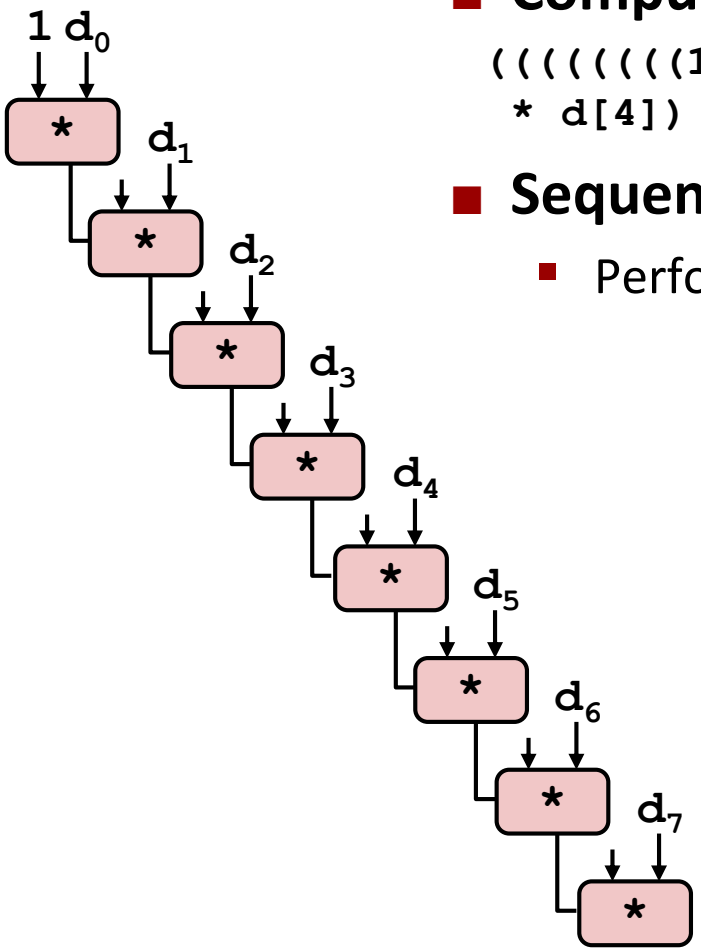
Combine4 = Serial Computation (OP = *)



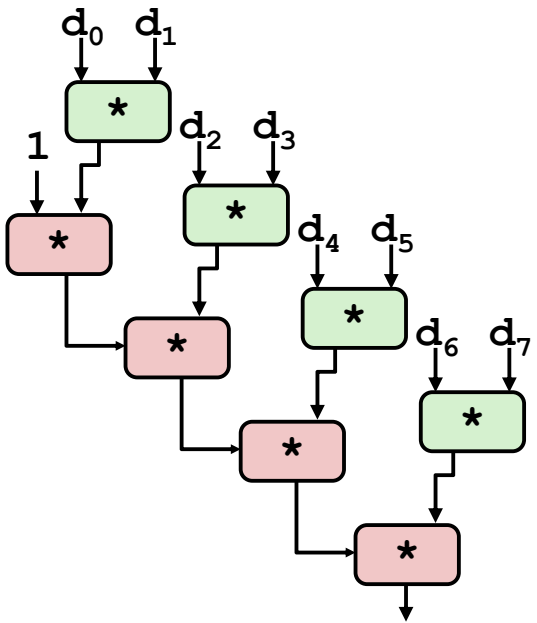
- **Computation (length=8)**

```
(((((((1 * d[0]) * d[1]) * d[2]) * d[3])
 * d[4]) * d[5]) * d[6]) * d[7])
```

- **Sequential dependence**
  - Performance: determined by latency of OP

Reassociated Computation

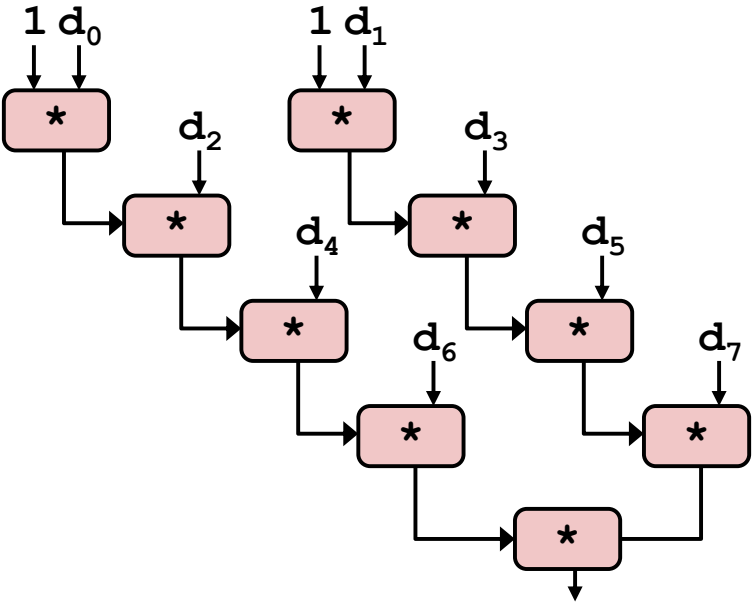
```
x = x OP (d[i] OP d[i+1]);
```



- **What changed:**
  - Ops in the next iteration can be started early (no dependency)
- **Overall Performance**
  - N elements, D cycles latency/op
  - Should be (N/2+1)*D cycles: **CPE = D/2**
  - Measured CPE slightly worse for FP mult

Separate Accumulators

```
x0 = x0 OP d[i];
x1 = x1 OP d[i+1];
```



- **What changed:**
  - Two independent "streams" of operations
- **Overall Performance**
  - N elements, D cycles latency/op
  - Should be (N/2+1)*D cycles: **CPE = D/2**
  - CPE matches prediction!

What Now?

FP *	Unrolling Factor L							
K	1	2	3	4	6	8	10	12
1	5.00	5.00	5.00	5.00	5.00	5.00		
2		2.50		2.50		2.50		
3			1.67					
4				1.25		1.25		
6					1.00			1.19
8						1.02		
10							1.01	
12								1.00

Accumulators

FP *	Unrolling Factor L							
K	1	2	3	4	6	8	10	12
1	2.00	2.00	1.00	1.01	1.02	1.03		
2		1.50		1.26		1.03		
3			1.00					
4				1.00		1.24		
6					1.00			1.02
8						1.03		
10							1.01	
12								1.09

Accumulators