### Comments

// one line /\* multiple lines \*/

# Basic types

bool - Booleans int - signed big integers str - string literals type Name = otherType type alias, starts with upper-case

### Literals

#### false true

123 123 000 0x12abcd

"Quint": str, a string

Int: Set[int] - all integers

Nat: Set[int] - all nonnegative integers

**Bool** = Set(false, true)

### Records

{ name: str, age: int } record type

{ name: "TLA+", age: 33 } new record of two fields

R.name the field value

R.with("name", "Quint") copy of R but with the field set to the new value

fields(R): Set[str] the set of field names

#### Sets - core data structure!

**Set**[*T*] – type: set with elements of type T Set(1, 2, 3) - new set, contains its arguments 1.to(4) - new set: Set(1, 2, 3, 4)

1.in(S) - true, if the argument is in S

 $S_{\bullet}$  contains (1) – the same

S.subseteq(T) - true, ifall elements of S are in T

 $S_{\bullet}$ union(T) – new set: elements in S or in T

S.intersect(T) - new set: elements both in S and in T

S-exclude(T) – new set: elements in S but not in T

 $S_map(x \Rightarrow 2 * x) - new$ set: elements of S are transformed by <u>expression</u>

 $S.filter(x \Rightarrow x > 0)$  new set: leaves the elements of S that satisfy condition

S\_exists( $x \Rightarrow x > 10$ ) true, if some element of S satisfies condition

 $S.forall(x \Rightarrow x \leq 10)$ true, if all elements of S satisfy condition

size(S) - the number of elements in S, unless S is infinite (Int or Nat)

**isFinite**(*S*) – true, if *S* is finite

Set(1, 2).powerset() all subsets: Set(Set(), Set(1), Set(2), Set(1, 2))

flatten(S) - union of all sets in S

chooseSome(S) - an element of S via a fixed rule

 $S.fold(i, (s, x) \Rightarrow s + x)$  go over elements of Basic algebraic data types S in some order, apply the expression, continue with the result; i is the initial value of s

# Maps - key/value bindings

 $a \rightarrow b - type$ : binds keys of type a to values of type b

 $Map(1 \rightarrow 2, 3 \rightarrow 6) - binds$ keys 1, 3 to values 2, 6

 $S_{mapBy}(x \Rightarrow 2 * x) - binds$ keys in *S* to expressions

M. keys() - the set of keys

 $M_{\bullet}$  get(key) - get the value bound to key

M.set(k, v) - copy of M: but binds k to v, if k has a value

 $M_{\bullet}$  put(key, v) – copy of M: but (re-)binds k to v

M.set(k, (old => old + 1))as M.set(k, v) but v is computed via anonymous operator with  $old == M_{\bullet} get(k)$ 

S.setOfMaps(T) - new set: contains all maps that bind elements of S to elements of T

Set((1, 2), (3, 6)).setToMap() new map: bind the first elements of tuples to the second elements

# **Tuples**

(str, int, bool) tuple type

("Quint", 2023, true) new tuple

T. 1 T. 2 T. 3 get tuple elements

tuples(*S1*, *S2*, *S3*) the set of all tuples with

elements in S1, S2, S3

#### Lists - use Set, if you can

**List**[*T*] – type: list with elements of type T

[1, 2, 3] - new list, contains its arguments in order

List(1, 2, 3) – the same

range(start, end) - new list [start, start + 1, ..., end - 1]

length(L) - the number of elements in the list L

L[i] - ith element, if  $0 \ll i \ll length(L)$ 

L.concat(K) – new list: start with elements of L, continue with elements of K

Lappend(x) - new list: just L.concat([x])

L.replaceAt(i, x) – L's copy but the ith element is set to x

Listice(s, e) – new list: [L[s], ..., L[e-1]]

L.select(x > 5) - new list: leaves the elements of L that satisfy condition

L.foldl(i,  $(s, x) \Rightarrow s + x$ ) go over elements of L in order, apply expression, continue with the result; i is the initial value of s

L.foldr(i,  $(s, x) \Rightarrow x + s$ ) as foldl, but in the reverse order of L

head(L) – the element L[0]

tail(L) - new list: all elements of L but the head

indices(L) - new set: 0.to(length(L) - 1)



### Boolean expressions

```
p == q - p equals q
not(b) - Boolean "not"
p != q - not(p == q)
p and q - Boolean "and"
p or q - Boolean "or"
p implies q - not(p) or q
p iff q - p == q
and { p1, ..., pk }
p1 and ... and pk
or { p1, ..., pk }
p1 or ... or pk
```

#### Control flow

```
if (p) e1 else e2 - e1 if p
is true, and e2 otherwise
```

### Pure definitions

may be nested

```
pure val N = 3 + 4 - bind
a constant expression to N
```

```
pure def max(i, j) = \{
  if (i > j) i else j
} - bind the operator over
constants to max
```

 $(x, y) \Rightarrow \max(i, j) - an$ anonymous operator (lambda). Pass to other operators.

# Integer expressions

```
no overflows, priority top-to-bottom
```

```
i^{i} - i to the power of i
-i - negation
i * j i / j i % j
i + j \quad i - j
i < j i \le j i >= j
```

### Modules

```
module A {
 // pure definitions
 // constants
 // state variables
 // actions
 // runs
 // temporal operators
                       under construction
module B {
  // make all names of A visible in B
  import A.*
```

### States and definitions

const Nodes: Set[str] -

```
declare a specification parameter,
bind later with instance
var active: Set[str] - declare
a state variable, uninitialized
val allActive =
  active == Nodes - define a
constant in the current state
def isActive(n) = {
  n_{\bullet}in(active)
} - define an operator of n and
of the current state
```

#### Actions - to make state transitions

active' = Nodes - record that active must be set to Nodes in a next machine state. Return true.

#### nondet n = one0f(Nodes)

A - pick an arbitrary element of *Nodes*, bind to n, call action A

assert(active != Set()) report error if condition is false

```
action \ activate(n) = \{
  active' = active.union(Set(n))
} - define an action
all {
  isActive("a"),
  activate("b"),
} - execute all actions in arbitrary
order. Only if all actions return
true, record the updates to the next
```

state and return true. Otherwise, return false.

```
any {
 activate("a"),
 activate("b"),
```

} - execute some action that returns true, record its updates to the next state, return true. If no such action is available, return false.

#### Runs - tests and execution examples

```
init.then(step) - execute init.
On true, update the state
variables, execute step.
On false, return false.
step.repeated(n) - execute step
n times, in sequence. Return true,
only if all actions returned true.
step.fail() - execute step.
If it returns false, return true.
If it returns true, return false.
run test1 =
  activate("a")
    .then(activate("b"))
    .then(all {
      assert("a".in(active)),
      assert("b".in(active)),
      active' = active,
    }) - a simple test
```

# Temporal operators

safety and liveness



under construction