Model that solves the regression and clustering together:

One popular approach that combines regression and clustering is the "Mixture of Experts" (MoE) model. The MoE model is a type of ensemble model where different experts (regression models) are trained on different subsets or clusters of the data, and a gating network is used to determine which expert to consult for a given input.

Here's a brief explanation of the Mixture of Experts model:

- 1. **Experts (Regression Models):** Each expert in the MoE model is a specialized regression model trained on a specific cluster or subset of the data. These experts are responsible for capturing the relationships within their assigned clusters.
- 2. **Gating Network:** A gating network is another component of the MoE model. It takes the input data and outputs a set of weights that determine the contribution of each expert to the final prediction. The gating network effectively decides which expert is most relevant for a given input.
- 3. **Final Prediction:** The final prediction is a weighted sum of the predictions from all the experts, where the weights are determined by the gating network. This allows the model to adaptively combine the predictions of different experts based on the characteristics of the input data.

Example:

Let's say you have a dataset of housing prices, and you observe that there are different patterns in housing prices based on geographical regions. A Mixture of Experts model could consist of:

- **Experts (Regression Models):** Each expert is a regression model trained on data from a specific geographical cluster (e.g., urban areas, suburban areas, rural areas).
- **Gating Network:** The gating network takes features related to the location of a house (e.g., zip code, proximity to city centers) and determines the weights for each expert based on this information.
- **Final Prediction:** When predicting the price of a new house, the model uses the weighted combination of predictions from the experts, with the weights determined by the gating network. This allows the model to account for the different price trends in urban, suburban, and rural areas.