Impact of Demographic Factors on Perception of Tertiary Colors

A two – way ANOVA

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Introduction

- Understanding the factors influencing color perception has been a subject of interest in various studies, with age and sex our primary focus in this report.
- Previous studies suggested that females observe more shades of colors and utilize a greater color spectrum than males.
- Other studies concluded pronounced differences due to varying age.
- In view of these insights, we decided to test for the presence of statistical disparity in color perception across different sexes and age groups by examining differences in the mean number of different tertiary colors correctly reported in a provided painting.

Methodology

- A sample of 120 individuals was gathered, distributed into 4 equal sized groups categorized by age (older/younger) and sex (male/female).
- A summary statistics of the data is provided, and results are interpreted.
- Visualization of data is performed via boxplots and interaction plots.
- Upon inspection of summary statistics, normality and equal variances tests are performed.
- Outlier analysis is performed to identify extreme values in the data.
- Under appropriate conditions established by previous tests, a balanced two way ANOVA is conducted to explore effects of age and sex on perception of tertiary colors. Results are interpreted accordingly.
- Ad hoc tests will be employed <u>if</u> the ANOVA provides significant results.
- All tests are subject to a 5% significance level.

| | Male | Female | | | |
|-------|---------|--------|---------|--|--|
| Older | Younger | Older | Younger | | |
| 8 | 2 | 4 | 6 | | |
| 1 | 7 | 4 | 11 | | |
| 1 | 2 | 4 | 11 | | |
| 2 | 3 | 5 | 11 | | |
| 2 | 3 | 5 | 11 | | |
| 2 | 3 | 5 | 11 | | |
| 2 | 3 | 5 | 11 | | |
| 3 | 4 | 6 | 10 | | |
| 3 | 4 | 6 | 10 | | |
| 3 | 4 | 6 | 10 | | |
| 3 | 4 | 6 | 10 | | |
| 3 | 4 | 6 | 9 | | |
| 4 | 2 | 7 | 10 | | |
| 4 | 5 | 5 | 9 | | |
| 4 | 5 | 7 | 9 | | |
| 4 | 5 | 7 | 12 | | |
| 0 | 5 | 7 | 12 | | |
| 4 | 5 | 7 | 12 | | |
| 5 | 6 | 8 | 12 | | |
| 5 | 6 | 8 | 12 | | |
| 5 | 6 | 8 | 13 | | |
| 5 | 6 | 8 | 13 | | |
| 5 | 6 | 8 | 15 | | |
| 6 | 7 | 9 | 13 | | |
| 6 | 7 | 9 | 14 | | |
| 6 | 7 | 9 | 14 | | |
| 6 | 7 | 9 | 17 | | |
| 7 | 8 | 10 | 7 | | |
| 7 | 8 | 11 | 7 | | |
| 6 | 10 | 10 | 7 | | |

Summary statistics

| Sex | Age | Sample Size | Mean | SE Mean | Standard Deviation | Minimum | Q1 | Median | Q 3 | Maximum | IQR | Skewness | Kurtosis (excess) |
|--------|---------|-------------|--------|---------|-----------------------|---------|-------|--------|------------|---------|-------|----------|----------------------|
| Female | Older | 30 | 6.967 | 0.351 | 1.921 | 4.000 | 5.000 | 7.000 | 8.250 | 11.000 | 3.250 | 0.21 | -0.78 |
| | Younger | 30 | 10.967 | 0.451 | 2.470 | 6.000 | 9.750 | 11.000 | 12.250 | 17.000 | 2.500 | 0.09 | 0.33 |
| Male | Older | 30 | 4.067 | 0.362 | 1.982 | 0.000 | 2.750 | 4.000 | 6.000 | 8.000 | 3.250 | -0.07 | -0.61 |
| | Younger | 30 | 5.133 | 0.364 | 1.995 | 2.000 | 3.750 | 5.000 | 7.000 | 11.000 | 3.250 | 0.28 | -0.29 |

Key Insights

Data Symmetry and possible Normality

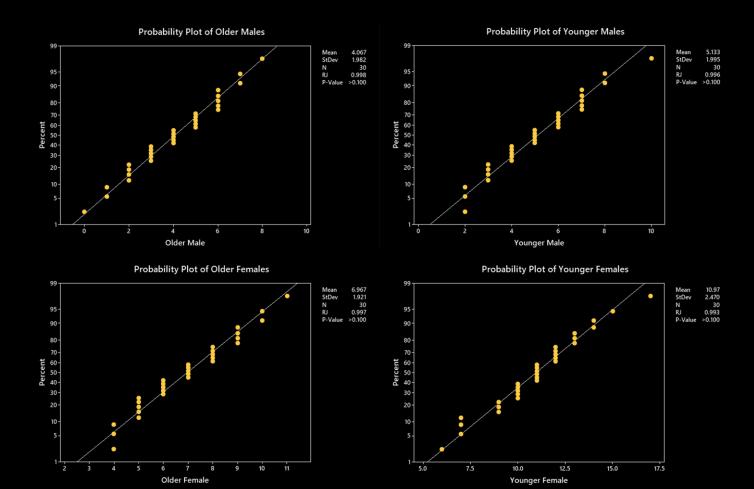
- Mean and Median are nearly equal per group.
- Skewness and (excess) Kurtosis are close to zero per group, suggesting symmetry and almost normal tails, respectively.

Differences in Sex alter the effects of Age

- For younger individuals, mean differences between sexes is nearly twice that of older individuals.
- For females, mean differences between age groups is nearly four times that of males.

Consistent Variability among all Groups

- All groups have nearly the same standard deviation.
- All groups have nearly the same interquartile range (IQR).

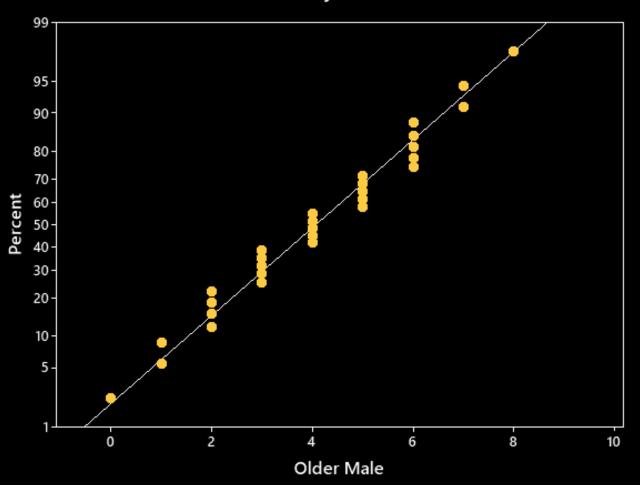


Normality Test

- Motivated by observations of summary statistics and wanting to perform a valid ANOVA, a normality test is carried.
- A Ryan Joiner test was applied to test the normality of every group.
- Results are shown in four different panels accompanied by probability plots per group.
- Test results are concluded via p value comparisons.

Results: p – values > 0.1 indicating <u>no</u> <u>statistical evidence</u> against normality, aligning with our observations.

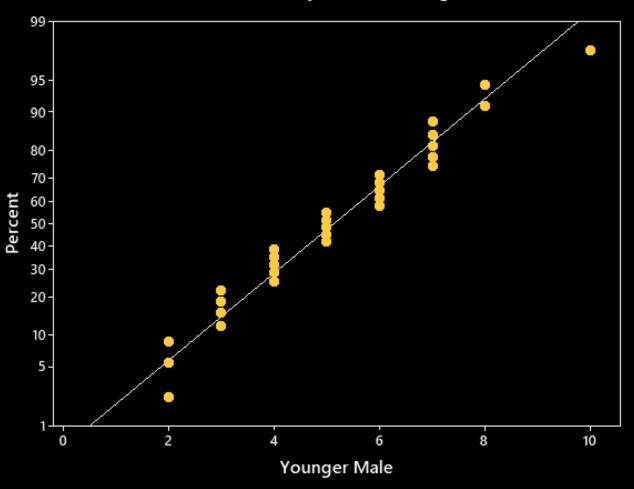
Probability Plot of Older Males



Mean 4.067 StDev 1.982 N 30 RJ 0.998 P-Value >0.100

Normality
Test (<u>Older</u>
<u>Males</u>)

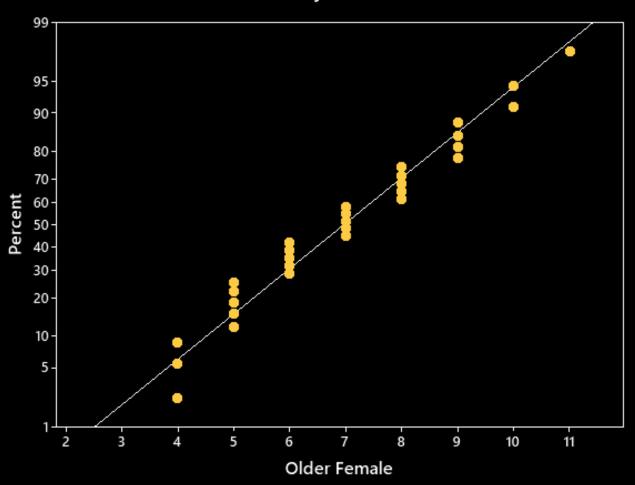
Probability Plot of Younger Males



Mean 5.133 StDev 1.995 N 30 RJ 0.996 P-Value >0.100

Normality
Test
(Younger
Males)

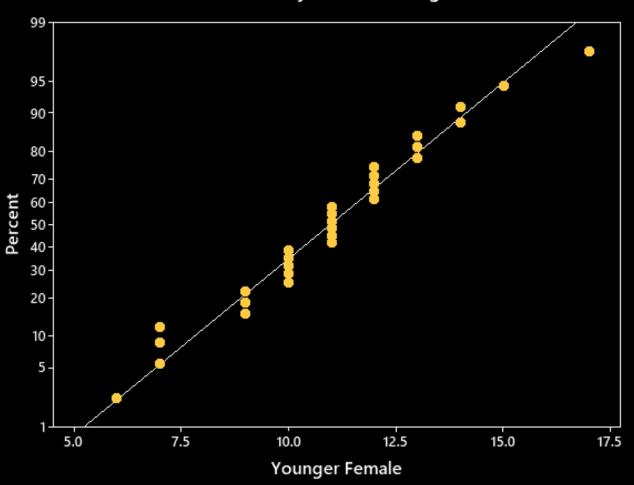
Probability Plot of Older Females



Mean 6.967 StDev 1.921 N 30 RJ 0.997 P-Value >0.100

> Normality Test (<u>Older</u> <u>Females</u>)

Probability Plot of Younger Females



Mean 10.97 StDev 2.470 N 30 RJ 0.993 P-Value >0.100

Normality
Test
(Younger
Females)

Equal Variances Test

- Multiple Comparisons and Levene tests were carried
- Results are shown on the right, accompanied by a 95% Bonferroni Confidence Intervals plot of standard deviations
- Test results are concluded via p value comparisons.

Results: p – values for both tests exceed the significance level, indicating *no statistical evidence* against equality of variances, aligning our observations.

| Sex | Age | StDev | CI |
|--------|---------|---------|--------------------|
| Female | Older | 1.92055 | (1.50769, 2.66864) |
| Female | Younger | 2.47028 | (1.77547, 3.74915) |
| Male | Older | 1.98152 | (1.53496, 2.79031) |
| Male | Younger | 1.99540 | (1.49913, 2.89715) |

Method

Null Hypothesis
Alternative Hypothesis

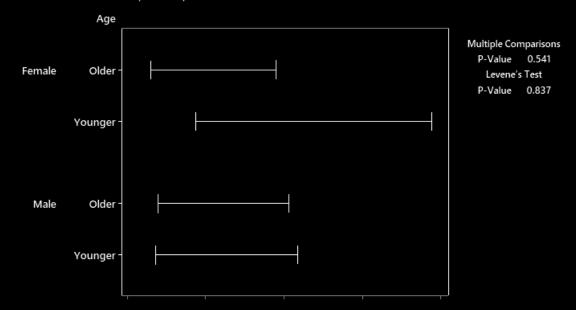
All variances are equal

At least one variance is different

Tests

| Method | Test statistic | p – value |
|-----------------------------|----------------|-----------|
| Multiple Comparisons | | 0.541 |
| Levene | 0.28 | 0.837 |

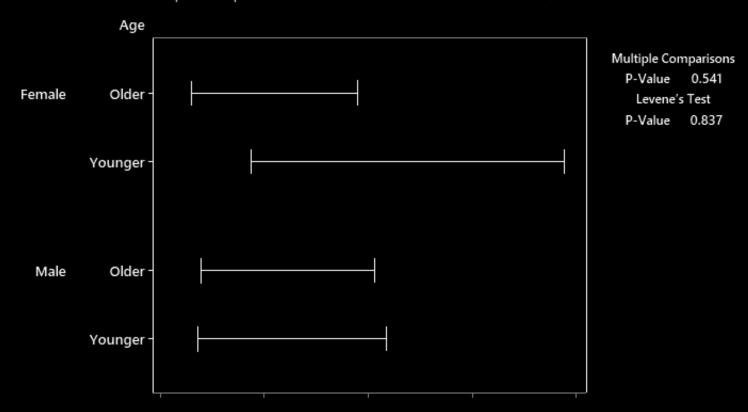
Multiple comparison intervals for the standard deviation, $\alpha = 0.05$



If intervals do not overlap, the corresponding standard deviations are significantly different.

Multiple comparison intervals for the standard deviation, $\alpha = 0.05$

Bonferroni Confidence Intervals plot of StDevs



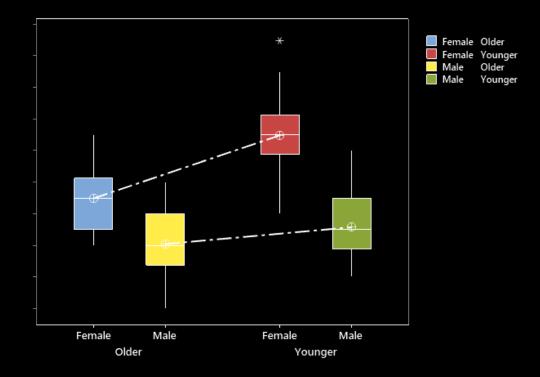
If intervals do not overlap, the corresponding standard deviations are significantly different.

Exploring Sex – Age Interaction and Outlier Analysis

From our boxplot, we observe:

- Younger people reported more tertiary colors than older people in both sexes.
- Females reported more tertiary colors than males in both age groups.
- Unparallel mean connecting lines suggests the possible presence of an interaction between the factors (difference between males and females in younger people differs from that of older people).
- The maximum value in the younger females' group may be an outlier. Under the normality assumption, we use Grubb's test and Dixon's Q test to check whether this maximum is an outlier.

Results: p – values for both tests exceed the significance level, indicating <u>no statistical evidence</u> that the maximum is an outlier. We will adopt this result in our analysis.



Method

Null Hypothesis

No outliers are present

Alternative Hypothesis

The maximum value is an outlier

Tests

Method p - value

Grubb's 0.154

Dixon's 0 0.160

Balanced Two – Way ANOVA

Under the normality, equal variances and no – outlier assumptions, we perform a Balanced Two – Way ANOVA. Results are shown below.

Analysis of Variance

| Source | DF | SS | MS | F | p |
|-------------|-----|---------|---------|--------|---------|
| Gender | 1 | 572.033 | 572.033 | 129.28 | < 0.001 |
| Age | 1 | 192.53 | 192.533 | 43.51 | < 0.001 |
| Interaction | 1 | 64.53 | 64.533 | 14.58 | < 0.001 |
| Error | 116 | 513.27 | 4.425 | | |
| Total | 119 | 1342.37 | | | |

Model Summary

The F – statistic of the model is given by:

$$F_{model} = rac{\left(rac{SS_{Total}}{DF_G + DF_A + DF_{G*A}}
ight)}{MSE} pprox 62.46$$

The model critical F – value is 2.683.

RESULTS:

- $F_{model} > F_{\alpha,3,116}$ so our model is significant (valid statistical evidence that mean differences are well assessed).
- Main effects and interaction are significant (p – values < 0.001).
- $R^2 = 61.76\%$ indicating more than 50% of the groups' variability is explained by our model.
- High significance in interaction level implies that each factor influences the effect of the other.

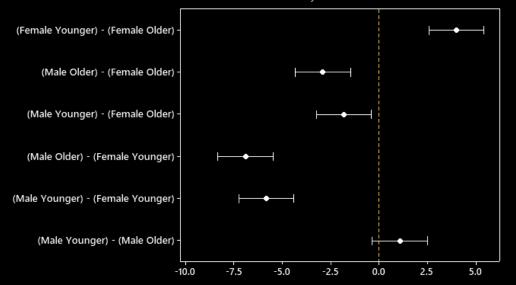
Tukey Pairwise Comparison Test

- Since the interaction is significant, we perform a Tukey Pairwise Comparison Test on the interaction to see which factor pairs contribute significantly to the observed interaction.
- Results: all group differences are <u>significant</u> except for the mean difference between younger and older males (all p values are less than the significance level except the younger and older males p value).

Tukey Simultaneous Tests for Differences of Means

| | Differences of Means | SE of Difference | Simultaneous 95% CI | Adjusted P – Value |
|-------------------|-------------------------|---------------------|------------------------|-----------------------|
| (F - Y) - (F - 0) | 4.000 | 0.543 | (2.583, 5.417) | < 0.001 |
| (M - 0) - (F - 0) | -2.900 | 0.543 | (-4.317, -1.483) | < 0.001 |
| (M - Y) - (F - 0) | -1.833 | 0.543 | (-3.250, -0.416) | 0.005 |
| (M - 0) - (F - Y) | -6.900 | 0.543 | (-8.317, -5.483) | < 0.001 |
| (M - Y) - (F - Y) | -5.833 | 0.543 | (-7.250, -4.416) | < 0.001 |
| (M - Y) - (M - O) | 1.067 | 0.543 | (-0.350, 2.484) | 0.208 |

Tukey Simultaneous 95% ClsDifferences of Means for Tertiary Colors



If an interval does not contain zero, the corresponding means are significantly different.

Conclusion

Our findings align with previous studies:

- Sex and Age impact the number of perceived tertiary colors by individuals.
- For each age group, females tend to perceive more tertiary colors than males.
- For each sex group, younger individuals perceive more tertiary colors than older individuals.
- Sex alters the effect age has on an individual's ability to perceive tertiary colors (and vice versa).
- Sex effects are more pronounced in younger individuals than older individuals.
- Effect of age is significant in females, whereas males show no significant difference.