```
Y = X\beta + \varepsilon, \mathbb{E}[\varepsilon] = 0, Cov(\varepsilon) = \mathbb{E}[\varepsilon \varepsilon^{\dagger}] = \sigma^{2}I_{n \times n}.
                                                                                                                                                                                                          (Linear) logistic regression
                                                                                                                                                                                                                                                                                                                                      In regression we have
                                                                                                     Linearity assumptions (for LS regression)
                                                                                                                                                                                                                                                                                                            \|\hat{\mathbf{Y}} - \overline{\mathbf{Y}}\|^2
                                                                                                                                                                                                                                                                                                                                      (which allows for
This means that assumption 1.-4, from section 1.3.2 are satisfied.
                                                                                                                                                                                                                                                                                                            \frac{\|\mathbf{Y} - \overline{\mathbf{Y}}\|^2}{\|\mathbf{Y} - \overline{\mathbf{Y}}\|^2}
                                                                                                                                                                                                                              =\sum_{j=1}^{r} \beta_{j} x_{j}
                                                                                                 The linear regression equation is correct. This means: \mathbb{E}[\varepsilon_i] = 0 for
                                                                                                                                                                                                                                                  LHS is logit transform of \boldsymbol{\pi}
                                                                                                                                                                                                                                                                                                                                      writing R^2 differently)
It can then be shown that:
                                                                                                                                                                                                                                                                                                 \|\mathbf{Y} - \overline{\mathbf{Y}}\|^2 = \|\hat{\mathbf{Y}} - \overline{\mathbf{Y}}\|^2 + \|\mathbf{Y} - \hat{\mathbf{Y}}\|^2
                                                                                                  All x<sub>i</sub>'s are exact. This means that we can observe them perfectly.
  (i) \mathbb{E}[\widehat{\beta}] = \beta: that is, \widehat{\beta} is unbiased
                                                                                                                                                                                                                  \pi_j(x)
                                                                                                                                                                                                                                = g_j(x) = \sum_r \beta_r^{(j)} x_r
                                                                                                                                                                                                        og \left(\frac{n_j(x)}{1 - \pi_j(x)}\right)
                                                                                                                                                                                                                                                                                                The following removes col. upo3:
 (ii) \mathbb{E}[\hat{\mathbf{Y}}] = \mathbb{E}[\mathbf{Y}] = X\beta which follows from (i). Moreover, \mathbb{E}[\mathbf{r}] = 0.
                                                                                                 The variance of the errors is constant ("homoscedasticity"). This
                                                                                                                                                                                                                                                                                               d.ozone <- subset(ozone, select=-upo3)
<- subset(transform(d.ozone, "log03" = log(03)), select = -03)
                                                                                                 Var(\varepsilon_i) = \sigma^2 \text{ for all } i.
                                                                                                                                                                                                         Likelihood (for Bernoulli x then for Binomial)
 (iii) Cov(\widehat{\beta}) = \sigma^2(X^{T}X)^{-1}
                                                                                                                                                                                                     L(\beta; (x_1, Y_1), \dots, (x_n, Y_n)) = \prod_{i=1}^n \pi(x_i)^{Y_i} (1 - \pi(x_i))^{1-Y_i}
                                                                                                                                                                                                                                                                                                       adds log(03) as a col. and removes 03
                                                                                                 The errors are uncorrelated. This means: Cov(\varepsilon_i, \varepsilon_j) = 0 for all i \neq j
(iv) Cov(\hat{\mathbf{Y}}) = \sigma^2 P, Cov(\mathbf{r}) = \sigma^2 (I - P)
(i) \widehat{\boldsymbol{\beta}} \sim \mathcal{N}_p(\boldsymbol{\beta}, \sigma^2(X^\intercal X)^{-1})
                                                                                                  The errors \{\varepsilon_i; i = 1,...,n\} are jointly normally distributed. This
                                                                                                                                                                                                     L(\beta; (x_1, m_1, N_1), ..., (x_n, m_n, N_n)) = \prod_{i=1}^{n} \binom{m_i}{N_i} \pi(x_i)^{N_t} (1 - \pi(x_i))^{m_t - N_t}
                                                                                                 that also \{Y_i; i = 1, ..., n\} are jointly normally distributed.
(ii) \hat{\mathbf{Y}} \sim \mathcal{N}_n(X\beta, \sigma^2 P), \mathbf{r} \sim \mathcal{N}_n(\mathbf{0}, \sigma^2(I - P))
                                                                                                                                                                                                                                                                                                         function(fitfn, formula = log03 ~ . ,
data = d.ozone.es, ...)
                                                                                                                                                                                                               <- glm(cbind(N, m - N) ~ age,
family = binomial, data = heart)
(iii) \hat{\sigma}^2 \sim \frac{\sigma^2}{n-p} \chi_{n-p}^2.
                                                                                                   oocv <- function(reg.data, reg.fcn)
                                                                                                                                                                                                                                                                                                                      model.frame(formula, data = data)
esponse(modFrame)
                                                                                                                                                                                                      predict(fit, new = data.frame(age
\widehat{\boldsymbol{\beta}} = (X^{\mathsf{T}}X)^{-1}X^{\mathsf{T}}\mathbf{Y}.
                                                                                                   new.age), type =
                                                                                                                                                                                                                                                               "response")
                                                                                                                                                                                                                                                                                                 #calculate ssr and sst
fit <- fitfn(formula—formula, data = data,
ssr <- sum((Y - predict(fit, modFrame))^2)
sst <- sum((Y-mean(Y))^2)
1-ssr/sst</pre>
col.partn <- 1*(partners==0) + 2*(partners==1) + 3*(partners==8)
                                                                                                                                                                                                                         glm(Survival ~
                                                                                                                                                                                                                                                                  ., data
                                                                                                                                                                                                                 d.baby, family = "binomial"
plot(thorax, longevity, pch=pch.type, col=col.partn,
                                                                                                   reg.data, reg.fcn)
mean((reg.data$y - loo.values)^2)
     ylim=range(longevity),xlim=range(thorax))
legend("topleft",c("1 pregnant","8 pregnant","1 virgin"
"8 virgin","0 partners"),
pch=c(1,2,1,2,3),col=c(2,2,3,3,1))
                                                                                                                                                                                                          will give the probability of heart disease (N/m)
                                                                                                                                                                                                                                                                                                          (Cross-validated LOOCV) R2 in R
                                                                                                                                                                                                          Multinomial logistic regression
                                                                                                                                                                                                                                                                                                    cv_r2 <- function(fitfn, formula = log03 ~ . , data
d.ozone.es, ..., trace = TRUE)
                                                                                                       Nadaraya Watson
                                                                                                                                                                                                                                                                                                       m <- multinom(Species ~ . , data = Iris)
    Does indicator variable affect thorax length?
                                                                                                   reg.fcn.nw <- function(reg.x, reg.y, x)
                                                                                                                                                                                       ZP <- predict(object, newdata = grid, type = "probs")</pre>
   Reject H<sub>0</sub> if Pr(>F) <= 0.05
                                                                                                      ksmooth(reg.x, reg.y, x.point = x,
kernel = "normal", bandwidth = h)$y
fitfull <-lm(thorax^-dummy.1.p+dummy.1.v+dummy.8.p+dummy.8.v)\\ fitintercept <-lm(thorax^-1)\\ anova(fitintercept,fitfull)
                                                                                                                                                                                                          where the probabilities of each class are stored in
                                                                                                                                                                                                                                                                                                          the columns (columns same order as levels (...))
                                                                                                        eg.fcn.lp <- function(reg.x, reg.y, x) {
lp.reg <- loess(reg.y ~ reg.x,
enp.target = df.nw, surface = "direct"
predict(lp.reg, x)
                                                                                                                                                                                                          but we can also achieve logistic regression by
                                                                                                                                                                                                                                                                                                           alculate sst
t <- fitfn(formula=formula, data = data, ...)
t <- sum((model.response(modFrame)-
mean(model.response(modFrame)))^2
data[order(data[, "People.per.Dr"], decreasing=T)[1:3],]
                                                                                                                                                                                                         using dummy encoding and glm:
datanew <-data[complete.cases(data),]</pre>
                                                                                                                                                                                                     levels(Iris1$Species) <- c("setosa
"not", "no
                                                                                                                                                                                                                                                                                                       mean(
if(trace) cat("\n")
1-ssr/sst
predict(fit, newdata=newcountry, interval="predict")
                                                                                                                                                                                                                                                                             "not")
                                                                                                      Smoothing splines
predict(fit. newdata=newcountry, interval="confidence")
                                                                                                                                                                                                     Iris1$Species <- relevel(Iris1$Species
                                                                                                                                   ion(reg.x, reg.y, x
                                                                                                                                                                                                                                                                                                           MARS in R
                                                                                                                                                                                                                                                          ref =
                                                                                                                                                                                                                                                                         "not
                                                                                                                                                                                                     fit.1 <- glm(Species ~ ., data = Iris1,
family = "binomial")
                                                                                                       ss.reg <- smooth.spline(reg.x, reg.y, spar = est.ss\spar
predict(ss.reg, x)\space{\space}y</pre>
                                                                                                                                                                                                                                                                                                   require("earth")
                                                                                                                                                                                                                                                                                                   Mfit <- earth(Volume ~ ., data = trees)
                                                                                                                                                                                                                                                                                                    summary(Mfit)
                                                                                                                                                                                                        ROC and Misclassification graph in R
                                                                                                    TODO: Hat matrix (serie 5 methods and non-parametric
                                                                                                                                                                                                                                                                                                    ict(Mfit.
                                                                                                                                                                                                       require(ROCR)
                                                                                                                                                                                                                                                                                                         data.frame(Girth= 5:15, Height= seq(60,80, length=11)))
                                                                                                                                                                                                     We can then find their \ensuremath{\mbox{R}}^2 as
                                                                                                      TODO: Equivalent ways of calculating LOOCV using hat
                                                                                                                                                                                                     d.baby$Survival)

perf <- performance( pred, "tpr", "fpr'
plot(perf, main = "title")
                                                                                                                                                                                                                                                                                                      follows:
                                                                                                     matrix and manually computation
                                                                                                                                                                                                                                                                                                    r2(earth, formula = log03 ~ .
  data = d.ozone.es, degree
cv_r2(earth, formula = log03
  data = d.ozone.es, degree
                                                                                                                                                                                                          which plots the TPR vs EPR. To plot the
                                                                                          https://docs.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.com/library.
                                                                                                                                                                                                          misclassification rate as a function of threshold
                                                                                                                                                                                                                                                                                                        MARS fits a function of the form
                                                                                                                                                                                                          prob. (i.e., after this it is considered positive)
                                                                                                                                                                                                                                                                                                  g(\mathbf{x}) = \mu + \sum_{m=1}^{\infty} \beta_m h_m(\mathbf{x}) = \sum_{m=1}^{\infty} \beta_m h_m(\mathbf{x}),
                                                                                                                                                                                                      perf.cost <- performance(pred, "cost")</pre>
                                                                                         plot(perf.cost, main = title)
                                                                                                                                                                                                                                                                                                     with the function h_0(\mathbf{x}) \equiv 1. Initialize the model set \mathcal{M} = \{h_0(\cdot) \equiv 1\}. Figure 1 in the function h_0 by least squares regression, yielding the estimate \hat{\mu} = n^{-1} \sum_{i=1}^{n} Y_i.
    Mallows Co statistic
                                                                                                                                                                                                          K-Fold CV in R
                                                                                                                                                                                                                                                                                             2. For r=1,2,\ldots do the following:
Search for the best pair of functions ((h_{2r-1}(\cdot),h_{2r}(\cdot)) which are of the following:
   The MSE can be estimated by:
                                                                                                                                                                                                       \begin{array}{rcl} h_{2r-1}(\cdot) & = & h_{\ell}(\cdot) \times (x_j - d)_+, \\ h_{2r}(\cdot) & = & h_{\ell}(\cdot) \times (d - x_j)_+, \end{array}
   n^{-1}SSE(M) - \hat{\sigma}^2 + 2\hat{\sigma}^2|M|/n,
                                                                                                                                                                                                                                                                                                  r some h_\ell in the model set M which does not contain x_\ell^3 and some b

\mathcal{B}. The best pair of functions is defined to be the one which reduces

squares most. The model fit is then
   which is prop. to Cp(M):
 C_p(\mathcal{M}) = \frac{SSE(\mathcal{M})}{2} - n + 2|\mathcal{M}|
                                                                                                                                                                                                                                                                                                                          \hat{g}(\mathbf{x}) = \hat{\mu} + \sum_{m=1}^{2r} \hat{\beta}_m h_m(\mathbf{x}),
                                                                                                    "basic" = "Reversed quantile
                            Cp <- function(object, sigma) {
                                                                                                    "norm" = "Normal"
                               res <- residuals(object)
                                                                                                                                                                                                           To plot the average ROC (across all folds)
    Cp in R
                                                                                                   "perc" = "Quantile"
                               n <- length(res)
                                                                                                                                                                                                           initialize a vector of lists and assign them as
    (note: object
                              p <- n - object$df.residual

SSE <- sum(res^2)

SSE / sigma^2 - n + 2 * p
                                                                                                                                                                                                                                                                                                                    \mathcal{M} = \mathcal{M}_{old} \cup \{h_{2r-1}(\cdot), h_{2r}(\cdot)\},\
    is of type fit.
                                                                                                  Expected size of out-of-bootstrap sample [roughly
                                                                                                                                                                                                           follows: all.y.true[[i]] <- y.true
                                                                                                                                                                                                                                                                                                with the functions h_{2r-1}, h_{2r} from (7.1).
                                                                                                  1/3 of points will be out of sample]:
                                                                                                                                                                                                                         all.y.pred[[i]] <- y.pred
                                                                                                                                                                                                                                                                                                   rate step 2 until a large enough number of basis functions h_m(\cdot) has been fit
    be found
                                                                                                                                                                                                           And then pred.cv <- prediction (all.y.pred, all.y.true)
                                                                                                                                                                                                                                                                                              . Do backward deletion ("pruning"), allowing to remove single functions from a pair h_{2r-1}(\cdot), h_{2r}(\cdot); i.e., of all single basis functions, delete the one which increases th residual sum of squares the least.
                                                                                                  \mathbb{E}^*[|\mathcal{L}_{out}^*|] = \mathbb{E}^*[\sum \mathbf{1}_{[Z_i \in \mathcal{L}_{out}^*]}] = n\mathbb{P}^*[Z_i \in \mathcal{L}_{out}^*] \approx 0.368n.
    using
                             # choose sigma
                                                                                                                                                                                                            and proceed as normal (but add avg = "threshold"
    sigma(fit))
                            sigma <- summary(fit5)$sigma
                                                                                                                                                                                                            for ROC and avg = "vertical" for misclassification) use
                                                                                                                                                                                                                                                                                               Stop the backward deletion by optimizing a GCV sc
   Forward selection (in case p. the nr. of predictors
                                                                                                                                                                                                            add = T to add them to same plot. One can specify
                                                                                                   \mathbb{P}[\mathcal{C}_{Bayes}(X_{new}) \neq Y_{new}] \mathcal{C}_{Bayes}(x) = \arg \max \pi_j(x).
                                                                                                                                                                                                                                                                                                     summary (mars fit) gives the importance of
    vars. Is too large for exhaustive search):
                                                                                                                                                                                                            the cost for FN and FP using cost.fp = 0.8, cost.fn =
                                                                                                                                                                                                                                                                                                     each variable. If we fitted a model of degree
    1) start with smallest model
                                                                                                                                                                                                           1.2 as args to performance().
                                                                                                                                                                                                                                                                                                     2, then we can get the graphs of the
    2) add predictor which reduces the MSE the most
                                                                                                                                                                                                                                                                                                     response variables as a function of each
    3) repeat 2 until all predictors or large nr. of
                                                                                                                                                                                                             Poly, regression using a polynomial of degree d
                                                                                                                                                                                                                                                                                                     predictor variable as follows:
    predictors selected (now a seg. models is produced)
                                                                                                                                                                                                           (no interaction term):
    4) choose the model in the seq. which has smallest
                                                                                                                                                                                                                                                                                                   plotmo(fit, degree2=FALSE
caption="main effect:
                                                                                                                                                                                                       y_i = \beta_0 + \beta_{1,1} x_{i1} + \beta_{1,2} x_{i1}^2 + \dots + \beta_{1,d} x_{i1}^a + \dots
                                                                                                                                                                                                                                                                                                   We can also get the 3D plots (effect of the
                                                                                                        Prediction of LDA found by taking argmax:
                                                                                                                                                                                                              +\beta_{p,1}x_{ip} + \beta_{p,2}x_{ip}^2 + ...\beta_{p,d}x_{ip}^d + \epsilon_i.
    Backward selection is obvious
                                                                                                                                                                                                                                                                                                   interaction of 2 terms on the response) using
                                                                                                                                                                                                     quire(sfsmisc)
                                                                                                                                                                                                                                                                                                    Note that the linear regression model
                                                                                                                = x^{\mathsf{T}} \hat{\mathbf{X}}^{-1} \hat{\mu}_{j} - \hat{\mu}_{j}^{\mathsf{T}} \hat{\mathbf{X}}^{-1} \hat{\mu}_{j} / 2 + \log(\hat{p}_{j}) =
                                                                                                                                                                                                form1 <- as.formula("logupo3~.")
form3 <- wrapFormula(form1, data =
    does not assume a normal distribution
                                                                                                                  = (x - \hat{\mu}_i/2)^{\mathsf{T}} \hat{\Sigma}^{-1} \hat{\mu}_i + \log(\hat{p}_i).
                                                                                                                                                                                                                                                                                                        Neural Networks (1 Layer with g units
    for the predictors, but a skewed
                                                                                                                                                                                               d.ozone.e, wrapString="poly(*,degree=d)"
fit3 <- lm(form3, data = d.ozone.e)</pre>
                                                                                                                                                                                                                                                                                                    g_k(\mathbf{x}) = f_0 \left( \alpha_k + \sum_{h=1}^q w_{hk} \phi(\tilde{\alpha}_h + \sum_{i=1}^p \tilde{w}_{jh} x_j) \right)
    distribution and outliers often result in
                                                                                                       Decision boundary between class 0 and 1:
    regression solutions that are largely
    determined by very few points.
                                                                                                                                                                                                           Generalized additive model in R
                                                                                                                                                                                                                                                                                                      where \phi(t) = \frac{\exp(\iota_f)}{1 + \exp(t)}
                                                                                                    B = \{x \mid \hat{\delta}_0(x) = \hat{\delta}_1(x)\} = \{x \mid (x - z)^T w = 0\}
library(lattice)
                                                                                                                                                                                          require(macv)
                                                                                                                                                                                                                                                                                                      and f_0 is typically identity for regression
splom(~mortality[,c("Mortality","Pop","HC","NOx","S02")],pscales=0
                                                                                                      if the covariance matrix \Sigma is diagonal and const.
                                                                                                                                                                                         form1 <- as.formula("logupo3~.")
                                                                                                                                                                                                                                                                                                     and sigmoid for classification. We can add a
                                                                                                       then w is parallel to the line connecting \mu_0\,\text{and}\,\,\mu_1
    Tukey Anscombe is residuals versus fitted values.
                                                                                                                                                                                         gamForm <- wrapFormula(form1, data = d.ozone.e)
                                                                                                                                                                                                                                                                                                     linear regression component (skip conxn):
   Q-Q is empirical quantiles vs standard normal
                                                                                                         DA Classifier (more easily overfits if p is big)
                                                                                                                                                                                        g1 <- gam(gamForm, data = d.ozone.e)</pre>
                                                                                                                   \frac{1}{n_j-1}\sum_{i=1}^n(X_i-\hat{\mu_j})(X_i-\hat{\mu_j})^{\intercal}\mathbf{1}_{[Y_i=j]}
                                                                                                                                                                                                                                                                                                                 \alpha + \sum_{i} w_{j,lin}x_{j} + \sum_{i} w_{k}\phi(\alpha_{k} + \sum_{i} w_{jk}x_{j})
   quantiles.
                                                                                                                                                                                                            Alternatively.
   Forward and backward selection in R
                                                                                                                                                                                                        fitA <- gam(03 ~ s(vdht)+ s(wind)+
                                                                                                                                                                                                                                                                                                     Make sure to scale the data (except for
                                                                                                  \hat{\delta}_{j}(x) = -\log(\det(\hat{\Sigma}_{j}))/2 - (x - \hat{\mu}_{j})^{\dagger}\hat{\Sigma}_{j}^{-1}(x - \hat{\mu}_{j})/2 + \log(\hat{p}_{j})
mortal.bw <- step(mortal.full, dir="backward")
                                                                                                                                                                                                          s(humidity)+ s(temp)+ s(ibht)+
s(dgpg)+ s(ibtp)+ s(vsty)+ s(day)
data = d.ozone)
                                                                                                                                                                                                                                                                                                     response) to avoid getting stuck in the flat
   nortal.fw=step(mortal.empty,
dir="forward", data=mortality,
scope = list(upper=mortal.full
lower=mortal.empty))
                                                                                                                                                                                                                                                                                                     regions of the sigmoid function. Weight
                                                                                                                                                                                                                                                                                                     decay is good as it reduces the dependency
                                                                              <- matrix(sample.int(n, n*B, replace = TRUE), nrow = n, ncol = B)</pre>
                                                                   index
                                                                                                                                                                                                                                                                                                     on the starting values and reduces the
                                                                                                                                                                                                       To plot the splines do: par(mfrow=c(3,3))
                                                                    fit_lda <- vector("list", B)
   For lm. Tukey Anscombe is given by
                                                                                                                                                                                                                                                                                                     importance of choosing the # of hidden units
                                                                              in 1:B)
                                                                                                                                                                                                                                           plot(g1, shade =
   plot(fit, which =1)
                                                                                   index[, i]
                                                                                                                                                                                                                                                                                           Nfit <- nnet(log.03 ~
                                                                                                                                                                                                                                                                                                                                        . , data = sc.ozone,
    Whereas Q-Q plot is given by
                                                                       To plot the same thing but for Im use:
   plot(fit, which =2)
                                                                                                                                                                                                                                                                                                                     size = 3,
                                                                                                                                                                                                                                                                                                                                                     # chooses 3 h
                                                                                                                                                                                                        par(mfrow=c(3,3)
                                                                                                                                                                                                                                                                                                                     decay = 4e-4,
                                                                                                                                                                                                        par(infrow=c(3,5))
termplot(fit5, partial.resid=TRUE,
rug=FALSE, se=TRUE,
col.res='#C0C0C050', pch=19)
                                                                                                                                                                                                                                                                                                                                                      # "weight dec
                                                                                           on boundary plot in F
                                                                                                                                                                                                                                                                                                                     linout = TRUE, # linear regr
                                                                                                                                                                                                                                                                                                                     skip = FALSE,
                                                                                                                                                                                                                                                                                                                                                      # a N.N. with
                                                                                         \begin{split} & \mathsf{seq}(\mathsf{min}(\mathsf{x}[\ ,\ 1]),\ \mathsf{max}(\mathsf{x}[\ ,\ 1]),\ \mathsf{length} = \mathsf{len}) \\ & \mathsf{seq}(\mathsf{min}(\mathsf{x}[\ ,\ 2]),\ \mathsf{max}(\mathsf{x}[\ ,\ 2]),\ \mathsf{length} = \mathsf{len}) \\ \end{aligned} 
                                                                                                                                                                                                                                                                                                                     maxit = 500)
                                                                             yp <- seq(min(x|, 2]), max(x|, 2]), length = len)
grid <- expand.grid(xp, yp)
Z <- predict(object, grid, ...)
zp <- as.numeric(Z$class),
zp <- Z$post[, 3] - pmax(Z$post[, 2], Z$post[, 1])
contour(xp, yp, matrix(zp, len),</pre>
                                                                                                                                                                                                           R2 describes the proportion of the total variation
                                                                                                                                                                                                                                                                                                 To get the weights use summary(Nfit), R prefixes
                                                                                                                                                                                                          of the response Y around its mean Y bar which is
                                                                                                                                                                                                                                                                                                input variables with i and hidden unit with h. To
                                                                                                                                                                                                          explained by the regression Y hat.
                                                                                                                                                                                                                                                                                                get the error use sum(residuals(Nfit)2)
                                                                                                     TRUE, levels = 0, drawlabels = FALSE, col = colcont)
```

optim(*, method="BFGS")

is equivalent to using a neural network (note results may differ due to different seed).

Optimization in R

Assume we have a fct. like this for the neg. log likelihood which we want to minimize (case of binomial distribution of response and logist. regr.),

Then the following will return the vector beta (same as that of logistic regression), optim(c(0, 0), neg.11, data = heart)par

- Start with M = 1 subset, P = {R} = {R^p}.
 Refine R into R_{left} ∪ R_{right} where:

$$\begin{array}{lll} \mathcal{R}_{left} & = & \mathbb{R} \times \mathbb{R} \times \ldots \times (-\infty, d] \times \mathbb{R} \ldots \times \mathbb{R}, \\ \mathcal{R}_{right} & = & \mathbb{R} \times \mathbb{R} \times \ldots \times (d, \infty) \times \mathbb{R} \ldots \times \mathbb{R}, \end{array}$$

where one of the axes is split at the split point d, where d is from the finite set of mid-points between observed values. The search for the axes to split and the split point d are determined such that the negative log-likelihood is maximally reduced with the refinement (search ever $f \in \{1, ..., p\}$ and $d \in \{\text{mid-points of observed values}\}$). Build the new partition $\mathcal{P} = \{\mathcal{R}_1, \mathcal{R}_2\}$ with $\mathcal{R}_1 = \mathcal{R}_{teft}$, $\mathcal{R}_2 = \mathcal{R}_{right}$.

3. Refine the current partition P as in step 2 by refining one of the partition cells from the current partition P. That is, we search for the best partition cell to refine which includes a search as in step 2 for the best axes to split and the best split point. Then, we up-date the partition:

- Iterate step 3 for a large number, M = M_{max}, of partition cells.
- Backward deletion: prune the tree (see below) until a reasonable model size, typically determined via cross-validation, is achieved.