## Analysis of Security-Cost Trade-off of Fully Homomorphic Encryption Schemes

Kais Chaabouni
ENSIMAG
Grenoble INP
Grenoble, France
kais.chaabouni@ensimag.imag.fr

Amrit Kumar ENSIMAG-Ecole Polytechnique Grenoble INP Grenoble, France amrit.kumar@ensimag.imag.fr

**ABSTRACT** 

Abstract

#### **Keywords**

Fully Homomorphic Encryption, Security, Cost

#### 1. INTRODUCTION

Motivation and significance of fully homomorphic encryption scheme such as Gentry's lattice-based scheme. This work evaluates the efficiency of FHE implementations for operations varying from XOR to sort on remote machines. Trade-off between cost and security is analyzed.

# 2.1 The Framework Overview of the algorithm and its complexity. 2.2 Example Description using a typical operation like modular multiplication of two *n*-bit vectors. Comparison with partial homomorphic encryption scheme such as RSA.

**3. EXPERIMENTAL EVALUATION OF COST** Describe the FHE algorithm and its corresponding implementation choice. Installation, set-up procedure and usage of the implementation. We detail the measurements to be

2. GENTRY'S FULLY HOMOMORPHIC SCHEME

FHE

taken, like Wall time, CPU time and memory usage based on certain security or algorithmic parameters.

Statistical analysis of the measurements using minimum, max, mean and standard deviation.

#### 4. EVALUATION ON BENCH MARKS

We describe the system parameters and test vectors. This section also includes description of the process of evaluation for the following operations:

#### 4.1 Operations

The HCRYPT implementation provides two gates: XOR and AND forming a complete set of functional gates. We hence define  $\neg a$  as XOR(a,1), while OR(a,b) as XOR(XOR(a,b), AND(a,b), where a,b are bits.

Using these gates we build and analyse the cost of the following operations.

XOR of n-bits. We start with the simplest operations on bits. XOR of n-bits requires n-1 XOR gates.

 ${\it Majority~of~n\text{-}bits}.$  Majority bit is evaluated with the following circuit :

$$\prod_{i=1}^{n} a_i + \sum_{i=1}^{n} \left( \prod_{j!=i} a_j \right) \neg a_i$$

where  $\sum$  is the successive OR, and  $\prod$  is the successive application of AND.

Hence it uses  $(n^2-1)$  AND gates, and n OR and NOT gates i.e.  $(n^2+n-1)$  AND, 3n XOR gates.

Sum of integers of n-bits. Sum of two integers can be performed using an n-bit adder based on full-adder circuits. The cost of a full adder circuit is 2 XOR to calculate the sum

and 2 AND, 1 XOR and 1 OR for the carry. Hence the total complexity is 3n AND, 5n XOR.

#### Sum of arbitrary integers

- Sum of:
  - bounded integers
  - unbounded integers
- String sorting with the following methods :
  - Insertion sort
  - Merge sort
  - Quick Sort
- Matrix product

Sorting is tested on a sorting network where comparator gates are used. Each comparator is designed using the following algorithm.

#### Algorithm 1: Comparator

```
Data: (a_0, a_1, \dots, a_{n-1}), (b_0, b_1, \dots, b_{n-1})

Result: Return Max(a,b) and Min(a,b)

1 aIsGreater=0;

2 for i \leftarrow n-1 to 0 do

3 \lfloor aIsGreater = aIsGreater + \neg(b_i)a_i;

4 for i \leftarrow 0 to n-1 do

5 \lfloor Max_i = aIsGreater * a_i + \neg(aIsGreater) * b_i;

6 \lfloor Min_i = \neg(aIsGreater) * a_i + aIsGreater * b_i;

7 return(Max, Min)
```

Each comparator gate uses n AND gates, n OR gates and n NOT gates to find the larger of the two bit sequences and then to regenerate the maximum and the minuimum 4n AND gates 2n NOT and OR gates i.e. 6n AND and XOR gates are required.

Insertion sort. n(n-1)/2 comparator gates are use for insertion sort.

For each operation, we provide the initial algorithm and the results obtained. Observations based on the measurements are described.

### 5. ANALYSIS OF THE RESULTS

Trade-off analysis on the results obtained. Comparison with other protocols in terms of gain with security-cost trade-off. Observations and recommendations on the cost and security trade-off.

Conclusion

7. REFERENCES		