### Slides PHY 480 and PHY 905 Introduction to programming (C++ and Fortran)

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### Extremely useful tools, strongly recommended

### and discussed at the lab sessions the first two weeks

- GIT for version control, discussed at the lab this week (and next week as well)
- ipvthon notebook, mentioned this week
- QTcreator for editing and mastering computational projects
- Armadillo as a useful numerical library for C++, highly recommended
- Unit tests

### A structured programming approach

- Before writing a single line, have the algorithm clarified and understood. It is crucial to have a logical structure of e.g., the flow and organization of data before one starts writing.
- Always try to choose the simplest algorithm. Computational speed can be improved upon later.
- Try to write a as clear program as possible. Such programs are easier to debug, and although it may take more time, in the long run it may save you time. If you collaborate with other people, it reduces spending time on debuging and trying to understand what the codes do. A clear program will also allow you to remember better what the program really does!

### A structured programming approach

- The planning of the program should be from top down to bottom, trying to keep the flow as linear as possible. Avoid jumping back and forth in the program. First you need to arrange the major tasks to be achieved. Then try to break the major tasks into subtasks. These can be represented by functions or subprograms. They should accomplish limited tasks and as far as possible be independent of each other. That will allow you to use them in other programs as well.
- Try always to find some cases where an analytical solution exists or where simple test cases can be applied. If possible, devise different algorithms for solving the same problem. If you get the same answers, you may have coded things correctly or made the same error twice or more.

### Getting Started

### Compiling and linking, without QTcreator

In order to obtain an executable file for a C++ program, the following instructions under Linux/Unix can be used

c++ -c -Wall myprogram.cpp c++ -o myprogram myprogram.o

where the compiler is called through the command c++/g++. The compiler option -Wall means that a warning is issued in case of non-standard language. The executable file is in this case myprogram. The option -c is for compilation only, where the program is translated into machine code, while the -o option links the produced object file myprogram. o and produces the executable myprogram.

For Fortran2008 we use the Intel compiler, replace c++ with ifort. Also, to speed up the code use compile options like

c++ -03 -c -Wall myprogram.cpp

### Makefiles and simple scripts

Under Linux/Unix it is often convenient to create a so-called makefile, which is a script which includes possible compiling commands.

```
# Comment lines
# General makefile for c - choose PROG = name of given program
# Here we define compiler option, libraries and the target
CC= gt+ -Wall
PROG= myprogram
# this is the math library in C, not necessary for C++
LIB = -lm
# Here we make the executable file
$ (PROG) :
$ (PROG) . o
$ (CC) $ (PROG) . o
$ (CC) $ (PROG) . o
$ (CC) $ (PROG) . c
$ (PROG) . c
$ (PROG) . c
$ (CC) - c
$ (PROG) . c
$ (CC) - c
$ (PROG) . c
```

If you name your file for makefile, simply type the command make and Linux/Unix executes all of the statements in the above makefile. Note that C++ files have the extension .cpp.

### Hello worl

### The C encounter

### Hello World, dissecting the code

### Dissection I

The compiler must see a declaration of a function before you can call it (the compiler checks the argument and return types). The declaration of library functions appears in so-called "header files" that must be included in the program, e.g.,

```
#include <stdlib.h> /* atof function */
```

We call three functions (atof, sin, printf) and these are declared in three different header files. The main program is a function called main with a return value set to an integer, int (0 if success). The operating system stores the return value, and other programs/utilities can check whether the execution was successful or not. The command-line arguments are transferred to the main

int main (int argc, char\* argv[])

### Hello World, more dissection

### Dissection II

The command-line arguments are transferred to the main function through

```
int main (int argc, char* argv[])
```

The integer argc is the no of command-line arguments, set to one in our case, while argv is a vector of strings containing the command-line arguments with argv [0] containing the name of the program and argv [1], argv [2], ... are the command-line args, i.e., the number of lines of input to the program. Here we define floating points, see also below, through the keywords float for single precision real numbers and double for double precision. The function atof transforms a text (argv [1]) to a float. The sine function is declared in math.h, a library which is not automatically included and needs to be linked when computing an executable file. With the command printf we obtain a formatted printout. The printf syntax is used for formatting output in many C-inspired languages (Perl, Python, Awk, partly C++).

### Hello World

function through

### Now in C++

Here we present first the C++ version.

```
// A comment line begins like this in C++ programs
// Standard ANSI-C++ include files
finclude <iostream // input and output
finclude <cmath // math functions
using namespace std;
int main (int argc, char* argv[])

// convert the text argv[i] to double using atof:
double r = atof(argv[i]); /* convert the text argv[i] to double */
double s = sin(r);
cout << "Hello, World! sin(" << r << ") =" << s << endl;
return 0; /* success execution of the program */
}
```

### C++ Hello World

### Dissection

We have replaced the call to printf with the standard C++ function cout. The header file <iostream.h> is then needed. In addition, we don't need to declare variables like r and s at the beginning of the program. I personally prefer however to declare all variables at the beginning of a function, as this gives me a feeling of greater readability.

### Brief summary

### C/C++ program

- A C/C++ program begins with include statements of header files (libraries,intrinsic functions etc)
- Functions which are used are normally defined at top (details next week)
- The main program is set up as an integer, it returns 0 (everything correct) or 1 (something went wrong)
- $\bullet$  Standard if, while and for statements as in Java, Fortran, Python...
- Integers have a very limited range.

### Brief summary

### Arrays

- A C/C++ array begins by indexing at 0!
- Array allocations are done by size, not by the final index value. If you allocate an array with 10 elements, you should index them from 0.1....9.
- Initialize always an array before a computation.

### Integer and Real Numbers Overflow Underflow Roundoff errors Loss of precision

### Limits, you must declare variables

### C++ and Fortran declarations type in C/C++ and Fortran2008 bits range 16 -32768 to 32767 int/INTEGER (2) unsigned int 16 0 to 65535 signed int 16 -32768 to 32767 16 -32768 to 32767 short int unsigned short int 16 0 to 65535 signed short int 16 -32768 to 32767 int/long int/INTEGER (4) 32 -2147483648 to 2147483647 32 -2147483648 to 2147483647 signed long int 32 $3.4 \times 10^{-44}$ to $3.4 \times 10^{+38}$ float/REAL(4) 64 $1.7 \times 10^{-322}$ to $1.7 \times 10^{+308}$ double/REAL(8) 64 $1.7 \times 10^{-322}$ to $1.7 \times 10^{+308}$ long double

### How to do it $a_n2^n+a_{n-1}2^{n-1}+a_{n-2}2^{n-2}+\cdots+a_02^0.$ In binary notation we have thus $(417)_{10}=(110110001)_2$ since we have $(110100001)_2=1\times 2^8+1\times 2^7+0\times 2^6+1\times 2^5+0\times 2^4+0\times 2^3\\ +0\times 2^2+0\times 2^2+0\times 2^1+1\times 2^0.$

From decimal to binary representation

### From decimal to binary representation, the actual operation

```
\underline{\text{To see this, we have performed the following}} divisions by 2
```

```
Integer numbers

#include <iostream>
#include <costdio>
#include <cstdio>
#include <cstdio>
#include <cstdio>
#include <cstdio>
using namespace std;
int main (int argc, char* argv[])

{
   int i;
   int terms[32]; // storage of a0, a1, etc, up to 32 bits
   int save;
   int number = atoi(argv[i]);
   save = number;
   // intitalise the term a0, a1 etc
   for (i=0; i < 32; i++){ terms[i] = 0;}
   for (i=0; i < 32; i++){ terms[i] = 0;}
   for (i=0; i < 32; i++){ terms[i] = 0;}
   // write out results
   cout <</pre>
   // write out results
   cout <</pre>
   // "Wumber of bytes used= " << sizeof(number) << endl;
   for (i=0; i < 32; i++){
        cout <</pre>
   // "Term nr: " << i << "Value= " << terms[i];
        cout << endl;
   }
   return 0;
}
```

### Integer numbers, Fortran PROGRAM binary\_integer IMPLICIT NONE INTEGER 1, number, terms(0:31) ! storage of a0, a1, etc, up to 32 b WRITE(\*,\*) 'Give a number to transform to binary notation' READ(\*,\*) number ! Initialise the terms a0, a1 etc terms = 0 ! Fortran takes only integer loop variables DD i=0, 31 terms(i) = MOD(number,2) number = number/2 ENDDO ! write out results WRITE(\*,\*) 'Binary representation' DD i=0, 31 WRITE(\*,\*) 'Term nr and value', i, terms(i) ENDDO END PROGRAM binary\_integer

### Possible Overflow for Integers // A comment line begins like this in C++ programs // Program to calculate 2\*\*n // Standard ANSI-C++ include files \*/ \*finclude <costream \*finclude <costr

### Loss of Precision

### Machine Numbers

In the decimal system we would write a number like 9.90625 in what is called the normalized scientific notation.

$$9.90625 = 0.990625 \times 10^{1}$$

and a real non-zero number could be generalized as

$$x = \pm r \times 10^{\rm n},\tag{1}$$

with r a number in the range  $1/10 \le r < 1$ . In a similar way we can use represent a binary number in scientific notation as

$$x = \pm q \times 2^{\mathsf{m}},\tag{2}$$

with q a number in the range  $1/2 \le q < 1$ . This means that the mantissa of a binary number would be represented by the general formula

$$(0.a_{-1}a_{-2}\dots a_{-n})_2 = a_{-1} \times 2^{-1} + a_{-2} \times 2^{-2} + \dots + a_{-n} \times 2^{-n}.$$
 (3)

### Loss of Precision

### Machine Numbers

In a typical computer, floating-point numbers are represented in the way described above, but with certain restrictions on  $\boldsymbol{q}$  and  $\boldsymbol{m}$  imposed by the available word length. In the machine, our number  $\boldsymbol{x}$  is represented as

$$x = (-1)^s \times \text{mantissa} \times 2^{\text{exponent}},$$
 (4)

where s is the sign bit, and the exponent gives the available range. With a single-precision word, 32 bits, 8 bits would typically be reserved for the exponent, 1 bit for the sign and 23 for the mantissa.

### Loss of Precision

### Machine Numbers

A modification of the scientific notation for binary numbers is to require that the leading binary digit 1 appears to the left of the binary point. In this case the representation of the mantissa q would be  $(1.f)_2$  and  $1 \leq q < 2$ . This form is rather useful when storing binary numbers in a computer word, since we can always assume that the leading bit 1 is there. One bit of space can then be saved meaning that a 23 bits mantissa has actually 24 bits. This means explicitly that a binary number with 23 bits for the mantissa reads

$$(1.a_{-1}a_{-2}\dots a_{-23})_2 = 1\times 2^0 + a_{-1}\times 2^{-1} + + a_{-2}\times 2^{-2} + \dots + a_{-23}\times 2^{-23}.$$
(5)

### Loss of Precision, example

As an example, consider the 32 bits binary number

where the first bit is reserved for the sign, 1 in this case yielding a negative sign. The exponent m is given by the next 8 binary numbers 01111101 resulting in 125 in the decimal system.

### Loss of Precision

### Machine Numbers

However, since the exponent has eight bits, this means it has  $2^8-1=255$  possible numbers in the interval  $-128 \leq m \leq 127$ , our final exponent is 125-127=-2 resulting in  $2^{-2}$ . Inserting the sign and the mantissa yields the final number in the decimal representation as

$$-2^{-2} \left(1 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2} + 1 \times 2^{-3} + 0 \times 2^{-4} + 1 \times 2^{-5}\right) =$$

$$(-0.4765625)_{10}$$

In this case we have an exact machine representation with 32 bits (actually, we need less than 23 bits for the mantissa).

### Loss of Precision, consequences

If our number x can be exactly represented in the machine, we call x a machine number. Unfortunately, most numbers cannot and are thereby only approximated in the machine. When such a number occurs as the result of reading some input data or of a computation, an inevitable error will arise in representing it as accurately as possible by a machine number.

### Loss of Precision

### Machine Numbers

A floating number x, labelled fl(x) will therefore always be represented as

$$fl(x) = x(1 \pm \epsilon_x),$$
 (6)

with x the exact number and the error  $|\epsilon_x| \leq |\epsilon_M|$ , where  $\epsilon_M$  is the precision assigned. A number like 1/10 has no exact binary representation with single or double precision. Since the mantissa

$$(1.a_{-1}a_{-2}...a_{-n})_2$$

is always truncated at some stage n due to its limited number of bits, there is only a limited number of real binary numbers. The spacing between every real binary number is given by the chosen machine precision. For a 32 bit words this number is approximately  $\epsilon_M \sim 10^{-7}$  and for double precision (64 bits) we have  $\epsilon_M \sim 10^{-16}$ , or in terms of a binary base as  $2^{-23}$  and  $2^{-52}$  for single and double precision, respectively.

### Loss of Precision

### Machine Numbers

In the machine a number is represented as

$$f(x) = x(1+\epsilon) \tag{7}$$

where  $|\epsilon| \leq \epsilon_M$  and  $\epsilon$  is given by the specified precision,  $10^{-7}$  for single and  $10^{-16}$  for double precision, respectively.  $\epsilon_M$  is the given precision. In case of a subtraction a=b-c, we have

$$fl(a) = fl(b) - fl(c) = a(1 + \epsilon_a), \tag{8}$$

or

$$fl(a) = b(1 + \epsilon_b) - c(1 + \epsilon_c), \tag{9}$$

### Loss of Precision

The above means that

$$fl(a)/a = 1 + \epsilon_b \frac{b}{a} - \epsilon_c \frac{c}{a},$$
 (10)

and if  $b \approx c$  we see that there is a potential for an increased error in  $\mathit{fl}(a)$ .

### Loss of Precision

### Machine Numbers

Define the absolute error as

$$|fl(a) - a|, \tag{11}$$

whereas the relative error is

$$\frac{|f(a)-a|}{a} \le \epsilon_a. \tag{12}$$

### Loss of Precision

The above subraction is thus

$$\frac{|fl(a) - a|}{a} = \frac{|fl(b) - fl(c) - (b - c)|}{a},$$
 (13)

yielding

$$\frac{|f(a)-a|}{a}=\frac{|b\epsilon_b-c\epsilon_c|}{a}.$$
 (14)

The relative error is the quantity of interest in scientific work. Information about the absolute error is normally of little use in the absence of the magnitude of the quantity being measured.

### Loss of numerical precision

Suppose we wish to evaluate the function

$$f(x) = \frac{1 - \cos(x)}{\sin(x)},$$

for small values of x. Five leading digits. If we multiply the denominator and numerator with  $1+\cos(x)$  we obtain the equivalent expression

$$f(x) = \frac{\sin(x)}{1 + \cos(x)}$$

If we now choose x = 0.007 (in radians) our choice of precision results in

$$\sin(0.007) \approx 0.69999 \times 10^{-2}$$

and

### Loss of numerical precision

The first expression for f(x) results in

$$f(x) = \frac{1 - 0.99998}{0.69999 \times 10^{-2}} = \frac{0.2 \times 10^{-4}}{0.69999 \times 10^{-2}} = 0.28572 \times 10^{-2},$$

while the second expression results in

$$f(x) = \frac{0.69999 \times 10^{-2}}{1 + 0.99998} = \frac{0.69999 \times 10^{-2}}{1.99998} = 0.35000 \times 10^{-2},$$

which is also the exact result. In the first expression, due to our choice of precision, we have only one relevant digit in the numerator, after the subtraction. This leads to a loss of precision and a wrong result due to a cancellation of two nearly equal numbers. If we had chosen a precision of six leading digits, both expressions yield the same answer.

### Loss of numerical precision

If we were to evaluate  $x \sim \pi$ , then the second expression for f(x) can lead to potential losses of precision due to cancellations of nearly equal numbers.

This simple example demonstrates the loss of numerical precision due to roundoff errors, where the number of leading digits is lost in a subtraction of two near equal numbers. The lesson to be drawn is that we cannot blindly compute a function. We will always need to carefully analyze our algorithm in the search for potential pitfalls. There is no magic recipe however, the only guideline is an understanding of the fact that a machine cannot represent correctly all numbers.

### Loss of precision can cause serious problems

### Real Numbers

- Overflow: When the positive exponent exceeds the max value, e.g., 308 for DOUBLE PRECISION (64 bits). Under such circumstances the program will terminate and some compilers may give you the warning OVERFLOW.
- Underflow: When the negative exponent becomes smaller than the min value, e.g., -308 for DOUBLE PRECISION.
   Normally, the variable is then set to zero and the program continues. Other compilers (or compiler options) may warn you with the UNDERFLOW message and the program terminates.

### Loss of precision, real numbers

Roundoff errors. A floating point number like

$$x = 1.234567891112131468 = 0.1234567891112131468 \times 10^{1}$$
 (15)

may be stored in the following way. The exponent is small and is stored in full precision. However, the mantissa is not stored fully. In double precision (64 bits), digits beyond the 15th are lost since the mantissa is normally stored in two words, one which is the most significant one representing 123456 and the least significant one containing 789111213. The digits beyond 3 are lost. Clearly, if we are summing alternating series with large numbers, subtractions between two large numbers may lead to roundoff errors, since not all relevant digits are kept. This leads eventually to the next problem, namely

### More on loss of precision

### Real Numbers

• Loss of precision: When one has to e.g., multiply two large numbers where one suspects that the outcome may be beyond the bonds imposed by the variable declaration, one could represent the numbers by logarithms, or rewrite the equations to be solved in terms of dimensionless variables. When dealing with problems in e.g., particle physics or nuclear physics where distance is measured in fm  $(10^{-15} \text{ m})$ , it can be quite convenient to redefine the variables for distance in terms of a dimensionless variable of the order of unity. To give an example, suppose you work with single precision and wish to perform the addition  $1 + 10^{-8}$ . In this case, the information containing in  $10^{-8}$  is simply lost in the addition. Typically, when performing the addition, the computer equates first the exponents of the two numbers to be added. For 10<sup>-8</sup> this has however catastrophic consequences since in order to obtain an exponent equal to  $10^0$ , bits in the mantissa are shifted to the right. At the end, all bits in the mantissa are zeros.

# A problematic case Three ways of computing $e^{-x}$ Brute force: $\exp(-x) = \sum_{n=0}^{\infty} (-1)^n \frac{x^n}{n!}$ Recursion relation for $\exp(-x) = \sum_{n=0}^{\infty} s_n = \sum_{n=0}^{\infty} (-1)^n \frac{x^n}{n!}$ $s_n = -s_{n-1} \frac{x}{n},$ $\exp(x) = \sum_{n=0}^{\infty} s_n$ $\exp(-x) = \frac{1}{\exp(x)}$

```
Brute Force

// Program to calculate function emp(-m)
// using straightforward summation with differing precision
using namespace std
#include <costream>
#include <costream>
#include <costream>
// type float: 22 bits precision
// type float: 22 bits precision
// type double: 64 bits precision
// type double: 64 bits precision
#define PHASE(a) double
#define PHASE(a) (1 - 2 * (abs(a) % 2))
#define TRUNCATION // function declaration
TYPE factorial(int);
```

```
Results \exp(-x)
  What is going on?
                           Series
                                     Number of terms in series
            \exp(-x)
    X
    0.0
          0.100000E+01 0.100000E+01
    10.0 0.453999E-04 0.453999E-04
    20.0 0.206115E-08
                       0.487460E-08
                                              72
    30.0 0.935762E-13 -0.342134E-04
                                             100
    40.0 0.424835E-17 -0.221033E+01
                                             127
    50.0 0.192875E-21 -0.833851E+05
                                             155
    60.0 0.875651E-26 -0.850381E+09
                                             171
    70.0 0.397545E-30
                           NaN
                                             171
    80.0 0.180485E-34
                           NaN
                                             171
    90.0 0.819401E-39
                           NaN
                                             171
   100.0 0.372008E-43
                                             171
```

```
// program to compute exp(-x) without exponentials
using namespace std
#include c(ostream>
#include c(ostream>
#include comth>
#define TRUNCATION 1.0E-10

int main()
{
   int loop, n;
   double x, term, sum;
   for(loop = 0; loop <= 100; loop += 10)
{
    x = (double) loop; // initialization
    sum = 1.0;
    term = 1;
    n = 1;
```

### 

### Results $\exp(-x)$ More Problems x exp(-x) Series 0.000000 0.10000000E+01 0.1000000E+01 Number of terms in series 10.000000 0.45399900E-04 0.45399900E-04 44 20.000000 0.20611536E-08 0.56385075E-08 72 30.000000 0.93576230E-13 -0.30668111E-04 100 40.000000 0.42483543E-17 -0.31657319E+01 127 50.000000 0.19287498E-21 0.11072933E+05 155 182 209 80.000000 0.18048514E-34 0.91805682E+17 237 90.000000 0.81940126E-39 -0.50516254E+22 264 100.000000 0.37200760E-43 -0.29137556E+26 291

### Most used formula for derivatives

### 3 point formulae

First derivative  $(f_0 = f(x_0), f_{-h} = f(x_0 - h))$  and  $f_{+h} = f(x_0 + h)$ 

$$\frac{f_h - f_{-h}}{2h} = f_0' + \sum_{i=1}^{\infty} \frac{f_0^{(2j+1)}}{(2j+1)!} h^{2j}.$$

Second derivative

$$\frac{f_h - 2f_0 + f_{-h}}{h^2} = f_0'' + 2\sum_{i=1}^{\infty} \frac{f_0^{(2j+2)}}{(2j+2)!} h^{2j}.$$

### Error Analysis

$$\epsilon = log_{10} \left( \left| rac{f''_{
m computed} - f''_{
m exact}}{f''_{
m exact}} 
ight| 
ight),$$

$$\epsilon_{tot} = \epsilon_{approx} + \epsilon_{ro}$$
.

For the computed second derivative we have

$$f_0'' = \frac{f_h - 2f_0 + f_{-h}}{h^2} - 2\sum_{j=1}^{\infty} \frac{f_0^{(2j+2)}}{(2j+2)!} h^{2j},$$

and the truncation or approximation error goes like

$$\epsilon_{\text{approx}} pprox rac{f_0^{(4)}}{12} h^2.$$

### Error Analysis

If we were not to worry about loss of precision, we could in principle make *h* as small as possible. However, due to the computed expression in the above program example

$$f_0'' = \frac{f_h - 2f_0 + f_{-h}}{h^2} = \frac{(f_h - f_0) + (f_{-h} - f_0)}{h^2},$$

we reach fairly quickly a limit for where loss of precision due to the subtraction of two nearly equal numbers becomes crucial. If  $(f_{\pm h} - f_0)$  are very close, we have  $(f_{\pm h} - f_0) \approx \epsilon_M$ , where  $|\epsilon_M| \leq 10^{-7}$  for single and  $|\epsilon_M| \leq 10^{-15}$  for double precision, respectively.

We have then

$$|f_0''| = \left| \frac{(f_h - f_0) + (f_{-h} - f_0)}{h^2} \right| \le \frac{2\epsilon_M}{h^2}.$$

### Error Analysis

Our total error becomes

$$|\epsilon_{\mathsf{tot}}| \leq \frac{2\epsilon_{\mathsf{M}}}{h^2} + \frac{f_0^{(4)}}{12}h^2.$$

It is then natural to ask which value of h yields the smallest total error. Taking the derivative of  $|\epsilon_{ ext{tot}}|$  with respect to h results in

$$h = \left(\frac{24\epsilon_M}{f_0^{(4)}}\right)^{1/4}.$$

With double precision and x = 10 we obtain

$$h \approx 10^{-4}$$
.

Beyond this value, it is essentially the loss of numerical precision which takes over.

### Error Analysis

Due to the subtractive cancellation in the expression for f'' there is a pronounced detoriation in accuracy as h is made smaller and

It is instructive in this analysis to rewrite the numerator of the computed derivative as

$$(f_h - f_0) + (f_{-h} - f_0) = (e^{x+h} - e^x) + (e^{x-h} - e^x),$$

a

$$(f_h - f_0) + (f_{-h} - f_0) = e^{x}(e^h + e^{-h} - 2),$$

since it is the difference  $(e^h + e^{-h} - 2)$  which causes the loss of precision.

### Error Analysis

×	h = 0.01	h = 0.001	h = 0.0001	h = 0.0000001	Exact
0.0	1.000008	1.000000	1.000000	1.010303	1.000000
1.0	2.718304	2.718282	2.718282	2.753353	2.718282
2.0	7.389118	7.389057	7.389056	7.283063	7.389056
3.0	20.085704	20.085539	20.085537	20.250467	20.085537
4.0	54.598605	54.598155	54.598151	54.711789	54.598150
5.0	148.414396	148.413172	148.413161	150.635056	148.413159

### Error Analysis

### Technical Matter in C/C++: Pointers

A pointer specifies where a value resides in the computer's memory (like a house number specifies where a particular family resides on a street).

A pointer points to an address not to a data container of any kind! Simple example declarations:

```
using namespace std; // note use of namespace int main() {
    // what are the differences?
    int var;
    cin >> var;
    int *p, q;
    int *s, *t;
    int *s, arew[var]; // dynamic memory allocation delete [] a;
}
```

### Technical Matter in C/C++:

```
using namespace std; // note use of namespace int main() {
  int var;
  int *p;
  p = &var;
  var = 421;
  printf("Address of integer variable var : %p\n",&var);
  printf("Its value: %d\n", var);
  printf("Value of integer pointer p : %p\n",p);
  printf("The value p points at : %d\n",*p);
  printf("The value p points at : %d\n",*p);
  printf("Address of the pointer p : %p\n",&p);
  return 0;
}
```

```
int matr[2];
int *p;
p = kmatr[0];
matr[0] = 321;
matr[1] = 322;
printf("\nAddress of matrix element matr[1]: %p",&matr[0]);
printf("\nYalue of the matrix element matr[1]: %d",matr[0]);
printf("\nYalue of the matrix element matr[2]: %d\n", matr[1]);
printf("\nYalue of the matrix element matr[2]: %d\n", matr[1]);
printf("\nYalue of the pointer p: %p",p);
printf("\nThe value p points to: %d",*p);
printf("\nThe value that (p+1) points to %d\n",*(p+1));
printf("\nAddress of pointer p: %p\n",&p);
```

```
int matr[2];  // Define integer array with two elements int *p;  // Define pointer to integer p = &matr[0];  // Point to the address of the first element in matr matr[0] = 321;  // Change the first element matr[1] = 322;  // Change the first element printf("\nhaddress of matrix element matr[1]: %p", &matr[0]; printf("\nhaddress of matrix element matr[1]: %p", &matr[0]); printf("\nhaddress of matrix element matr[2]: %p", &matr[1]); printf("\nhaddress of matrix element matr[2]: %d\n", matr[1]); printf("\nhaddress of matrix element matr[2]: %d\n", matr[1]); printf("\nhaddress of pointer p: %p", p); printf("\nhaddress of pointer p: %p\n", &p); printf("\nhaddress of pointer p: %p\n", &p);
```

```
Address of the matrix element matr[1]: 0xbfffef70
Value of the matrix element matr[1]: 321
Address of the matrix element matr[2]: 0xbfffef74
Value of the matrix element matr[2]: 322
Value of the pointer: 0xbfffef70
The value pointer points at: 321
The value that (pointer*1) points at: 322
Address of the pointer variable: 0xbfffef6c
```

```
wsing namespace std;
#include <iostream>
int main(int argc, char *argv[])
{
    FILE *in_file, *out_file;
    if( argc < 3) {
        printf("The programs has the following structure :\n");
        printf("rite in the name of the input and output files \n");
        exit(0);
    }
    in_file = fopen( argv[1], "r");// returns pointer to the input file if( in_file == NULL ) { // NULL means that the file is missing printf("Can't find the input file %s\n", argv[1]);
    exit(0);</pre>
```

## File handling, C++-way \*include <fstream> // input and output file as global variable ofstream ofile; ifstream ifile;

```
const char* filename1 = "myfile";
ifstream ifile(filename1);
string filename2 = filename1 + ".out"
ofstream ofile(filename2); // new output file
ofstream ofile(filename2); ios_base::app); // append

// Read something from the file:
double a; int b; char c[200];
ifile >> a >> b >> c; // skips white space in between

// Can test on success of reading:
if (!(ifile >> a >> b >> c)) ok = 0;
```

### Call by value or reference

} ....

C++ allows the programmer to use solely call by reference (note that call by reference is implemented as pointers). To see the difference between C and C++, consider the following simple examples. In C we would write

```
int n; n =8;
func(&n); /* &n is a pointer to n */
....
void func(int *i) {
    *i = 10; /* n is changed to 10 */
}

whereas in C++ we would write
int n; n =8;
func(n); // just transfer n itself
....
void func(int& i) {
    i = 10; // n is changed to 10
```

### Call by value or reference

The reason why we emphasize the difference between call by value and call by reference is that it allows the programmer to avoid pitfalls like unwanted changes of variables. However, many people feel that this reduces the readability of the code.

### Call by value and reference, F90/95

In Fortran we can use INTENT(IN), INTENT(OUT), INTENT(INOUT) to let the program know which values should or should not be changed.

```
SUBROUTINE coulomb_integral(np,lp,n,l,coulomb)
USE effective_interaction_declar
USE energy_variables
USE wave_functions
IMPLICIT NOME
INTEGER, INTENT(IN) :: n, l, np, lp
INTEGER :: i
REAL(KIND-8) :: z_rel, oscl_r, sum_coulomb
```

This hinders unwanted changes and increases readability.

```
finclude <iostream>
finclude <costream>
f
```

```
Example codes in c++, writing to the and dynamic

allocation for arrays

#include <iostream>
#include <ifistream>
#include <iostream>
#include <iostream
#include <iostream>
#include <iostream
#include <iostream>
#include <iostrea
```

```
Example codes in c+-+, transfer of data using call by value
and call by reference

#include (iostream)
using namespace std;
// Declare functions before main
void func(int, int*);
int main(int argc, char *argv[])
{
   int a;
   int *b;
   a = 10;
   b = nev int[10];
   for (int i = 0; i < 10; i++) {
      b[i] = i;
      cout << b[i] << endl;
} // the variable a is transferred by call by value. This means
// that the function func cannot change a in the calling function
func(a,b);

   delete [] b;
   return 0;
} // End: function main()

void func( int x, int *y)
{
   // a becomes locally x and it can be changed locally
   x+=7;</pre>
```

```
Example codes in c+++ operating in several arrays and
printing time used

#include <cstdlib>
#include <costneum>
#include <ionamip>
#include (*ionamip)
#include "time.h"

using namespace std; // note use of namespace
int main (int argc, char* argv[])
{
   int i = atoi(argv[1]);
   double *a, *b, *c;
   a = new double[i];
   b = new double[i];
   c = new double[i];
   clock_t start, finish;
   start = clock();
   for (int j = 0; j < i; j++) {
        a[j] = cos[j+1:0];
        b[j] = sin[j+3:0);
        c[j] = a[j]+b[j];
   }
   for (int j = 0; j < i; j++) {
        c[j] = a[j]+b[j];
   }
   finish = clock();</pre>
```