Study guide: Scientific software engineering; wave equation model

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2 Migrating loops to Fortran

Migrating loops to C via Cython

- Vectorization: 5-10 times slower than pure C or Fortran code
- Cython: extension of Python for translating functions to C
- Principle: declare variables with type

Declaring variables and annotating the code

Pure Python code:

- Copy this function and put it in a file with .pyx extension.
- Add type of variables:
 - function(a, b) \rightarrow cpdef function(int a, double b)
 - $v = 1.2 \rightarrow cdef double v = 1.2$
 - Array declaration: np.ndarray[np.float64_t, ndim=2, mode='c'] u

Cython version of the functions

```
import numpy as np
cimport numpy as np
cimport cython
ctypedef np.float64_t DT # data type
@cython.boundscheck(False) # turn off array bounds check
Q_{cython.wraparound}(False) # turn off negative indices (u[-1,-1])
cpdef advance (
   np.ndarray[DT, ndim=2, mode='c'] u,
   np.ndarray[DT, ndim=2, mode='c'] u_1,
   np.ndarray[DT, ndim=2, mode='c'] u_2,
   np.ndarray[DT, ndim=2, mode='c'] f.
    double Cx2, double Cy2, double dt2):
    cdef int Nx, Ny, i, j
    cdef double u_xx, u_yy
   Nx = u.shape[0]-1
   Ny = u.shape[1]-1
    for i in xrange(1, Nx):
        for j in xrange(1, Ny):
           u_x = u_1[i-1,j] - 2*u_1[i,j] + u_1[i+1,j]
           u_yy = u_1[i,j-1] - 2*u_1[i,j] + u_1[i,j+1]
           u[i,j] = 2*u_1[i,j] - u_2[i,j] + 
                     Cx2*u_xx + Cy2*u_yy + dt2*f[i,i]
```

Note: from now in we skip the code for setting boundary values

Visual inspection of the C translation

See how effective Cython can translate this code to C:

```
Terminal> cython -a wave2D_u0_loop_cy.pyx
```

Load wave2D_u0_loop_cy.html in a browser (white lines indicate code that was successfully translated to pure C, while yellow lines indicate code that is still in Python):

```
Raw output: wave20 u0 loop cv.c
1: import numpy as np
2: cimport numpy as np
3: cimport cython
4: ctypedef np.float64 t DT # data type
6: @cython.boundscheck(False) # turn off array bounds check
7: @cython.wraparound(False) # turn off negative indices (u[-1,-1])
8: cpdef advance(
      np.ndarrav[DT, ndim=2, mode='c'] u,
     np.ndarray[DT, ndim-2, mode-'c'] u 1,
11: np.ndarray[DT, ndim=2, mode='c'] u 2,
12: np.ndarray[DT, ndim-2, mode-'c'] f,
     double Cx2, double Cv2, double dt2):
     cdef int Tx start = 0
        cdef int Iv start - 0
        cdef int Ix end = u.shape[0]-1
     cdef int Iv end = u.shape[1]-1
19: cdef int i, j
      cdef double u_xx, u_yy
22: for i in range(Ix start+1, Ix end):
         for j in range(Iy start+1, Iy end):
               u \times x = u \cdot 1[i-1,j] - 2^*u \cdot 1[i,j] + u \cdot 1[i+1,j]
                u[yy = u[1[i,j-1] - 2*u[1[i,j] + u[1[i,j+1]
26.
                u[i, i] = 2*u 1[i, i] - u 2[i, i] + \
27:
                         Cx2*u xx + Cy2*u yy + dt2*f[i, j]
28:
        # Boundary condition u=0
29:
        j - Iy_start
30:
       for i in range(Ix start, Ix end+1): u(i,i) = 0
31 -
        i - Iv end
32:
        for i in range(Ix start, Ix end+1): u[i,j] = 0
        i = Ix start
        for i in range(Iv start, Iv end+1): u[i,i] = 0
        i = Iv end
        for j in range(Iy start, Iy end+1): u[i,j] = 0
```

Can click on wave2D_u0_loop_cy.c to see the generated C code...

Building the extension module

- Cython code must be translated to C
- C code must be compiled
- Compiled C code must be linked to Python C libraries
- Result: C extension module (.so file) that can be loaded as a standard Python module
- Use a setup.py script to build the extension module

```
from distutils.core import setup
from distutils.extension import Extension
from Cython.Distutils import build_ext

cymodule = 'wave2D_u0_loop_cy'
setup(
   name=cymodule
   ext_modules=[Extension(cymodule, [cymodule + '.pyx'],)],
   cmdclass={'build_ext': build_ext},
)
Terminal> python setup.py build_ext --inplace
```

Calling the Cython function from Python

Efficiency:

- 120×120 cells in space:
 - Pure Python: 1370 CPU time units
 - Vectorized numpy: 5.5
 - Cython: 1
- \bullet 60 \times 60 cells in space:
 - Pure Python: 1000 CPU time units
 - Vectorized numpy: 6
 - Cython: 1

Migrating loops to Fortran

Migrating loops to C via Cython

Migrating loops to Fortran

- Write the advance function in pure Fortran
- Use f2py to generate C code for calling Fortran from Python
- Full manual control of the translation to Fortran

The Fortran subroutine

```
subroutine advance(u, u_1, u_2, f, Cx2, Cy2, dt2, Nx, Ny)
      integer Nx. Nv
      real *8 u(0:Nx,0:Ny), u_1(0:Nx,0:Ny), u_2(0:Nx,0:Ny)
      real*8 f(0:Nx, 0:Ny), Cx2, Cy2, dt2
      integer i, j
Cf2py intent(in, out) u
C
      Scheme at interior points
      do j = 1, Ny-1
         do i = 1, Nx-1
            u(i,j) = 2*u_1(i,j) - u_2(i,j) +
            Cx2*(u_1(i-1,j) - 2*u_1(i,j) + u_1(i+1,j)) +
            Cy2*(u_1(i,j-1) - 2*u_1(i,j) + u_1(i,j+1)) +
            dt2*f(i,j)
         end do
      end do
```

Note: Cf2py comment declares u as input argument and return value back to Python

Building the Fortran module with f2py

f2py changes the argument list (!)

- Array limits have default values
- Examine doc strings from £2py!

How to avoid array copying

- Two-dimensional arrays are stored row by row in Python and C
- Two-dimensional arrays are stored column by column in Fortran
- f2py takes a copy of a numpy (C) array and transposes it when calling Fortran
- Such copies are time and memory consuming
- Remedy: declare numpy arrays with Fortran storage

```
order = 'Fortran' if version == 'f77' else 'C'
u = zeros((Nx+1,Ny+1), order=order)
u_1 = zeros((Nx+1,Ny+1), order=order)
u_2 = zeros((Nx+1,Ny+1), order=order)
```

Option -DF2PY_REPORT_ON_ARRAY_COPY=1 makes f2py write out array copying:

Efficiency of translating to Fortran

- Same efficiency (in this example) as Cython and C
- About 5 times faster than vectorized numpy code
- ullet > 1000 faster than pure Python code

2 Migrating loops to Fortran

Migrating loops to C via Cython

Migrating loops to C via Cython

- Write the advance function in pure C
- Use Cython to generate C code for calling C from Python
- Full manual control of the translation to C

The C code

- numpy arrays transferred to C are one-dimensional in C
- Need to translate [i,j] indices to single indices

```
/* Translate (i, j) index to single array index */
#define idx(i,j) (i)*(Ny+1) + j
void advance(double* u, double* u_1, double* u_2, double* f,
     double Cx2, double Cy2, double dt2,
     int Nx, int Ny)
  int i, j;
  /* Scheme at interior points */
 for (i=1; i \le Nx-1; i++) {
   for (j=1; j<=Ny-1; j++) {
        u[idx(i,j)] = 2*u_1[idx(i,j)] - u_2[idx(i,j)] +
        Cx2*(u_1[idx(i-1,j)] - 2*u_1[idx(i,j)] + u_1[idx(i+1,j)]) +
        Cy2*(u_1[idx(i,j-1)] - 2*u_1[idx(i,j)] + u_1[idx(i,j+1)]) +
        dt2*f[idx(i,i)];
```

The Cython interface file

```
import numpy as np
cimport numpy as np
cimport cython
cdef extern from "wave2D_u0_loop_c.h":
    void advance (double * u, double * u_1, double * u_2, double * f,
                 double Cx2, double Cy2, double dt2,
                 int Nx, int Ny)
@cython.boundscheck(False)
@cython.wraparound(False)
def advance_cwrap(
   np.ndarray[double, ndim=2, mode='c'] u,
   np.ndarray[double, ndim=2, mode='c'] u_1,
   np.ndarray[double, ndim=2, mode='c'] u_2,
   np.ndarray[double, ndim=2, mode='c'] f,
    double Cx2, double Cy2, double dt2):
    advance (\&u[0,0], \&u_1[0,0], \&u_2[0,0], \&f[0,0],
            Cx2, Cy2, dt2,
            u.shape[0]-1, u.shape[1]-1)
    return u
```

Building the extension module

Compile and link the extension module with a setup.py file:

```
from distutils.core import setup
 from distutils.extension import Extension
 from Cython.Distutils import build_ext
 sources = ['wave2D_u0_loop_c.c', 'wave2D_u0_loop_c_cy.pyx']
module = 'wave2D_u0_loop_c_cy'
 setup(
   name=module,
   ext_modules=[Extension(module, sources,
                          libraries=[], # C libs to link with
   cmdclass={'build_ext': build_ext},
 Terminal> python setup.py build_ext --inplace
In Python:
 import wave2D_u0_loop_c_cy
 advance = wave2D_u0_loop_c_cy.advance_cwrap
f_a[:,:] = f(xv, yv, t[n])
 u = advance(u, u_1, u_2, f_a, Cx2, Cy2, dt2)
```

2 Migrating loops to Fortran

3 Migrating loops to C via Cython

- Write the advance function in pure C
- Use f2py to generate C code for calling C from Python
- Full manual control of the translation to C

The C code and the Fortran interface file

- Write the C function advance as before
- Write a Fortran 90 module defining the signature of the advance function
- Or: write a Fortran 77 function defining the signature and let f2py generate the Fortran 90 module

Fortran 77 signature (note intent(c)):

```
subroutine advance(u, u_n, u_nm1, f, Cx2, Cy2, dt2, Nx, Ny)
Cf2py intent(c) advance
    integer Nx, Ny, N
        real*8 u(0:Nx,0:Ny), u_n(0:Nx,0:Ny), u_nm1(0:Nx,0:Ny)
        real*8 f(0:Nx, 0:Ny), Cx2, Cy2, dt2
Cf2py intent(in, out) u
Cf2py intent(c) u, u_n, u_nm1, f, Cx2, Cy2, dt2, Nx, Ny
    return
    end
```

Building the extension module

Generate Fortran 90 module (wave2D_u0_loop_c_f2py.pyf):

The compile and build step must list the C files:

- C++ can be used as an alternative to C
- C++ code often applies sophisticated arrays
- Challenge: translate from numpy C arrays to C++ array classes
- Can use SWIG to make C++ classes available as Python classes
- Easier (and more efficient):
 - Make C API to the C++ code
 - Wrap C API with f2py
 - Send numpy arrays to C API and let C translate numpy arrays into C++ array classes