ASSIGNMENT 4

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Download all python codes from

https://github.com/AmulyaTallamraju/EE3900/blob/ main/Assignment-4/codes/Assignment-4.py

and latex-tikz codes from

https://github.com/AmulyaTallamraju/EE3900/blob/ main/Assignment-4/Assignment-4.tex

1 Linear forms 2.36

Find the coordinates of the point where the line through $\begin{bmatrix} 1 \\ 6 \end{bmatrix}$ and $\begin{bmatrix} 4 \\ 1 \end{bmatrix}$ crosses the YZ-plane.

2 SOLUTION

The equation of the line is

$$\mathbf{x} = \mathbf{A} + \lambda \left(\mathbf{B} - \mathbf{A} \right) \tag{2.0.1}$$

The equation of the plane can be represented as

$$\mathbf{n}^T \mathbf{x} = c \tag{2.0.2}$$

The point of intersection of the line and the plane satisfies the plane equation and is given by

$$c = \mathbf{n}^T(\mathbf{x}) \tag{2.0.3}$$

$$= \mathbf{n}^{T} (\mathbf{A} + \lambda (\mathbf{B} - \mathbf{A})) \tag{2.0.4}$$

Thus,

$$\lambda = \frac{c - \mathbf{n}^T \mathbf{A}}{\mathbf{n}^T (\mathbf{B} - \mathbf{A})}$$
 (2.0.5)

The point of intersection is then given by

$$\mathbf{x} = \mathbf{A} + \left(\frac{c - \mathbf{n}^T \mathbf{A}}{\mathbf{n}^T (\mathbf{B} - \mathbf{A})}\right) (\mathbf{B} - \mathbf{A})$$
 (2.0.6)

For the given problem,

$$\mathbf{A} = \begin{pmatrix} 5\\1\\6 \end{pmatrix} \tag{2.0.7}$$

$$\mathbf{B} = \begin{pmatrix} 2 \\ -3 \\ 5 \end{pmatrix} \tag{2.0.8}$$

$$\mathbf{n} = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} \tag{2.0.9}$$

$$c = 0 (2.0.10)$$

Solving the above we get

$$\lambda = \frac{-5}{2} \tag{2.0.11}$$

Substituting the value of λ we have the point of contact as

$$\mathbf{x} = \begin{pmatrix} 5 \\ 1 \\ 6 \end{pmatrix} - \frac{5}{2} \begin{pmatrix} 2 \\ -3 \\ 5 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 0 \\ 17 \\ -13 \end{pmatrix}$$
 (2.0.12)

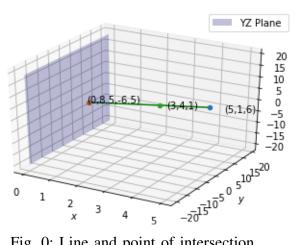


Fig. 0: Line and point of intersection