
Documentation of the pygpc package

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PYGPC PACKAGE

A package that provides submodules in order to perform polynomial chaos uncertainty analysis on complex dynamic systems.

1.1 Submodules

1.2 pygpc.gpc module

Class that provides general polynomial chaos methods

```
class pygpc.gpc.gPC
    General gPC base class

    N_grid
        number of grid points
        Type int

    N_poly
        number of polynomials psi
        Type int

    N_samples
        number of samples xi
        Type int

    N_out
        number of output coefficients
        Type int

    dim
        number of uncertain parameters to process
        Type int

    pdf_type
        type of pdf 'beta' or 'norm'
        Type [dim] list of str

    pdf_shape
        shape parameters of pdfs beta-dist: [[alpha], [beta] ] normal-dist: [[mean], [variance]]
        Type list of list of float
```

limits

upper and lower bounds of random variables beta-dist: [[a1 ...], [b1 ...]] normal-dist: [[0 ...], [0 ...]]
(not used)

Type list of list of float

order

maximum individual expansion order generates individual polynomials also if maximum expansion order in order_max is exceeded

Type [dim] list of int

order_max

maximum expansion order (sum of all exponents) the maximum expansion order considers the sum of the orders of combined polynomials only

Type int

interaction_order

number of random variables, which can interact with each other all polynomials are ignored, which have an interaction order greater than the specified

Type int

grid

grid object generated in grid.py including grid.coords and grid.coords_norm

Type grid object

random_vars

string labels of the random variables

Type [dim] list of str

sobol

Sobol indices of N_out output quantities

Type [N_sobol x N_out] np.ndarray

sobol_idx

List of parameter label indices belonging to Sobol indices

Type [N_sobol] list of np.ndarray

cpu

flag to execute the calculation on the cpu

Type bool

gpu

flag to execute the calculation on the gpu

Type bool

verbose

boolean value to determine if to print out the progress into the standard output

Type bool

gpc_matrix

generalized polynomial chaos matrix

Type [N_samples x N_poly] np.ndarray

gpc_matrix_inv

pseudo inverse of the generalized polynomial chaos matrix

Type [N_poly x N_samples] np.ndarray

gpc_coeffs

coefficient matrix of independent regions of interest for every coefficient

Type [N_poly x N_out] np.ndarray

poly

polynomial objects containing the coefficients that are used to build the gpc matrix

Type [dim x order_span] list of list of np.poly1d:

poly_gpu

polynomial coefficients stored in a np.ndarray that can be processed on a graphic card

Type np.ndarray

poly_idx

multi indices to determine the degree of the used sub-polynomials

Type [N_poly x dim] np.ndarray

poly_idx_gpu [N_poly x dim] np.ndarray

multi indices to determine the degree of the used sub-polynomials stored in a np.ndarray that can be processed on a graphic card

poly_der

derivative of the polynomial objects containing the coefficients that are used to build the gpc matrix

Type [dim x order_span] list of list of np.poly1d:

poly_norm

normalizing scaling factors of the used sub-polynomials

Type [order_span x dim] np.ndarray

poly_norm_basis

normalizing scaling factors of the polynomial basis functions

Type [N_poly] np.ndarray

sobol_idx_bool

boolean mask that determines which multi indices are unique

Type list of np.ndarray of bool

extend_gpc_matrix_samples (*samples_poly_ratio, seed=None*)

Add sample points according to input pdfs to grid and extend the gpc matrix such that the ratio of rows/columns equals samples_poly_ratio.

extend_gpc_matrix_samples(samples_poly_ratio, seed=None):

Parameters

- **samples_poly_ratio** (*float*) – ratio between number of samples and number of polynomials the matrix will be extended until
- **seed** (*float, optional, default=None*) – random seeding point

extend_polynomial_basis (*poly_idx_added*)

Extend polynomial basis functions and add new columns to gpc matrix.

extend_polynomial_basis(poly_idx_added)

Parameters **poly_idx_added** (*[N_poly_added x dim] np.ndarray*) – array of added polynomials (order)

get_global_sens (*coeffs*)

Determine the global derivative based sensitivity coefficients.

Reference: D. Xiu, Fast Numerical Methods for Stochastic Computations: A Review, Commun. Comput. Phys., 5 (2009), pp. 242-272 eq. (3.14) page 255

```
get_global_sens = calc_globalsens(coeffs)
```

Parameters **coeffs** ($[N_coeffs \times N_out]$ *np.ndarray*) – gpc coefficients

Returns **get_global_sens** – global derivative based sensitivity coefficients

Return type $[dim \times N_out]$ *np.ndarray*

get_local_sens (*coeffs*, *xi*)

Determine the local derivative based sensitivity coefficients in the point of operation *xi* in normalized coordinates.

```
get_local_sens = calc_localsens(coeffs, xi)
```

Parameters

- **coeffs** ($[N_coeffs \times N_out]$ *np.ndarray*) – gpc coefficients
- **xi** ($[N_coeffs \times N_out]$ *np.ndarray*) – point in variable space to evaluate local sensitivity in (normalized coordinates!)

Returns **get_local_sens** – local sensitivity

Return type $[dim \times N_out]$ *np.ndarray*

get_mean_random_vars ()

Determine the average values of the input random variables from their pdfs.

Returns **mean_random_vars** – average values of the input random variables

Return type $[N_random_vars]$ *np.ndarray*

static get_mean_value (*coeffs*)

Calculate the expected mean value.

```
mean = get_mean_value(coeffs)
```

Parameters **coeffs** ($[N_coeffs \times N_out]$ *np.ndarray*) – gpc coefficients

Returns **mean** – expected mean value

Return type $[1 \times N_out]$ *np.ndarray*

get_pce (*coeffs=None*, *xi=None*, *output_idx=None*)

Calculates the gPC approximation in points with *output_idx* and normalized parameters *xi* (interval: [-1, 1]).

```
pce = get_pce(coeffs=None, xi=None, output_idx=None)
```

Parameters

- **coeffs** ($[N_coeffs \times N_out]$ *np.ndarray*, *optional*, *default=None*) – gpc coefficients
- **xi** ($[1 \times dim]$ *np.ndarray*, *optional*, *default=None*) – point in variable space to evaluate local sensitivity in normalized coordinates
- **output_idx** ($[1 \times N_out]$ *np.ndarray*, *optional*, *default=None*) – idx of output quantities to consider (Default: all outputs)

Returns **pce** – gpc approximation at normalized coordinates *xi*

Return type $[N_{xi} \times N_{out}]$ np.ndarray

Example

```
pce = get_pce([[xi_1_p1 ... xi_dim_p1] , [xi_1_p2 ... xi_dim_p2]], np.array([[0,5,13]]))
```

get_pdf (*coeffs*, *N_samples*, *output_idx=None*)

Determine the estimated pdfs of the output quantities

```
pdf_x, pdf_y = get_pdf(coeffs, N_samples, output_idx=None)
```

Parameters

- **coeffs** ($[N_{coeffs} \times N_{out}]$ np.ndarray) – gpc coefficients
- **N_samples** (*int*) – number of samples used to estimate output pdf
- **output_idx** ($[1 \times N_{out}]$ np.ndarray, optional, default=None) – idx of output quantities to consider if output_idx=None, all output quantities are considered

Returns

- **pdf_x** ($[100 \times N_{out}]$ np.ndarray) – x-coordinates of output pdf (output quantity),
- **pdf_y** ($[100 \times N_{out}]$ np.ndarray) – y-coordinates of output pdf (probability density of output quantity)

get_pdf_monte_carlo (*N_samples*, *coeffs=None*, *output_idx=None*)

Randomly sample the gPC expansion to determine output pdfs in specific points.

```
xi = get_pdf_mc(N_samples, coeffs=None, output_idx=None)
```

Parameters

- **N_samples** (*int*) – number of random samples drawn from the respective input pdfs
- **output_idx** ($[1 \times N_{out}]$ np.ndarray, optional, default=None) – idx of output quantities to consider
- **coeffs** ($[N_{coeffs} \times N_{out}]$ np.ndarray, optional, default=None) – gPC coefficients

Returns **xi** – generated samples in normalized coordinates

Return type $[N_{samples} \times dim]$ np.ndarray

get_sobol_indices (*coeffs=None*)

Determine the available sobol indices.

```
sobol, sobol_idx = get_sobol_indices(coeffs=None)
```

Parameters **coeffs** ($[N_{coeffs} \times N_{out}]$ np.ndarray, optional, default=None) – gpc coefficients

Returns

- **sobol** ($[N_{sobol} \times N_{out}]$ np.ndarray) – unnormalized sobol_indices
- **sobol_idx** (list of $[N_{sobol} \times dim]$ np.ndarray) – list containing the parameter combinations in rows of sobol
- **sobol_idx_bool** (list of np.ndarray of bool) – boolean mask that determines which multi indices are unique

get_sobol_order (*sobol=None, sobol_idx=None, sobol_idx_bool=None*)

Evaluate order of determined sobol indices.

```
sobol, sobol_idx, sobol_rel_order_mean, sobol_rel_order_std, sobol_rel_1st_order_mean,
sobol_rel_1st_order_std = get_sobol_order(coeffs=None, sobol=None, sobol_idx=None,
sobol_idx_bool=None)
```

Parameters

- **sobol** (*[N_sobol x N_out] np.ndarray*) – unnormalized sobol_indices
- **sobol_idx** (*list of [N_sobol x dim] np.ndarray*) – list containing the parameter combinations in rows of sobol
- **sobol_idx_bool** (*list of np.ndarray of bool*) – boolean mask that determines which multi indices are unique

Returns

- **sobol_rel_order_mean** (*np.ndarray*) – average proportion of the Sobol indices of the different order to the total variance (1st, 2nd, etc..) over all output quantities
- **sobol_rel_order_std** (*np.ndarray*) – standard deviation of the proportion of the Sobol indices of the different order to the total variance (1st, 2nd, etc..) over all output quantities
- **sobol_rel_1st_order_mean** (*np.ndarray*) – average proportion of the random variables of the 1st order Sobol indices to the total variance over all output quantities
- **sobol_rel_1st_order_std** (*np.ndarray*) – standard deviation of the proportion of the random variables of the 1st order Sobol indices to the total variance over all output quantities

static get_standard_deviation (*coeffs*)

Calculate the standard deviation.

```
std = get_standard_deviation(coeffs)
```

Parameters **coeffs** (*np.array of float [N_coeffs x N_out]*) – gpc coefficients

Returns **std** – standard deviation

Return type [1 x N_out] np.ndarray

init_gpc_matrix ()

Construct the gPC matrix and the Moore-Penrose-pseudo-inverse.

```
init_gpc_matrix()
```

init_polynomial_basis ()

Initialize polynomial basis functions for a maximum order expansion.

```
init_polynomial_basis()
```

init_polynomial_basis_gpu ()

Initialized polynomial basis coefficients for graphic card. Converts list of lists of self.polynomial_bases into np.ndarray that can be processed on a graphic card.

```
init_polynomial_basis_gpu()
```

init_polynomial_coeffs (*order_begin, order_end*)

Calculate polynomial basis functions of a given order range and add it to the polynomial lookup tables.

The size, including the polynomials that won't be used, is [max_individual_order x dim].

Polynomial	Dimension 1	Dimension 2	...	Dimension M
Polynomial 1	[Coefficients]	[Coefficients]	⋮	[Coefficients]
Polynomial 2	0	[Coefficients]	⋮	[Coefficients]
⋮	⋮	⋮	⋮	⋮
Polynomial N	[Coefficients]	[Coefficients]	0	[Coefficients]

`init_polynomial_coeffs(poly_idx_added)`

Parameters

- **order_begin** (*int*) – order of polynomials to begin with
- **order_end** (*int*) – order of polynomials to end with

init_polynomial_index()

Initialize polynomial multi indices. Determine 2D multi-index array (order) of basis functions and generate multi-index list up to maximum order. The size is [No. of basis functions x dim].

Polynomial Index	Dimension 1	Dimension 2	...	Dimension M
Basis 1	[Order D1]	[Order D2]	⋮	[Order M]
Basis 2	[Order D1]	[Order D2]	⋮	[Order M]
⋮	[Order D1]	[Order D2]	⋮	[Order M]
Basis N	[Order D1]	[Order D2]	⋮	[Order M]

`init_polynomial_index()`

replace_gpc_matrix_samples (*idx*, *seed=None*)

Replace distinct sample points from the gpc matrix.

`replace_gpc_matrix_samples(idx, seed=None)`

Parameters

- **idx** (*np.ndarray*) – array of grid indices of `obj.grid.coords[idx,:]` which are going to be replaced (rows of gPC matrix will be replaced by new ones)
- **seed** (*float, optional, default=None*) – random seeding point

write_log_sobol (*fname*, *sobol_rel_order_mean*, *sobol_rel_1st_order_mean*, *sobol_extracted_idx_1st*)

Write sobol indices into logfile.

Parameters

- **fname** (*str*) – path to output file
- **sobol_rel_order_mean** (*np.ndarray*) – average proportion of the Sobol indices of the different order to the total variance (1st, 2nd, etc...) over all output quantities
- **sobol_rel_1st_order_mean** (*np.ndarray*) – average proportion of the random variables of the 1st order Sobol indices to the total variance over all output quantities
- **#TODO** (*add description*) –
- **sobol_extracted_idx_1st** –

1.3 pygpc.grid module

Functions and classes that provide data and methods for the generation and processing of numerical grids

class `pygpc.grid.RandomGrid` (*pdf_type, grid_shape, limits, N, seed=None*)

Generate RandomGrid object instance.

`RandomGrid(pdf_type, grid_shape, limits, N, seed=None)`

pdf_type

variable specific type of pdf (“beta”, “normal”)

Type `[N_vars]` list of str

grid_shape

shape parameters of PDF beta (jacobi): `[alpha, beta]` norm (hermite): `[mean, std]`

Type `[2 x N_vars]` list of list of float

limits

Upper and lower bounds of PDF beta (jacobi): `[min, max]` norm (hermite): `[0, 0]` (unused)

Type `[2 x N_vars]` list of list of float

N

number of random samples to generate

Type int

seed

seeding point to replicate random grids

Type float

dim

number of uncertain parameters to process

Type int

coords

denormalized coordinates xi

Type `[N_samples x dim]` np.ndarray

coords_norm

normalized `[-1, 1]` coordinates xi

Type `[N_samples x dim]` np.ndarray

Parameters

- **pdf_type** (`[N_vars]` list of str) – variable specific type of pdf (“beta”, “normal”)
- **grid_shape** (`[2 x N_vars]` list of list of float) – shape parameters of PDF beta (jacobi): `[alpha, beta]` norm (hermite): `[mean, std]`
- **limits** (`[2 x N_vars]` list of list of float) – Upper and lower bounds of PDF beta (jacobi): `[min, max]` norm (hermite): `[0, 0]` (unused)
- **N** (int) – number of random samples to generate
- **seed** (float, optional, default=None) – seeding point to replicate random grids

class `pygpc.grid.SparseGrid` (*pdf_type, grid_type, grid_shape, limits, level, level_max, interaction_order, order_sequence_type, make_grid=True, verbose=True*)

Generate SparseGrid object instance.

SparseGrid(pdf_type, grid_type, grid_shape, limits, level, level_max, interaction_order, order_sequence_type, make_grid=True, verbose=True)

pdf_type

variable specific type of PDF (“beta”, “normal”)

Type [N_vars] list of str

grid_type

specify type of quadrature used to construct sparse grid (‘jacobi’, ‘hermite’, ‘cc’, ‘fejer2’)

Type [N_vars] list of str

grid_shape

shape parameters of PDF beta (jacobi): [alpha, beta] norm (hermite): [mean, std]

Type [2 x N_vars] list of list of float

limits

upper and lower bounds of PDF beta (jacobi): [min, max] norm (hermite): [0, 0] (unused)

Type [2 x N_vars] list of list of float

level

number of levels in each dimension

Type [N_vars] list of int

level_max

global combined level maximum

Type int

interaction_order

interaction order of parameters and grid, i.e. the grid points are lying between this number of dimensions

Type int

order_sequence_type

type of order sequence (‘lin’, ‘exp’) common: ‘exp’

Type str

make_grid

boolean value to determine if to generate grid during initialization

Type boolean

verbose

boolean value to determine if to print out the progress into the standard output

Type bool

coords_norm

normalized [-1, 1] coordinates xi

Type [N_samples x dim] np.ndarray

weights

weights of the grid

Type np.ndarray

coords

denormalized coordinates xi

Type [N_samples x dim] np.ndarray

level_sequence

list containing the levels

Type list of int

order_sequence

list containing the polynomial order of the levels

Type list of int

dim

number of uncertain parameters to process

Type int

Parameters

- **pdf_type** ([N_vars] list of str) – variable specific type of PDF (“beta”, “normal”)
- **grid_type** ([N_vars] list of str) – specify type of quadrature used to construct sparse grid (‘jacobi’, ‘hermite’, ‘cc’, ‘fejer2’)
- **grid_shape** ([2 x N_vars] list of list of float) – shape parameters of PDF beta (jacobi): [alpha, beta] norm (hermite): [mean, std]
- **limits** ([2 x N_vars] list of list of float) – upper and lower bounds of PDF beta (jacobi): [min, max] norm (hermite): [0, 0] (unused)
- **level** ([N_vars] list of int) – number of levels in each dimension
- **level_max** (int) – global combined level maximum
- **interaction_order** (int) – interaction order of parameters and grid, i.e. the grid points are lying between this number of dimensions
- **order_sequence_type** (str) – type of order sequence (‘lin’, ‘exp’) common: ‘exp’
- **make_grid** (boolean, optional, default=True) – boolean value to determine if to generate grid during initialization
- **verbose** (bool, optional, default=True) – boolean value to determine if to print out the progress into the standard output

calc_coords_weights()

Find similar points in grid and formulate calculate a list containing these points.

calc_grid()

Calculate a cubature lookup table for knots and weights.

dl_k, dl_w = calc_grid()

Returns

- **dl_k** (list of list of float) – cubature lookup table for knots
- **dl_w** (list of list of float) – cubature lookup table for weights

calc_l_level()

Calculate the l-level needed for the Fejer grid type 2.

`l_level = calc_l_level()`

Returns `l_level` – multi indices filtered by level capacity and interaction order

Return type `np.ndarray`

calc_multi_index_lst()

Calculate the multi index list needed for the calculation of the SparseGrid.

calc_tensor_products()

Calculate the tensor products of the knots and the weights.

`dL_k, dL_w = calc_tensor_products()`

Returns

- `dL_k` (*np.ndarray*) – tensor product of knots
- `dL_w` (*np.ndarray*) – tensor product of weights

class `pygpc.grid.TensorGrid(pdf_type, grid_type, grid_shape, limits, N)`

Generate TensorGrid object instance.

`TensorGrid(pdf_type, grid_type, grid_shape, limits, N):`

pdf_type

variable specific type of PDF (“beta”, “normal”)

Type `[N_vars]` list of str

grid_type

specify type of quadrature used to construct sparse grid (‘jacobi’, ‘hermite’, ‘cc’, ‘fejer2’)

Type `[N_vars]` list of str

grid_shape

shape parameters of PDF beta (jacobi): [alpha, beta] norm (hermite): [mean, std]

Type `[2 x N_vars]` list of list of float

limits

upper and lower bounds of PDF beta (jacobi): [min, max] norm (hermite): [0, 0] (unused)

Type `[2 x N_vars]` list of list of float

N

number of nodes in each dimension

Type `[N_vars]` list of int

dim

number of uncertain parameters to process

Type int

knots_dim_list

knots of grid in each dimension

Type `[dim]` list of `np.ndarray`

weights_dim_list

weights of grid in each dimension

Type `[dim]` list of `np.ndarray`

coords_normnormalized $[-1, 1]$ coordinates xi**Type** $[N_samples \times dim]$ np.ndarray**weights**

weights of the grid

Type np.ndarray**coords**

denormalized coordinates xi

Type $[N_samples \times dim]$ np.ndarray**Parameters**

- **pdf_type** ($[N_vars]$ list of str) – variable specific type of PDF (“beta”, “normal”)
- **grid_type** ($[N_vars]$ list of str) – specify type of quadrature used to construct sparse grid (‘jacobi’, ‘hermite’, ‘cc’, ‘fejer2’)
- **grid_shape** ($[2 \times N_vars]$ list of list of float) – shape parameters of PDF beta (jacobi): [alpha, beta] norm (hermite): [mean, std]
- **limits** ($[2 \times N_vars]$ list of list of float) – upper and lower bounds of PDF beta (jacobi): [min, max] norm (hermite): [0, 0] (unused)
- **N** ($[N_vars]$ list of int) – number of nodes in each dimension

pygpc.grid.get_denormalized_coordinates(coords_norm, pdf_type, grid_shape, limits)

Denormalize grid from standardized $[-1, 1]$ except hermite) to original parameter space for simulations.

coords = get_denormalized_coordinates(coords_norm, pdf_type, grid_shape, limits)

Parameters

- **pdf_type** ($[dim]$ list of str) – type of pdf ‘beta’ or ‘norm’
- **grid_shape** ($[2 \times N_vars]$ list of list of float) – shape parameters of PDF beta (jacobi): [alpha, beta] norm (hermite): [mean, std]
- **limits** ($[2 \times N_vars]$ list of list of float) – upper and lower bounds of PDF beta (jacobi): [min, max] norm (hermite): [0, 0] (unused)
- **coords_norm** ($[N_samples \times dim]$ np.ndarray) – normalized $[-1, 1]$ coordinates xi

Returns coords – denormalized coordinates xi

Return type $[N_samples \times dim]$ np.ndarray

pygpc.grid.get_normalized_coordinates(coords, pdf_type, grid_shape, limits)

Normalize grid from original parameter (except hermite) to standardized $[-1, 1]$ space for simulations.

coords_norm = get_normalized_coordinates(coords, pdf_type, grid_shape, limits)

Parameters

- **pdf_type** ($[dim]$ list of str) – type of pdf ‘beta’ or ‘norm’
- **grid_shape** ($[2 \times N_vars]$ list of list of float) – shape parameters of PDF beta (jacobi): [alpha, beta] norm (hermite): [mean, std]

- **limits** ($[2 \times N_{\text{vars}}]$ list of list of float) – upper and lower bounds of PDF beta (jacobi): [min, max] norm (hermite): [0, 0] (unused)
- **coords** ($[N_{\text{samples}} \times \text{dim}]$ np.ndarray) – denormalized coordinates xi

Returns **coords_norm** – normalized [-1, 1] coordinates xi

Return type $[N_{\text{samples}} \times \text{dim}]$ np.ndarray

`pygpc.grid.get_quadrature_clenshaw_curtis_1d(N)`

Get the Clenshaw Curtis nodes and weights.

knots, weights = get_quadrature_clenshaw_curtis_1d(N)

Parameters **N** (*int*) – number of knots

Returns

- **knots** (np.ndarray) – knots of the grid
- **weights** (np.ndarray) – weights of the grid

`pygpc.grid.get_quadrature_fejer1_1d(N)`

Computes the Fejer type 1 nodes and weights.

This method uses a direct approach. The paper by Waldvogel exhibits a more efficient approach using Fourier transforms.

Reference: Philip Davis, Philip Rabinowitz, Methods of Numerical Integration, Second Edition, Dover, 2007, ISBN: 0486453391 Titel anhand dieser ISBN in Citavi-Projekt übernehmen, LC: QA299.3.D28.

Walter Gautschi, Numerical Quadrature in the Presence of a Singularity, SIAM Journal on Numerical Analysis, Volume 4, Number 3, 1967, pages 357-362.

Joerg Waldvogel, Fast Construction of the Fejer and Clenshaw-Curtis Quadrature Rules, BIT Numerical Mathematics, Volume 43, Number 1, 2003, pages 1-18.

knots, weights = get_quadrature_fejer1_1d(N)

Parameters **N** (*int*) – number of knots

Returns

- **knots** (np.ndarray) – knots of the grid
- **weights** (np.ndarray) – weights of the grid

`pygpc.grid.get_quadrature_fejer2_1d(N)`

Computes the Fejer type 2 nodes and weights (Clenshaw Curtis without boundary nodes).

This method uses a direct approach. The paper by Waldvogel exhibits a more efficient approach using Fourier transforms.

Reference: Philip Davis, Philip Rabinowitz, Methods of Numerical Integration, Second Edition, Dover, 2007, ISBN: 0486453391 Titel anhand dieser ISBN in Citavi-Projekt übernehmen, LC: QA299.3.D28.

Walter Gautschi, Numerical Quadrature in the Presence of a Singularity, SIAM Journal on Numerical Analysis, Volume 4, Number 3, 1967, pages 357-362.

Joerg Waldvogel, Fast Construction of the Fejer and Clenshaw-Curtis Quadrature Rules, BIT Numerical Mathematics, Volume 43, Number 1, 2003, pages 1-18.

knots, weights = get_quadrature_fejer2_1d(N)

Parameters **N** (*int*) – number of knots

Returns

- **knots** (*np.ndarray*) – knots of the grid
- **weights** (*np.ndarray*) – weights of the grid

`pygpc.grid.get_quadrature_hermite_1d(N)`

Get knots and weights of Hermite polynomials (normal distribution).

`knots, weights = get_quadrature_hermite_1d(N)`

Parameters **N** (*int*) – number of knots

Returns

- **knots** (*np.ndarray*) – knots of the grid
- **weights** (*np.ndarray*) – weights of the grid

`pygpc.grid.get_quadrature_jacobi_1d(N, b, a)`

Get knots and weights of Jacobi polynomials (beta distribution).

`knots, weights = get_quadrature_jacobi_1d(N, b, a)`

Parameters

- **N** (*int*) – number of knots
- **a** (*float*) – lower limit of quadrature coefficients
- **b** (*float*) – upper limit of quadrature coefficients

Returns

- **knots** (*np.ndarray*) – knots of the grid
- **weights** (*np.ndarray*) – weights of the grid

`pygpc.grid.get_quadrature_patterson_1d(N)`

Computes the nested Gauss-Patterson nodes and weights for $N = 1, 3, 7, 15, 31$.

`knots, weights = get_quadrature_patterson_1d(N)`

Parameters **N** (*int*) – number of knots possible values: 1, 3, 7, 15, 31

Returns

- **knots** (*np.ndarray*) – knots of the grid
- **weights** (*np.ndarray*) – weights of the grid

1.4 pygpc.misc module

Functions and classes that provide data and methods with general usage in the pygpc package

class `pygpc.misc.NoDaemonProcess` (*group=None, target=None, name=None, args=(), kwargs={}*)

Bases: `multiprocessing.process.Process`

Helper class to create a non daemonic process. From <https://stackoverflow.com/questions/6974695/python-process-pool-non-daemonic> make 'daemon' attribute always return False

daemon

class `pygpc.misc.NonDaemonicPool` (*processes=None, initializer=None, initargs=(), maxtasksperchild=None*)

Bases: `multiprocessing.pool.Pool`

Helper class to create a non daemonic pool. We sub-class multiprocessing.pool.Pool instead of multiprocessing.Pool because the latter is only a wrapper function, not a proper class.

Process

alias of *NoDaemonProcess*

`pygpc.misc.display_fancy_bar(text, i, n_i, more_text=None)`

Display a simple progress bar. Call for each iteration and start with i=1.

Parameters

- **text** (*str*) – text to display in front of actual iteration
- **i** (*str or int*) – actual iteration
- **n_i** (*int*) – number of iterations
- **more_text** (*str, optional, default=None*) – text that displayed at an extra line.

Examples

`fancy_bar('Run',7,10):` Run 07 from 10 [=====] 70%

`fancy_bar(Run,9,10,'Some more text'):` Some more text Run 09 from 10
[=====] 90%

`pygpc.misc.get_array_unique_rows(array)`

Compute unique rows of array and delete rows that are linearly dependent.

`unique = get_array_unique_rows(array)`

Parameters **array** (*np.ndarray*) – matrix with k linearly dependent rows

Returns **unique** – matrix without k linearly dependent rows

Return type *np.ndarray*

`pygpc.misc.get_betapdf_fit(data, beta_tolerance=0, uni_intervall=0)`

Fit data to a beta distribution in the interval [a, b].

`beta_parameters, moments, p_value, uni_parameters = get_betapdf_fit(data, beta_tolerance=0, uni_intervall=0)`

Parameters

- **data** (*np.ndarray*) – data to fit
- **beta_tolerance** (*float, optional, default=0*) – tolerance interval to calculate the bounds of beta distribution from observed data, e.g. 0.2 (+20% tolerance)
- **uni_intervall** (*float, optional, default=0*) – uniform distribution interval defined as fraction of beta distribution interval range: [0...1], e.g. 0.90 (90%)

Returns

- **beta_parameters** (*[4] list of float*) – 2 shape parameters and limits [p, q, a, b]
- **moments** (*[4] list of float*) – [data_mean, data_std, beta_mean, beta_std]
- **p_value** (*float*) – p-value of the Kolmogorov Smirnov test
- **uni_parameters** (*[2] list of float*) – limits a and b [a, b]

`pygpc.misc.get_cartesian_product(array_list, cartesian_product=None)`

Generate a cartesian product of input arrays.

`cartesian_product = get_cartesian_product(array_list, cartesian_product=None)`

Parameters

- **array_list** (*list of np.ndarray*) – arrays to form the cartesian product with
- **cartesian_product** (*np.ndarray*) – array to write the cartesian product

Returns **cartesian_product** – array to write the cartesian product (M, len(arrays))

Return type `np.ndarray`

Examples

`cartesian([(1, 2, 3), [4, 5], [6, 7]]) =`

`array([[1, 4, 6], [1, 4, 7], [1, 5, 6], [1, 5, 7], [2, 4, 6], [2, 4, 7], [2, 5, 6], [2, 5, 7], [3, 4, 6], [3, 4, 7], [3, 5, 6], [3, 5, 7]])`

`pygpc.misc.get_list_multi_delete(input_list, index)`

Delete multiple entries from list.

`input_list = get_list_multi_delete(input_list, index)`

Parameters

- **input_list** (*list*) – simple list
- **index** (*list of integer*) – list of indices to delete

Returns **input_list** – input list without entries specified in index

Return type `list`

`pygpc.misc.get_multi_indices(length, max_order)`

Computes all multi-indices with a maximum overall order of `max_order`.

`multi_indices = get_multi_indices(length, max_order)`

Parameters

- **length** (*int*) – length of multi-index tuples
- **max_order** (*int*) – maximum overall interaction order

Returns **multi_indices** – matrix of multi-indices

Return type `np.ndarray`

`pygpc.misc.get_normalized_rms(array, ref)`

Determine the normalized root mean square deviation between input data and reference data in [%].

`normalized_rms = get_normalized_rms(array, ref)`

Parameters

- **array** (*np.ndarray*) – input data [(x), y0, y1, y2 ...]
- **ref** (*np.ndarray*) – reference data [(xref), yref] if ref is 1D, all sizes have to match

Returns **normalized_rms** – normalized root mean square deviation

Return type `float`

`pygpc.misc.get_num_coeffs (order, dim)`

Calculate the number of PCE coefficients by the used order and dimension.

$\text{num_coeffs} = (\text{order} + \text{dim})! / (\text{order}! * \text{dim}!)$

`num_coeffs = get_num_coeffs(order, dim)`

Parameters

- **order** (*int*) – global order of expansion
- **dim** (*int*) – number of random variables

Returns `num_coeffs` – number of coefficients and polynomials

Return type `int`

`pygpc.misc.get_num_coeffs_sparse (order_dim_max, order_glob_max, order_inter_max, dim)`

Calculate the number of PCE coefficients for a specific maximum order in each dimension `order_dim_max`, maximum order of interacting polynomials `order_glob_max` and the interaction order `order_inter_max`.

`num_coeffs_sparse = get_num_coeffs_sparse(order_dim_max, order_glob_max, order_inter_max, dim)`

Parameters

- **order_dim_max** (*int or np.ndarray*) – maximum order in each dimension
- **order_glob_max** (*int*) – maximum global order of interacting polynomials
- **order_inter_max** (*int*) – interaction order
- **dim** (*int*) – number of random variables

Returns `num_coeffs_sparse` – number of coefficients and polynomials

Return type `int`

`pygpc.misc.get_pdf_beta (x, p, q, a, b)`

Calculate the probability density function of the beta distribution in the interval [a,b].

$\text{pdf} = (\text{gamma}(p) * \text{gamma}(q) / \text{gamma}(p+q)) * (\text{b}-\text{a})^{-(p+q-1)} * (\text{x}-\text{a})^{p-1} * (\text{b}-\text{x})^{q-1};$

`pdf = get_pdf_beta(x, p, q, a, b)`

Parameters

- **x** (*np.ndarray*) – values of random variable
- **a** (*float*) – min boundary
- **b** (*float*) – max boundary
- **p** (*float*) – parameter defining the distribution shape
- **q** (*float*) – parameter defining the distribution shape

Returns `pdf` – probability density

Return type `np.ndarray`

`pygpc.misc.get_rotation_matrix (theta)`

Generate rotation matrix from euler angles.

`rotation_matrix = get_rotation_matrix(theta)`

Parameters **theta** (*list of float*) – list of euler angles

Returns `rotation_matrix` – rotation matrix computed from euler angles

Return type [3,3] `np.ndarray`

`pygpc.misc.get_set_combinations(array, number_elements)`

Computes all k-tuples (e_1, e_2, \dots, e_k) of combinations of the set of elements of the first row of the input matrix where $e_{n+1} > e_n$

`combination_vectors = get_set_combinations(array, number_elements)`

Parameters

- **array** (*np.ndarray*) – matrix containing a first row of input elements
- **number_elements** (*int*) – number of elements in tuple

Returns `combination_vectors` – matrix of combination vectors

Return type `np.ndarray`

`pygpc.misc.mutcoh(array)`

Calculate the mutual coherence of a matrix A. It can also be referred as the cosine of the smallest angle between two columns.

`mutual_coherence = mutcoh(array)`

Parameters **array** (*np.ndarray*) – input matrix

Returns `mutual_coherence`

Return type `float`

`pygpc.misc.vprint(message, verbose=True)`

Function that prints out a message if verbose argument is true.

`vprint(message, verbose=True)`

Parameters

- **message** (*string*) – string to print in standard output
- **verbose** (*bool, optional, default=True*) – determines if string is printed out

`pygpc.misc.wrap_function(fn, x, args)`

Function wrapper to call anonymous function with variable number of arguments (tuple).

`wrap_function(fn, x, args)`

Parameters

- **fn** (*function*) – anonymous function to call
- **x** (*tuple*) – parameters of function
- **args** (*tuple*) – arguments of function

Returns `function_wrapper` – wrapped function

Return type `function`

1.5 pygpc.ni module

Functions that provide adaptive regression approaches to perform uncertainty analysis on dynamic systems.

`pygpc.ni.run_reg_adaptive2(random_vars, pdf_type, pdf_shape, limits, func, args=(), order_start=0, order_end=10, interaction_order_max=None, eps=0.001, print_out=False, seed=None, save_res_fn="")`

Perform adaptive regression approach based on leave one out cross validation error estimation.

Parameters

- **random_vars** (*list of str*) – string labels of the random variables
- **pdf_type** (*list*) – type of probability density functions of input parameters, i.e. ["beta", "norm", ...]
- **pdf_shape** (*list of lists*) – shape parameters of probability density functions
s1=[...] "beta": p, "norm": mean s2=[...] "beta": q, "norm": std pdf_shape = [s1,s2]
- **limits** (*list of lists*) – upper and lower bounds of random variables (only "beta")
a=[...] "beta": lower bound, "norm": n/a define 0 b=[...] "beta": upper bound, "norm": n/a define 0 limits = [a,b]
- **func** (*function*) – the objective function to be minimized func(x,*args)
- **args** (*tuple, optional, default=()*) – extra arguments passed to function i.e. f(x,*args)
- **order_start** (*int, optional, default=0*) – initial gpc expansion order
- **order_end** (*int, optional, default=10*) – maximum gpc expansion order
- **interaction_order_max** (*int, optional, default=None*) – define maximum interaction order of parameters if None, perform all interactions
- **eps** (*float, optional, default=1E-3*) – relative mean error bound of leave one out cross validation
- **print_out** (*boolean, optional, default=False*) – boolean value that determines if to print output the iterations and subiterations
- **seed** (*int, optional, default=None*) – seeding point to replicate random grids
- **save_res_fn** (*str, optional, default*) – hdf5 filename where the output data should be saved

Returns

- **gobj** (*gpc object*) – gpc object
- **res** (*[N_grid x N_out] np.ndarray*) – function values at grid points of the N_out output variables

```
pygpc.ni.run_reg_adaptive_E_gpc(pdf_type, pdf_shape, limits, func, args=(), fname=None,
                                order_start=0, order_end=10, interaction_order_max=None,
                                eps=0.001, print_out=False, seed=None, do_mp=False,
                                n_cpu=4, dispy=False, dispy_sched_host='localhost', random_vars="", hdf5_geo_fn="")
```

Perform adaptive regression approach based on leave one out cross validation error estimation.

Parameters

- **random_vars** (*list of str*) – string labels of the random variables
- **pdf_type** (*list*) – type of probability density functions of input parameters, i.e. ["beta", "norm", ...]
- **pdf_shape** (*list of lists*) – shape parameters of probability density functions
s1=[...] "beta": p, "norm": mean s2=[...] "beta": q, "norm": std pdf_shape = [s1,s2]
- **limits** (*list of lists*) – upper and lower bounds of random variables (only "beta")
a=[...] "beta": lower bound, "norm": n/a define 0 b=[...] "beta": upper bound, "norm": n/a define 0 limits = [a,b]
- **func** (*function*) – the objective function to be minimized func(x,*args)

- **args** (*tuple, optional, default=()*) – extra arguments passed to function i.e. $f(x, *args)$
- **fname** (*str, optional, default=None*) – if fname exists, reg_obj will be created from it if not exist, it will be created
- **order_start** (*int, optional, default=0*) – initial gpc expansion order
- **order_end** (*int, optional, default=10*) – maximum gpc expansion order
- **interaction_order_max** (*int, optional, default=None*) – define maximum interaction order of parameters if None, perform all interactions
- **eps** (*float, optional, default=1E-3*) – relative mean error bound of leave one out cross validation
- **print_out** (*boolean, optional, default=False*) – boolean value that determines if to print output the iterations and subiterations
- **seed** (*int, optional, default=None*) – seeding point to replicate random grids
- **do_mp** (*boolean, optional, default=False*) – boolean value that determines if to do each $func(x, *args)$ in each iteration with `parmap.starmap(func)`
- **n_cpu** (*int, optional, default=4*) – if multiprocessing is enabled, utilize n_cpu cores
- **dispy** (*boolean, optional, default=False*) – boolean value that determines if to compute function with dispy cluster
- **dispy_sched_host** (*str, optional, default='localhost'*) – host name where dispy scheduler will be running
- **hdf5_geo_fn** (*str, optional, default=''*) – hdf5 filename with spatial information: /mesh/elm/*

Returns

- **gobj** (*gpc object*) – gpc object
- **res** (*[N_grid x N_out] np.ndarray*) – function values at grid points of the N_out output variables

1.6 pygpc.postproc module

Functions that provide postprocessing implementations

`pygpc.postproc.get_extracted_sobol_order(sobol, sobol_idx, order=1)`

Extract Sobol indices with specified order from Sobol data.

`sobol_1st, sobol_idx_1st = extract_sobol_order(sobol, sobol_idx, order=1)`

Parameters

- **sobol** (*[N_sobol x N_out] np.ndarray*) – Sobol indices of N_out output quantities
- **sobol_idx** (*[N_sobol] list or np.ndarray of int*) – list of parameter label indices belonging to Sobol indices
- **order** (*int, optional, default=1*) – Sobol index order to extract

Returns

- **sobol_n_order** (*np.ndarray*) – n-th order Sobol indices of N_out output quantities
- **sobol_idx_n_order** (*np.ndarray*) – List of parameter label indices belonging to n-th order Sobol indices

1.7 pygpc.quad module

Class that provides polynomial chaos quadratur methods

class `pygpc.quad.Quad` (*pdf_type, pdf_shape, limits, order, order_max, interaction_order, grid, random_vars=None*)

Bases: `pygpc.gpc.gPC`

Quadratur gPC subclass

`Quad(pdf_type, pdf_shape, limits, order, order_max, interaction_order, grid, random_vars=None)`

N_grid

number of grid points

Type int

dim

number of uncertain parameters to process

Type int

pdf_type

type of pdf ‘beta’ or ‘norm’

Type [dim] list of str

pdf_shape

shape parameters of pdfs beta-dist: [[alpha], [beta]] normal-dist: [[mean], [variance]]

Type list of list of float

limits

upper and lower bounds of random variables beta-dist: [[a1 ...], [b1 ...]] normal-dist: [[0 ...], [0 ...]]
(not used)

Type list of list of float

order

maximum individual expansion order generates individual polynomials also if maximum expansion order in order_max is exceeded

Type [dim] list of int

order_max

maximum expansion order (sum of all exponents) the maximum expansion order considers the sum of the orders of combined polynomials only

Type int

interaction_order

number of random variables, which can interact with each other all polynomials are ignored, which have an interaction order greater than the specified

Type int

grid

grid object generated in grid.py including grid.coords and grid.coords_norm

Type grid object

random_vars

string labels of the random variables

Type [dim] list of str

Parameters

- **pdf_type** ([dim] list of str) – type of pdf ‘beta’ or ‘norm’
- **pdf_shape** (list of list of float) – shape parameters of pdfs beta-dist: [[alpha], [beta]] normal-dist: [[mean], [variance]]
- **limits** (list of list of float) – upper and lower bounds of random variables beta-dist: [[a1 ...], [b1 ...]] normal-dist: [[0 ...], [0 ...]] (not used)
- **order** ([dim] list of int) – maximum individual expansion order generates individual polynomials also if maximum expansion order in order_max is exceeded
- **order_max** (int) – maximum expansion order (sum of all exponents) the maximum expansion order considers the sum of the orders of combined polynomials only
- **interaction_order** (int) – number of random variables, which can interact with each other all polynomials are ignored, which have an interaction order greater than the specified
- **grid** (grid object) – grid object generated in grid.py including grid.coords and grid.coords_norm
- **random_vars** ([dim] list of str, optional, default=None) – string labels of the random variables

get_coeffs_expand (sim_results)

Determine the gPC coefficients by the quadrature method

coeffs = get_coeffs_expand(self, sim_results)

Parameters **sim_results** ([N_grid x N_out] np.ndarray of float) – results from simulations with N_out output quantities

Returns **coeffs** – gPC coefficients

Return type [N_coeffs x N_out] np.ndarray of float

1.8 pygpc.reg module

Class that provides polynomial chaos regression methods

class pygpc.reg.Reg (pdf_type, pdf_shape, limits, order, order_max, interaction_order, grid, random_vars=None)

Bases: [pygpc.gpc.gPC](#)

Regression gPC subclass

Reg(pdf_type, pdf_shape, limits, order, order_max, interaction_order, grid, random_vars=None)

N_grid

number of grid points

Type int

dim
number of uncertain parameters to process
Type int

pdf_type
type of pdf 'beta' or 'norm'
Type [dim] list of str

pdf_shape
shape parameters of pdfs beta-dist: [[alpha], [beta]] normal-dist: [[mean], [variance]]
Type list of list of float

limits
upper and lower bounds of random variables beta-dist: [[a1 ...], [b1 ...]] normal-dist: [[0 ...], [0 ...]]
(not used)
Type list of list of float

order
maximum individual expansion order generates individual polynomials also if maximum expansion order in order_max is exceeded
Type [dim] list of int

order_max
maximum expansion order (sum of all exponents) the maximum expansion order considers the sum of the orders of combined polynomials only
Type int

interaction_order
number of random variables, which can interact with each other all polynomials are ignored, which have an interaction order greater than the specified
Type int

grid
grid object generated in grid.py including grid.coords and grid.coords_norm
Type grid object

random_vars
string labels of the random variables
Type [dim] list of str

relative_error_loocv
relative error of the leave-one-out-cross-validation
Type list of float

nan_elm
which elements were dropped due to NaN
Type list of float

Parameters

- **pdf_type** (*[dim] list of str*) – type of pdf 'beta' or 'norm'
- **pdf_shape** (*list of list of float*) – shape parameters of pdfs beta-dist: [[alpha], [beta]] normal-dist: [[mean], [variance]]

- **limits** (*list of list of float*) – upper and lower bounds of random variables
beta-dist: [[a1 ...], [b1 ...]] normal-dist: [[0 ...], [0 ...]] (not used)
- **order** (*[dim] list of int*) – maximum individual expansion order generates individual polynomials also if maximum expansion order in order_max is exceeded
- **order_max** (*int*) – maximum expansion order (sum of all exponents) the maximum expansion order considers the sum of the orders of combined polynomials only
- **interaction_order** (*int*) – number of random variables, which can interact with each other all polynomials are ignored, which have an interaction order greater than the specified
- **grid** (*grid object*) – grid object generated in grid.py including grid.coords and grid.coords_norm
- **random_vars** (*[dim] list of str, optional, default=None*) – string labels of the random variables

get_coeffs_expand (*sim_results*)

Determine the gPC coefficients by the regression method.

`coeffs = get_coeffs_expand(sim_results)`

Parameters **sim_results** (*[N_grid x N_out] np.ndarray of float*) – results from simulations with N_out output quantities,

Returns **coeffs** – gPC coefficients

Return type [N_coeffs x N_out] np.ndarray of float

get_loocv (*sim_results*)

Perform leave one out cross validation of gPC with maximal 100 points and add result to self.relative_error_loocv.

`relative_error_loocv = get_loocv(sim_results)`

Parameters **sim_results** (*[N_grid x N_out] np.ndarray*) – Results from N_grid simulations with N_out output quantities

Returns **relative_error_loocv** – relative mean error of leave one out cross validation

Return type float

1.9 pygpc.rw module

Functions that provide input and output functionality

`pygpc.rw.read_data_hdf5 (fname, loc)`

Read data from .hdf5 file (e.g. coeffs, mean, std, ...).

`load_data_hdf5(fname, loc)`

Parameters

- **fname** (*str*) – path to input file
- **loc** (*str*) – location (folder and name) in hdf5 file (e.g. data/phi)

`pygpc.rw.read_gpc_pk1 (fname)`

Read gPC object including infos about input pdfs, polynomials, grid etc.

`object = read_gpc_obj(fname)`

Parameters **fname** (*str*) – path to input file

`pygpc.rw.read_gpc_yaml(fname)`

Read gPC infos about input pdfs, polynomials, grid etc. as .yaml file and initialize gpc object.

`obj = read_gpc_yaml(fname)`

Parameters **fname** (*str*) – path to input file

`pygpc.rw.read_sobol_idx_txt(fname)`

Read sobol_idx list from file.

`read_sobol_idx_txt(fname)`

Parameters **fname** (*str*) – path to input file

Returns **sobol_idx** – list of parameter label indices belonging to Sobol indices

Return type [N_sobol] list of np.array

`pygpc.rw.write_data_hdf5(data, fname, loc)`

Write quantity of interest in .hdf5 file (e.g. coeffs, mean, std, ...).

`write_data_hdf5(data, fname, loc)`

Parameters

- **data** (*np.ndarray*) – data to save
- **fname** (*str*) – path to output file
- **loc** (*str*) – location (folder and name) in hdf5 file (e.g. data/phi)

`pygpc.rw.write_data_txt(data, fname)`

Write data (quantity of interest) in .txt file (e.g. coeffs, mean, std, ...).

`write_data_txt(data, fname)`

Parameters

- **data** (*np.ndarray*) – data to save
- **fname** (*str*) – path to output file

`pygpc.rw.write_gpc_pkl(obj, fname)`

Write gPC object including infos about input pdfs, polynomials, grid etc. as pickle file.

`write_gpc_obj(obj, fname)`

Parameters

- **obj** (*gPC or derived class*) – class instance containing gpc data
- **fname** (*str*) – path to output file

`pygpc.rw.write_gpc_yaml(obj, fname)`

Write gPC infos about input pdfs, polynomials, grid etc. as .yaml file.

`write_gpc_yaml(obj, fname)`

Parameters

- **obj** (*gPC or derived class*) – class instance containing gpc data
- **fname** (*str*) – path to output file

`pygpc.rw.write_sobol_idx_txt(sobol_idx, fname)`

Write sobol_idx list in file.

`write_sobol_idx_txt(sobol_idx, filename)`

Parameters

- **sobol_idx** (*[N_sobol]* list of *np.ndarray*) – list of parameter label indices belonging to Sobol indices
- **fname** (*str*) – path to output file

1.10 pygpc.testfun module

Testfunctions and electromagnetic field calculations

`pygpc.testfun.calc_B_field_outside_sphere(sphere_radius, dipole_pos, dipole_moment, detector_positions)`

Calculate the B field outside a sphere, does not depend on conductivity. Dipole in SI units, positions in mm

J.Savras - Basic mathematical and electromagnetic concepts of the biomagnetic inverse problem

`B = calc_B_field_outside_sphere(sphere_radius, dipole_pos, dipole_moment, detector_positions)`

Parameters

- **sphere_radius** (*float*) – radius of sphere
- **dipole_pos** (*[3 x 1]* *np.ndarray*) – position of dipole
- **dipole_moment** (*[3 x 1]* *np.ndarray*) – moment of dipole
- **detector_positions** (*[n x 3]* *np.ndarray*) – position of detectors, must lie outside sphere

Returns **B** – array with B fields in detector positions

Return type *[N x 3]* *np.ndarray*

`pygpc.testfun.calc_fibonacci_sphere(nr_points, R=1)`

Creates N points around evenly spread through a unit sphere.

`points = calc_fibonacci_sphere(nr_points, R=1)`

Parameters

- **nr_points** (*int*) – number of points to be spread, must be odd
- **R** (*float, optional, default=1*) – radius of sphere

Returns **points** – evenly spread points through a unit sphere

Return type *[N x 3]* *np.ndarray*

`pygpc.testfun.calc_potential_dipole_3layers(radii, cond_brain_scalp, cond_skull, dipole_pos, dipole_moment, surface_points, nbr_polynomials=100)`

Calculates the electric potential in a 3-layered sphere caused by a dipole Calculations assumes dimensions in SI units

Ary, James P., Stanley A. Klein, and Derek H. Fender. "Location of sources of evoked scalp potentials: corrections for skull and scalp thicknesses." Biomedical Engineering 28.6 (1981). eq. 2 and 2a

Parameters

- **radii** (*[3] list*) – radius of each of the 3 layers (innermost to outermost), in mm
- **cond_brain_scalp** (*float*) – conductivity of the brain and scalp layers, in S/m
- **cond_skull** (*float*) – conductivity of the skull layer, in S/m
- **dipole_pos** (*[3 x 1] np.ndarray*) – position of the dipole, in mm
- **dipole_moment** (*[3 x 1] np.ndarray*) – moment of dipole, in C x m
- **surface_points** (*[N x 3] np.ndarray*) – list of positions where the potential should be calculated, in mm
- **nbr_polynomials** (*int*) – number of legendre polynomials to use (default = 100)

Returns **potential** – values of the electric potential, in V

Return type *[N x 1] np.ndarray*

```
pygpc.testfun.calc_potential_homogeneous_dipole(sphere_radius, conductivity,
                                                  dipole_pos, dipole_moment, de-
                                                  tector_positions)
```

Calculate the surface potential generated by a dipole inside a homogeneous conducting sphere.

Dezhong Yao, Electric Potential Produced by a Dipole in a Homogeneous Conducting Sphere

potential = **calc_potential_homogeneous_dipole**(**sphere_radius**, **conductivity**, **dipole_pos**, **dipole_moment**, **detector_positions**):

Parameters

- **sphere_radius** (*float*) – radius of sphere, in mm
- **conductivity** (*float*) – conductivity of medium, in S/m
- **dipole_pos** (*[3 x 1] np.ndarray*) – position of dipole, in mm
- **dipole_moment** (*[3 x 1] np.ndarray*) – moment of dipole, in C.m
- **detector_positions** (*[n x 3] np.ndarray*) – position of detectors, will be projected into the sphere surface, in mm

Returns **potential** – potential at the points

Return type *[n x 1] np.ndarray*

```
pygpc.testfun.calc_potentials_3layers_surface_electrodes(conductivities, radii, an-
                                                           ode_pos, cathode_pos, p,
                                                           nbr_polynomials=50)
```

Calculate the electric potential in a 3-layered sphere caused by point-like electrodes.

S.Rush, D.Driscoll EEG electrode sensitivity—an application of reciprocity

potential = **calc_potentials_3layers_surface_electrodes**(**conductivities**, **radii**, **anode_pos**, **cathode_pos**, **p**, **nbr_polynomials**=50):

Parameters

- **conductivities** (*[3] list*) – conductivity of the 3 layers (innermost to outermost), in S/m
- **radii** (*[3] list*) – radius of each of the 3 layers (innermost to outermost), in mm
- **anode_pos** (*[3 x 1] np.ndarray*) – position of the anode_pos, in mm
- **cathode_pos** (*[3 x 1] np.ndarray*) – position of cathode_pos, in mm

- **p** ($[N \times 3]$ *np.ndarray*) – list of positions where the poteitial should be calculated, in mm
- **nbr_polynomials** (*int, optional, default=50*) – number of of legendre polynomials to use

Returns **potential** – values of the electric potential, in V

Return type $[N \times 1]$ *np.ndarray*

`pygpc.testfun.calc_tms_E_field(dipole_pos, dipole_moment, didt, positions)`

Calculate the E field in a sphere caused by external magnetic dipoles. Dipole in SI units, positions in mm. Everything should be in SI Independent of conductivity, see references

L. Heller and D. van Hulsteyn, Brain stimulation using electromagnetic sources: theoretical aspects

`E = calc_tms_E_field(dipole_pos, dipole_moment, didt, positions)`

Parameters

- **dipole_pos** ($[M \times 3]$ *np.ndarray*) – position of dipoles, must be outside sphere
- **dipole_moment** ($[m \times 3]$ *np.ndarray*) – moment of dipoles
- **didt** (*float*) – variation rate of current in the coil
- **positions** ($[N \times 3]$ *np.ndarray*) – position where fields should be calculated, must lie inside sphere

Returns **E** – array with E-fields at detector positions

Return type $[N \times 3]$ *np.ndarray*

`pygpc.testfun.g_function(x, a)`

N-dimensional g-function used by Saltelli and Sobol

this test function is used as an integrand for various numerical estimation methods, including sensitivity analysis methods, because it is fairly complex, and its sensitivity indices can be expressed analytically. The exact value of the integral with this function as an integrand is 1.

Saltelli, Andrea; Sobol, I. M. (1995): Sensitivity analysis for nonlinear mathematical models: numerical experience. In: Mathematical models and computer experiment 7 (11), S. 16-28.

`y = g_function(x, a)`

Parameters

- **x** ($[N_input \times N_dims]$ *np.ndarray*) – input data
- **a** ($[N_dims]$ *np.ndarray*) – importance factor of dimensions

Returns **y** – output data

Return type $[N_input \times 1]$ *np.ndarray*

`pygpc.testfun.ishigami(x, a, b)`

Three-dimensional test function of Ishigami

The Ishigami function of Ishigami & Homma (1990) is used as an example for uncertainty and sensitivity analysis methods, because it exhibits strong nonlinearity and nonmonotonicity. It also has a peculiar dependence on x_3 , as described by Sobol' & Levitan (1999).

Ishigami, T., & Homma, T. (1990, December). An importance quantification technique in uncertainty analysis for computer models. In Uncertainty Modeling and Analysis, 1990. Proceedings., First International Symposium on (pp. 398-403). IEEE.

Sobol', I. M., & Levitan, Y. L. (1999). On the use of variance reducing multipliers in Monte Carlo computations of a global sensitivity index. *Computer Physics Communications*, 117(1), 52-61.

$$f(x) = \sin(x_1) + a \cdot \sin(x_2)^2 + b \cdot x_3^4 \cdot \sin(x_1)$$

`y = ishigami(x,a,b)`

Parameters

- **x** (`[N x 3] np.ndarray`) – input data $x_i \sim \text{Uniform}[-\pi, \pi]$, for all $i = 1, 2, 3$
- **a** (`float`) – shape parameter
- **b** (`float`) – shape parameter

Returns **y** – output data

Return type `[N x 1] np.ndarray`

`pygpc.testfun.lim_2002(x)`

Two-dimensional test function of Lim et al

This function is a polynomial in two dimensions, with terms up to degree 5. It is nonlinear, and it is smooth despite being complex, which is common for computer experiment functions (Lim et al., 2002).

Lim, Y. B., Sacks, J., Studden, W. J., & Welch, W. J. (2002). Design and analysis of computer experiments when the output is highly correlated over the input space. *Canadian Journal of Statistics*, 30(1), 109-126.

$$f(x) = 9 + 5/2 \cdot x_1 - 35/2 \cdot x_2 + 5/2 \cdot x_1 \cdot x_2 + 19 \cdot x_2^2 - 15/2 \cdot x_1^3$$

$$+ 5/2 \cdot x_1 \cdot x_2^2 - 11/2 \cdot x_2^4 + x_1^3 \cdot x_2^2$$

`y = lim_2002(x)`

Parameters **x** (`[N x 2] np.ndarray`) – input data x_i is element of $[0, 1]$, for all $i = 1, 2$

Returns **y** – output data

Return type `[N x 1] np.ndarray`

`pygpc.testfun.oakley_ohagan_2004(x)`

15-dimensional test function of OAKLEY & O'HAGAN (2004)

This function's a-coefficients are chosen so that 5 of the input variables contribute significantly to the output variance, 5 have a much smaller effect, and the remaining 5 have almost no effect on the output variance.

Oakley, J. E., & O'Hagan, A. (2004). Probabilistic sensitivity analysis of complex models: a Bayesian approach. *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 66(3), 751-769.

`y = oakley_ohagan_2004(x)`

Parameters **x** (`[N_input x 15] np.ndarray`) – input data $x_i \sim N(\mu=0, \sigma=1)$, for all $i = 1, 2, \dots, 15$.

Returns **y** – output data

Return type `[N_input x 1] np.ndarray`

`pygpc.testfun.peaks(x)`

Two-dimensional peaks function.

`y = peaks(x)`

Parameters **x** (`[N x 2] np.ndarray`) – input data

Returns **y** – output data

Return type `[N x 1] np.ndarray`

`pygpc.testfun.sphere(x)`
N-dimensional sphere function.

`y = sphere(x)`

Parameters `x` (`[N_input x N_dims] np.ndarray`) – input data

Returns output data

Return type `y` `[N_input x 1] np.ndarray`

`pygpc.testfun.sphere_zero_mean(x, a, b)`
N-dimensional sphere function with zero mean.

`y = sphere_zero_mean(x,a,b)`

Parameters

- `x` (`[N_input x N_dims] np.ndarray`) – input data
- `a` (`[N_dims] np.ndarray`) – lower bound of input data
- `b` (`[N_dims] np.ndarray`) – upper bound of input data

Returns `y` – output data

Return type `[N_input] np.ndarray`

`pygpc.testfun.welch_1992(x)`
20-dimensional test function of WELCH (1992)

For input variable screening purposes, it can be found that some input variables of this function have a very high effect on the output, compared to other input variables. As Welch et al. (1992) point out, interactions and nonlinear effects make this function challenging.

Welch, W. J., Buck, R. J., Sacks, J., Wynn, H. P., Mitchell, T. J., & Morris, M. D. (1992). Screening, predicting, and computer experiments. *Technometrics*, 34(1), 15-25.

`y = welch_1992(x)`

Parameters `x` (`[N_input x 20] np.ndarray`) – input data $x_i \sim U(-0.5, 0.5)$, for all $i = 1, \dots, 20$.

Returns `y` – output data

Return type `[N_input x 1] np.ndarray`

`pygpc.testfun.wing_weight(x)`
10-dimensional test function which models a light aircraft wing

Forrester, A., Sobester, A., & Keane, A. (2008). *Engineering design via surrogate modelling: a practical guide*. Wiley.

`y = wing_weight(x)`

Parameters `x` (`[N_input x 10] np.ndarray`) – input data `x1(Sw)` is element of `[150, 200]` `x2(Wfw)` is element of `[220, 300]` `x3(A)` is element of `[6, 10]` `x4(Lambda)` is element of `[-10, 10]` `x5(q)` is element of `[16, 45]` `x6(lambda)` is element of `[0.5, 1]` `x7(tc)` is element of `[0.08, 0.18]` `x8(Nz)` is element of `[2.5, 6]` `x9(Wdg)` is element of `[1700, 2500]` `x10(Wp)` is element of `[0.025, 0.08]`

Returns `y` – output data

Return type `[N_input x 1] np.ndarray`

1.11 pygpc.vis module

Functions and classes that provide visualisation functionalities

class `pygpc.vis.Visualization` (*dims*=(10, 10))

Creates a new visualization in a new window. Any added subcharts will be added to this window.

`Visualisation(dims=(10, 10))`

`Visualisation.figure_number`

number of figures that have been created

Type `int`, `begin=0`

`Visualisation.horizontal_padding`

horizontal padding of plot

Type `float`, `default=0.4`

`Visualisation.font_size_label`

font size of title

Type `int`, `default=12`

`Visualisation.font_size_label`

font size of label

Type `int`, `default=12`

`Visualisation.graph_lind_width`

line width of graph

Type `int`, `default 2`

fig

handle of figure created by `matplotlib.pyplot`

Type `mpl.figure`

Parameters *dims* (*list of int, optional, default=(10, 10)*) – size of the newly created window

add_heat_map (*title, labels, grid_points, data_points, v_lim=(None, None), x_lim=None, y_lim=None, colormap=None*)

Draw a 2D heatmap into the current figure.

`add_heat_map(title, labels, grid_points, data_points, v_lim=(None, None), x_lim=None, y_lim=None, colormap=None)`

Parameters

- **title** (*str*) – title of the graph
- **labels** (*{str:str} dict*) – {'x': name of x-axis, 'y': name of y-axis}
- **grid_points** (*[2] list of np.ndarray*) – arrays of the x and y positions of the grid points
- **data_points** (*np.ndarray of the data points that are placed into the grid*) –
- **x_lim** (*[2] list of float, optional, default=None*) – x limits for the function argument or value

- **y_lim** ([2] list of float, optional, default=None) – y limits for the function argument or value
- **v_lim** ([2] list of float, optional, default=(None, None)) – limits of the color scale
- **colormap** (str, optional, default=None) – the colormap to use

add_line_plot (title, labels, data, x_lim=None, y_lim=None)

Draw a 1D line graph into the current figure.

add_line_plot(title, labels, data, x_lim=None, y_lim=None)

Parameters

- **title** (str) – title of the graph
- **labels** ({str:str} dict) – {'x': name of x-axis, 'y': name of y-axis}
- **x_lim** ([2] list of float, optional, default=None) – x limits for the function argument or value
- **y_lim** ([2] list of float, optional, default=None) – y limits for the function argument or value
- **data** (np.ndarray) – data that should be plotted

static add_scatter_plot (shape, plot_size, color_sequence, colormap=None, v_lim=(None, None))

Draw a scatter plot onto the current chart.

add_scatter_plot(shape, plot_size, color_sequence, colormap=None, v_lim=(None, None))

Parameters

- **shape** ({str: np.ndarray} dict) – {'x': positions on x-axis, 'y': positions on y-axis}
- **plot_size** (np.ndarray) – the marker size in the squared number of points
- **color_sequence** (str or list) – marker colors
- **colormap** (str, optional, default=None) – the colormap to use
- **v_lim** ([2] list of float, optional, default=(None, None)) – limits of the color scale

create_new_chart (layout_id=None)

Add a new subplot to the current visualization, so that multiple graphs can be overlaid onto one chart (e.g. scatterplot over heatmap).

create_new_chart(layout_id=None)

Parameters layout_id ((3-digit) int, optional, default=None) – denoting the position of the graph in figure (xyn : 'x'=width, 'y'=height of grid, 'n'=position within grid)

static create_sub_plot (title, labels, x_lim, y_lim)

Set the title, labels and the axis limits of a plot.

create_sub_plot(title, labels, x_lim, y_lim)

Parameters

- **title** (str) – title of the plot
- **labels** ({str:str} dict) – {'x': name of x-axis, 'y': name of y-axis}

- **x_lim**(*[2] list of float*) – x limits for the function argument or value
- **y_lim**(*[2] list of float*) – y limits for the function argument or value

figure_number = 0

font_size_label = 12

font_size_title = 12

graph_line_width = 2

horizontal_padding = 0.4

static show()

Show plots.

`pygpc.vis.plot_sobol_indices(sobol_rel_order_mean, sobol_rel_1st_order_mean, fn_plot, random_vars)`

Plot the Sobol indices into different sub-plots.

`plot_sobol_indices(sobol_rel_order_mean, sobol_rel_1st_order_mean, fn_plot, random_vars)`

Parameters

- **sobol_rel_order_mean** (*np.ndarray*) – average proportion of the Sobol indices of the different order to the total variance (1st, 2nd, etc...) over all output quantities
- **sobol_rel_1st_order_mean** (*np.ndarray*) – average proportion of the random variables of the 1st order Sobol indices to the total variance over all output quantities
- **fn_plot** (*str*) – filename of plot
- **random_vars** (*[dim] list of str*) – string labels of the random variables

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