mul#2!#1!%
1288
                                  \fi
                           \fi
1289
1290
                   \fi
1291 }
1292 \def\IntCalcMul#1!#2!{%
                   \number\InCa@Mul#1!#2! %
1294 }
1295 \def\InCa@Mul#1!#2!{%
                    \ifcase#2 %
1296
1297
                           0%
1298
1299
                            #1%
1300
                           \csname InCa@Empty%
1301
                           \expandafter\InCa@Shl#1!%
1302
```

\IntCalcMul

\InCa@Mul

```
1303
                                                          \else
                                                                 \ifnum#2<10 %
                                        1304
                                                                       \InCa@Tim{#1}#2%
                                        1305
                                        1306
                                         1307
                                                                       \InCa@ProcessMul!#2!#1!%
                                        1308
                                                                 \fi
                                        1309
                                                           \fi
                                        1310 }
     \InCa@Mul
                                        1311 \def\InCa@ProcessMul#1!#2#3!#4!{%
                                                         \ifx\InCa@Empty#3\InCa@Empty
                                        1313
                                                                 \expandafter\InCa@Add\number
                                                                  #10\expandafter\expandafter\expandafter!%
                                        1314
                                                                 \label{localim} $$\prod_{a\in\mathbb{Z}_{+}^{2}}\
                                        1315
                                                          \else
                                        1316
                                                                 \ifx\InCa@Empty#1\InCa@Empty
                                        1317
                                                                       \verb|\expandafter| expandafter \\| In Ca@Process \\| Mullipse \\| Mull
                                        1318
                                        1319
                                                                       \InCa@Tim{#4}#2!%
                                                                       #3!#4!%
                                        1320
                                        1321
                                                                 \else
                                        1322
                                                                        \expandafter\InCa@ProcessMul\number
                                        1323
                                                                        \expandafter\InCa@Add\number%
                                        1324
                                                                       #10\expandafter\expandafter!%
                                        1325
                                                                       \InCa@Tim{#4}#2!!%
                                                                       #3!#4!%
                                        1326
                                        1327
                                                                 \fi
                                        1328
                                                          \fi
                                        1329 }
                                        2.5.9 Sqr, Fac
\intcalcSqr
                                        1330 \def\intcalcSqr#1{%
                                                          \number\expandafter\InCa@Sqr\number#1! %
                                        1332 }
     \InCa@Sqr
                                        1333 \def\InCa@Sqr#1#2!{%
                                                       \ifx#1-%
                                        1334
                                                                 \InCa@Mul#2!#2!%
                                        1335
                                        1336
                                                           \else
                                        1337
                                                                 \InCa@Mul#1#2!#1#2!%
                                        1338
                                                        \fi
                                        1339 }
\intcalcFac
                                        1340 \def\intcalcFac#1{%
                                                          \number\expandafter\InCa@Fac\number#1! %
                                        1342 }
                                        2.5.10 Pow
\intcalcPow
                                        1343 \def\intcalcPow#1#2{%
                                                        \number\expandafter\InCa@Pow
                                        1344
                                                          \number\number#1\expandafter!%
                                        1345
                                        1346 \number#2! %
                                        1347 }
      \InCa@Pow
```

```
1348 \def\InCa@Pow#1#2!#3#4!{%
              1349
                    \left( \frac{3}{4} \right) = 0
              1350
                      1%
              1351
                    1352
                      #1#2%
              1353
                    1354
                      \ifx#1-%
                        \InCa@Mul#2!#2!%
              1355
              1356
                       \else
                        \InCa@Mul#1#2!#1#2!%
              1357
                      \fi
              1358
              1359
                    \else
                      \footnote{1} \iftit if case #1#2 % basis = 0, power <> 0
              1360
              1361
              1362
                         \int x#3-\% power < 0
                          0\IntCalcError:DivisionByZero%
              1363
                        \fi
              1364
              1365
                      \or
              1366
                        1% basis = 1
                      \else
              1367
                         1368
                           \ifodd#3#4 %
              1369
                             -%
              1370
                           \fi
              1371
              1372
                          1%
                         \else % |basis| > 1
              1373
                          ifx#3-% power < 0
              1374
                             0%
              1375
                           \else % power > 2
              1376
                             1377
                               \ifodd#3#4 %
              1378
              1379
                                 -%
                               \fi
              1380
                               \InCa@PowRec#2!#3#4!1!%
              1381
              1382
              1383
                               \InCa@PowRec#1#2!#3#4!1!%
              1384
                             \fi
                           \fi
              1385
              1386
                        \fi
                       \fi
              1387
              1388
                    \fi
              1389 }
\InCa@PowRec
                    Pow(b, p) {
                      PowRec(b, p, 1)
                    PowRec(b, p, r) {
                      if p == 1 then
                        return r
                      else
                        ifodd p then
                          return PowRec(b*b, p div 2, r*b) % p div 2 = (p-1)/2
                        else
                          return PowRec(b*b, p div 2, r)
                        fi
                     fi
                   }
              1390 \ensuremath{\mbox{\sc #1!#2!#3!}} \%
              1391
                    \lim 2=\0
                       \ifnum#1>#3 %
              1392
                         \InCa@Mul#1!#3!%
              1393
              1394
                       \else
              1395
                         \InCa@Mul#3!#1!%
```

```
\fi
               1396
               1397
                      \else
                         \expandafter\InCa@PowRec
               1398
               1399
                         \number\InCa@Mul#1!#1!\expandafter!%
               1400
                         \number\intcalcShr{#2}\expandafter!%
               1401
                         \number
               1402
                         \ifodd#2 %
                           \ifnum#1>#3 %
               1403
                             \InCa@Mul#1!#3!%
               1404
                           \else
               1405
                             \InCa@Mul#3!#1!%
               1406
                           \fi
               1407
                         \else
               1408
               1409
                           #3%
               1410
                         \fi
                         \expandafter!%
               1411
               1412
               1413 }
               2.5.11 Div
\intcalcDiv
               1414 \ensuremath{\mbox{\mbox{$1$}}}414 \ensuremath{\mbox{$4$}} 142 \ensuremath{\mbox{$1$}}
                      \number\expandafter\InCa@Div
                      \number\number#1\expandafter!%
               1416
                      \number#2! %
               1418 }
  \InCa@Div
               1419 \def\InCa@Div#1!#2!{%
                     \ifcase#2 %
               1420
                        0\IntCalcError:DivisionByZero%
               1421
               1422
                      \else
               1423
                         \ifcase#1 %
               1424
                           0%
               1425
                         \else
               1426
                           \expandafter\InCa@DivSwitch
               1427
                           \number#1\expandafter!%
                           \number#2!%
               1428
                         \fi
               1429
               1430
                      \fi
               1431 }
\IntCalcDiv
               1432 \ensuremath{\mbox{lnCa@Temp#1}{\mbox{\%}}}
                      \def\IntCalcDiv##1!##2!{%
               1433
               1434
                         \number
                         \ifcase##2 %
               1435
                           0\IntCalcError:DivisionByZero%
               1436
                         \else
               1437
                           \ifcase##1 %
               1438
               1439
                             0%
               1440
                           \else
               1441
                             \InCa@@Div##1!##2!%
               1442
                           \fi
                         \fi
               1443
                         #1%
               1444
               1445
                      }%
               1446 }
               1447 \InCa@Temp{ }%
```

\InCa@DivSwitch Decision table for \InCa@DivSwitch.

x < 0	y < 0	+	$\mathrm{Div}(-x,-y)$
	else	_	$\operatorname{Div}(-x,y)$
else	y < 0	_	$\operatorname{Div}(x, -y)$
	else	+	$\mathrm{Div}(x,y)$

```
1448 \ensuremath{\mbox{\mbox{lnCa@DivSwitch#1!#2!}{\%}}
                 1449
                       \ifnum#1<\z0
                         \lim 2<\z0
                 1450
                            \expandafter\InCa@@Div\number-#1\expandafter!%
                 1451
                 1452
                            \@gobble#2!%
                          \else
                 1453
                 1454
                            -%
                            \expandafter\InCa@@Div\@gobble#1!#2!%
                 1455
                 1456
                          \fi
                 1457
                        \else
                         \lim 2<\z0
                 1458
                            -%
                 1459
                            \expandafter\InCa@@Div\number#1\expandafter!%
                 1460
                            \@gobble#2!%
                 1461
                 1462
                            \InCa@@Div#1!#2!%
                 1463
                 1464
                          \fi
                 1465
                       \fi
                 1466 }
    \InCa@@Div
                 1467 \def\InCa@@Div#1!#2!{%
                       \ifnum#1>#2 %
                         \ifcase#2 % 0 already catched
                 1469
                            \IntCalcError:ThisCannotHappen%
                 1470 ?
                 1471
                         \or % 1
                 1472
                           #1%
                         \or % 2
                 1473
                           \InCa@Shr#1!%
                 1474
                 1475
                         \else
                 1476
                           \InCa@DivStart!#1!#2!#2!%
                 1477
                         \fi
                 1478
                       \else
                         \ifnum#1=#2 %
                 1479
                 1480
                            1%
                          \else
                 1481
                            0%
                 1482
                          \fi
                 1483
                       \fi
                 1484
                 1485 }
\InCa@DivStart
                 1486 \def\InCa@DivStart#1!#2#3!#4#5{%
                       \ifx#5!%
                 1487
                          \@ReturnAfterElseFi{%
                 1488
                 1489
                            \InCa@DivStartI{#1#2}#3=!%
                 1490
                         }%
                 1491
                 1492
                          \@ReturnAfterFi{%
                            \InCa@DivStart{#1#2}!#3!#5%
                 1493
                         }%
                 1494
                 1495
                       \fi
                 1496 }
  \InCa@StartI
                 1497 \def\InCa@DivStartI#1!#2!{%
                 1498 \expandafter\InCa@DivStartII
```

```
\number#2\expandafter\expandafter\expandafter!%
                   1499
                         \intcalcShl{#2}!%
                   1500
                   1501
                   1502 }
   \InCa@StartII
                   1503 \def\InCa@DivStartII#1!#2!{%
                   1504
                         \expandafter\InCa@DivStartIII
                   1505
                         \number#1\expandafter!%
                   1506
                         \number#2\expandafter\expandafter\expandafter!%
                   1507
                         \intcalcShl{#2}!%
                   1508 }
  \InCa@StartIII
                   1509 \def\InCa@DivStartIII#1!#2!#3!{%
                   1510
                         \expandafter\InCa@DivStartIV
                   1511
                         \number#1\expandafter!%
                   1512
                         \number#2\expandafter!%
                         \number#3\expandafter!%
                         \number\InCa@Add#3!#2!\expandafter\expandafter\expandafter!%
                   1514
                   1515
                         \intcalcShl{#3}!%
                   1516 }
   \InCa@StartIV
                   1517 \def\InCa@DivStartIV#1!#2!#3!#4!#5!#6!{%
                   1518 \InCa@ProcessDiv#6!#1!#2!#3!#4!#5!/%
                   1519 }
\InCa@ProcessDiv
                   1520 \def\InCa@ProcessDiv#1#2#3!#4!#5!#6!#7!#8!#9/{%
                   1521
                         #9%
                   1522
                         \ifnum#1<#4 % 0
                   1523
                           0%
                   1524
                           \ifx#2=%
                   1525
                           \else
                   1526
                             \InCa@ProcessDiv{#1#2}#3!#4!#5!#6!#7!#8!%
                           \fi
                   1527
                         \else % 1-9
                   1528
                           \ifnum#1<#5 % 1
                   1529
                             1%
                   1530
                             \ifx#2=%
                   1531
                   1532
                             \else
                                \expandafter\InCa@ProcessDiv\expandafter{%
                   1533
                                  \number\InCa@Sub#1!#4!%
                   1534
                   1535
                   1536
                               }#3!#4!#5!#6!#7!#8!%
                   1537
                             \fi
                   1538
                           \else % 2-9
                             \footnote{1<\#7 \% 2 3 4 5}
                   1539
                               \ifnum#1<#6 % 2 3
                   1540
                                  \@ReturnAfterElseFi{%
                   1541
                                    \expandafter\InCa@@ProcessDiv
                   1542
                                    \number\InCa@Sub#1!#5!!%
                   1543
                                    23%
                   1544
                                 }%
                   1545
                               \else % 4 5
                   1546
                   1547
                                  \@ReturnAfterFi{%
                                    \expandafter\InCa@@ProcessDiv
                   1548
                                    \number\InCa@Sub#1!#6!!%
                   1549
                                    45%
                   1550
                                 }%
                   1551
                               \fi
                   1552
```

```
#2#3!#4!#5!#6!#7!#8!%
                    1553
                    1554
                               \else % 6 7 8 9
                                 \ifnum#1<#8 % 6 7
                    1555
                    1556
                                   \@ReturnAfterElseFi{%
                    1557
                                      \expandafter\InCa@@ProcessDiv
                    1558
                                      \number\InCa@Sub#1!#7!!%
                    1559
                                     67%
                                   }%
                    1560
                                 \else % 8 9
                    1561
                                   \@ReturnAfterFi{%
                    1562
                                     \expandafter\InCa@@ProcessDiv
                    1563
                                     \number\InCa@Sub#1!#8!!%
                    1564
                    1565
                    1566
                                   }%
                    1567
                                 \fi
                                 #2#3!#4!#5!#6!#7!#8!%
                    1568
                    1569
                               \fi
                             \fi
                    1570
                           \fi
                    1571
                          \ifx#2=%
                    1572
                             \expandafter\@gobble
                    1573
                          \fi
                    1574
                    1575
                          /%
                    1576 }
\InCa@@ProcessDiv
                    1577 \def\InCa@@ProcessDiv#1!#2#3#4#5!#6!{%
                          \ifnum#1<#6 %
                    1578
                    1579
                             \@ReturnAfterElseFi{%
                    1580
                               \ifx#4=%
                    1581
                    1582
                                 \expandafter\InCa@CleanupIV
                    1583
                               \else
                                 \@ReturnAfterFi{%
                    1584
                                   \InCa@ProcessDiv{#1#4}#5!#6!%
                    1585
                                 }%
                    1586
                    1587
                               \fi
                             }%
                    1588
                    1589
                          \else
                             #3%
                    1590
                             \@ReturnAfterFi{%
                    1591
                    1592
                               \ifx#4=%
                                 \expandafter\InCa@CleanupIV
                    1593
                    1594
                               \else
                                 \@ReturnAfterFi{%
                    1595
                                   \expandafter\InCa@ProcessDiv\expandafter{%
                    1596
                                      \number\InCa@Sub#1!#6! %
                    1597
                                     #4%
                    1598
                                   }#5!#6!%
                    1599
                    1600
                                 }%
                               \fi
                    1601
                             }%
                    1602
                    1603
                          \fi
                    1604 }
  \InCa@CleanupIV
                    1605 \def\InCa@CleanupIV#1!#2!#3!#4!{}
                    2.5.12 Mod
      \intcalcMod
```

1606 \def\intcalcMod#1#2{%

```
\number\expandafter\InCa@Mod
               1607
                      \number\number#1\expandafter!%
               1608
                      \number#2! %
               1609
               1610 }
\intcalc@Mod Pseudocode/decision table for \intcalc@Mod.
                            y = 0
                                    DivisionByZero
                     elsif
                           y < 0
                                    -\operatorname{Mod}(-x, -y)
                     elsif
                           x = 0
                                    0
                     elsif
                           y = 1
                     elsif
                           y = 2 ifodd(x) ? 1 : 0
                                   z \leftarrow x - (x/y) * y; \quad (z < 0) ? z + y : z
                     elsif
                           x < 0
                     else
                                    x - (x/y) * y
               1611 \def\InCa@Mod#1!#2!{%
                      \ifcase#2 %
               1612
               1613
                        0\IntCalcError:DivisionByZero%
               1614
                      \else
               1615
                        \int \frac{1}{z} dz
                          -%
               1616
               1617
                           \expandafter\InCa@Mod
                          \verb|\number-#1| expandafter!%|
               1618
                          \number-#2!%
               1619
                        \else
               1620
                          \ifcase#1 %
               1621
               1622
                            0%
               1623
                          \else
                             \ifcase#2 % 0 already catched
               1624
                               \IntCalcError:ThisCannotHappen%
               1625 ?
               1626
                            \or % 1
               1627
                              0%
               1628
                             \or % 2
                              \ifodd#1 1\else 0\fi
               1629
                            \else
               1630
                               \int 1 < x^2 
               1631
                                 \expandafter\InCa@ModShift
               1632
               1633
                                 \number-%
               1634
                                   \expandafter\InCa@Sub
               1635
                                   \number\@gobble#1\expandafter!%
               1636
                                   \number\intcalcMul{#2}{%
               1637
                                     \expandafter\InCa@Div\@gobble#1!#2!%
               1638
                                   }!%
                                 !#2!%
               1639
               1640
                                 \expandafter\InCa@Sub\number#1\expandafter!%
               1641
                                 \number\intcalcMul{#2}{\InCa@Div#1!#2!}!%
               1642
                               \fi
               1643
                             \fi
               1644
                          \fi
               1645
               1646
                        \fi
               1647
                      \fi
               1648 }
 \IntCalcMod
               1649 \def\InCa@Temp#1{%
               1650
                      \def\IntCalcMod##1!##2!{%
               1651
                        \number
                        \ifcase##2 %
               1652
                          0\IntCalcError:DivisionByZero%
               1653
               1654
                        \else
                          \ifcase##1 %
               1655
```

```
0%
                                                                                                          1656
                                                                                                                                                             \else
                                                                                                          1657
                                                                                                                                                                       \ifcase##2 % 0 already catched
                                                                                                          1658
                                                                                                                                                                                \IntCalcError:ThisCannotHappen
                                                                                                          1659 ?
                                                                                                          1660
                                                                                                                                                                      \or % 1
                                                                                                          1661
                                                                                                                                                                               0%
                                                                                                          1662
                                                                                                                                                                      \or % 2
                                                                                                          1663
                                                                                                                                                                                \ifodd ##1 1\else 0\fi
                                                                                                          1664
                                                                                                                                                                       \else
                                                                                                                                                                                  \expandafter\InCa@Sub\number##1\expandafter!%
                                                                                                          1665
                                                                                                                                                                                  \label{localcond} $$\operatorname{InCa@Div}$#1!$#2!}!%
                                                                                                          1666
                                                                                                          1667
                                                                                                                                                                       \fi
                                                                                                                                                            \fi
                                                                                                          1668
                                                                                                          1669
                                                                                                                                                   \fi
                                                                                                          1670
                                                                                                                                                   #1%
                                                                                                          1671
                                                                                                                                      }%
                                                                                                          1672 }
                                                                                                          \InCa@ModShift
                                                                                                          1674 \ensuremath{\mbox{\sc 1}674} \ensurema
                                                                                                                                      1676
                                                                                                                                                   \expandafter\InCa@Sub\number#2\expandafter!%
                                                                                                          1677
                                                                                                                                                   \@gobble#1!%
                                                                                                          1678
                                                                                                                                        \else
                                                                                                          1679
                                                                                                                                                  #1%
                                                                                                          1680
                                                                                                                                      \fi
                                                                                                          1681 }
                                                                                                          2.5.13 Help macros
                                       \InCa@Empty
                                                                                                          1682 \def\InCa@Empty{}
                                                        \@gobble
                                                                                                          1683 \verb|\expandafter\ifx\csname @gobble\endcsname\relax|
                                                                                                          1684 \qquad \verb|\long\def\@gobble#1{}|%
                                                                                                          1685 \fi
                   \@ReturnAfterFi
                                                                                                           1686 \long\def\@ReturnAfterFi#1\fi{\fi#1}%
\@ReturnAfterElseFi
                                                                                                          1687 \end{center} $1687 \end{center} IeseFi#1\else#2\fi{fi#1}% $1687 \end{center} $1687
                                                                                                          1688 \InCa@AtEnd%
                                                                                                          1689 (/package)
                                                                                                          3
                                                                                                                                  Test
                                                                                                                                        Catcode checks for loading
                                                                                                          3.1
                                                                                                          1690 (*test1)
                                                                                                          1691 \catcode`\{=1 %
                                                                                                           1692 \catcode \}=2 %
                                                                                                          1693 \catcode \#=6 %
                                                                                                          1694 \catcode \@=11 %
                                                                                                          1695 \expandafter\ifx\csname count@\endcsname\relax
                                                                                                          1696 \countdef\count@=255 %
```

1697 \fi

```
1698 \expandafter\ifx\csname @gobble\endcsname\relax
      \label{longdef_Qgobble#1} $$ \oddef_Qgobble#1{}%
1700 \fi
1701 \expandafter\ifx\csname @firstofone\endcsname\relax
      \long\def\@firstofone#1{#1}%
1703 \fi
1704 \verb|\expandafter\ifx\csname loop\endcsname\relax|
      \expandafter\@firstofone
1706 \ensuremath{\setminus} \texttt{else}
     \expandafter\@gobble
1707
1708\fi
1709 {%
      \def\loop#1\repeat{%
1710
         \left( \frac{1}{x} \right)
1711
         \iterate
1712
1713
     }%
      \def\iterate{%
1714
        \body
1715
           \let\next\iterate
1716
1717
         \else
           \let\next\relax
1718
         \fi
1719
1720
         \next
      }%
1721
      \let\repeat=\fi
1722
1723 }%
1724 \def\RestoreCatcodes{}
1725 \count@=0 %
1726 \loop
      \edef\RestoreCatcodes{%
1727
         \RestoreCatcodes
1728
1729
         \catcode\the\count@=\the\catcode\count@\relax
1730
     }%
1731 \ifnum\count@<255 %
1732 \advance\count@ 1 %
1733 \repeat
1734
1735 \def\RangeCatcodeInvalid#1#2{%
1736
      \count@=#1\relax
1737
      \loop
        \catcode\count@=15 %
1738
      \ifnum\count@<#2\relax
1739
        \advance\count@ 1 %
1740
1741
      \repeat
1742 }
1743 \def\RangeCatcodeCheck#1#2#3{%
      \count@=#1\relax
1745
      \loop
1746
        \ifnum#3=\catcode\count@
1747
         \else
           \errmessage{%
1748
1749
             Character \the\count@\space
             with wrong catcode \the\catcode\count@\space
1750
1751
             instead of \number#3%
          }%
1752
1753
1754
      \ifnum\count@<#2\relax
1755
         \advance\count@ 1 %
1756
      \repeat
1757 }
1758 \def\space{}
1759 \verb|\constant| LoadCommand\endcsname\relax|
```

```
\def\LoadCommand{\input intcalc.sty\relax}%
1760
1761 \fi
1762 \left\lceil \text{Test} \right\rceil
      \RangeCatcodeInvalid{0}{47}%
1763
      \RangeCatcodeInvalid{58}{64}%
1764
1765
      \RangeCatcodeInvalid{91}{96}%
      \RangeCatcodeInvalid{123}{255}%
1766
      \catcode`\@=12 %
1767
      \color= \color= 0 \%
1768
      \catcode`\%=14 %
1769
      \LoadCommand
1770
      \RangeCatcodeCheck{0}{36}{15}%
1771
      \RangeCatcodeCheck{37}{37}{14}%
1772
      \RangeCatcodeCheck{38}{47}{15}%
1773
      \RangeCatcodeCheck{48}{57}{12}%
1774
1775
      \RangeCatcodeCheck{58}{63}{15}%
1776
      \RangeCatcodeCheck{64}{64}{12}%
      \RangeCatcodeCheck{65}{90}{11}%
1777
      \RangeCatcodeCheck{91}{91}{15}%
1778
      1779
1780
      \RangeCatcodeCheck{93}{96}{15}%
      \RangeCatcodeCheck{97}{122}{11}%
1781
      \RangeCatcodeCheck{123}{255}{15}%
1782
      \RestoreCatcodes
1783
1784 }
1785 \Test
1786 \csname @@end\endcsname
1787 \end
1788 (/test1)
```

3.2 Macro tests

3.2.1 Preamble with test macro definitions

```
1789 (*test2 j test4)
1790 \NeedsTeXFormat{LaTeX2e}
1791 \nofiles
1792 \documentclass{article}
1793 \langle noetex \rangle \ | \ Let \ Saved Numexpr \ | \ numexpr
1794 \langle noetex \rangle \ let \ numexpr \ UNDEFINED
1795 \makeatletter
1796 \chardef\InCa@TestMode=1 %
1797 \makeatother
1798 \usepackage{intcalc}[2007/09/27]
1799 (noetex) \let\numexpr\SavedNumexpr
1800 \usepackage{qstest}
1801 \IncludeTests{*}
1802 \LogTests{log}{*}{*}
1803 \langle \text{/test2 j test4} \rangle
1804 (*test2)
1805 \newcommand*{\TestSpaceAtEnd}[1]{%
1806 (noetex) \let\SavedNumexpr\numexpr
1807 (noetex) \let\numexpr\UNDEFINED
1808 \edef\resultA{#1}%
1809 \ensuremath{\mbox{\mbox{\mbox{$\mbox{$}}}} 1809 \ensuremath{\mbox{\mbox{$\mbox{$}$}}} 1809
1810 (noetex) \let\numexpr\SavedNumexpr
1811
      \Expect*{\resultA\space}*{\resultB}%
1812 }
1813 \newcommand*{\TestResult}[2]{%
1814 (noetex) \let\SavedNumexpr\numexpr
1815 (noetex) \let\numexpr\UNDEFINED
1816 \edef\result{#1}%
1817 (noetex) \let\numexpr\SavedNumexpr
```

```
\Expect*{\result}{#2}%
1818
1819 }
1820 \newcommand*{\TestResultTwoExpansions}[2]{%
1821 (*noetex)
      \begingroup
1823
        \let\numexpr\UNDEFINED
1824
        \expandafter\expandafter\expandafter
1825
      \endgroup
1826 \langle /noetex \rangle
      \expandafter\expandafter\Expect
1827
      \expandafter\expandafter\expandafter{#1}{#2}%
1828
1829 }
1830 \newcount\TestCount
1831 \langle etex \rangle \newcommand*{\TestArg}[1]{\numexpr#1\relax}
1832 \langle noetex \rangle \setminus mewcommand * \{ \setminus TestArg \} [1] \{ \#1 \}
1833 \newcommand*{\TestTeXDivide}[2]{%
      \TestCount=\TestArg{#1}\relax
      \divide\TestCount by \TestArg{#2}\relax
1835
      1836
1837 }
1838 \newcommand*{\Test}[2]{%
      \TestResult{#1}{#2}%
1839
      \TestResultTwoExpansions{#1}{#2}%
1840
      \TestSpaceAtEnd{#1}%
1841
1842 }
1843 \mbox{newcommand}*{\mbox{TestExch}[2]{\mbox{#2}{#1}}}
1844 \newcommand*{\TestInv}[2]{%
1845
     Test{\left\{ intcalcInv{#1} \right\} {#2}}
1846 }
1847 \newcommand*{\TestNum}[2]{%
     \Test{\intcalcNum{#1}}{#2}%
1848
1849 }
1850 \newcommand*{\TestAbs}[2]{%
1851
      Test{\left(Abs{#1}\right){#2}}
1853 \newcommand*{\TestSgn}[2]{%
     \Test{\intcalcSgn{#1}}{#2}%
1855 }
1856 \newcommand*{\TestMin}[3]{%
      \Test{\intcalcMin{#1}{#2}}{#3}%
1857
1858 }
1859 \newcommand*{\TestMax}[3]{%
     \Test{\intcalcMax{#1}{#2}}{#3}%
1860
1861 }
1862 \newcommand*{\TestCmp}[3]{%
     \Test{\intcalcCmp{#1}{#2}}{#3}%
1864 }
1865 \newcommand*{\TestInc}[2]{%
1866
     \Test{\intcalcInc{#1}}{#2}%
1867
      \ifnum\intcalcNum{#1}>-1 %
        \edef\x{%
1868
          \noexpand\Test{%
1869
             \noexpand\IntCalcInc\intcalcNum{#1}!%
1870
1871
          }{#2}%
        }%
1872
1873
        \x
1874
     \fi
1876 \newcommand*{\TestDec}[2]{%
     \Test{\intcalcDec{#1}}{#2}%
1877
      \ifnum\intcalcNum{#1}>0 %
1878
1879
        \left( x_{x}\right)
```

```
\noexpand\Test{%}
1880
              \noexpand\IntCalcDec\intcalcNum{#1}!%
1881
           }{#2}%
1882
1883
1884
         /x
1885
       \fi
1886 }
1887 \newcommand*{\TestAdd}[3]{%
       \texttt{\Test{\intcalcAdd{\#1}{\#2}}{\#3}\%}
1888
       \ifnum\intcalcNum{#1}>0 %
1889
         \ifnum\intcalcNum{#2}> 0 %
1890
            \ifnum\intcalcCmp{#1}{#2}>0 %
1891
1892
              \left( x_{x}\right) 
                \noexpand\Test{%}
1893
                   \noexpand\IntCalcAdd
1894
1895
                   \intcalcNum{#1}!\intcalcNum{#2}!%
1896
                }{#3}%
              }%
1897
              /x
1898
1899
           \else
1900
              \left( x_{x}\right) 
                \noexpand\Test{%}
1901
                   \noexpand\IntCalcAdd
1902
                   \intcalcNum{#2}!\intcalcNum{#1}!%
1903
                }{#3}%
1904
1905
              }%
1906
              /x
           \fi
1907
         \fi
1908
       \fi
1909
1910 }
1911 \newcommand*{\TestSub}[3]{%
1912
       \texttt{Test{\intcalcSub{#1}{#2}}{#3}%
       \ifnum\intcalcNum{#1}>0 %
1913
1914
         \ifnum\intcalcNum{#2}> 0 %
1915
           \int Cmp{#1}{#2}>0 %
1916
              \left( x_{x}\right) 
                \verb|\noexpand\Test{%|}
1917
1918
                   \noexpand\IntCalcSub
                   \intcalcNum{#1}!\intcalcNum{#2}!%
1919
                }{#3}%
1920
              }%
1921
1922
              \x
1923
           \fi
1924
         \fi
1925
1926 }
1927 \newcommand*{\TestSh1}[2]{%
1928
       \texttt{\Test{\intcalcShl{#1}}{#2}}\%
1929
       \left( x_{x}\right) 
         \noexpand\Test{\%}
1930
           \label{lintCalcShl} $$\operatorname{LAbs}{\#1}!\%
1931
         }{\intcalcAbs{#2}}%
1932
1933
      }%
1934
       \x
1935 }
1936 \newcommand*{\TestShr}[2]{%
1937
       \texttt{\Test{\intcalcShr{#1}}{#2}}\%
1938
       \left( x_{x}\right) 
         \noexpand\Test{%}
1939
            \noexpand\IntCalcShr\intcalcAbs{#1}!%
1940
1941
         }{\intcalcAbs{#2}}%
```

```
1942
              }%
1943
               \x
1944 }
1945 \newcommand*{\TestMul}[3]{%
1946
               \Test{\intcalcMul{#1}{#2}}{#3}%
1947
               \left( x_{x}\right) 
1948
                     \noexpand\Test{%
1949
                         \noexpand\IntCalcMul\intcalcAbs{#1}!\intcalcAbs{#2}!%
                    }{\intcalcAbs{#3}}%
1950
              }%
1951
1952
               \x
1953 }
1954 \newcommand*{\TestSqr}[2]{%
               \Test{\intcalcSqr{#1}}{#2}%
1955
1956 }
1957 \newcommand*{\TestFac}[2]{%
               1958
1959 }
1960 \newcommand*{\TestPow}[3]{%
1961
              \Test{\intcalcPow{#1}{#2}}{#3}%
1962 }
1963 \newcommand*{\TestDiv}[3]{%
               \Test{\intcalcDiv{#1}{#2}}{#3}%
1964
                \TestTeXDivide{#1}{#2}%
1965
                \left( x_{x}\right) 
1966
1967
                     \noexpand\Test{%
                         \label{lintCalcDiv} $$\operatorname{LAbs}${#1}!\operatorname{LAbs}${#2}!% $$
1968
1969
                    }{\intcalcAbs{#3}}%
1970
              }%
1971 }
1972 \newcommand*{\TestMod}[3]{%
1973
               \Test{\intcalcMod{#1}{#2}}{#3}%
1974
               \ifcase\ifcase\intcalcSgn{#1} 0%
1975
                                 \or
1976
                                      \ifcase\intcalcSgn{#2} 1%
1977
                                      \or 0%
1978
                                      \else 1%
1979
                                      \fi
1980
                                 \else
                                      \ifcase\intcalcSgn{#2} 1%
1981
                                      \or 1%
1982
                                      \else 0%
1983
                                      \fi
1984
1985
                                 \fi\relax
1986
                    \left( x_{x}\right) 
1987
                         \noexpand\Test{%
1988
                               \noexpand\IntCalcMod
1989
                               \intcalcAbs{#1}!\intcalcAbs{#2}!%
1990
                         }{\intcalcAbs{#3}}%
1991
                    }%
1992
                     \x
1993
               \fi
1994 }
1995 (/test2)
3.2.2 Time
1996 (*test2)
1997 \verb|\begingroup\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandaft
1998 \expandafter\ifx\csname pdfresettimer\endcsname\relax
1999 \else
               \makeatletter
2000
2001
               \newcount\SummaryTime
               \newcount\TestTime
2002
```

```
\SummaryTime=\z@
2003
      \newcommand*{\PrintTime}[2]{%
2004
        \typeout{%
2005
           [Time #1: \strip@pt\dimexpr\number#2sp\relax\space s]%
2006
2007
2008
      }%
2009
      \newcommand*{\StartTime}[1]{%
2010
        \renewcommand*{\TimeDescription}{#1}%
        \pdfresettimer
2011
      }%
2012
      \newcommand*{\TimeDescription}{}%
2013
      \newcommand*{\StopTime}{%
2014
        \TestTime=\pdfelapsedtime
2015
2016
        \global\advance\SummaryTime\TestTime
2017
        \PrintTime\TimeDescription\TestTime
2018
      2019
      \let\saved@endqstest\endqstest
2020
      \def\qstest#1#2{\%}
2021
2022
        \saved@qstest{#1}{#2}%
        \StartTime{#1}%
2023
2024
      }%
      \def\endqstest{%
2025
        \StopTime
2026
        \saved@endqstest
2027
2028
      }%
      \AtEndDocument{%
2029
        \PrintTime{summary}\SummaryTime
2030
      }%
2031
2032
      \makeatother
2033 \fi
2034 (/test2)
3.2.3 Test 4: additional mod/div operations
2036 \newcommand*{\TestDo}[2]{%
2037
      \ifcase\numexpr#2\relax
2038
2039
        \edef\temp{\intcalcMod{#1}{#2}}%
2040
        \Expect*{%
          \the\numexpr
2041
2042
          \intcalcMul{%
2043
            \intcalcDiv{\intcalcAbs{#1}}{\intcalcAbs{#2}}%
2044
          }{\intcalcAbs{#2}}%
          +\intcalcMod{\intcalcAbs{#1}}{\intcalcAbs{#2}}\relax
2046
        }*{\the\numexpr\intcalcAbs{#1}\relax}%
2047
2048 }
2049 \newcommand*{\TestOne}[2]{%}
2050
      \TestDo{#1}{#1}%
2051 }
2052 \newcommand*{\TestTwo}[3]{%
2053
      \TestDo{#1}{#2}%
2054
      \TestDo{#2}{#1}%
2055 }
2056 \left| \text{TestNum} \right|
2057 \let\TestInv\TestOne
2058 \let\TestAbs\TestOne
2059 \l TestSgn\TestOne
2060 \left| \text{TestMin} \right|
2061 \text{let}\TestMax\TestTwo
2062 \text{TestCmp}\TestTwo
2063 \left| \text{TestInc} \right|
```

```
2064 \let\TestDec\TestOne
2065 \ \text{TestAdd} \ \text{TestTwo}
2066 \text{TestSub}TestTwo
2067 \ \text{TestShl}\
2068 \let\TestShr\TestOne
2069 \let\TestMul\TestTwo
2070 \let\TestSqr\TestOne
2071 \left\{ \text{TestFac} # 1 # 2 \right\}
2072 \let\TestPow\TestTwo
2073 \let\TestDiv\TestTwo
2074 \let\TestMod\TestTwo
2075 (/test4)
3.2.4 Test sets
2076 (*test2 j test4)
2077 \makeatletter
2078
2079 \begin{qstest}{num}{num}\%
     TestNum{0}{0}
2080
      TestNum{1}{1}%
2081
      TestNum{-1}{-1}%
2082
      \TestNum{10}{10}%
2083
      TestNum{-10}{-10}%
2084
      \TestNum{2147483647}{2147483647}%
2086
      \TestNum{-2147483647}{-2147483647}%
2087
      \TestNum{ 0 }{0}%
2088
      \TestNum{ 1 }{1}%
      \texttt{TestNum}\{--1\}\{1\}\%
2089
      TestNum{ - + - + 4 }{4}%
2090
      TestNum{z@}{0}%
2091
2092
     \TestNum{\@ne}{1}%
2093
     TestNum{m@ne}{-1}%
2094 (*etex)
      \TestNum{-10+30}{20}%
2095
      \TestNum{10-30}{-20}%
2097 (/etex)
2098 \end{qstest}
2099
2100 \begin{qstest}{inv}{inv}%
2101 \TestInv{0}{0}%
2102
     TestInv{1}{-1}%
      TestInv{-1}{1}%
2103
2104
      \TestInv{10}{-10}%
2105
      TestInv{-10}{10}%
2106
      \TestInv{2147483647}{-2147483647}%
2107
      \TestInv{-2147483647}{2147483647}%
2108
      \TestInv{ 0 }{0}%
2109
      \TestInv{ 1 }{-1}%
2110
      \TestInv{--1}{-1}%
2111
      TestInv{\z0}{0}
     TestInv{\0ne}{-1}%
2112
2113 \TestInv{\m@ne}{1}\%
2114 (*etex)
2115 \TestInv{-10+30}{-20}%
     \TestInv{10-30}{20}%
2116
2117 (/etex)
2118 \end{qstest}
2119
2120 \begin{qstest}{abs}{abs}%
2121 \TestAbs{0}{0}%
2122
      TestAbs{1}{1}%
      \TestAbs{-1}{1}%
2123
2124 \TestAbs{10}{10}%
```

```
\TestAbs{-10}{10}%
2125
      \TestAbs{2147483647}{2147483647}%
2126
      \TestAbs{-2147483647}{2147483647}%
2127
      \TestAbs{ 0 }{0}%
2129
      \TestAbs{ 1 }{1}%
2130
      \TestAbs{--1}{1}%
2131
      TestAbs{\z@}{0}%
     TestAbs{\0ne}{1}%
2132
     \texttt{TestAbs}\{\texttt{m@ne}\}\{1\}\%
2133
2134 (*etex)
2135 \TestAbs{-10+30}{20}%
2136
     \TestAbs{10-30}{20}%
2137 (/etex)
2138 \end{qstest}
2139
2140 \begin{qstest}{sign}{sign}%
2141 \TestSgn{0}{0}%
      \text{TestSgn}{1}{1}%
2142
2143
      \TestSgn{-1}{-1}%
2144
      TestSgn{10}{1}%
      \texttt{\TestSgn}\{-10\}\{-1\}\%
2145
2146
      \TestSgn{2147483647}{1}%
2147
      \TestSgn{-2147483647}{-1}%
      \TestSgn{ 0 }{0}%
2148
      \TestSgn{ 2 }{1}%
2149
2150
      \TestSgn{ -2 }{-1}%
2151
      TestSgn{--2}{1}%
     \TestSgn{\z@}{0}%
2152
     \TestSgn{\0ne}{1}%
2153
2154 \qquad \texttt{TestSgn}\{\texttt{m@ne}\}\{\texttt{-1}\}\%
2155 (*etex)
2156
      \TestSgn{-10+30}{1}%
2157
      \TestSgn{10-30}{-1}%
2158 (/etex)
2159 \end{qstest}
2160
2161 \begin{qstest}{min}{min}%
2162 \TestMin{0}{1}{0}%
2163 \TestMin{1}{0}{0}%
2164 \ \text{TestMin}{-10}{-20}{-20}%
     \TestMin{ 1 }{ 2 }{1}%
2165
      \texttt{\TestMin{ 2 }{1 }{1}}{\ }
2166
2167
      \TestMin{1}{1}{1}}%
2168
      TestMin{\z0}{\0ne}{0}
2169
      TestMin{\{0ne}_{n@ne}_{-1}\%
2170 (*etex)
2171
      \TestMin{1+2}{3+4}{3}%
2172 (/etex)
2173 \end{qstest}
2174
2175 \begin{qstest}{max}{max}%
2176 \TestMax{0}{1}{1}%
2177
      \text{TestMax}\{1\}\{0\}\{1\}\%
2178 \TestMax{-10}{-20}{-10}%
2179 \TestMax{ 1 }{ 2 }{2}%
2180 \TestMax{ 2 }{ 1 }{2}%
2181 \TestMax{1}{1}{1}%
2182 \TestMax{\z0}{\0ne}{1}%
2183 \TestMax{\encomp}{\norm{1}}%
2184 (*etex)
2185 \TestMax{1+2}{3+4}{7}%
2186 (/etex)
```

```
2187 \end{qstest}
2188
2189 \begin{qstest}{cmp}{cmp}%
      \TestCmp{0}{0}{0}%
2191
      TestCmp{-21}{17}{-1}%
2192
      \TestCmp{3}{4}{-1}%
2193
      TestCmp{-10}{-10}{0}%
      TestCmp{-10}{-11}{1}%
2194
      TestCmp{100}{5}{1}%
2195
      \TestCmp{2147483647}{-2147483647}{1}%
2196
      \TestCmp{-2147483647}{2147483647}{-1}%
2197
      \TestCmp{2147483647}{2147483647}{0}%
2198
2199
      \TestCmp{\z@}{\cne}{-1}%
      \TestCmp{\Qne}{\mone}{1}%
      TestCmp{ 4 }{ 5 }{-1}%
2201
2202
      TestCmp{ -3 }{ -7 }{1}%
2203 (*etex)
      TestCmp{1+2}{3+4}{-1}%
2204
2205 (/etex)
2206 \end{qstest}
2207
2208 \begin{qstest}{fac}{fac}
      \TestFac{0}{1}%
2209
      \TestFac{1}{1}%
2210
      \TestFac{2}{2}%
2211
2212
      \TestFac{3}{2*3}%
2213
      \TestFac{4}{2*3*4}%
2214
      \TestFac{5}{2*3*4*5}%
2215
      \TestFac{6}{2*3*4*5*6}%
      \TestFac{7}{2*3*4*5*6*7}%
2216
      \TestFac{8}{2*3*4*5*6*7*8}%
2217
2218
      \TestFac{9}{2*3*4*5*6*7*8*9}%
2219
      \TestFac{10}{2*3*4*5*6*7*8*9*10}%
      \TestFac{11}{2*3*4*5*6*7*8*9*10*11}%
2220
2221
      \TestFac{12}{2*3*4*5*6*7*8*9*10*11*12}%
2222 \end{qstest}
2223
2224 \ensuremath{\verb| linc|{inc}{|}} \\
2225 \TestInc{0}{1}%
2226
      \TestInc{1}{2}%
2227
      \TestInc{-1}{0}%
2228
      \TestInc{10}{11}%
2229
      TestInc{-10}{-9}%
2230
      \TestInc{999}{1000}%
2231
      \TestInc{-1000}{-999}%
2232
      \TestInc{129}{130}%
2233
      \TestInc{2147483646}{2147483647}%
2234
      \TestInc{-2147483647}{-2147483646}\%
2235 \end{qstest}
2236
2237 \begin{qstest}{dec}{dec}%
2238
      \TestDec{0}{-1}%
      \TestDec{1}{0}%
2239
2240
     \TestDec{-1}{-2}%
2241
      \TestDec{10}{9}%
2242
      \TestDec{-10}{-11}%
2243
     \TestDec{1000}{999}%
2244
     \TestDec{-999}{-1000}%
2245
      \TestDec{130}{129}%
      \TestDec{2147483647}{2147483646}%
2246
      \TestDec{-2147483646}{-2147483647}%
2247
2248 \end{qstest}
```

```
2249
2250 \geq 250 \leq (qstest){add}{add}
      \TestAdd{0}{0}{0}%
2251
      TestAdd{1}{0}{1}%
2253
      TestAdd{0}{1}{1}%
2254
      \TestAdd{1}{2}{3}%
2255
      TestAdd{-1}{-1}{-2}%
2256
      \TestAdd{2147483646}{1}{2147483647}%
      \TestAdd{-2147483647}{2147483647}{0}%
2257
      \TestAdd{20}{-5}{15}%
2258
      TestAdd{-4}{-1}{-5}%
2259
      TestAdd{-1}{-4}{-5}%
2260
2261
      TestAdd{-4}{1}{-3}%
     TestAdd{-1}{4}{3}%
2262
     TestAdd{4}{-1}{3}%
2263
2264
      TestAdd{1}{-4}{-3}%
2265
      TestAdd{-4}{-1}{-5}%
2266
      TestAdd{-1}{-4}{-5}%
      TestAdd{ -4 }{ -1 }{-5}%
2267
2268
      TestAdd{ -1 }{ -4 }{-5}%
      TestAdd{ -4 }{ 1 }{-3}%
2269
      TestAdd{ -1 }{ 4 }{3}%
2270
2271
      TestAdd{ 4 }{ -1 }{3}%
2272
      TestAdd{ 1 }{ -4 }{-3}%
      TestAdd{ -4 }{ -1 }{-5}%
2273
2274
      TestAdd{ -1 }{ -4 }{-5}%
2275
      \TestAdd{876543210}{111111111}{987654321}%
2276
      \TestAdd{999999999}{2}{1000000001}%
2277 (*etex)
      \TestAdd{100}{50+150}{300}%
2278
      \TestAdd{2147483647}{10-2147483647}{10}%
2279
2280 (/etex)
2281 \end{qstest}
2282
2283 \begin{qstest}{sub}{sub}
2284
     \TestSub{0}{0}{0}%
2285
      \TestSub{1}{0}{1}%
2286
      TestSub{1}{2}{-1}%
2287
      TestSub{-1}{-1}{0}%
      \TestSub{2147483646}{-1}{2147483647}\%
2288
      TestSub{-2147483647}{-2147483647}{0}%
2289
2290
      TestSub{-4}{-1}{-3}%
2291
      TestSub{-1}{-4}{3}%
2292
      TestSub{-4}{1}{-5}%
2293
      TestSub{-1}{4}{-5}%
2294
      TestSub{4}{-1}{5}%
2295
      TestSub{1}{-4}{5}%
2296
      TestSub{-4}{-1}{-3}%
2297
      TestSub{-1}{-4}{3}%
2298
      TestSub{ -4 }{ -1 }{-3}%
      TestSub{ -1 }{ -4 }{3}%
2299
      TestSub{ -4 }{ 1 }{-5}%
2300
      TestSub{ -1 }{ 4 }{-5}%
2301
2302
      \TestSub{ 4 }{ -1 }{5}%
      TestSub{ 1 }{ -4 }{5}%
2303
2304
      TestSub{ -4 }{ -1 }{-3}%
2305
      TestSub{ -1 }{ -4 }{3}%
2306
      \TestSub{1000000000}{2}{999999998}%
2307
      \TestSub{987654321}{111111111}{876543210}\%
2308 (*etex)
      \TestSub{100}{50+150}{-100}%
2309
      \TestSub{2147483647}{-10+2147483647}{10}%
2310
```

```
2311 (/etex)
2312 \end{qstest}
2313
2314 \begin{qstest}{shl}{shl}
2315
      \TestSh1{0}{0}%
2316
      TestShl{1}{2}%
2317
      \TestSh1{5621}{11242}%
2318
      \TestSh1{1073741823}{2147483646}%
2319
      TestShl{-1}{-2}%
      \TestSh1{-5621}{-11242}%
2320
2321 \end{qstest}
2322
2323 \begin{qstest}{shr}{shr}
      TestShr{0}{0}%
2324
2325
      TestShr{1}{0}%
2326
      TestShr{2}{1}%
2327
      TestShr{3}{1}%
      TestShr{4}{2}%
2328
      TestShr{5}{2}%
2329
      TestShr{6}{3}%
2330
2331
      TestShr{7}{3}%
      \TestShr{8}{4}%
2332
2333
      TestShr{9}{4}%
      \TestShr{10}{5}%
2334
      \TestShr{11}{5}%
2335
2336
      \TestShr{12}{6}%
2337
      \TestShr{13}{6}%
2338
      \TestShr{14}{7}%
2339
      \TestShr{15}{7}%
2340
      \TestShr{16}{8}%
      \TestShr{17}{8}%
2341
      \texttt{TestShr}\{18\}\{9\}\%
2342
2343
      \TestShr{19}{9}%
2344
      \TestShr{20}{10}%
2345
      \TestShr{21}{10}%
2346
      \TestShr{22}{11}%
2347
      \TestShr{11241}{5620}%
2348
      \TestShr{73054202}{36527101}%
2349
      \TestShr{2147483646}{1073741823}%
      TestShr{-1}{0}%
2350
2351
      TestShr{-2}{-1}%
      \texttt{TestShr}{-3}{\{-1\}}\%
2352
2353
      \TestShr{-11241}{-5620}%
2354 \end{qstest}
2355
2356 \begin{qstest}{mul}{mul}
2357
      \TestMul{0}{0}{0}%
2358
      \TestMul{1}{0}{0}%
2359
      \TestMul{0}{1}{0}%
2360
      \TestMul{1}{1}{1}%
      TestMul{3}{1}{3}%
2361
2362
      \TestMul{1}{-3}{-3}%
      TestMul{-4}{-5}{20}%
2363
2364
      \TestMul{3}{7}{21}%
2365
      \TestMul{7}{3}{21}%
2366
      \TestMul{3}{-7}{-21}%
2367
      TestMul{7}{-3}{-21}%
2368
      TestMul{-3}{7}{-21}%
2369
      TestMul{-7}{3}{-21}%
2370
      \TestMul{-3}{-7}{21}%
      TestMul{-7}{-3}{21}%
2371
2372
      \TestMul{12}{11}{132}%
```

```
\TestMul{999}{333}{332667}%
2373
      \TestMul{1000}{4321}{4321000}%
2374
      \TestMul{12345}{173955}{2147474475}%
2375
      \TestMul{1073741823}{2}{2147483646}%
2377
      TestMu1{2}{1073741823}{2147483646}%
2378
      \TestMul{-1073741823}{2}{-2147483646}%
2379
      \TestMul{2}{-1073741823}{-2147483646}%
2380 (*etex)
      TestMu1{2+3}{5+7}{60}%
2381
      \TestMul{2147483647}{2147483647/2147483647}{2147483647}%
2382
2383 (/etex)
2384 \end{qstest}
2385
2386 \begin{qstest}{sqr}{sqr}
      \TestSqr{0}{0}%
2388
      \TestSqr{1}{1}%
      \texttt{\TestSqr}\{2\}\{4\}\%
2389
      \TestSqr{3}{9}%
2390
      \TestSqr{4}{16}%
2391
2392
      \TestSqr{9}{81}%
      \TestSqr{10}{100}%
2393
      \TestSqr{46340}{2147395600}%
2394
2395
      \TestSqr{-1}{1}%
      \TestSqr{-2}{4}%
2396
      \TestSqr{-46340}{2147395600}%
2398 \end{qstest}
2399
2400 \begin{qstest}{pow}{pow}
2401
      TestPow{-2}{0}{1}%
      TestPow{-1}{0}{1}%
2402
      \TestPow{0}{0}{1}%
2403
2404
      \TestPow{1}{0}{1}%
2405
      \TestPow{2}{0}{1}%
2406
     \TestPow{3}{0}{1}%
      TestPow{-2}{1}{-2}%
2407
2408
     \TestPow{-1}{1}{-1}%
2409
      \TestPow{1}{1}{1}%
2410
      \TestPow{2}{1}{2}%
      \texttt{\TestPow}\{3\}\{1\}\{3\}\%
2411
2412
      \TestPow{-2}{2}{4}%
2413
      TestPow{-1}{2}{1}%
2414
      TestPow{0}{2}{0}%
2415
      \TestPow{1}{2}{1}%
2416
      \TestPow{2}{2}{4}%
2417
      \TestPow{3}{2}{9}%
      \TestPow{0}{1}{0}%
2419
      TestPow{1}{-2}{1}%
2420
      TestPow{1}{-1}{1}%
2421
      TestPow{-1}{-2}{1}%
2422
      TestPow{-1}{-1}{-1}%
      TestPow{-1}{3}{-1}%
2423
2424
      TestPow{-1}{4}{1}%
      TestPow{-2}{-1}{0}%
2425
2426
      TestPow{-2}{-2}{0}%
2427
      TestPow{2}{3}{8}%
2428
      \TestPow{2}{4}{16}%
2429
      \TestPow{2}{5}{32}%
2430
      \TestPow{2}{6}{64}%
2431
      \TestPow{2}{7}{128}%
2432
      \TestPow{2}{8}{256}%
2433
      \TestPow{2}{9}{512}%
2434
     \TestPow{2}{10}{1024}%
```

```
TestPow{-2}{3}{-8}%
2435
      \TestPow{-2}{4}{16}%
2436
      \TestPow{-2}{5}{-32}%
2437
      TestPow{-2}{6}{64}%
2439
      \TestPow{-2}{7}{-128}%
2440
      TestPow{-2}{8}{256}%
2441
      \TestPow{-2}{9}{-512}%
      TestPow{-2}{10}{1024}%
2442
2443
      \TestPow{3}{3}{27}%
      \TestPow{3}{4}{81}%
2444
      \TestPow{3}{5}{243}%
2445
      TestPow{-3}{3}{-27}%
2446
      TestPow{-3}{4}{81}%
2447
      TestPow{-3}{5}{-243}%
2448
      \TestPow{2}{30}{1073741824}%
2449
2450
      \TestPow{-3}{19}{-1162261467}%
2451
      \TestPow{5}{13}{1220703125}%
      \TestPow{-7}{11}{-1977326743}%
2452
2453 \end{qstest}
2454
2455 \geq 2455 \leq qstest}{div}{div}
2456
      \TestDiv{1}{1}{1}%
      \TestDiv{2}{1}{2}%
2457
      \TestDiv{-2}{1}{-2}%
2458
      TestDiv{2}{-1}{-2}%
2459
2460
      TestDiv{-2}{-1}{2}%
2461
      \TestDiv{15}{2}{7}%
2462
      \TestDiv{-16}{2}{-8}%
2463
      \TestDiv{1}{2}{0}%
2464
      \TestDiv{1}{3}{0}%
      \TestDiv{2}{3}{0}%
2465
2466
      TestDiv{-2}{3}{0}%
2467
      TestDiv{2}{-3}{0}%
2468
      TestDiv{-2}{-3}{0}%
      TestDiv{13}{3}{4}%
2469
2470
      \TestDiv{-13}{-3}{4}%
2471
      TestDiv{-13}{3}{-4}%
2472
      TestDiv{-6}{5}{-1}%
2473
      TestDiv{-5}{5}{-1}%
2474
      TestDiv{-4}{5}{0}%
      TestDiv{-3}{5}{0}%
2475
      TestDiv{-2}{5}{0}%
2476
      \TestDiv{-1}{5}{0}%
2477
2478
      \TestDiv{0}{5}{0}%
2479
      \TestDiv{1}{5}{0}%
      \TestDiv{2}{5}{0}%
2481
      \TestDiv{3}{5}{0}%
2482
      \TestDiv{4}{5}{0}%
2483
      \TestDiv{5}{5}{1}%
2484
      \TestDiv{6}{5}{1}%
      TestDiv{-5}{4}{-1}%
2485
2486
      TestDiv{-4}{4}{-1}%
      TestDiv{-3}{4}{0}%
2487
2488
      TestDiv{-2}{4}{0}%
2489
      TestDiv{-1}{4}{0}%
2490
      \TestDiv{0}{4}{0}%
2491
      \TestDiv{1}{4}{0}%
2492
      \TestDiv{2}{4}{0}%
2493
      \TestDiv{3}{4}{0}%
2494
      \TestDiv{4}{4}{1}%
      \TestDiv{5}{4}{1}%
2495
```

\TestDiv{12345}{678}{18}%

2496

```
\TestDiv{32372}{5952}{5}%
2497
2498
      \TestDiv{284271294}{18162}{15651}%
      \TestDiv{217652429}{12561}{17327}%
2499
      \TestDiv{462028434}{5439}{84947}%
2500
2501
      TestDiv{2147483647}{1000}{2147483}%
2502
      \TestDiv{2147483647}{-1000}{-2147483}%
2503
      \TestDiv{-2147483647}{1000}{-2147483}%
2504
      \TestDiv{-2147483647}{-1000}{2147483}%
2505 \end{qstest}
2506
    \begin{qstest}{mod}{mod}
2507
      TestMod{-6}{5}{4}%
2508
      TestMod{-5}{5}{0}%
2509
      TestMod{-4}{5}{1}%
2510
      TestMod{-3}{5}{2}%
2511
2512
      TestMod{-2}{5}{3}%
2513
      TestMod{-1}{5}{4}%
2514
      \TestMod{0}{5}{0}%
      \TestMod{1}{5}{1}%
2515
2516
      TestMod{2}{5}{2}%
2517
      \TestMod{3}{5}{3}%
      TestMod{4}{5}{4}%
2518
2519
      \TestMod{5}{5}{0}%
2520
      TestMod{6}{5}{1}%
      \TestMod{-5}{4}{3}%
2521
      TestMod{-4}{4}{0}%
2522
2523
      \TestMod{-3}{4}{1}%
2524
      TestMod{-2}{4}{2}%
2525
      \TestMod{-1}{4}{3}%
2526
      TestMod{0}{4}{0}%
      TestMod{1}{4}{1}%
2527
2528
      \TestMod{2}{4}{2}%
2529
      TestMod{3}{4}{3}%
2530
      TestMod{4}{4}{0}%
      TestMod{5}{4}{1}%
2531
2532
      TestMod{-6}{-5}{-1}%
2533
      TestMod{-5}{-5}{0}%
2534
      TestMod{-4}{-5}{-4}%
2535
      TestMod{-3}{-5}{-3}%
2536
      TestMod{-2}{-5}{-2}%
      TestMod{-1}{-5}{-1}%
2537
2538
      TestMod{0}{-5}{0}%
      \TestMod{1}{-5}{-4}%
2539
2540
      TestMod{2}{-5}{-3}%
2541
      TestMod{3}{-5}{-2}%
2542
      TestMod{4}{-5}{-1}%
2543
      TestMod{5}{-5}{0}%
2544
      TestMod{6}{-5}{-4}%
2545
      TestMod{-5}{-4}{-1}%
2546
      TestMod{-4}{-4}{0}%
      TestMod{-3}{-4}{-3}%
2547
      TestMod{-2}{-4}{-2}%
2548
      TestMod{-1}{-4}{-1}%
2549
      TestMod{0}{-4}{0}
2550
2551
      TestMod{1}{-4}{-3}%
2552
      TestMod{2}{-4}{-2}%
2553
      TestMod{3}{-4}{-1}%
2554
      TestMod{4}{-4}{0}%
2555
      TestMod{5}{-4}{-3}%
      \label{testMod} $$\operatorname{TestMod}_{2147483647}_{1000}_{647}%$
2556
      \label{testMod} $$\operatorname{TestMod}_{2147483647}_{-1000}_{-353}\%$
2557
      TestMod{-2147483647}{1000}{353}%
```

2558

```
\TestMod{-2147483647}{-1000}{-647}%
2559
      \TestMod{ 0 }{ 4 }{0}%
2560
      TestMod{1}{4}{1}%
2561
      TestMod{ -1 }{ 4 }{3}%
2562
      TestMod{ 0 }{ -4 }{0}
2563
2564
      TestMod{ 1 }{ -4 }{-3}%
      TestMod{ -1 }{ -4 }{-1}%
2565
2566 (*etex)
      TestMod{1+2}{1+3}{3}%
2567
      TestMod{1-2}{1+3}{3}%
2568
      \TestMod{1-2}{1-4}{-1}%
2569
      \TestMod{1+2}{1-4}{0}%
2570
2571
      \TestMod{1+2}{1-5}{-1}%
2572 (/etex)
2573 \end{qstest}
2574 (/test2 j test4)
2575 (*test2)
2576 \newcommand*{\TestError}[2]{%
      \begingroup
2577
        \expandafter\def\csname IntCalcError:#1\endcsname{}%
2578
2579
        \Expect*{#2}{0}%
2580
        \expandafter\def\csname IntCalcError:#1\endcsname{ERROR}%
2581
        \Expect*{#2}{OERROR }%
2582
      \endgroup
2583 }
2584 \begin{qstest}{error}{error}
      \TestError{FacNegative}{\intcalcFac{-1}}%
2585
      \TestError{FacNegative}{\intcalcFac{-2147483647}}%
2586
      \TestError{FacOverflow}{\intcalcFac{13}}%
2587
      \TestError{FacOverflow}{\intcalcFac{2147483647}}%
2588
      \TestError{DivisionByZero}{\intcalcPow{0}{-1}}%
2589
      \TestError{DivisionByZero}{\intcalcDiv{1}{0}}%
2590
      \TestError{DivisionByZero}{\intcalcMod{1}{0}}%
2591
      \TestError{DivisionByZero}{\IntCalcDiv1!0!}%
2592
      \TestError{DivisionByZero}{\IntCalcMod1!0!}%
2594 \end{qstest}
2595 (/test2)
2596 (*test2 j test4)
2597 \begin{document}
2598 \end{document}
2599 (/test2 j test4)
```

4 Installation

4.1 Download

Package. This package is available on CTAN¹:

CTAN:macros/latex/contrib/oberdiek/intcalc.dtx The source file.

CTAN:macros/latex/contrib/oberdiek/intcalc.pdf Documentation.

Bundle. All the packages of the bundle 'oberdiek' are also available in a TDS compliant ZIP archive. There the packages are already unpacked and the documentation files are generated. The files and directories obey the TDS standard.

CTAN:install/macros/latex/contrib/oberdiek.tds.zip

TDS refers to the standard "A Directory Structure for TEX Files" (CTAN:tds/tds.pdf). Directories with texmf in their name are usually organized this way.

¹ftp://ftp.ctan.org/tex-archive/

4.2 Bundle installation

Unpacking. Unpack the oberdiek.tds.zip in the TDS tree (also known as texmf tree) of your choice. Example (linux):

```
unzip oberdiek.tds.zip -d ~/texmf
```

Script installation. Check the directory TDS:scripts/oberdiek/ for scripts that need further installation steps. Package attachfile2 comes with the Perl script pdfatfi.pl that should be installed in such a way that it can be called as pdfatfi. Example (linux):

```
chmod +x scripts/oberdiek/pdfatfi.pl
cp scripts/oberdiek/pdfatfi.pl /usr/local/bin/
```

4.3 Package installation

Unpacking. The .dtx file is a self-extracting docstrip archive. The files are extracted by running the .dtx through plain TFX:

```
tex intcalc.dtx
```

TDS. Now the different files must be moved into the different directories in your installation TDS tree (also known as texmf tree):

```
\label{eq:control_control} intcalc.sty & \to tex/generic/oberdiek/intcalc.sty intcalc.pdf & \to doc/latex/oberdiek/intcalc.pdf \\ test/intcalc-test1.tex & \to doc/latex/oberdiek/test/intcalc-test1.tex \\ test/intcalc-test2.tex & \to doc/latex/oberdiek/test/intcalc-test2.tex \\ test/intcalc-test3.tex & \to doc/latex/oberdiek/test/intcalc-test3.tex \\ test/intcalc-test4.tex & \to doc/latex/oberdiek/test/intcalc-test4.tex \\ intcalc.dtx & \to source/latex/oberdiek/intcalc.dtx \\ \end{aligned}
```

If you have a docstrip.cfg that configures and enables docstrip's TDS installing feature, then some files can already be in the right place, see the documentation of docstrip.

4.4 Refresh file name databases

If your TEX distribution (teTEX, mikTEX, ...) relies on file name databases, you must refresh these. For example, teTEX users run texhash or mktexlsr.

4.5 Some details for the interested

Attached source. The PDF documentation on CTAN also includes the .dtx source file. It can be extracted by AcrobatReader 6 or higher. Another option is pdftk, e.g. unpack the file into the current directory:

```
pdftk intcalc.pdf unpack_files output .
```

Unpacking with IATEX. The .dtx chooses its action depending on the format:

plain TEX: Run docstrip and extract the files.

LATEX: Generate the documentation.

If you insist on using LATEX for docstrip (really, docstrip does not need LATEX), then inform the autodetect routine about your intention:

```
latex \let\install=y\input{intcalc.dtx}
```

Do not forget to quote the argument according to the demands of your shell.

Generating the documentation. You can use both the .dtx or the .drv to generate the documentation. The process can be configured by the configuration file ltxdoc.cfg. For instance, put this line into this file, if you want to have A4 as paper format:

\PassOptionsToClass{a4paper}{article}

An example follows how to generate the documentation with pdfIATEX:

```
pdflatex intcalc.dtx
makeindex -s gind.ist intcalc.idx
pdflatex intcalc.dtx
makeindex -s gind.ist intcalc.idx
pdflatex intcalc.dtx
```

5 Catalogue

The following XML file can be used as source for the TeX Catalogue. The elements caption and description are imported from the original XML file from the Catalogue. The name of the XML file in the Catalogue is intcalc.xml.

```
2600 (*catalogue)
2601 <?xml version='1.0' encoding='us-ascii'?>
2602 <! DOCTYPE entry SYSTEM 'catalogue.dtd'>
2603 <entry datestamp='$Date$' modifier='$Author$' id='intcalc'>
2604
     <name>intcalc</name>
      <caption>Expandable arithmetic operations with integers.</caption>
2605
2606
      <authorref id='auth:oberdiek'/>
      <copyright owner='Heiko Oberdiek' year='2007'/>
2607
      <license type='lppl1.3'/>
2608
      <version number='1.1'/>
2609
2610
      <description>
       This package provides expandable arithmetic operations
2611
        with integers, using the e-TeX extension <tt>\numexpr</tt> if it
2612
2613
        is available.
2614
        2615
        The package is part of the <xref refid='oberdiek'>oberdiek</xref>
2616
       bundle.
2617 </description>
2618 <documentation details='Package documentation'
2619
         href='ctan:/macros/latex/contrib/oberdiek/intcalc.pdf'/>
2620 <ctan file='true' path='/macros/latex/contrib/oberdiek/intcalc.dtx'/>
2621 <miktex location='oberdiek'/>
2622 <texlive location='oberdiek'/>
2623
     <install path='/macros/latex/contrib/oberdiek/oberdiek.tds.zip'/>
2624 </entry>
2625 (/catalogue)
```

6 History

```
[2007/09/09 \text{ v}1.0]
```

First version.

[2007/09/27 v1.1]

- \intcalcNum added.
- \intcalcSh1 and \intcalcShr allow negative numbers. The sign is preserved.
- Reuse \@gobble instead of own macro \IntCalc@Gobble.

- Small fixes.
- Shorter internal prefix.
- $\bullet\,$ Some programmer's interface.

7 Index

Numbers written in italic refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; plain numbers refer to the code lines where the entry is used.

$\mathbf{Symbols}$	\csname $14, 21, 50,$
\# 1693	66, 76, 114, 184, 481, 484, 494,
\% 1769	500, 506, 509, 513, 515, 520,
\@ 1694, 1767	539, 549, 551, 556, 575, 682,
\@ReturnAfterElseFi	694, 706, 709, 717, 720, 727,
$\dots \dots 660, 671, 683, 695,$	745, 753, 865, 992, 995, 1001,
$1055, 1488, 1541, 1556, 1580, \underline{1687}$	1006, 1008, 1014, 1018, 1095,
\@ReturnAfterFi	1104, 1106, 1113, 1127, 1131,
. 664, 675, 687, 699, 710, 721,	1135, 1139, 1238, 1246, 1247, 1301, 1683, 1695, 1698, 1701,
1009, 1053, 1107, 1240, 1492,	1704, 1759, 1786, 1998, 2578, 2580
1547, 1562, 1584, 1591, 1595, <u>1686</u>	1704, 1703, 1700, 1930, 2070, 2000
\\0firstofone \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	D
\@gobble 601, 604, 609, 612, 619, 622,	\dimexpr 2006
1260, 1263, 1268, 1271, 1279,	\divide
1281, 1452, 1455, 1461, 1573, 1635, 1637, 1677, <u>1683</u> , 1699, 1707	\documentclass
\Que 311, 1391, 2092, 2112, 2132, 2153,	Adocumentciass 1792
2168, 2169, 2182, 2183, 2199, 2200	${f E}$
\Qundefined	\empty 17, 18
\\	\end 1787.
\{	2098, 2118, 2138, 2159, 2173,
\} 1692	2187, 2206, 2222, 2235, 2248,
	2281, 2312, 2321, 2354, 2384,
\mathbf{A}	2398, 2453, 2505, 2573, 2594, 2598
\advance 1732, 1740, 1755, 2016	\endcsname 14, 21, 50, 66, 76, 114, 184,
\aftergroup 29	513, 520, 521, 539, 540, 549,
\AtEndDocument 2029	556, 557, 575, 576, 706, 717,
	727, 729, 731, 745, 747, 749,
В	753, 755, 757, 865, 867, 869,
\begin 2079, 2100, 2120, 2140, 2161,	1006, 1014, 1015, 1018, 1019,
2175, 2189, 2208, 2224, 2237,	1104, 1113, 1114, 1127, 1128,
2250, 2283, 2314, 2323, 2356,	1131, 1133, 1135, 1139, 1238,
2386, 2400, 2455, 2507, 2584, 2597	1247, 1683, 1695, 1698, 1701,
\body 1711, 1715	
(body 1111, 1110	1704, 1759, 1786, 1998, 2578, 2580
	\endinput 29, 112
\mathbf{C}	\endinput
C \catcode 2, 3, 5,	\endinput
C \catcode	\endinput
C \catcode	\endinput
$ \begin{array}{c} \textbf{C} \\ \texttt{(catcode} \ \ldots \ldots \ 2, 3, 5, \\ 6, 7, 8, 9, 10, 11, 12, 13, 33, 34, \\ 36, 37, 38, 39, 40, 41, 42, 43, 44, \\ 45, 46, 47, 48, 49, 69, 70, 72, 73, \end{array} $	\endinput
$ \begin{array}{c} \textbf{C} \\ \texttt{(catcode} \ \ldots \ \ldots \ \ldots \ 2, \ 3, \ 5, \\ 6, \ 7, \ 8, \ 9, \ 10, \ 11, \ 12, \ 13, \ 33, \ 34, \\ 36, \ 37, \ 38, \ 39, \ 40, \ 41, \ 42, \ 43, \ 44, \\ 45, \ 46, \ 47, \ 48, \ 49, \ 69, \ 70, \ 72, \ 73, \\ 74, \ 78, \ 79, \ 80, \ 81, \ 82, \ 83, \ 84, \ 87, \\ \end{array} $	\endinput
C \catcode	\endinput
$ \begin{array}{c} \textbf{C} \\ \texttt{(catcode} \dots \dots 2, 3, 5, \\ 6, 7, 8, 9, 10, 11, 12, 13, 33, 34, \\ 36, 37, 38, 39, 40, 41, 42, 43, 44, \\ 45, 46, 47, 48, 49, 69, 70, 72, 73, \\ 74, 78, 79, 80, 81, 82, 83, 84, 87, \\ 88, 90, 91, 92, 93, 97, 99, 116, \\ 1691, 1692, 1693, 1694, 1729, \\ \end{array} $	\endinput 29, 112 \endlinechar 4, 35, 71, 77, 89 \endqstest 2020, 2025 \errmessage 1748 \Expect 1811,
$ \begin{array}{c} \textbf{C} \\ \texttt{(catcode} \ \ldots \ \ldots \ \ldots \ 2, 3, 5, \\ 6, 7, 8, 9, 10, 11, 12, 13, 33, 34, \\ 36, 37, 38, 39, 40, 41, 42, 43, 44, \\ 45, 46, 47, 48, 49, 69, 70, 72, 73, \\ 74, 78, 79, 80, 81, 82, 83, 84, 87, \\ 88, 90, 91, 92, 93, 97, 99, 116, \\ 1691, 1692, 1693, 1694, 1729, \\ 1738, 1746, 1750, 1767, 1768, 1769 \\ \end{array} $	\endinput 29, 112 \endlinechar 4, 35, 71, 77, 89 \endqstest 2020, 2025 \errmessage 1748 \Expect 1811,
$ \begin{array}{c} \textbf{C} \\ \texttt{(catcode} & \ldots & \ldots & 2, 3, 5, \\ 6, 7, 8, 9, 10, 11, 12, 13, 33, 34, \\ 36, 37, 38, 39, 40, 41, 42, 43, 44, \\ 45, 46, 47, 48, 49, 69, 70, 72, 73, \\ 74, 78, 79, 80, 81, 82, 83, 84, 87, \\ 88, 90, 91, 92, 93, 97, 99, 116, \\ 1691, 1692, 1693, 1694, 1729, \\ 1738, 1746, 1750, 1767, 1768, 1769 \\ \texttt{(chardef} & \ldots & \ldots & \ldots & 1796 \\ \end{array} $	\endinput 29, 112 \endlinechar 4, 35, 71, 77, 89 \endqstest 2020, 2025 \errmessage 1748 \Expect 1811,
$ \begin{array}{c} \textbf{C} \\ \texttt{(catcode} \dots \dots 2, 3, 5, \\ 6, 7, 8, 9, 10, 11, 12, 13, 33, 34, \\ 36, 37, 38, 39, 40, 41, 42, 43, 44, \\ 45, 46, 47, 48, 49, 69, 70, 72, 73, \\ 74, 78, 79, 80, 81, 82, 83, 84, 87, \\ 88, 90, 91, 92, 93, 97, 99, 116, \\ 1691, 1692, 1693, 1694, 1729, \\ 1738, 1746, 1750, 1767, 1768, 1769, \\ \texttt{(count@} \dots 1696, 1725, 1729, 1731, \\ \end{array} $	\endinput 29, 112 \endlinechar 4, 35, 71, 77, 89 \endqstest 2020, 2025 \errmessage 1748 \Expect 1811,
$ \begin{array}{c} \mathbf{C} \\ \texttt{(catcode} \ \ldots \ \ldots \ 2, 3, 5, \\ 6, 7, 8, 9, 10, 11, 12, 13, 33, 34, \\ 36, 37, 38, 39, 40, 41, 42, 43, 44, \\ 45, 46, 47, 48, 49, 69, 70, 72, 73, \\ 74, 78, 79, 80, 81, 82, 83, 84, 87, \\ 88, 90, 91, 92, 93, 97, 99, 116, \\ 1691, 1692, 1693, 1694, 1729, \\ 1738, 1746, 1750, 1767, 1768, 1769, \\ \texttt{(count@} \ \ldots \ 1696, 1725, 1729, 1731, \\ 1732, 1736, 1738, 1739, 1740, \\ \end{array} $	\endinput 29, 112 \endlinechar 4, 35, 71, 77, 89 \endqstest 2020, 2025 \errmessage 1748 \Expect 1811,
$ \begin{array}{c} \textbf{C} \\ \texttt{(catcode} \dots \dots 2, 3, 5, \\ 6, 7, 8, 9, 10, 11, 12, 13, 33, 34, \\ 36, 37, 38, 39, 40, 41, 42, 43, 44, \\ 45, 46, 47, 48, 49, 69, 70, 72, 73, \\ 74, 78, 79, 80, 81, 82, 83, 84, 87, \\ 88, 90, 91, 92, 93, 97, 99, 116, \\ 1691, 1692, 1693, 1694, 1729, \\ 1738, 1746, 1750, 1767, 1768, 1769, \\ \texttt{(count@} \dots 1696, 1725, 1729, 1731, \\ \end{array} $	\endinput 29, 112 \endlinechar 4, 35, 71, 77, 89 \endqstest 2020, 2025 \errmessage 1748 \Expect 1811,

	\
1469, 1612, 1621, 1624, 1652,	\InCa@Fac <u>161</u> , 272, 1341
1655, 1658, 1974, 1976, 1981, 2037	\InCa@FirstOfOne 451 , 454 , 456
\ifnum 138,	\InCa@Inc $485, 495, 506, 511$
145, 152, 155, 176, 295, 311,	\InCa@IncDigit9 <u>539</u>
341, 348, 391, 398, 596, 597,	\InCa@IncDigit[0-8] <u>519</u>
599, 607, 616, 617, 625, 652,	\InCa@IncSwitch 476, 478
746, 754, 866, 1237, 1256, 1257,	\InCa@Max $\underline{144}$, $\underline{204}$, $\overline{468}$
1258, 1267, 1275, 1277, 1284,	\InCa@Min \frac{137}{137}, 199, 464
1304, 1368, 1391, 1392, 1403,	\InCa@Mod 378, 382, 1607, 1611, 1617
1449, 1450, 1458, 1468, 1479,	\InCa@ModShift 1632, 1674
1522, 1529, 1539, 1540, 1555,	\InCa@ModX 428, 434, 441
1578, 1615, 1631, 1675, 1731,	· · · · · · · · · · · · · · · · · · ·
1739, 1746, 1754, 1867, 1878,	\InCa@Mul 1259, 1262, 1268, 1270,
1889, 1890, 1891, 1913, 1914, 1915	1278, 1281, 1285, 1287, 1293,
\ifodd 246, 252, 296, 314,	<u>1295</u> , <u>1311</u> , 1335, 1337, 1355,
1054, 1369, 1378, 1402, 1629, 1663	1357, 1393, 1395, 1399, 1404, 1406
	\InCa@MulSwitch 1251, <u>1255</u>
\ifx 15, 18, 21, 50, 58, 61, 114, 120, 127, 130, 184,	\InCa@Param[0-9] <u>1112</u>
	\InCa@Pow $275, \underline{279}, 1344, \underline{1348}$
249, 289, 301, 479, 492, 497,	$\label{localPowRec} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
512, 548, 659, 670, 681, 693,	$\InCa@ProcessAdd \dots 684, \underline{704}$
705, 716, 991, 1005, 1040, 1051,	\InCa@ProcessDiv 1518, <u>1520</u> , 1585, 1596
1103, 1312, 1317, 1334, 1354,	\InCa@ProcessMul 1307, 1311, 1318, 1322
1362, 1374, 1377, 1487, 1524,	\InCa@ProcessSub 696, 715
1531, 1572, 1581, 1592, 1683,	\InCa@ProcessTim 1096, 1102
1695, 1698, 1701, 1704, 1759, 1998	\InCa@Sgn <u>126</u> , 196, 461
\immediate 23, 52	\InCa@Shl
\InCa@@@Add	. 993, 996, 1002, 1004, 1010, 1302
\InCa@@@Sub	\InCa@ShlDigit0 <u>1014</u>
\InCa@@Add	\InCa@ShlDigit[1-9] 1017
\InCa@@Div	\InCa@ShlSwitch 988, 990
$. 339, \underline{373}, 426, 429, 435, 437, $	\InCa@Shr 240,
1441, 1451, 1455, 1460, 1463, 1467	<u>248</u> , 1041, 1043, 1047, <u>1049</u> , 1474
\InCa@@Mod 389, <u>423</u>	\InCa@ShrDigit 1050, 1064
\InCa@@ProcessDiv	\InCa@ShrSwitch 1037, 1039
\dots 1542, 1548, 1557, 1563, <u>1577</u>	\InCa@Space <u>639</u> , 648, 655
\InCa@@Sub 655, <u>669</u>	\InCa@Sqr 266, 268, 1331, 1333
\InCa@@TestMode 118	\InCa@StartI 1497
\InCa@@TimDigitCarry 1241 , 1245	\InCa@StartII 1503
\InCa@Abs <u>119, 193, 458</u>	\InCa@StartIII
$\verb InCa@Add 600, 603 ,$	\InCa@StartIV
$626, 628, 634, \underline{644}, 1313, 1323, 1514$	\InCa@Sub 609, 611, 618, 622, 637,
\InCa@AddDigit0 <u>745</u>	651, 1534, 1543, 1549, 1558,
\InCa@AddDigit[1-9] <u>752</u>	1564, 1597, 1634, 1641, 1665, 1676
\InCa@AddSwitch 585, 591, 595	
\InCa@AtEnd 95, 96, 112, 448, 1688	\InCa@SubDigit[0-9]
\InCa@CleanupIV 1582, 1593, 1605	
\InCa@Cmp <u>151</u> , 209, 472	407, 422, 519, 530, 531, 532,
\InCa@Dec $482, \frac{1}{501}, 509, \frac{547}{509}$	533, 534, 535, 536, 537, 538,
\InCa@DecDigitO 575	555, 566, 567, 568, 569, 570,
\InCa@DecDigit[1-9] 555	571, 572, 573, 574, 726, 735,
\InCa@DecSwitch 489, 491	736, 737, 738, 739, 740, 741,
\InCa@DigitCarry[0-9] 726	742, 743, 744, 752, 765, 776,
\InCa@Div 328,	787, 798, 809, 820, 831, 842,
332, 1415, 1419, 1637, 1642, 1666	853, 864, 877, 888, 899, 910,
\InCa@DivStart 1476, 1486	921, 932, 943, 954, 965, 976,
\InCa@DivStartI 1476, 1480 \InCa@DivStartI 1489, 1497	1017, 1027, 1028, 1029, 1030,
	1031, 1032, 1033, 1034, 1035,
\InCa@DivStartII 1498, 1503	1087, 1101, 1112, 1117, 1118,
\InCa@DivStartIII 1504, 1509	1119, 1120, 1121, 1122, 1123,
\InCa@DivStartIV 1510, 1517	1124, 1125, 1126, 1138, 1148,
\InCa@DivSwitch 1426, 1448	1159, 1170, 1181, 1192, 1203,
\InCa@Empty 659, 670,	1214, 1225, 1432, 1447, 1649, 1673
681, 693, 705, 716, 1312, 1317, <u>1682</u>	\InCa@TestMode 118, 1796

\InCa@Tim . <u>1087</u> , 1305, 1315, 1319, 1325	N
\InCa@TimDigit0 1127	\NeedsTeXFormat 1790
\InCa@TimDigit1 1131	\newcommand 1805, 1813, 1820, 1831,
\InCa@TimDigit[2-9] <u>1138</u>	1832, 1833, 1838, 1843, 1844,
\InCa@TimDigitCarry 1140 , $\underline{1236}$	1847, 1850, 1853, 1856, 1859,
\IncludeTests 1801	1862, 1865, 1876, 1887, 1911,
\input 1760	1927, 1936, 1945, 1954, 1957,
\IntCal@ShlDigit 1004	1960, 1963, 1972, 2004, 2009,
\intcalc@Mod <u>1611</u>	2013, 2014, 2036, 2049, 2052, 2576
\intcalcAbs	\newcount 1830, 2001, 2002 \next 1716, 1718, 1720
1941, 1949, 1950, 1968, 1969,	\nofiles 1710, 1718, 1720
1989, 1990, 2043, 2044, 2045, 2046	\number 190, 193,
\IntCalcAdd 7, 230, 633, 1894, 1902	196, 199, 204, 209, 240, 266,
\intcalcAdd 5, <u>224</u> , <u>583</u> , <u>1888</u>	272, 275, 323, 328, 342, 344,
\intcalcCmp 4, 208, 471, 1863, 1891, 1915	349, 351, 359, 378, 392, 394,
\IntCalcDec 7, <u>221</u> , <u>508</u> , 1881	399, 401, 409, 451, 454, 458,
\intcalcDec 5, <u>215</u> , <u>488</u> , 1877	461, 464, 465, 468, 469, 472,
\IntCalcDiv 7, <u>357</u> , <u>1432</u> , 1968, 2592	473, 476, 489, 506, 509, 584,
\intcalcDiv	586, 587, 590, 592, 593, 600,
327, <u>1414</u> , 1836, 1964, 2043, 2590	603, 611, 618, 634, 637, 988,
\IntCalcError 177, 179, 290,	1000, 1037, 1047, 1089, 1141, 1250, 1252, 1253, 1259, 1262,
334, 361, 384, 411, 1363, 1421, 1436, 1470, 1613, 1625, 1653, 1659	1270, 1278, 1293, 1313, 1322,
\intcalcFac	1323, 1331, 1341, 1344, 1345,
1340, 1958, 2585, 2586, 2587, 2588	1346, 1399, 1400, 1401, 1415,
\IntCalcInc 7, <u>218</u> , <u>505</u> , 1870	1416, 1417, 1427, 1428, 1434,
\intcalcInc $5, \frac{5}{212}, \frac{475}{475}, 1866$	1451, 1460, 1499, 1505, 1506,
\intcalcInv 4, <u>189</u> , <u>453</u> , <u>1845</u>	1511, 1512, 1513, 1514, 1534,
\intcalcMax 4, <u>203</u> , <u>467</u> , <u>1860</u>	1543, 1549, 1558, 1564, 1597,
\intcalcMin 4, <u>198</u> , <u>463</u> , <u>1857</u>	1607, 1608, 1609, 1618, 1619,
\IntCalcMod 7, 407, 1649, 1988, 2593	1633, 1635, 1636, 1641, 1642,
\intcalcMod	1651, 1665, 1666, 1676, 1751, 2006
377, 1606, 1973, 2039, 2045, 2591 \IntCalcMul 7, 262, 1292, 1949	\numexpr 187, 193, 196, 200, 201, 205, 206, 210, 213, 216, 219, 222,
\intcalcMul 7, <u>202</u> , <u>1292</u> , 1949 \intcalcMul 5, 259,	225, 228, 231, 234, 237, 240,
1249, 1636, 1642, 1666, 1946, 2042	243, 246, 253, 255, 260, 263,
\intcalcNum 3, <u>186</u> , 190, <u>450</u> , 1848,	266, 269, 272, 276, 277, 285,
1867, 1870, 1878, 1881, 1889,	312, 316, 317, 318, 321, 322,
1890, 1895, 1903, 1913, 1914, 1919	329, 330, 366, 375, 379, 380,
\intcalcPow 6 , 274 , 1343 , 1961 , 2589	416, 426, 429, 435, 437, 445,
\intcalcSgn	1793, 1794, 1799, 1806, 1807,
<u>195, 460,</u> 1854, 1974, 1976, 1981	1810, 1814, 1815, 1817, 1823,
\IntCalcShl 7, <u>242</u> , <u>999</u> , <u>1931</u>	1831, 1958, 2037, 2041, 2046, 2612
\intcalcShl	P
236, 987, 1500, 1507, 1515, 1928 \IntCalcShr 7, 245, 1046, 1940	\PackageInfo 26
\intcalcShr 5, 239, 1036, 1400, 1937	\pdfelapsedtime 2015
\intcalcSqr $6, \underline{265}, \underline{1330}, \underline{1955}$	\pdfresettimer 2011
\IntCalcSub 7, 233, 636, 1918	\PrintTime 2004, 2017, 2030
\intcalcSub $5, \overline{227}, \overline{589}, 1912$	\ProvidesPackage 19, 67
\iterate 1712, 1714, 1716	Q
T	\qstest 2019, 2021
L \LoadCommand 1760, 1770	R
\LogTests	\RangeCatcodeCheck 1743, 1771,
\loop	1772, 1773, 1774, 1775, 1776,
,	1777, 1778, 1779, 1780, 1781, 1782
${f M}$	\RangeCatcodeInvalid
\m@ne $295, 1368, 2093,$	1735, 1763, 1764, 1765, 1766
2113, 2133, 2154, 2169, 2183, 2200	\renewcommand 2010
\makeatletter 1795, 2000, 2077	\repeat 1710, 1722, 1733, 1741, 1756
\makeatother 1797, 2032	\RestoreCatcodes 1724, 1727, 1728, 1783

```
\result ..... 1816, 1818
                                       \TestInc ..... 1865,
                                              2063, 2225, 2226, 2227, 2228,
\resultA ..... 1808, 1811
                                              2229, 2230, 2231, 2232, 2233, 2234
\resultB ..... 1809, 1811
                                       \TestInv .... 1844,
\romannumeral ......
                                              2057, 2101, 2102, 2103, 2104,
      ..... 340, 347, 390, 397, 707, 718
                                              2105, 2106, 2107, 2108, 2109,
                                              2110, 2111, 2112, 2113, 2115, 2116
                  \mathbf{S}
                                       \TestMax 1859, 2061, 2176, 2177, 2178,
\saved@endqstest ..... 2020, 2027
                                              2179, 2180, 2181, 2182, 2183, 2185
\saved@qstest ..... 2019, 2022
                                        TestMin 1856, 2060, 2162, 2163, 2164,
\SavedNumexpr ......
                                              2165, 2166, 2167, 2168, 2169, 2171
       1793, 1799, 1806, 1810, 1814, 1817
                                       \TestMod ... 1972, 2074, 2508, 2509,
\space .... 1749, 1750, 1758, 1811, 2006
                                              2510, 2511, 2512, 2513, 2514,
\StartTime ..... 2009, 2023
                                              2515, 2516, 2517, 2518, 2519,
\verb|\StopTime| ..... 2014, 2026|
                                              2520, 2521, 2522, 2523, 2524,
\strip@pt ..... 2006
                                              2525, 2526, 2527, 2528, 2529,
\SummaryTime .. 2001, 2003, 2016, 2030
                                              2530, 2531, 2532, 2533, 2534,
                                              2535, 2536, 2537, 2538, 2539,
                 \mathbf{T}
                                              2540, 2541, 2542, 2543, 2544,
\temp ..... 2039
                                              2545, 2546, 2547, 2548, 2549,
\Test .... 1762,
                                              2550, 2551, 2552, 2553, 2554,
      1785, 1838, 1843, 1845, 1848,
                                              2555, 2556, 2557, 2558, 2559,
      1851, 1854, 1857, 1860, 1863,
                                              2560, 2561, 2562, 2563, 2564,
      1866, 1869, 1877, 1880, 1888,
                                              2565, 2567, 2568, 2569, 2570, 2571
      1893, 1901, 1912, 1917, 1928,
                                       \TestMul ..... 1945,
      1930, 1937, 1939, 1946, 1948,
                                              2069, 2357, 2358, 2359, 2360,
      1955, 1961, 1964, 1967, 1973, 1987
                                              2361, 2362, 2363, 2364, 2365,
\TestAbs ..... 1850,
                                              2366, 2367, 2368, 2369, 2370,
      2058, 2121, 2122, 2123, 2124,
                                              2371, 2372, 2373, 2374, 2375,
      2125, 2126, 2127, 2128, 2129,
                                              2376, 2377, 2378, 2379, 2381, 2382
      2130, 2131, 2132, 2133, 2135, 2136
                                       \TestNum ..... 1847, 2056,
\TestAdd ... 1887, 2065, 2251, 2252,
                                              2080, 2081, 2082, 2083, 2084,
      2253, 2254, 2255, 2256, 2257,
                                              2085, 2086, 2087, 2088, 2089,
      2258, 2259, 2260, 2261, 2262,
                                              2090, 2091, 2092, 2093, 2095, 2096
      2263, 2264, 2265, 2266, 2267,
                                       \TestOne ... 2049, 2056, 2057, 2058,
      2268, 2269, 2270, 2271, 2272,
                                              2059, 2063, 2064, 2067, 2068, 2070
      2273, 2274, 2275, 2276, 2278, 2279
                                       \TestPow ..... 1960, 2072, 2401,
\TestArg ..... 1831, 1832, 1834, 1835
                                              2402, 2403, 2404, 2405, 2406,
\TestCmp 1862, 2062, 2190, 2191, 2192,
                                              2407, 2408, 2409, 2410, 2411,
      2193, 2194, 2195, 2196, 2197,
                                              2412, 2413, 2414, 2415, 2416,
      2198, 2199, 2200, 2201, 2202, 2204
                                              2417, 2418, 2419, 2420, 2421,
\TestCount .... 1830, 1834, 1835, 1836
                                              2422, 2423, 2424, 2425, 2426,
\TestDec ..... 1876,
                                              2427, 2428, 2429, 2430, 2431,
      2064, 2238, 2239, 2240, 2241,
                                              2432, 2433, 2434, 2435, 2436,
                                              2437, 2438, 2439, 2440, 2441,
      2242, 2243, 2244, 2245, 2246, 2247
                                              2442, 2443, 2444, 2445, 2446,
\TestDiv 1963, 2073, 2456, 2457, 2458,
                                              2447, 2448, 2449, 2450, 2451, 2452
      2459, 2460, 2461, 2462, 2463,
      2464, 2465, 2466, 2467, 2468,
                                       \TestResult ..... 1813, 1839
      2469, 2470, 2471, 2472, 2473,
                                       \texttt{TestResultTwoExpansions} . 1820, 1840
      2474, 2475, 2476, 2477, 2478,
                                       \TestSgn ..... 1853, 2059,
      2479, 2480, 2481, 2482, 2483,
                                              2141, 2142, 2143, 2144, 2145,
      2484, 2485, 2486, 2487, 2488,
                                              2146, 2147, 2148, 2149, 2150,
      2489, 2490, 2491, 2492, 2493,
                                              2151, 2152, 2153, 2154, 2156, 2157
      2494, 2495, 2496, 2497, 2498,
                                        \verb|\TestShl| \dots \dots 1927, 2067,
      2499, 2500, 2501, 2502, 2503, 2504
                                              2315, 2316, 2317, 2318, 2319, 2320
\TestDo ..... 2036, 2050, 2053, 2054
                                       \TestShr ..... 1936,
\TestError . 2576, 2585, 2586, 2587,
                                              2068, 2324, 2325, 2326, 2327,
      2588, 2589, 2590, 2591, 2592, 2593
                                              2328, 2329, 2330, 2331, 2332,
\TestExch ..... 1843, 1958
                                              2333,\ 2334,\ 2335,\ 2336,\ 2337,
\TestFac ... 1957, 2071, 2209, 2210,
                                              2338, 2339, 2340, 2341, 2342,
      2211, 2212, 2213, 2214, 2215,
                                              2343, 2344, 2345, 2346, 2347,
      2216, 2217, 2218, 2219, 2220, 2221
                                              2348, 2349, 2350, 2351, 2352, 2353
```

\TestSpaceAtEnd 1805, 1841 \TestSqr 1954, 2070, 2387, 2388, 2389, 2390, 2391, 2392, 2393, 2394, 2395, 2396, 2397 \TestSub 1911, 2066,	\TimeDescription 2010, 2013, 2017 \TMP@EnsureCode
2284, 2285, 2286, 2287, 2288, 2289, 2290, 2291, 2292, 2293, 2294, 2295, 2296, 2297, 2298, 2299, 2300, 2301, 2302, 2303, 2304, 2305, 2306, 2307, 2309, 2310	U \UNDEFINED 1794, 1807, 1815, 1823 \usepackage 1798, 1800
\TestTextDivide 1833, 1965 \TestTime 2002, 2015, 2016, 2017	W \write
\TestTwo 2052, 2060, 2061, 2062,	X
2065, 2066, 2069, 2072, 2073, 2074 \the \the \the, 79, 80, 81, 82, 83, 84, 97, 187, \text{193, 196, 200, 201, 205, 206,} \text{210, 213, 216, 219, 222, 225,} \text{228, 231, 234, 237, 240, 243,} \text{246, 253, 255, 260, 263, 266,} \text{269, 272, 276, 277, 285, 312,} \text{316, 317, 318, 321, 322, 329,} \text{330, 366, 375, 379, 380, 416,} \text{426, 429, 435, 437, 445, 1729,} \text{1749, 1750, 1836, 1958, 2041, 2046}	\x 14, 15, 18, 22, 26, 28, 51, 56, 66, 75, 87, 640, 643, 1868, 1873, 1879, 1884, 1892, 1898, 1900, 1906, 1916, 1922, 1929, 1934, 1938, 1943, 1947, 1952, 1966, 1986, 1992 Z \ze Z \ze