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Chapter 1

Class Index

1.1 Class List

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2 Class Index

Chapter 2

File Index

2.1 File List

Here is a list of all documented files with brief descriptions:

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Chapter 3

Class Documentation

3.1 APSP Class Reference

```
All-Pairs Shortest Path (APSP) class.
```

```
#include <algorithms.hpp>
```

Public Member Functions

• APSP (int n)

Constructor for the APSP class.

void addEdge (int i, int j, int cost)

Adds an edge to the graph.

• int getCost (int i, int j)

Gets the cost of the edge from vertex i to vertex j.

void printAdjacency (std::ostream &out=std::cout)

Prints the adjacency matrix of the graph.

3.1.1 Detailed Description

All-Pairs Shortest Path (APSP) class.

This class implements the Floyd-Warshall algorithm to find the shortest paths between all pairs of vertices in a directed, weighted graph. Negative vertex cycles will be detected and will throw runtime errors.

3.1.2 Constructor & Destructor Documentation

3.1.2.1 APSP()

```
APSP::APSP (
          int n) [inline]
```

Constructor for the APSP class.

Initializes the adjacency matrix for n vertices.

Parameters

n Number of vertices in the graph

3.1.3 Member Function Documentation

3.1.3.1 addEdge()

```
void APSP::addEdge (
    int i,
    int j,
    int cost) [inline]
```

Adds an edge to the graph.

Parameters

i	The starting vertex (0-indexed)
j	The ending vertex (0-indexed)
cost	The cost of the edge from vertex i to vertex j

3.1.3.2 getCost()

Gets the cost of the edge from vertex i to vertex j.

Parameters

i	The starting vertex (0-indexed)
j	The ending vertex (0-indexed)

3.1.3.3 printAdjacency()

Prints the adjacency matrix of the graph.

Parameters

out Output stream to print to (default is std::cout

The documentation for this class was generated from the following file:

 $\bullet \ / Users/jace/Documents/GitHub/CPP-Structs-Algorithms/algorithms.hpp$

3.2 CircularDynamicArray< elmtype > Class Template Reference

Implements a circular dynamic array that can dynamically resize itself.

#include <datastructs.hpp>

Public Member Functions

• CircularDynamicArray ()

Default Constructor.

CircularDynamicArray (int capacity)

Constructor for a set capacity.

CircularDynamicArray (CircularDynamicArray const &src)

Copy constructor (deep copy)

∼CircularDynamicArray ()

Destructor.

• int length ()

Returns the size of the array.

• int capacity ()

Returns the capacity of the array.

• elmtype atRef (int i)

Returns the value of the element at index i.

elmtype * atPoint (int i)

Returns a pointer to the element at index i.

• elmtype & operator[] (int i)

Bracket operator. Returns burner element if index is invalid.

CircularDynamicArray & operator= (const CircularDynamicArray &R)

Equals operator. Deep copies all values.

void addFront (elmtype v)

Adds an element to the front of the array.

void addEnd (elmtype v)

Adds an element to the end of the array.

void delFront ()

Removes the element at the front of the array.

• void delEnd ()

Removes the element at the end of the array.

· void clear ()

Clears all array data and resets the array to its default state.

void swap (elmtype *a, elmtype *b)

Swaps two elements.

elmtype QuickSelect (int k)

Returns the Kth smallest element of the array using the median as the partition element.

elmtype WCSelect (int k)

Returns the Kth smallest element of the array using the median of medians (subarray size = 5) as the partition element.

void stableSort ()

Performs a mergesort on the array.

• int linearSearch (elmtype e)

Performs a linear search for element e.

• int binSearch (elmtype e)

Performs a binary search for element e.

3.2.1 Detailed Description

```
template<typename elmtype> class CircularDynamicArray< elmtype >
```

Implements a circular dynamic array that can dynamically resize itself.

Template Parameters

elmtype The type of element stored in the circular dynamic array

3.2.2 Constructor & Destructor Documentation

3.2.2.1 CircularDynamicArray() [1/3]

```
template<typename elmtype>
CircularDynamicArray< elmtype >::CircularDynamicArray () [inline]
```

Default Constructor.

Initializes the circular dynamic array with a capacity of 2. End is set to -1 for addEnd() and addFront() functionality.

3.2.2.2 CircularDynamicArray() [2/3]

Constructor for a set capacity.

Initializes the circular dynamic array with a set capacity. End is set to capacity - 1 for addEnd() and addFront() functionality.

Parameters

capacity The capacity of the circular dynamic array

3.2.2.3 CircularDynamicArray() [3/3]

Copy constructor (deep copy)

Deep copies all values from the source circular dynamic array

Parameters

src The source circular dynamic array to copy

3.2.2.4 ∼CircularDynamicArray()

```
template<typename elmtype>
CircularDynamicArray< elmtype >::~CircularDynamicArray () [inline]
```

Destructor.

Deletes the array data

3.2.3 Member Function Documentation

3.2.3.1 addEnd()

Adds an element to the end of the array.

Time complexity: O(1) (Amortized)

3.2.3.2 addFront()

Adds an element to the front of the array.

Time complexity: O(1) (Amortized)

3.2.3.3 binSearch()

Performs a binary search for element e.

Time complexity: O(lg(size))

Parameters

e The element to search for

Returns

The index of the element if found, -1 otherwise

3.2.3.4 delEnd()

```
template<typename elmtype>
void CircularDynamicArray< elmtype >::delEnd () [inline]
```

Removes the element at the end of the array.

Time complexity: O(1) (Amortized)

3.2.3.5 delFront()

```
template<typename elmtype>
void CircularDynamicArray< elmtype >::delFront () [inline]
```

Removes the element at the front of the array.

Time complexity: O(1) (Amortized)

3.2.3.6 linearSearch()

Performs a linear search for element e.

Time complexity: O(size)

Parameters

e The element to search for

Returns

The index of the element if found, -1 otherwise

3.2.3.7 QuickSelect()

Returns the Kth smallest element of the array using the median as the partition element.

Time complexity: O(size)

Parameters

k The index of the element to find

Returns

The Kth smallest element of the array

3.3 Fib Class Reference

3.2.3.8 stableSort()

```
template<typename elmtype>
void CircularDynamicArray< elmtype >::stableSort () [inline]
```

Performs a mergesort on the array.

Time complexity: O(size * lg(size))

3.2.3.9 WCSelect()

Returns the Kth smallest element of the array using the median of medians (subarray size = 5) as the partition element.

Time complexity: O(size)

Parameters

k The index of the element to find

Returns

The Kth smallest element of the array

The documentation for this class was generated from the following file:

• /Users/jace/Documents/GitHub/CPP-Structs-Algorithms/datastructs.hpp

3.3 Fib Class Reference

Calculates fibonacci numbers using a recursive, dynamic programming approach.

```
#include <algorithms.hpp>
```

Public Member Functions

• Fib ()

Constructor to initialize the Fibonacci class.

void print (int n, std::ostream &out=std::cout)

Print the Fibonacci number for a given n.

void printAll (int n, std::ostream &out=std::cout)

Print all Fibonacci numbers from 0 to n.

3.3.1 Detailed Description

Calculates fibonacci numbers using a recursive, dynamic programming approach.

3.3.2 Constructor & Destructor Documentation

3.3.2.1 Fib()

```
Fib::Fib () [inline]
```

Constructor to initialize the Fibonacci class.

Initializes the first two Fibonacci numbers and clears the rest of the array

3.3.3 Member Function Documentation

3.3.3.1 print()

```
void Fib::print (
          int n,
          std::ostream & out = std::cout) [inline]
```

Print the Fibonacci number for a given n.

Parameters

n The integer value for which to calculate and print the Fibonacci number

3.3.3.2 printAll()

```
void Fib::printAll (
                int n,
                 std::ostream & out = std::cout) [inline]
```

Print all Fibonacci numbers from 0 to n.

Parameters

n Max number to print Fibonacci numbers for (inclusive) (max 185)

The documentation for this class was generated from the following file:

• /Users/jace/Documents/GitHub/CPP-Structs-Algorithms/algorithms.hpp

${\bf 3.4}\quad {\bf Heap < keyType > Class\ Template\ Reference}$

Implements a Minimum Heap.

#include <datastructs.hpp>

Public Member Functions

• Heap ()

Default Constructor.

• **Heap** (keyType K[], int s)

Constructs a heap with keys K and size s.

• \sim Heap ()

Destructor.

• int size ()

Returns the size of the heap.

• keyType peekKey ()

Returns the minimum key in the heap.

void insert (keyType k)

Inserts a new node with key k.

void printKeys (std::ostream &out=std::cout)

Prints all keys in the heap in level order.

keyType extractMin ()

Removes the minimum key from the heap and restores heap priority.

3.4.1 Detailed Description

```
template<typename keyType> class Heap< keyType >
```

Implements a Minimum Heap.

Template Parameters

keyType The type of key stored in the heap

3.4.2 Member Function Documentation

3.4.2.1 extractMin()

```
template<typename keyType>
keyType Heap< keyType >::extractMin () [inline]
```

Removes the minimum key from the heap and restores heap priority.

Time complexity: O(lg(n)), n = size

Returns

The minimum key

3.4.2.2 insert()

Inserts a new node with key k.

Time complexity: O(lg(n)), n = size

Parameters

k The key to insert

3.4.2.3 peekKey()

```
template<typename keyType>
keyType Heap< keyType >::peekKey () [inline]
```

Returns the minimum key in the heap.

Time complexity: O(1)

Returns

The minimum key

3.4.2.4 printKeys()

Prints all keys in the heap in level order.

Parameters

out The output stream to print to, defaulting to std::cout

The documentation for this class was generated from the following file:

• /Users/jace/Documents/GitHub/CPP-Structs-Algorithms/datastructs.hpp

3.5 Knapsack Class Reference

Stores information for and solves the 0-1 knapsack problem using dynamic programming.

```
#include <algorithms.hpp>
```

3.6 LCS Class Reference 15

Public Member Functions

```
    Knapsack (int n, int max, int *p, int *w)
```

Constructor.

• void printTable ()

Print the dynamic programming table for the knapsack problem.

void printPWO (std::ostream &out=std::cout)

Print the profits, weights, and objects chosen for the knapsack problem.

• int getProfit ()

Get the maximum profit of the knapsack problem.

3.5.1 Detailed Description

Stores information for and solves the 0-1 knapsack problem using dynamic programming.

3.5.2 Constructor & Destructor Documentation

3.5.2.1 Knapsack()

```
Knapsack::Knapsack (
    int n,
    int max,
    int * p,
    int * w) [inline]
```

Constructor.

NOTE: p and w MUST be 1-indexed

Parameters

n	Number of items in the knapsack		
max	Maximum weight of the knapsack		
p Array of profits for each item (1-indexe			
W	Array of weights for each item (1-indexed)		

The documentation for this class was generated from the following file:

• /Users/jace/Documents/GitHub/CPP-Structs-Algorithms/algorithms.hpp

3.6 LCS Class Reference

Finds the longest common subsequence (LCS) of two strings.

```
#include <algorithms.hpp>
```

Public Member Functions

```
• LCS (std::string a, std::string b)
```

Constructor to initialize the LCS object.

• ∼LCS ()

Destructor for the LCS object.

• std::string get ()

Retrieve the longest common subsequence of the two strings.

• int lcsLength ()

Get the length of the longest common subsequence.

• void printMatrix ()

Print the matrix used to find the LCS.

void newStrings (std::string a, std::string b)

Update the strings for which to find the LCS.

3.6.1 Detailed Description

Finds the longest common subsequence (LCS) of two strings.

Functions requiring the LCS will calculate it before returning.

3.6.2 Constructor & Destructor Documentation

3.6.2.1 LCS()

Constructor to initialize the LCS object.

Parameters

	First std::string for which to find the LCS
b	Second std::string for which to find the LCS

3.6.2.2 ∼LCS()

```
LCS::\sim LCS () [inline]
```

Destructor for the LCS object.

Nothing special, but destructor should be declared even if empty

3.7 Matrix Class Reference 17

3.6.3 Member Function Documentation

3.6.3.1 get()

```
std::string LCS::get () [inline]
```

Retrieve the longest common subsequence of the two strings.

Returns

The longest common subsequence of the two strings

3.6.3.2 newStrings()

Update the strings for which to find the LCS.

Parameters

а	New first std::string for which to find the LCS
b	New second std::string for which to find the LCS

The documentation for this class was generated from the following file:

• /Users/jace/Documents/GitHub/CPP-Structs-Algorithms/algorithms.hpp

3.7 Matrix Class Reference

Represents a matrix.

```
#include <algorithms.hpp>
```

Public Member Functions

```
    Matrix (std::vector< std::vector< int > > m)
```

Default constructor.

• Matrix (int r, int c)

Constructor with dimensions; initializes the matrix with 0s.

• bool operator== (const Matrix &m)

Equality operator for matrices.

• void clear ()

Clears the matrix data.

void print (std::ostream &out=std::cout)

Prints the matrix.

Public Attributes

• int row

Number of rows in the matrix.

• int col

Number of columns in the matrix.

• std::vector < std::vector < int > > data

Data of the matrix.

3.7.1 Detailed Description

Represents a matrix.

3.7.2 Member Function Documentation

3.7.2.1 print()

Prints the matrix.

Parameters

```
out Output stream to print to (default is std::cout)
```

The documentation for this class was generated from the following file:

• /Users/jace/Documents/GitHub/CPP-Structs-Algorithms/algorithms.hpp

3.8 MatrixChain Class Reference

Represents a chain of matrices.

```
#include <algorithms.hpp>
```

Public Member Functions

```
    MatrixChain (std::vector< Matrix * > m)
```

Copy constructor (deep copy)

void addMatrix (Matrix *m)

Add a matrix to the chain.

• Matrix * solve ()

Multiply the matrices and return the product.

3.8.1 Detailed Description

Represents a chain of matrices.

Given a chain of matrices, this class finds the optimal parenthesization of the matrices and returns the product

The documentation for this class was generated from the following file:

/Users/jace/Documents/GitHub/CPP-Structs-Algorithms/algorithms.hpp

3.9 RBNode< keyType, valueType > Class Template Reference

Node for a Red-Black Tree.

```
#include <datastructs.hpp>
```

Public Member Functions

• RBNode ()

Default constructor.

RBNode (keyType k, valueType v)

Constructor for a node with specified key and value.

• RBNode (bool nilCon)

Constructor for a nil node.

• RBNode (keyType k, valueType v, color setc, int s, RBNode< keyType, valueType > *parent)

Constructor for a node with specified key, value, color, size, and parent.

RBNode (const RBNode < keyType, valueType > &src)

Copy constructor (deep copy)

• ∼RBNode ()

Destructor.

void cascade (RBNode *nil)

Deletes a node and all its children.

RBNode & operator= (RBNode R)

Copy equals operator.

void preorder (std::ostream &out=std::cout)

Prints the preorder traversal of the tree.

void inorder (std::ostream &out=std::cout)

Prints the inorder traversal of the tree.

void postorder (std::ostream &out=std::cout)

Prints the postorder traversal of the tree.

void printNode (std::ostream &out=std::cout)

Prints the node's key.

void printk (int &k, std::ostream &out=std::cout)

Prints the K smallest elements of the subtree rooted at this node.

valueType * searchValue (keyType k)

Searches for the node with key k and returns a pointer to the value.

RBNode< keyType, valueType > * searchNode (keyType k)

Searches the subtree rooted at this node for the node with key k.

RBNode< keyType, valueType > * predecessor ()

Returns the predecessor of the node.

RBNode< keyType, valueType > * min ()

Returns the smallest node of the subtree rooted at this node.

keyType select (int k)

Returns the Kth smallest element in the subtree rooted at this node.

Public Attributes

keyType * key

The key of the node.

valueType * val

The value of the node.

• RBNode * I

The left child of the node.

RBNode * r

The right child of the node.

RBNode * p

The parent of the node.

· color c

The color of the node.

· int size

The size of the subtree rooted at this node.

3.9.1 Detailed Description

template<typename keyType, typename valueType> class RBNode< keyType, valueType >

Node for a Red-Black Tree.

This class represents a node in a Red-Black Tree. It contains pointers to its left and right children, its parent, and its key and value. It also contains the color of the node (Red or Black) and the size of the subtree rooted at this node.

This class also has all of its elements set to public. This is because it is not intended to be used on its own; rather, it is for use by the RBTree class, which requires direct access to the node's elements to avoid unnecessary function calls.

Template Parameters

keyType	The type of key stored in the node
valueType	The type of value stored in the node

3.9.2 Constructor & Destructor Documentation

3.9.2.1 RBNode() [1/4]

```
template<typename keyType, typename valueType>
RBNode< keyType, valueType >::RBNode () [inline]
```

Default constructor.

Initializes the node with default values. The key and value pointers are dynamically allocated. Color is set to Red.

3.9.2.2 RBNode() [2/4]

Constructor for a node with specified key and value.

Initializes the node with the specified key and value. The color is set to Red, size is set to 1, and relatives are set to null.

Parameters

k	The key of the node
V	The value of the node

3.9.2.3 RBNode() [3/4]

Constructor for a nil node.

Initializes the node as a nil node. The key and value pointers are set to null, and the color is set to Black.

Parameters

3.9.2.4 RBNode() [4/4]

Constructor for a node with specified key, value, color, size, and parent.

Parameters

k	The key of the node
V	The value of the node
setc	The color of the node
s	The size of the subtree rooted at this node
parent	The parent of the node

3.9.2.5 ∼RBNode()

```
template<typename keyType, typename valueType>
RBNode< keyType, valueType >::~RBNode () [inline]
```

Destructor.

Checks if the key and value pointers are not null before deleting them.

3.9.3 Member Function Documentation

3.9.3.1 cascade()

Deletes a node and all its children.

Deletes the node and all its children recursively. The nil node is passed as a parameter to avoid deleting it.

Parameters

nil The nil node of the tree

3.9.3.2 inorder()

Prints the inorder traversal of the tree.

Parameters

out The output stream to print, default is cout

3.9.3.3 min()

```
template<typename keyType, typename valueType>
RBNode< keyType, valueType > * RBNode< keyType, valueType >::min () [inline]
```

Returns the smallest node of the subtree rooted at this node.

Returns the smallest node of the subtree rooted at this node. The smallest node is the leftmost node in the subtree. If the left child is null, it returns this node. Time complexity is O(lg(size))

Returns

A pointer to the smallest node in the subtree rooted at this node

3.9.3.4 postorder()

Prints the postorder traversal of the tree.

Parameters

out The output stream to print, default is cout

3.9.3.5 predecessor()

```
template<typename keyType, typename valueType>
RBNode< keyType, valueType > * RBNode< keyType, valueType >::predecessor () [inline]
```

Returns the predecessor of the node.

Returns the predecessor of the node. The predecessor is the largest node in the left subtree. If the left child is null, it returns nullptr. Time complexity is O(lg(size))

Returns

A pointer to the predecessor node, or nullptr if the left child is null

3.9.3.6 preorder()

Prints the preorder traversal of the tree.

Parameters

out The output stream to print, default is cout

3.9.3.7 printk()

Prints the K smallest elements of the subtree rooted at this node.

Prints the K smallest elements of the subtree rooted at this node. The function is called recursively on the left and right children. Time complexity is $O(k + \lg(size))$

Parameters

k The number of elements to print

3.9.3.8 printNode()

Prints the node's key.

Parameters

out The output stream to print, default is cout

3.9.3.9 searchNode()

Searches the subtree rooted at this node for the node with key k.

Performs a DFS search for the node with key k. If the key is found, it returns a pointer to the node. Otherwise, it returns nullptr. Time complexity is O(lg(size))

Parameters

```
k The key to search for
```

Returns

A pointer to the node with key k, or nullptr if the key is not found

3.9.3.10 searchValue()

Searches for the node with key k and returns a pointer to the value.

Performs a DFS search for the node with key k. If the key is found, it returns a pointer to the value of the node. Otherwise, it returns nullptr. Time complexity is O(lg(size))

Parameters

```
k The key to search for
```

Returns

A pointer to the value of the node with key k, or nullptr if the key is not found

3.9.3.11 select()

Returns the Kth smallest element in the subtree rooted at this node.

Returns the Kth smallest element in the subtree rooted at this node. The function is called recursively on the left and right children. Time complexity is O(lg(size))

Parameters

k The index of the smallest element to return

The documentation for this class was generated from the following file:

• /Users/jace/Documents/GitHub/CPP-Structs-Algorithms/datastructs.hpp

3.10 RBTree < keyType, valueType > Class Template Reference

Implements a Red-Black Tree.

#include <datastructs.hpp>

Public Member Functions

· RBTree ()

Default constructor.

• RBTree (keyType k, valueType v)

Constructs a tree with a single node with key k and value v.

RBTree (keyType *k, valueType *v, int s)

Constructs a tree with arrays k and v as the insert values and size = s.

RBTree (const RBTree < keyType, valueType > &src)

Copy constructor (deep copy)

∼RBTree ()

Destructor.

RBTree< keyType, valueType > & operator= (const RBTree< keyType, valueType > &R)

Copy equals operator.

void preorder (std::ostream &out)

Prints the preorder traversal of the tree.

· void inorder (std::ostream &out)

Prints the inorder traversal of the tree.

void postorder (std::ostream &out)

Prints the postorder traversal of the tree.

void printk (int k, std::ostream &out)

Prints the K smallest elements of the tree.
• int size ()

Returns the size of the tree.

valueType * search (keyType k)

Searches the tree for key k and returns a pointer to the node's value.

void insert (keyType k, valueType v)

Inserts a new node with key k and value v into the tree.

int remove (keyType k)

Removes the node with key k from the tree.

int rank (keyType k)

Returns the rank of the node with key k.

keyType select (int k)

Returns the Kth smallest element in the tree.

keyType * successor (keyType k)

Finds the successor of the node with key k and returns a pointer to its key.

keyType * predecessor (keyType k)

Finds the predecessor of the node with key k and returns a pointer to its key.

3.10.1 Detailed Description

template<typename keyType, typename valueType> class RBTree< keyType, valueType >

Implements a Red-Black Tree.

Template Parameters

keyType	The type of key stored in the tree
valueType	The type of value stored in the tree

This class implements a Red-Black Tree, a self-balancing binary search tree. It maintains balance using rotations and recoloring during insertions and deletions, ensuring efficient operations with a time complexity of O(log n).

The tree has the following properties:

- · Each node has a color (Red or Black).
- · The root node is always Black.
- Red nodes cannot have Red children (no two consecutive Red nodes).
- · Every path from a node to its descendant nil nodes has the same number of Black nodes (Black height).
- The nil node (a sentinel node representing the end of the tree) is always Black.

These properties ensure that the tree remains approximately balanced, making it suitable for applications requiring fast lookups, insertions, and deletions.

3.10.2 Constructor & Destructor Documentation

3.10.2.1 RBTree() [1/2]

Constructs a tree with a single node with key k and value v.

This constructor initializes the tree with a single node with the given key and value. The nil node is created, and the root is set to the new node. The color of the root is set to Black. Time complexity: O(1)

Parameters

k	The key of the root node
V	The value of the root node

3.10.2.2 RBTree() [2/2]

Constructs a tree with arrays k and v as the insert values and size = s.

This constructor initializes the tree with the given arrays of keys and values. It creates a nil node and inserts each key-value pair into the tree. The root is set to nil initially. Time complexity: O(s)

Note

If s is larger than the size of either array, this will cause a segmentation fault. Any s smaller than the size of either array will work up to the specified index, but the rest of the array will be ignored.

Parameters

k	The array of keys to insert
V	The array of values to insert
s	The size of the arrays

3.10.2.3 ∼RBTree()

```
template<typename keyType, typename valueType>
RBTree< keyType, valueType >::~RBTree () [inline]
```

Destructor.

This destructor deletes the tree by calling the cascade function on the root node. The cascade function recursively deletes all nodes in the tree. Time complexity: O(size)

3.10.3 Member Function Documentation

3.10.3.1 inorder()

Prints the inorder traversal of the tree.

This function prints the inorder traversal of the tree. It calls the root's inorder function, which prints the nodes in inorder. Time complexity: O(n)

3.10.3.2 insert()

Inserts a new node with key k and value v into the tree.

This function inserts a new node with key k and value v into the tree. It first creates a new node and sets its size to 1. Then, it traverses the tree to find the correct position for the new node. Finally, it calls the insertFixTree function to restore the Red-Black Tree properties. Time complexity: O(lg(size))

Parameters

k	The key of the new node
V	The value of the new node

3.10.3.3 operator=()

Copy equals operator.

This operator assigns the values of the source tree to the current tree. It first deletes the current tree and then copies the values from the source tree. Time complexity: O(n), n = R.root->size

Parameters

```
R The source tree to copy from
```

Returns

A reference to the current tree

3.10.3.4 postorder()

Prints the postorder traversal of the tree.

This function prints the postorder traversal of the tree. It calls the root's postorder function, which prints the nodes in postorder. Time complexity: O(n)

3.10.3.5 predecessor()

Finds the predecessor of the node with key k and returns a pointer to its key.

This function finds the predecessor of the node with key k. The predecessor is the largest node in the left subtree. If the left child is null, it returns nullptr. Time complexity: O(lg(size))

Parameters

```
k The key of the node whose predecessor is to be found
```

Returns

A pointer to the key of the predecessor node, or nullptr if there is no predecessor

3.10.3.6 preorder()

Prints the preorder traversal of the tree.

This function prints the preorder traversal of the tree. It calls the root's preorder function, which prints the nodes in preorder. Time complexity: O(n)

3.10.3.7 printk()

Prints the K smallest elements of the tree.

This function prints the K smallest elements of the tree. It calls the root's printk function, which prints the K smallest elements in preorder traversal. Time complexity: O(k + lg(size))

3.10.3.8 rank()

Returns the rank of the node with key k.

This function returns the rank of the node with key k. The rank is the number of nodes with keys less than k. If the key is not found, it returns 0. Time complexity: O(lg(root->size))

3.10.3.9 remove()

Removes the node with key k from the tree.

This function removes the node with key k from the tree. It first searches for the node with key k. If the node is found, it removes it and restores the Red-Black Tree properties. Time complexity: $O(\lg(size))$

Parameters

```
k The key of the node to be removed
```

Returns

1 if the node was removed, 0 if the node was not found.

3.10.3.10 search()

Searches the tree for key k and returns a pointer to the node's value.

This function searches the tree for key k and returns a pointer to the node's value. If the key is not found, it returns nullptr. Time complexity: O(lg(size))

Parameters

k The key to search for

Returns

A pointer to the value of the node with key k, or nullptr if the key is not found

3.10.3.11 select()

Returns the Kth smallest element in the tree.

Note

This function currently is delegated to a function in the Node but should be migrated to the tree. This was done due to the original project specifications.

This function returns the Kth smallest element in the tree. The Kth smallest element is the node with rank k. If k is out of bounds or not found, it returns nullptr.

Parameters

k The rank of the smallest element to return

Returns

A pointer to the Kth smallest element in the tree, or nullptr if k is out of bounds

3.10.3.12 size()

```
template<typename keyType, typename valueType>
int RBTree< keyType, valueType >::size () [inline]
```

Returns the size of the tree.

Returns

The size of the tree

3.10.3.13 successor()

Finds the successor of the node with key k and returns a pointer to its key.

This function finds the successor of the node with key k. The successor is the smallest node in the right subtree. If the right child is null, it returns nullptr. Time complexity: O(lg(size))

32 Class Documentation

Parameters

k The key of the node whose successor is to be found

Returns

A pointer to the key of the successor node, or nullptr if there is no successor

The documentation for this class was generated from the following file:

 $\bullet \ \ / Users/jace/Documents/GitHub/CPP-Structs-Algorithms/datastructs.hpp$

Chapter 4

File Documentation

4.1 /Users/jace/Documents/GitHub/CPP-Structs Algorithms/algorithms.hpp

```
00001
00014
00015 #ifndef ALGORITHMS_H
00016 #define ALGORITHMS_H
00018 #include <iostream>
00019 #include <climits>
00020 #include <vector>
00021 #include <ctime>
00022
00030 class APSP {
00031
00037
          std::vector< std::vector<int> > adjacency;
00038
00042
          int n:
00043
          bool built;
00048
00052
          void build() {
             for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        for (int k = 0; k < n; k++) {
00053
00054
00055
                           if (adjacency[j][i] == INT_MAX || adjacency[i][k] == INT_MAX) {
00056
00057
00058
                           if (adjacency[j][i] + adjacency[i][k] < adjacency[j][k]) {</pre>
00059
00060
                                adjacency[j][k] = adjacency[j][i] + adjacency[i][k];
00061
00062
                       }
00063
                  }
00064
00065
              // After table is built, check for negative cycles and set built to true
00066
00067
              checkNegativeCycle();
00068
              built = true;
         }
00070
00074
          void checkNegativeCycle() {
00075
             for (int i = 0; i < n; i++) {</pre>
00076
                  if (adjacency[i][i] < 0) {</pre>
                       throw std::runtime_error("Negative cycle detected at vertex " + std::to_string(i) +
00077
     "\n");
00078
00079
08000
00081
00082
        public:
00083
00091
        APSP(int n) {
           this->n = n;
00092
00093
              built = false;
              for (int i = 0; i < n; i++) {
00094
00095
                  std::vector<int> row;
00096
                   for (int j = 0; j < n; j++) {
                       if (i == j) {
```

```
00098
                             row.push_back(0);
00099
                             continue;
00100
00101
                         row.push_back(INT_MAX);
00102
00103
                    adiacency.push back(row);
00104
               }
00105
00106
00114
           void addEdge(int i, int j, int cost) {
               adjacency[i][j] = cost;
00115
00116
                built = false;
00117
           }
00118
00125
           int getCost(int i, int j) {
00126
               if (!built) {
00127
                    build();
               }
00128
00129
00130
               return adjacency[i][j];
00131
00132
00138
           void printAdjacency(std::ostream &out = std::cout) {
00139
               if (!built) {
00140
                    build();
00141
00142
               for (int i = 0; i < n; i++) {
    std::cout « i + 1 « ": ";
    for (int j = 0; j < n; j++) {
        if (adjacency[i][j] == INT_MAX) {
            std::cout « "inf ";
        }
}</pre>
00143
00144
00145
00146
00147
00148
00149
00150
                         std::cout « adjacency[i][j] « " ";
00151
00152
                    std::cout « std::endl;
00153
               }
00154
           }
00155 };
00156
00160 class Fib {
00161
00162
           __uint128_t fibList[186];
00163
00169
           \__uint128_t fib(int *n) {
00170
                // Check if number is too large for __uint128_t
00171
                if (*n > 185) {
00172
00173
                    throw std::runtime_error("Fibonacci number too large for unsigned 128-bit int\n");
00174
00175
00176
                if (*n == 0) {
00177
                   return 0;
00178
               }
00179
00180
                // Check if number is stored
00181
                if (fibList[*n] != 0) {
00182
                    return fibList[*n];
00183
00184
                // If number is not stored, calculate it
00185
               int a = *n - 1;
int b = *n - 2;
00186
00187
00188
                fibList[*n] = fib(&a) + fib(&b);
00189
00190
               return fibList[*n];
00191
           }
00192
00193
           public:
00194
00200
           Fib() {
                \ensuremath{//} Set first two fibonacci numbers and clear all other data in map
00201
                fibList[0] = 0;
00202
                fibList[1] = 1;
for (int i = 2; i < 186; i++) {
00203
00204
00205
                    fibList[i] = 0;
00206
00207
           }
00208
00214
           void print(int n, std::ostream &out = std::cout) {
00215
00216
                 _uint128_t fibNum = fib(&n);
                if (fibNum == 0) {
    out « "fib(" « n « ") = 0\n";
00217
00218
00219
                    return;
00220
                }
```

```
00221
00222
               std::string fibString;
               while (fibNum > 0) {
00223
                  fibString.insert(fibString.begin(), '0' + (fibNum % 10));
00224
00225
                   fibNum /= 10;
00226
              }
00228
               out « "fib(" « n « ") = " « fibString « std::endl;
00229
          }
00230
00236
          void printAll(int n, std::ostream &out = std::cout) {
00237
00238
               if (n > 185) {
                   throw std::runtime_error("Cannot print Fibonacci numbers greater than 185 with unsigned
     128-bit intn");
00240
00241
00242
               // Print all fibonacci numbers up to n (inclusive)
               for (int i = 0; i < n; i++) {
00243
00244
                 print(i, out);
00245
00246
          }
00247 };
00248
00252 class Knapsack {
00253
00257
           int n;
00258
00262
          int max;
00263
00267
          int *weights:
00268
00272
          int *profits;
00273
00277
          bool built;
00278
00282
          bool *objects;
00283
00287
          std::vector< std::vector<int> > table;
00288
00292
          void build() {
00293
               // Table building loop
00294
               for (int j = 0; j <= n; j++) {
    for (int k = 0; k <= max; k++) {
00295
00296
00297
                        if (j == 0) {
00298
                            table[j][k] = 0;
                        } else if (k < weights[j]) {
   table[j][k] = table[j - 1][k];</pre>
00299
00300
00301
                        } else {
                            // max() function is not functioning properly, so I manually find the max
00302
00303
                                a = table[j - 1][k],
00304
00305
                                b = table[j - 1][k - weights[j]] + profits[j];
                            if (a > b) {
00306
00307
                                table[j][k] = a;
00308
                            } else {
00309
                                table[j][k] = b;
00310
                            }
00311
                        }
00312
                   }
00313
00314
00315
               // After table is built, choose the objects and set built to true
00316
               choose();
00317
              built = true;
00318
          }
00319
00323
          void choose() {
00324
00325
               \ensuremath{//} Start at the bottom right corner of the table and work backwards
               int k = max;
00326
               for (int i = n; i > 0; i--) {
   if (table[i-1][k] == table[i][k]) {
      objects[i] = false;
00327
00328
00329
00330
                   } else {
00331
                       objects[i] = true;
00332
                        k -= weights[i];
00333
                   }
00334
              }
00335
          }
00336
00337
00338
00349
          Knapsack(int n, int max, int *p, int *w) {
00350
00351
              this->n = n;
```

```
00352
                this->max = max;
00353
                built = false;
                objects = new bool[n+1];
weights = w;
00354
00355
                profits = p;
00356
00357
00358
                for (int i = 0; i <= n; i++) {</pre>
00359
                     std::vector<int> temp;
00360
                     for (int j = 0; j \le max; j++) {
00361
                          temp.push_back(0);
00362
00363
                     table.push_back(temp);
00364
                }
00365
00366
00370
           void printTable() {
                for (int i = 0; i <= n; i++) {
    for (int j = 0; j <= max; j++) {
        std::cout « table[i][j] « " ";</pre>
00371
00372
00373
00374
00375
                     std::cout « std::endl;
00376
                }
00377
           }
00378
00382
           void printPWO(std::ostream &out = std::cout) {
00383
              if (!built) {
00384
                     build();
00385
                out « "Profit: ";

for (int i = 1; i <= n; i++) {

   out « profits[i] « " ";
00386
00387
00388
00389
00390
                out « std::endl;
00391
                out « "Weight: ";
                for (int i = 1; i <= n; i++) {
  out « weights[i] « " ";</pre>
00392
00393
00394
00395
                out « std::endl;
00396
                out « "Objects Chosen: ";
                for (int i = 1; i <= n; i++) {
    out « objects[i] « " ";</pre>
00397
00398
00399
                }
00400
           }
00401
00405
           int getProfit() {
00406
                if (!built) {
00407
                     build();
00408
00409
                return table[n][max];
00410
00411
00412 };
00413
00421 class LCS {
00422
00423
           private:
00424
00428
                std::string s1;
00429
00433
                std::string s2;
00434
00438
                std::string foundLCS;
00439
00443
                std::vector< std::vector<int> > L;
00444
00448
                bool built;
00449
                std::string build(int j, int k) {
    if (j == 0 || k == 0) {
        return "";
00458
00459
00460
00461
                     if (s1[j - 1] == s2[k - 1]) {
00462
                         return build(j - 1, k - 1) + s1[j - 1];
00463
00464
                     if (L[j][k - 1] >= L[j - 1][k]) {
    return build(j, k - 1);
00465
00466
00467
                     } else {
00468
                         return build(j - 1, k);
00469
                     }
00470
                }
00471
00472
           public:
00473
00480
                LCS(std::string a, std::string b) : s1(std::move(a)), s2(std::move(b)), built(false) {}
00481
                ~LCS() {
00487
00488
                }
```

```
00489
00495
                std::string get() {
00496
                    if (built)
00497
                          return foundLCS;
00498
00499
                    int n = s1.length();
00500
00501
                     int m = s2.length();
00502
                    L = std::vector < std::vector < int > (n + 1, std::vector < int > (m + 1, 0));
00503
                     for (int j = 1; j \le n; j++) {
00504
                         for (int k = 1; k <= m; k++) {
    if (s1[j-1] == s2[k-1]) {
00505
00506
00507
                                   L[j][k] = L[j-1][k-1] + 1;
00508
                              } else
00509
                                   L[j][k] = std::max(L[j-1][k], L[j][k-1]);
                              }
00510
00511
                          }
00512
                     }
00513
00514
                     foundLCS = build(n, m);
                    built = true;
return foundLCS;
00515
00516
00517
                }
00518
00522
                int lcsLength() {
00523
                     if (!built)
00524
                         get();
00525
00526
                     return foundLCS.length();
00527
                }
00528
00532
                void printMatrix() {
00533
00534
                     // Ensure LCS is built before printing the matrix
                     if (!built) {
00535
00536
                          get();
00537
00538
                    std::cout « "Matrix L: " « std::endl;
for (int i = 0; i <= s1.length(); i++) {
    for (int j = 0; j <= s2.length(); j++) {
        std::cout « L[i][j] « " ";</pre>
00539
00540
00541
00542
00543
00544
                          std::cout « std::endl;
00545
                    }
00546
                }
00547
                void newStrings(std::string a, std::string b) {
00554
00555
                   s1 = a;
                     s2 = b;
00556
00557
                    built = false;
00558
                     foundLCS = "";
00559
                    L.clear();
00560
00561 };
00562
00569 class Matrix {
00570
         public:
00571
00575
           int row;
00576
00580
           int col;
00581
00585
           std::vector< std::vector<int> > data;
00586
00590
           Matrix(std::vector< std::vector<int> > m): row(m.at(0).size()), col(m.size()), data(m) {};
00591
00595
           Matrix(int r, int c) : row(r), col(c), data(r, std::vector<int>(c, 0)) {}
00596
00600
           bool operator==(const Matrix &m) {
00601
                if (row != m.row || col != m.col) {
00602
                    return false;
00603
                for (int i = 0; i < row; i++) {
    for (int j = 0; j < col; j++) {
        if (data[i][j] != m.data[i][j]) {</pre>
00604
00605
00606
00607
                              return false;
00608
00609
                    }
00610
                }
00611
                return true;
00612
           }
00613
00617
           void clear() {
               row = -1;

col = -1;
00618
00619
```

```
data.clear();
00621
           }
00622
00628
           void print(std::ostream &out = std::cout) {
               for (int i = 0; i < col; i++) {
   for (int j = 0; j < row; j++) {
     out « data[i][j] « " ";</pre>
00629
00630
00631
00632
00633
                     out « std::endl;
00634
                }
00635
           }
00636 };
00637
00646 class MatrixChain {
00647
00651
           int n;
00652
00656
           bool calculated;
00657
00661
           Matrix *solution;
00662
00666
           Matrix *bestK;
00667
00671
           Matrix *cost:
00672
00676
           std::vector<int> dim;
00677
00681
           std::vector<Matrix*> data;
00682
00686
           void calcCosts() {
               for (int L = 1; L < n; L++) {
   for (int i = 0; i < n - L; i++) {
      int j = i + L;
   }</pre>
00687
00688
00689
                          cost->data[i][j] = INT_MAX;
for (int k = i; k < j; k++) {
   int q = cost->data[i][k] + cost->data[k + 1][j] + dim[i] * dim[k + 1] * dim[j +
00690
00691
00692
      1];
00693
                               if (q < cost->data[i][j]) {
00694
                                    cost->data[i][j] = q;
00695
                                    bestK->data[i][j] = k;
00696
00697
                          }
00698
                     }
00699
                }
00700
00701
00705
           Matrix *matrixMult(Matrix *a, Matrix *b) {
                Matrix *c = new Matrix(a->row, b->col);
for (int i = 0; i < a->row; i++) {
00706
00707
                     for (int j = 0; j < b->col; j++) {
    for (int k = 0; k < a->col; k++) {
00708
00709
00710
                               c->data[i][j] += a->data[i][k] * b->data[k][j];
00711
00712
                    }
00713
                }
00714
                return c;
00715
           }
00716
00725
           Matrix *chainProduct(int i, int j) {
               if (i == j) {
    return data[i];
00726
00727
00728
00729
                int k = bestK->data[i][j];
                Matrix *a = chainProduct(i, k);
Matrix *b = chainProduct(k + 1, j);
00730
00731
00732
                return matrixMult(a, b);
00733
           }
00734
00735
           public:
00736
00740
           MatrixChain(std::vector<Matrix*> m) {
00741
                n = m.size();
00742
                calculated = false;
00743
                solution = new Matrix(n, n);
00744
                bestK = new Matrix(n, n);
00745
                cost = new Matrix(n, n);
00746
00747
                for (int i = 0; i < n; i++) {</pre>
00748
                     data.push_back(m[i]);
00749
                }
00750
00751
                for (int i = 0; i < n; i++) {</pre>
00752
                     dim.push_back(m[i]->row);
00753
                     if (i == 0) {
00754
                          continue;
00755
00756
                     if (m[i-1]->col != m[i]->row) {
```

```
00757
                          throw std::runtime_error(
      "Matrix dimensions do not match in MatrixChain constructor between matrices " + std::to_string(i-1) + " and " + std::to_string(i) + "\n" + 

"Col size of matrix " + std::to_string(i-1) + " (" + std::to_string(m[i-1]->col) + 

") != Row size of matrix " + std::to_string(i) + " (" + std::to_string(m[i]->row)
00758
00759
00760
       + ")\n"
00761
                         );
00762
                     }
00763
               }
00764
           }
00765
           void addMatrix(Matrix *m) {
00769
                if (m->row != data[n - 1]->col) {
00770
00771
                     throw std::runtime_error("Matrix dimensions do not match in MatrixChain::addMatrix");
00772
00773
00774
00775
                 data.push_back(m);
                if (calculated) {
                     calculated = false;
00777
                     delete solution;
00778
00779
00780
                n++;
00781
           }
00782
00786
           Matrix *solve() {
00787
                if (!calculated)
                     calcCosts();
00788
00789
                     solution = chainProduct(0, n - 1);
00790
00791
                return solution;
00792
           }
00793
00794 };
00795
00806 std::vector<std::vector<double> worldSeries(int n, double *aProb) {
00807
            // Create matrix (Use std::vector as variable length array is not allowed in most compilers)
00809
           std::vector<std::vector<double> x(n + 1, std::vector<double>(n + 1, 0.0));
00810
00811
           for (int i = 0; i <= n; i++) {</pre>
                for (int j = 0; j <= n; j++) {</pre>
00812
00813
00814
                      // Base cases
                      if (i == 0 && j == 0) {
00816
                          x[0][0] = 1;
00817
                      } else if (i == n \&\& j == n) {
                          x[n][n] = 0;
00818
00819
00820
                      // Fill in matrix
                     } else if ((i != 0 && j == 0) || (i == n && j != n)) {
00821
                         x[i][j] = x[i - 1][j] * aProb[i + j];
lse if ((i == 0 && j != 0) || (i != n && j == n)) {
x[i][j] = x[i][j - 1] * (1 - aProb[i + j]);
00822
00823
                     } else i
00824
                     } else
00825
                          x[i][j] = x[i-1][j] * aProb[i+j] + x[i][j-1] * (1 - aProb[i+j]);
00826
00828
                }
00829
           }
00830
00831
           return x:
00832 }
00833
00834 #endif
```

4.2 /Users/jace/Documents/GitHub/CPP-Structs Algorithms/datastructs.hpp

```
00001
00011
00012 #ifndef DATASTRUCTS_H
00013 #define DATASTRUCTS_H
00014
00015 #include <iostream>
00016
00022 template <typename elmtype> class CircularDynamicArray {
00023
00024
         public:
00030
          CircularDynamicArray() {
              cap = 2;
size = 0;
00031
00032
```

```
00033
               start = 0;
               end = -1;
00034
00035
               info = new elmtype[2];
00036
          }
00037
00045
          CircularDynamicArray(int capacity) {
00046
              cap = capacity;
00047
               size = capacity;
00048
               start = 0;
00049
               end = capacity - 1;
               info = new elmtype[capacity];
00050
00051
          };
00052
00060
          CircularDynamicArray(CircularDynamicArray const &src) {
               cap = src.cap;
size = src.size;
start = src.start;
00061
00062
00063
00064
               end = src.end;
               elmtype *tempInfo = new elmtype[cap];
for (int i = 0; i < cap; i++) {</pre>
00065
00066
00067
                   tempInfo[i] = src.info[i];
00068
00069
               info = tempInfo;
00070
00071
00077
           ~CircularDynamicArray() { if (info != nullptr) {delete[] info;} };
00078
00082
          int length() { return size; }
00083
00087
          int capacity() { return cap; }
00088
00092
           elmtype atRef(int i) {
00093
               if (i < 0 || i > cap) {
00094
                   return burner;
00095
00096
               return info[(i + start) % cap];
00097
          }
00098
00102
           elmtype *atPoint(int i) {
00103
              if (i < 0 || i > cap) {
00104
                   return &burner;
00105
00106
               return &info[(i + start) % cap];
00107
           }
00108
00112
           elmtype &operator[](int i) {
00113
              if (i < 0 || i > cap) {
00114
                   return burner;
00115
00116
               return info[(i + start) % cap];
00117
          }
00118
00122
          CircularDynamicArray &operator=(const CircularDynamicArray &R) {
              cap = R.cap;
size = R.size;
start = R.start;
00123
00124
00125
00126
               end = R.end;
00127
               delete[] info;
00128
               info = new elmtype[cap];
               for (int i = 0; i < cap; i++) {
   info[i] = R.info[i];</pre>
00129
00130
00131
00132
               return *this;
00133
          }
00134
00140
          void addFront(elmtype v) {
00141
              checkCapIncrease();
00142
               if (start > 0) {
00143
                   info[start - 1] = v;
00144
               } else {
00145
                  info[cap - 1] = v;
00146
                   start = cap;
00147
00148
               start--;
00149
               size++;
00150
          };
00151
00157
          void addEnd(elmtype v) {
00158
               checkCapIncrease();
00159
               info[(end + 1) % cap] = v;
00160
               end++;
               end %= cap;
00161
               size++;
00162
00163
          }
00164
          void delFront() {
00170
00171
               start++;
```

```
00172
               start %= cap;
00173
00174
                checkCapDecrease();
00175
           } ;
00176
00182
           void delEnd() {
00183
               end--;
00184
               if (end == -1) {
00185
                   end = cap -1;
00186
00187
               size--:
               checkCapDecrease();
00188
00189
           };
00190
00194
           void clear() {
              size = 0;
cap = 2;
start = 0;
end = -1;
00195
00196
00197
00198
00199
                delete[] info;
00200
               info = new elmtype[cap];
00201
           };
00202
           void swap(elmtype *a, elmtype *b) {
  elmtype temp = (*a);
  (*a) = (*b);
00206
00207
00208
00209
                (*b) = temp;
00210
           }
00211
           elmtype QuickSelect(int k) {
00221
               if (k <= 0 || k > size) {
00222
00223
                   return burner;
00224
00225
                return select(k, standard);
00226
           }
00227
00237
           elmtype WCSelect(int k) {
               if (k <= 0 || k > size) {
00239
                    return burner;
00240
00241
                return select(k, worstCase);
00242
           }
00243
00249
           void stableSort() { mergeSort(0, size - 1); };
00250
00260
           int linearSearch(elmtype e) {
              for (int i = 0; i < size; i++) {
   if (atRef(i) == e) return i;</pre>
00261
00262
00263
00264
                return -1:
00265
           };
00266
00276
           int binSearch(elmtype e) {
               for (int m = size / 2, 1 = 0, r = size; 1 <= r; m = (r + 1) / 2) {
   if (e == atRef(m)) {</pre>
00277
00278
00279
                         return m;
00280
                    } else if (e > atRef(m)) {
00281
                        1 = m + 1;
00282
                    } else {
00283
                        r = m - 1;
                    }
00284
00285
               }
00286
               return -1;
00287
          }
00288
          private:
00289
           // Array Data
00290
00291
00295
          int cap;
00296
00300
           int size;
00301
00305
           int start;
00306
00310
           int end;
00311
00315
           elmtype *info;
00316
00320
           elmtype burner;
00321
           enum searchType { standard, worstCase };
00328
00329
00335
           void checkCapDecrease() {
00336
                if (((cap / 4) - 1) > size) {
                    elmtype *newArr = new elmtype[cap / 2];
for (int i = 0; i < size; i++) {
    newArr[i] = info[start + i];</pre>
00337
00338
00339
```

```
00340
00341
                     cap /= 2;
                     start = 0;
00342
                     delete[] info;
00343
00344
                    info = newArr;
00345
00346
                     if (size > 0) {
00347
                         end = size -1;
00348
                     } else {
                         end = 0;
00349
                    };
00350
00351
                }
00352
                return;
00353
           };
00354
00360
           void checkCapIncrease() {
00361
                if (size == cap) {
00362
                    elmtype *newArr = new elmtype[cap * 2];
for (int i = 0; i < size; i++) {</pre>
00363
00364
                         newArr[i] = info[(start + i) % cap];
00365
00366
                    delete[] this->info;
                    info = newArr;
cap *= 2;
00367
00368
00369
                    start = 0;
00370
                    end = size -1;
00371
                }
00372
                return;
00373
           };
00374
           void merge(int 1, int m, int r) {
   int sub1 = m - 1 + 1, sub2 = r - m;
00384
00385
00386
00387
                elmtype *linfo = new elmtype[sub1], *rinfo = new elmtype[sub2];
00388
                for (int i = 0; i < sub1; i++) {
  int tempIndex = (1 + i + start) % cap;</pre>
00389
00390
                     linfo[i] = info[tempIndex];
00392
                for (int j = 0; j < sub2; j++) {
   int tempIndex = (m + j + 1 + start) % cap;</pre>
00393
00394
                     rinfo[j] = info[tempIndex];
00395
00396
00397
00398
                int indexL = 0, indexR = 0, indexM = 1;
00399
00400
                // Primary Merge Loop
                while (indexL < sub1 && indexR < sub2) {</pre>
00401
                    if (linfo[indexL] <= rinfo[indexR]) {
  info[(indexM + start) % cap] = linfo[indexL];</pre>
00402
00403
00404
                         indexL++;
00405
00406
                         info[(indexM + start) % cap] = rinfo[indexR];
00407
                         indexR++;
00408
00409
                    indexM++;
00410
                }
00411
00412
                // Merge Remaining Lefts
00413
                while (indexL < sub1) {</pre>
                    info[(indexM + start) % cap] = linfo[indexL];
00414
00415
                    indexL++;
00416
                    indexM++;
00417
00418
00419
                // Merge Remaining Rights
00420
                while (indexR < sub2) {</pre>
                     info[(indexM + start) % cap] = rinfo[indexR];
00421
00422
                    indexR++;
00423
                    indexM++;
00424
00425
                // Clean Up and Return
delete[] linfo;
00426
00427
00428
                delete[] rinfo;
00429
                return;
00430
          };
00431
           void mergeSort(int 1, int r) {
00440
               if (1 >= r) {
00441
00442
                    return;
00443
00444
00445
                int m = 1 + (r - 1) / 2;
                mergeSort(1, m);
mergeSort(m + 1, r);
00446
00447
00448
                merge(1, m, r);
```

```
00449
           };
00450
00461
            elmtype select(int k, searchType type) {
00462
00463
                elmtype tempArr[size];
00464
                for (int i = 0; i < size; i++) {</pre>
                    tempArr[i] = atRef(i);
00465
00466
00467
00468
                \ensuremath{//} Selects the correct function based on the type
00469
                if (type == standard) {
00470
                     return KthSmallest(tempArr, 0, size - 1, k);
00471
                return KthSmallestWC(tempArr, 0, size - 1, k);
00472
00473
           }
00474
           elmtype KthSmallest(elmtype *arr, int 1, int r, int k) {
   elmtype pivot = arr[(1 + r) / 2];
   int pos = partition(arr, 1, r, pivot);
00487
00488
00489
00490
00491
                if (pos - 1 == k - 1) {
                return arr[pos];
} else if (pos - 1 > k - 1) {
00492
00493
00494
                    return KthSmallest(arr, 1, pos - 1, k);
00495
                } else {
00496
                    return KthSmallest(arr, pos + 1, r, k - pos + 1 - 1);
00497
00498
           }
00499
00512
           elmtype KthSmallestWC(elmtype *arr, int 1, int r, int k) {
00513
                int n = r - 1 + 1, i:
                elmtype median[(n + 4) / 5];
for (i = 0; i < n / 5; i++) {
00514
00515
00516
                     median[i] = getMedian(arr + 1 + i * 5, 5);
00517
                if (n > i * 5) {
00518
00519
                     median[i] = getMedian(arr + 1 + i * 5, n % 5);
                     i++;
00521
00522
                elmtype medOfMed =
00523
                     (i == 1) ? median[i - 1] : KthSmallestWC(median, 0, i - 1, i / 2);
                int pos = partition(arr, 1, r, medOfMed);
00524
00525
00526
                if (pos - 1 == k - 1) {
                return arr[pos];
} else if (pos - 1 > k - 1) {
00527
00528
00529
                     return KthSmallestWC(arr, 1, pos - 1, k);
00530
                } else {
00531
                     return KthSmallestWC(arr, pos + 1, r, k - pos + 1 - 1);
00532
00533
           }
00534
00540
            elmtype getMedian(elmtype *arr, int n) {
00541
               sort(arr, n);
00542
                return arr[n / 2];
00543
           }
00544
00557
            int partition(elmtype arr[], int l, int r, elmtype pivot) {
               int i;
for (i = 1; i < r; i++) {
00558
00559
                    if (arr[i] == pivot) {
00560
00561
                         break;
00562
                     }
00563
00564
                swap(&arr[i], &arr[r]);
00565
                i = 1;
                for (int j = 1; j <= r - 1; j++) {
    if (arr[j] <= pivot) {</pre>
00566
00567
                         swap(&arr[i], &arr[j]);
00568
                         i++;
00569
00570
                    }
00571
00572
                swap(&arr[i], &arr[r]);
00573
                return i;
00574
           }
00575
00581
           void sort(elmtype *arr, int n) {
               for (int i = 0; i < n; i++) {
    elmtype *smallest = &arr[0];
    for (int j = i + 1; j < n; j++) {
        if (arr[j] < (*smallest)) {
            smallest = &arr[j];
        }
}</pre>
00582
00583
00584
00585
00586
00587
00588
00589
                     if (&arr[i] != smallest) {
00590
                          swap(&arr[i], smallest);
00591
                     }
```

```
00592
             }
00593
00594 };
00595
00601 template<typename keyType> class Heap {
00602
00604
00608
          Heap() { info = new CircularDynamicArray<keyType>; }
00609
          Heap(keyType K[], int s) {
00613
00614
              info = new CircularDynamicArray<keyType>(s);
00615
00616
              for (int i = 0; i < s; i++) {</pre>
00617
                  (*info)[i] = K[i];
00618
00619
00620
              heapify();
00621
          }
00622
00626
          ~Heap() {
00627
             // The CDA is deleted in its cleanup, deleting here will segfault
00628
00629
00633
          int size() {
00634
            return info->length();
00635
00636
00644
          keyType peekKey() {
             return (*info)[0];
00645
00646
00647
00655
          void insert(keyType k) {
00656
             info->addEnd(k);
00657
              siftUp(info->length() - 1);
00658
00659
00665
          void printKeys(std::ostream &out = std::cout) {
00666
              for (int i = 0; i < info->length(); i++) {
00667
                 out « (*info)[i];
                  if (i != info->length() - 1) {
   out « " ";
00668
00669
00670
00671
00672
              if (info->length() != 0) {out « std::endl;}
00673
00674
00682
          keyType extractMin() {
              keyType min = (*info)[0];
(*info)[0] = (*info)[info->length() - 1];
00683
00684
              info->delEnd();
00685
00686
              siftDown(0);
00687
              return min;
00688
          }
00689
00690
          private:
00695
          CircularDynamicArray<keyType> *info;
00696
          void heapify() {
    for (int i = info->length() / 2; i >= 0; i--) {
00702
00703
00704
                  siftDown(i);
00705
00706
          }
00707
00715
          void siftDown(int i) {
00716
              int l = lIndex(i), r = rIndex(i), min = i;
00717
              00718
00719
00720
              if (min != i) { swap(i, min); siftDown(min); }
00721
          }
00722
          void siftUp(int i) {
00730
00731
             for (; i != 0 && (*info)[i] < (*info)[pIndex(i)]; i = pIndex(i)) {</pre>
00732
                  swap(i, pIndex(i));
00733
00734
          }
00735
00744
          void swap(int a, int b) {
             keyType temp = (*info)[a];
(*info)[a] = (*info)[b];
(*info)[b] = temp;
00745
00746
00747
00748
          }
00749
          int pIndex(int i) {
    return (i-1) / 2;
00759
00760
```

```
00761
          }
00762
00772
           int lIndex(int i) {
00773
            return (i*2) + 1;
00774
          }
00775
00785
          int rIndex(int i) {
00786
              return (i*2) + 2;
00787
00788 };
00789
00793 enum color {Red, Black};
00794
00804 template<typename keyType, typename valueType> class RBNode {
00805
           public:
00806
          keyType *key;
00810
00811
00815
          valueType *val;
00816
00820
          RBNode *1;
00821
          RBNode *r;
00825
00826
00830
          RBNode *p;
00835
           color c;
00836
00840
          int size;
00841
          RBNode() {
00847
              key = new keyType;
val = new valueType;
00848
00849
00850
               1 = nullptr;
00851
              r = nullptr;
               p = nullptr;
00852
00853
               size = 0;
00854
               c = Red;
00855
          }
00856
00865
          RBNode(keyType k, valueType v) {
              key = new keyType; *key = k;
val = new valueType; *val = v;
00866
00867
00868
               1 = nullptr;
00869
              r = nullptr;
00870
              p = nullptr;
00871
               size = 1;
00872
               c = Red;
00873
          }
00874
00882
          RBNode(bool nilCon) {
00883
             1 = nullptr;
00884
               r = nullptr;
              p = nullptr;
00885
              key = nullptr;
val = nullptr;
00886
00887
               size = 0;
               c = Black;
00889
00890
         }
00891
          RBNode (keyType k, valueType v, color setc, int s, RBNode<keyType, valueType> *parent) {
   key = new keyType(k);
   val = new valueType(v);
00901
00902
00903
00904
               1 = nullptr;
00905
               r = nullptr;
00906
              p = parent;
               c = setc;
00907
00908
              size = s;
00909
          }
00910
00914
          RBNode(const RBNode<keyType, valueType> &src) {
           *key = *src.key;
*val = *src.val;
00915
00916
               1 = src.1;
00917
00918
              r = src.r;
00919
              p = src.p;
00920
               c = src.c;
00921
               size = src.size;
00922
          }
00923
00929
           ~RBNode() {
               if (key != nullptr) {delete key;}
00931
               if (val != nullptr) {delete val;}
00932
00933
          void cascade(RBNode *nil) {
   if (this == nil) {return;}
00941
00942
```

```
if (1 != nil && 1 != nullptr) {
00944
                   1->cascade(nil);
00945
00946
               if (r != nil && r != nullptr) {
00947
                   r->cascade(nil);
00948
               delete this;
00950
          }
00951
          RBNode &operator=(RBNode R) {
00955
00956
              if (this == R) {
                   return *this;
00957
00958
00959
               delete key; key = new keyType(R.key);
00960
               delete val; val = new valueType(R.val);
00961
               c = R.c;
00962
               return *this;
00963
          }
00964
00970
          void preorder (std::ostream &out = std::cout) {
00971
              if (key == nullptr) {
00972
                   return;
00973
00974
               printNode(out);
               if (1->key != nullptr) {out « " "; 1->preorder(out);}
if (r->key != nullptr) {out « " "; r->preorder(out);}
00975
00976
00977
00978
00984
           void inorder (std::ostream &out = std::cout) {
00985
              if (key == nullptr) {
00986
                   return:
00987
00988
               if (l->key != nullptr) {l->inorder(out); out « " ";}
               printNode(out);
00989
00990
               if (r->key != nullptr) {out « " "; r->inorder(out);}
00991
          }
00992
           void postorder (std::ostream &out = std::cout) {
00999
             if (key == nullptr) {
01000
                  return;
01001
               if (1->key != nullptr) {1->postorder(out); out « " ";}
if (r->key != nullptr) {r->postorder(out); out « " ";}
01002
01003
01004
              printNode(out);
01005
          }
01006
01012
           void printNode(std::ostream &out = std::cout) {
01013
              if (key == nullptr) {
                   return:
01014
01015
01016
              out « *key;
01017
01018
          void printk(int &k, std::ostream &out = std::cout) {
   if (l->key != nullptr) {
01026
01027
01028
                   1->printk(k, out);
                   if (k > 0) {
01030
                       out « " ";
01031
                   }
01032
               if (k < 1) {
01033
01034
                   return;
01035
01036
               out « *key;
01037
01038
               if (k < 1) {
01039
                    return;
01040
               if (r->key != nullptr) {
    out « " ";
01041
01042
01043
                   r->printk(k, out);
01044
01045
          }
01046
01056
          valueType *searchValue(keyType k) {
01057
01058
               if (key == nullptr) {
01059
                   return nullptr;
               }
01060
01061
               if (k == *key) {
01062
01063
                   return val;
01064
01065
               if (k < *key && 1 != nullptr) {
    return 1->searchValue(k);
01066
01067
01068
               }
```

```
01069
01070
              if (k > *key && r != nullptr) {
01071
                  return r->searchValue(k);
             }
01072
01073
01074
             return nullptr:
01075
         }
01076
01086
         RBNode<keyType, valueType> *searchNode(keyType k) {
01087
             if (k == *key) {
                 return this;
01088
             } else if (k < *key && 1->key != nullptr) {
01089
01090
                 return 1->searchNode(k);
01091
             } else if (k > *key && r->key != nullptr) {
01092
                 return r->searchNode(k);
01093
             } else {
01094
                 return nullptr;
01095
             }
01096
        }
01097
01105
         RBNode<keyType, valueType> *predecessor() {
          if (1 == nullptr) {
01106
                return nullptr;
01107
01108
             RBNode *curr;
01109
01110
             for (curr = 1; curr->1 != nullptr; curr = curr->1) {continue;}
01111
             return curr;
01112
        }
01113
         RBNode<keyType, valueType> *min() {
01121
            if (1 == nullptr) {
01122
01123
                 return this;
01124
             RBNode *curr;
01125
01126
              for (curr = 1; curr->1 != nullptr; curr = curr->1) {continue;}
01127
             return curr;
01128
        }
01129
01137
         keyType select(int k) {
01138
            if (k == 1->size + 1) {
01139
                 return (*key);
             } else if (k <= 1->size) {
01140
                 return 1->select(k);
01141
01142
             } else {
01143
                 return r->select(k - 1->size - 1);
01144
             }
01145
         }
01146 };
01147
01166 template<typename keyType, typename valueType> class RBTree {
01167
         public:
01168
01172
01173
          nil = new RBNode<keyType, valueType>(true);
01174
             root = nil;
01175
         }
01176
01185
         RBTree(keyType k, valueType v) {
01186
          nil = new RBNode<keyType, valueType>(true);
01187
              root = new RBNode<keyType, valueType>(k, v);
01188
             root->c = Black; // root is black
01189
         }
01190
01202
         RBTree(keyType *k, valueType *v, int s) {
01203
             nil = new RBNode<keyType, valueType>(true); // nil node's special constructor
             root = nil;

for (int i = 0; i < s; i++) {
01204
01205
01206
                 insert(k[i], v[i]);
01207
01208
         }
01209
01214
         RBTree(const RBTree<keyType, valueType> &src) {
01215
          nil = new RBNode<keyType, valueType>(true);
              root = nil;
01216
             copy(src.nil, src.root, root, nil);
01217
01218
01219
01225
         ~RBTree() {
             root->cascade(nil);
01226
         }
01227
01228
01238
         RBTree<keyType, valueType> &operator=(const RBTree<keyType, valueType> &R) {
01239
            if (this == &R) {
01240
                  return *this;
01241
01242
01243
             root->cascade(nil);
```

```
01244
              nil = new RBNode<keyType, valueType>(true);
01245
01246
               copy(*&R.nil, *&R.root, root, nil);
01247
               return *this;
01248
          }
01249
01255
          void preorder (std::ostream &out) {
01256
              root->preorder(out);
01257
               out « std::endl;
01258
01259
01265
          void inorder (std::ostream &out) {
01266
              root->inorder(out);
01267
              out « std::endl;
01268
01269
01275
          void postorder (std::ostream &out) {
01276
              root->postorder(out);
              out « std::endl;
01278
          }
01279
01285
          void printk (int k, std::ostream &out) {
           root->printk(k, out);
01286
01287
               out « std::endl;
01288
          }
01289
01295
          int size() {
            return root->size;
01296
01297
          }
01298
01308
          valueType *search (keyType k) {
01309
              return root->searchValue(k);
01310
01311
01320
          void insert(keyType k, valueType v) {
              RBNode<keyType, valueType> *z = new RBNode<keyType, valueType>(k, v); z->size = 1;
01321
01322
               z->1 = nil; z->r = nil;
01323
              RBNode<keyType, valueType> *y = nil;
RBNode<keyType, valueType> *x = root;
01324
01325
01326
              while (x != nil) {
01327
                  (x->size)++;
01328
01329
01330
                  y = x;
01331
01332
                   if (*(z->key) < *(x->key)) {
                   x = x->1;
} else {
01333
01334
01335
                       x = x->r;
01336
                   }
01337
              }
01338
              z->p = y;
if (y == nil) {
01339
01340
01341
                   root = z;
01342
               } else if (*(z->key) < *(y->key)) {
01343
                  y->1 = z;
01344
               } else {
01345
                 y \rightarrow r = z;
              }
01346
01347
01348
              z \rightarrow 1 = nil;
01349
01350
               insertFixTree(z);
01351
         }
              \ensuremath{//} Removes the node with key k from the tree.
01352
               // Time complexity: O()
01353
01354
01364
          int remove(keyType k) {
01365
              RBNode<keyType, valueType> *z = root->searchNode(k);
01366
               if (z == nullptr) {
01367
                   return 0;
01368
               RBNode<keyType, valueType> *y = z;
RBNode<keyType, valueType> *x;
01369
01370
01371
01372
               for (RBNode<keyType, valueType> \stari = z->p; i != nil; i = i->p) {
                   i->size--;
01373
01374
               }
01375
01376
              color yOrigcolor = y->c;
01377
01378
               if (z->1 == nil) {
                   x = z -> r;
01379
                   transplant(z, z \rightarrow r);
01380
01381
               } else if (z->r == nil) {
```

```
01382
                  x = z -> 1;
01383
                  transplant(z, z \rightarrow 1);
01384
              } else {
01385
                 y = \max(z->1);
01386
                  yOrigcolor = y->c;
01387
                  x = v -> 1;
                  if (y->p'==z) {
01388
01389
                      x->p = y;
01390
                  } else {
01391
                      transplant(y, y->1);
                     y->1 = z->1;

y->1->p = y;
01392
01393
01394
                      for (RBNode<keyType, valueType> *i = x->p; i != nil && i != y; i = i->p) {
01395
01396
01397
01398
                  transplant(z, y);
01399
                 y->r = z->r;
                  y->r->p = y;
01400
01401
                  y -> c = z -> c;
01402
                  y->size = y->l->size + y->r->size + 1;
01403
              }
01404
              if (yOrigcolor == Black) {
01405
01406
                  deleteFixTree(x);
01407
01408
              return 1;
01409
01410
        }
01411
01417
         int rank(keyType k) {
              rank(kg)Type, valueType> *node = root->searchNode(k);
if (node == nullptr) {
01418
01419
01420
                  return 0;
01421
              int rank = node->1->size + 1;
01422
01423
01424
              for (RBNode<keyType, valueType> *curr = node; curr != root; curr = curr->p) {
01425
                 if (curr == curr->p->r) {
01426
                      rank += curr->p->l->size + 1;
01427
                  }
01428
01429
              return rank:
01430
         }
01431
01443
          keyType select(int k) {
01444
             return root->select(k);
01445
          }
01446
01456
          keyType *successor(keyType k) {
           RBNode<keyType, valueType> *curr = root->searchNode(k);
01457
01458
              if (curr == nullptr) {
01459
                  return nullptr;
01460
              }
01461
01462
              if (curr->r != nil) {
                  for (curr = curr->r; curr->l != nil; curr = curr->l) {continue;}
01464
                  return curr->key;
01465
              } else {
01466
                  RBNode<keyType, valueType> *i;
                  for (i = curr->p; i != nil && curr == i->r; i = i->p) {curr = i;}
01467
                  return i->key;
01468
01469
              }
01470
01471
01472
01482
         keyType *predecessor(keyType k) {
              RBNode<keyType, valueType> *curr = root->searchNode(k);
if (curr == nullptr) {
01483
01484
01485
                  return nullptr;
01486
01487
01488
              if (curr->1 != nil) {
                  for (curr = curr->1; curr->r != nil; curr = curr->r) {continue;}
01489
                  return curr->key;
01490
01491
              } else {
01492
                  RBNode<keyType, valueType> *i;
01493
                  for (i = curr->p; i != nil && curr == i->l; i = i->p) {curr = i;}
                  return i->key;
01494
01495
              }
01496
         }
01497
01498
01499
01503
          RBNode<keyType, valueType> *root;
01504
01508
          RBNode<kevTvpe, valueTvpe> *nil;
```

```
void copy(RBNode<keyType, valueType> *copiedNil, RBNode<keyType, valueType> *copiedNode,
01520
      RBNode<keyType, valueType> *&newParent) {
    newNode = new RBNode<keyType, valueType>(*(copiedNode->key), *(copiedNode->val),
01521
      copiedNode->c, copiedNode->size, newParent);
01522
                if (copiedNode->1 == copiedNil || copiedNode->1 == nullptr) {
01523
01524
                     newNode->1 = nil;
01525
                } else {
01526
                    copy(copiedNil, copiedNode->1, newNode->1, newNode);
01527
01528
                if (copiedNode->r == copiedNil || copiedNode->r == nullptr) {
01529
                     newNode->r = nil;
01530
                } else {
01531
                     copy(copiedNil, copiedNode->r, newNode->r, newNode);
01532
01533
           }
01534
01546
           RBNode<keyType, valueType> *min(RBNode<keyType, valueType> *node) {
               for (node; node->1 != nil; node = node->1) {
01547
01548
01549
01550
                return node;
01551
           }
01552
01564
           RBNode<keyType, valueType> *max(RBNode<keyType, valueType> *node) {
01565
                for (; node->r != nil; node = node->r) {
                    continue;
01566
01567
01568
                return node;
01569
           }
01578
           void insertFixTree(RBNode<keyType, valueType> *z) {
01579
                RBNode<keyType, valueType> *y;
01580
                while (z->p->c == Red) {
01581
                  if (z->p == z->p->p->1) {
01582
                         y = z - p - p - r;
01584
01585
                          if (y->c == Red) {
01586
                              z \rightarrow p \rightarrow c = Black;
                              y \rightarrow c = Black;
01587
01588
                              z \rightarrow p \rightarrow p \rightarrow c = Red;
01589
                              z = z \rightarrow p \rightarrow p;
01590
                          } else {
01591
                              if (z == z->p->r) {
01592
                                   z = z - > p;
01593
                                   lRotate(z);
01594
01595
01596
                              z \rightarrow p \rightarrow c = Black;
01597
                              z \rightarrow p \rightarrow p \rightarrow c = Red;
01598
                              rRotate(z->p->p);
01599
01600
                     } else {
                         y = z->p->p->1;
01601
01602
01603
                          if (y->c == Red) {
01604
                              z \rightarrow p \rightarrow c = Black;
01605
                              y->c = Black;
                              z \rightarrow p \rightarrow p \rightarrow c = Red;
01606
01607
                              z = z - p - p;
01608
                          } else {
01609
                              if (z == z->p->1) {
01610
                                   z = z - > p;
01611
                                   rRotate(z);
01612
                              }
01613
01614
                              z \rightarrow p \rightarrow c = Black;
                              z \rightarrow p \rightarrow p \rightarrow c = Red;
01615
01616
                              1Rotate(z->p->p);
01617
01618
                    }
                }
01619
01620
                root->c = Black;
01621
01622
01630
           void deleteFixTree(RBNode<keyType, valueType> *x) {
01631
01632
                RBNode<keyType, valueType> *w;
                while (x != root && x->c == Black) {
01633
                     if(x == x->p->1) {
01634
01635
                          w = x - > p - > r;
01636
                          if (w->c == Red) {
01637
                              w->c = Black;
01638
                              x->p->c = Red;
01639
                              lRotate(x->p);
```

```
01640
                             w = x - > p - > r;
01641
01642
                        if (w->l->c == Black && w->r->c == Black) {
01643
01644
                             w->c = Red;
01645
                             x = x - > p;
01646
                         } else {
01647
                            if (w->r->c == Black) {
                                w->1->c = Black;
01648
01649
                                 w->c = Red;
01650
                                 rRotate(w);
01651
                                 W = x - > p - > r;
01652
                             }
01653
01654
                             w->c = x->p->c;
                             x->p->c = Black;

w->r->c = Black;
01655
01656
                             lRotate(x->p);
01657
01658
                             x = root;
01660
                    } else {
01661
                        W = X->p->1;
                        if (w->c == Red) {
   w->c = Black;
01662
01663
01664
                            x->p->c = Red;
                            rRotate(x->p);
01665
01666
                             w = x->p->1;
01667
01668
                        if (w->r->c == Black && w->l->c == Black) {
01669
01670
                             w->c = Red;
01671
                             x = x->p;
01672
                         } else {
01673
                            if (w->1->c == Black) {
                                  w->r->c = Black;
01674
                                 w->c = Red;
01675
01676
                                 lRotate(w);
01677
                                 W = X - > p - > 1;
01678
01679
01680
                             W->c = X->p->c;
                            x->p->c = Black;

w->l->c = Black;
01681
01682
01683
                             rRotate(x->p);
01684
                             x = root;
01685
                        }
01686
                  }
              }
01687
         }
01688
01689
           void rRotate(RBNode<keyType, valueType> *x) {
01697
            RBNode<keyType, valueType> *y = x->1;
01698
               x->1 = y->r;
if (y->r != nil) {
01699
01700
               y->r->p = x;
01701
01702
01703
               y->p = x->p;
01704
               if (x->p == nil) {
               root = y;
} else if (x == x->p->r) {
01705
01706
                   x->p->r = y;
01707
01708
               } else {
                  x->p->1 = y;
01709
01710
01711
               y \rightarrow r = x;
01712
               x->p = y;
01713
               v->size = x->size;
               x \rightarrow size = x \rightarrow 1 \rightarrow size + x \rightarrow r \rightarrow size + 1;
01714
01715
         }
01724
         void lRotate(RBNode<keyType, valueType> *x) {
           RBNode<keyType, valueType> *y = x->r;
01725
               x->r = y->1;
if (y->1 != nil) {
01726
01727
                   y -> 1 -> p = x;
01728
01729
01730
               y->p = x->p;
               if (x->p == nil) {
   root = y;
01731
01732
01733
               } else if (x == x->p->1) {
01734
                   x - > p - > 1 = y;
01735
               } else {
                  x->p->r = y;
01736
               }
01737
               y->1 = x;
x->p = y;
y->size = x->size;
01738
01739
01740
```

```
x->size = x->l->size + x->r->size + 1;
01741
01742
01743
01750
            void transplant(RBNode<keyType, valueType> *u, RBNode<keyType, valueType> *v) {
01751
01752
                 // If u is the root, set the root to \ensuremath{\text{v}}
                if (u->p == nil) {
    root = v;
01753
01754
01755
                // If u is the left child of its parent, set the left child of its parent to v } else if (u == u->p->l) {    u->p->l = v;
01756
01757
01758
01759
01760
                 // If u is the right child of its parent, set the right child of its parent to v
01761
01762
01763
                    u \rightarrow p \rightarrow r = v;
01764
01765
                // Set the parent of v to the parent of u
01766
                v->p = u->p;
01767 }
01768 };
01769 #endif
```

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