```
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F7
APS Lab Week 11_12
Ans 1-
```

The approach which I have used to solve this problem is told by neeraj sir in the class.

The time complexity of the below code is: O(n)
The below code is giving wrong output for the strings which
contains repeated vowels.

```
#include <bits/stdc++.h>
using namespace std;
bool isVovel(char c){
           return (c=='a'||c=='e'||c=='i'||c=='o'||c=='u');
int solve(string arr ,int sizei,int k){
     int dp[sizei];
     if(isVovel(arr[0]))dp[0]=1;
     else dp[0]=0;
     for(int i=1;i<sizei;i++){</pre>
          if(isVovel(arr[i]))dp[i]=dp[i-1]+1;
          else dp[i]=dp[i-1];
    //for(int i=0;i<sizei;i++)cout<<dp[i]<<" ";
int i = 0, j = 0, ans = -1;
           while (j < sizei) {
                       if (dp[i] - dp[i] == k) {
                                   //int temp=ans;
                                   ans = max(ans, j - i);
                                   //if(temp!=ans)cout<<endl<<i<" "<<j<<endl;
                                   j++;
                                   j++;
                       ellipsymbol{} else if ellipsymbol{} else is else if ellipsymbol{} else if ellipsymbol{} else is else 
                                   j++;
                       } else {
                                   j++;
```

```
}
}
return ans;
}
int main()
{
    string s = "artyebui";
    int k=2;
    cout<<"The length of the longest substring of S which contains exactly K distinct vowels is:"<<solve(s,8,k);
    return 0;
}
</pre>
```

```
#include <bits/stdc++.h>
using namespace std;
bool isVovel(char c){
  return (c=='a'||c=='e'||c=='i'||c=='o'||c=='u');
int solve(string arr ,int sizei,int k){
 int dp[sizei];
 unordered_set<char>us;
 if(isVovel(arr[0])){
    dp[0]=1;
    us.insert(arr[0]);
 else dp[0]=0;
 for(int i=1;i<sizei;i++){</pre>
  if(isVovel(arr[i])&&us.find(arr[i])==us.end()){
     dp[i]=dp[i-1]+1;
     us.insert(arr[i]);
  }
  else dp[i]=dp[i-1];
```

```
//for(int i=0;i<sizei;i++)cout<<dp[i]<<" ";
int i = 0, j = 0, ans = -1;
  while (j < sizei) {
     if (dp[j] - dp[i] == k) {
        //int temp=ans;
        ans = max(ans, j - i+1);
        //if(temp!=ans)cout<<endl<<i<" "<<j<<endl;
        j++;
        //i++;
     ellipsymbol{} else if (dp[j] - dp[i] > k) {
        j++;
     } else {
        j++;
 return ans;
int main()
  //string s = "nitiiijeetiuch";
  string s = "nittttjehtluch";
  int k=2;
  cout<<"The length of the longest substring of S which contains exactly K distinct vowels
is:"<<solve(s,14,k);
  return 0;
}
```

```
The length of the longest substring of S which contains exactly K distinct vowels is:6
...Program finished with exit code 0
Press ENTER to exit console.
```

Below is the correct working code of above question understood from gfg-

```
#include <bits/stdc++.h>
using namespace std;
```

```
#define MAX 128
bool isVowel(char x)
{
  return (x == 'a' || x == 'e' || x == 'i' ||
        x == 'o' || x == 'u');
}
int KDistinctVowel(char s[], int k)
  int n = strlen(s);
  int c[MAX];
  memset(c, 0, sizeof(c));
  int result = -1;
  for (int i = 0, j = -1; i < n; ++i) {
     int x = s[i];
     if (isVowel(x)) {
        if (++c[x] == 1) {
           --k;
        }
     }
     while (k < 0) {
        x = s[++j];
        if (isVowel(x)) {
           if (--c[x] == 0) {
              ++k;
           }
        }
     if (k == 0)
        result = max(result, i - j);
  }
  return result;
int main(void)
  char s[] = "artyebui";
```

```
int k = 2;
  cout <<"the length of the longest substring of S which contains exactly K distinct
vowels."<< KDistinctVowel(s, k);
  return 0;
}
the length of the longest substring of S which contains exactly K distinct vowels.6
...Program finished with exit code 0
Press ENTER to exit console.</pre>
```

Ans 2-

```
//This question can be easily solved using the kdanes algorithm.
#include <bits/stdc++.h>
using namespace std;
int solve(int s[],int size){
  int curSum=0;
  int maxSum=INT MIN;
  int curIndex;
  int maxIndex=0;
 for(int i=0;i<size;i++){</pre>
    curSum+=s[i];
    if(curSum>maxSum){
      maxSum=curSum;
      maxIndex=curIndex;
    if(curSum<0){
      curIndex=i+1;
      curSum=0;
    }
 }
 int temp=0;
 cout<<"The subsequence which will create the maximum sum will be :\n";
 while(temp!=maxSum){
    cout<<s[maxIndex]<<" ";
    temp+=s[maxIndex];
    maxIndex++;
 return maxSum;
int main()
```

```
int s[]={5,15,-30,10,-5,40,10};
int size=7;
int ans=solve(s,size);
cout<<"\nThe maximum sum will be :"<<ans<<endl;
return 0;
}</pre>
```

```
The subsequence which will create the maximum sum will be:

10 -5 40 10

The maximum sum will be:55

...Program finished with exit code 0

Press ENTER to exit console.
```

The solution of the above problem by using the approach of creating an array to maintain the sum as told by sir in class-

```
#include <bits/stdc++.h>
using namespace std;
int solve(int arr[] ,int size){
  int dp[size];
  dp[0]=arr[0];
  for(int i=1;i<size;i++){
     if(dp[i-1]>0)dp[i]=dp[i-1]+arr[i];
     else dp[i]=arr[i];
  }
  int ans=INT_MIN;
  for(int i=0;i<size;i++){
     ans=max(dp[i],ans);
  }
  return ans;
}
int main()
{
  int s[]={5,15,-30,10,-5,40,10};</pre>
```

```
int size=7;
int ans=solve(s,size);
cout<<"\nThe maximum sum will be :"<<ans<<endl;
return 0;
}</pre>
```

```
The maximum sum will be :55

...Program finished with exit code 0
Press ENTER to exit console.
```

Ans 3-

//The below given code is written by me as per the class lecture. //Ask how to code the trace back to get what operation to be done at what index.

```
#include <bits/stdc++.h>
using namespace std;
int main()
{
string src="vish";
int col=src.size();
string dst="vishal";
int rows=dst.size();
int arr[rows][col];
for(int j=0;j<col;j++)arr[0][j]=j;
for(int i=0;i<rows;i++)arr[i][0]=i;
for(int i=1;i<rows;i++){</pre>
  for(int j=1;j<col;j++){
     if(dst[i]==src[j])arr[i][j]=arr[i-1][j-1];
        arr[i][j]=(min(arr[i-1][j-1],min(arr[i][j-1],arr[i-1][j])))+1;
  }
}
```

```
cout<<"Number of operations required will be "<< arr[rows-1][col-1]<<endl;
return 0;
}
```

```
Number of operations required will be 2
...Program finished with exit code 0
Press ENTER to exit console.
```

Ans 4-

Code-

```
#include <bits/stdc++.h>
using namespace std;
int main()
 int p[]={40, 20, 30, 10, 30};
  int n=5;
  int m[5][5];
  for (int i = 1; i < n; i++)m[i][i] = 0;
  for(int d=1;d< n-1;d++){
    for(int i=1;i< n-d;i++){
       int j=i+d;
       int minval=INT MAX;
       for(int k=i;k \le j-1;k++){
          int a=m[i][k]+m[k+1][j]+p[i-1]*p[k]*p[j];
         minval=min(minval,a);
       }
       m[i][j]=minval;
    }
 }
  cout<<"Minimum number of operations required are:"<<m[1][n-1]<<endl;
  return 0;
}
```

```
Minimum number of operations required are:26000

...Program finished with exit code 0

Press ENTER to exit console.
```

Ans 5-

Code-

```
#include <bits/stdc++.h>
using namespace std;
string solve(string s1,string s2,int row,int col){
  int dp[row+1][col+1];
  for(int j=0;j<=col;j++)dp[0][j]=0;
  for(int i=0;i <= row;i++)dp[i][0]=0;
  for(int i=1;i <= row;i++){
     for(int j=1;j <= col;j++){
       if(s1[i]==s2[j])dp[i][j]=dp[i-1][j-1]+1;
       else dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
       // cout<<dp[i][j]<<" ";
     }
    // cout<<endl;
  }
  int i=row;
  int j=col;
  cout<<"The length of longest common subsequence available is:"<<dp[i][j]<<endl;
  string answer="";
  while(i>0&&j>0){
     if(s1[i-1]==s2[j-1]){
        answer+=s1[i-1];
       i--;
       j--;
```

```
else if(dp[i-1][j]>dp[i][j-1]){
       i--;
     }
     else j--;
     //cout<<answer<<endl;
  }
  reverse(answer.begin(),answer.end());
  return answer;
}
int main()
  //My code of trace back fails for below commented test case. This is happening
because we are not handling the tie up cases in the traceback
  //string s1 ="ACADB";
  //string s2 = "CBDB";
  string s1 ="nitin";
  string s2 = "iin";
  int row=s1.size();
  int col=s2.size();
  string ans=solve(s1,s2,row,col);
  cout<<"The longest common subsequence which is available in both the given strings
is: "<<ans<<endl;
  return 0;
}
```

```
The length of longest common subsequence available is:3
The longest common subsequence which is available in both the given strings is: iin
...Program finished with exit code 0
Press ENTER to exit console.
```

Ans 6-

This code is taken from gfg because I am not able to implement this completely by own. #include
bits/stdc++.h> using namespace std;

```
class NAryTree
         int N; // No. of nodes in Tree
         // Pointer to an array containing list of children
         list<int> *adj;
         // A function used by getMinIter(), it basically does postorder
         void getMinIterUtil(int v, int minItr[]);
public:
         NAryTree(int N); // Constructor
         // function to add a child w to v
         void addChild(int v, int w);
         // The main function to find minimum iterations
         int getMinIter();
         static int compare(const void * a, const void * b);
};
NAryTree::NAryTree(int N)
         this->N = N;
         adj = new list<int>[N];
}
// To add a child w to v
void NAryTree::addChild(int v, int w)
{
         adj[v].push_back(w); // Add w to v's list.
}
void NAryTree::getMinIterUtil(int u, int minItr[])
         minItr[u] = adj[u].size();
         int *minItrTemp = new int[minItr[u]];
         int k = 0, tmp = 0;
         // Recur for all the vertices adjacent to this vertex
         list<int>::iterator i;
         for (i = adj[u].begin(); i!= adj[u].end(); ++i)
         {
                   getMinIterUtil(*i, minItr);
                   minltrTemp[k++] = minltr[*i];
         qsort(minItrTemp, minItr[u], sizeof (int), compare);
         for (k = 0; k < adj[u].size(); k++)
         {
                   tmp = minItrTemp[k] + k + 1;
                   minItr[u] = max(minItr[u], tmp);
         delete[] minItrTemp;
}
```

```
// The function to do PostOrder traversal. It uses
// recursive getMinIterUtil()
int NAryTree::getMinIter()
         // Set minimum iteration all the vertices as zero
         int *minItr = new int[N];
         int res = -1;
         for (int i = 0; i < N; i++)
                  minItr[i] = 0;
         // Start Post Order Traversal from Root
         getMinIterUtil(0, minItr);
         res = minItr[0];
         delete[] minItr;
         return res;
}
int NAryTree::compare(const void * a, const void * b)
                  return ( *(int*)b - *(int*)a );
}
// Driver function to test above functions
int main()
{
         // TestCase 1
         NAryTree tree1(17);
         tree1.addChild(0, 1);
         tree1.addChild(0, 2);
         tree1.addChild(0, 3);
         tree1.addChild(0, 4);
         tree1.addChild(0, 5);
         tree1.addChild(0, 6);
         tree1.addChild(1, 7);
         tree1.addChild(1, 8);
         tree1.addChild(1, 9);
         tree1.addChild(4, 10);
         tree1.addChild(4, 11);
         tree1.addChild(6, 12);
         tree1.addChild(7, 13);
         tree1.addChild(7, 14);
         tree1.addChild(10, 15);
         tree1.addChild(11, 16);
         cout << "TestCase 1 - Minimum Iteration: "
                   << tree1.getMinIter() << endl;
         // TestCase 2
         NAryTree tree2(3);
         tree2.addChild(0, 1);
```

```
tree2.addChild(0, 2);
cout << "TestCase 2 - Minimum Iteration: "
         << tree2.getMinIter() << endl;
// TestCase 3
NAryTree tree3(1);
cout << "TestCase 3 - Minimum Iteration: "
         << tree3.getMinIter() << endl;
// TestCase 4
NAryTree tree4(6);
tree4.addChild(0, 1);
tree4.addChild(1, 2);
tree4.addChild(2, 3);
tree4.addChild(3, 4);
tree4.addChild(4, 5);
cout << "TestCase 4 - Minimum Iteration: "
         << tree4.getMinIter() << endl;
// TestCase 5
NAryTree tree5(6);
tree5.addChild(0, 1);
tree5.addChild(0, 2);
tree5.addChild(2, 3);
tree5.addChild(2, 4);
tree5.addChild(2, 5);
cout << "TestCase 5 - Minimum Iteration: "
         << tree5.getMinIter() << endl;
// TestCase 6
NAryTree tree6(6);
tree6.addChild(0, 1);
tree6.addChild(0, 2);
tree6.addChild(2, 3);
tree6.addChild(2, 4);
tree6.addChild(3, 5);
cout << "TestCase 6 - Minimum Iteration: "
         << tree6.getMinIter() << endl;
// TestCase 7
NAryTree tree7(14);
tree7.addChild(0, 1);
tree7.addChild(0, 2);
tree7.addChild(0, 3);
tree7.addChild(1, 4);
tree7.addChild(2, 5);
tree7.addChild(2, 6);
tree7.addChild(4, 7);
tree7.addChild(5, 8);
tree7.addChild(5, 9);
tree7.addChild(7, 10);
tree7.addChild(8, 11);
tree7.addChild(8, 12);
tree7.addChild(10, 13);
```

```
cout << "TestCase 7 - Minimum Iteration: "
         << tree7.getMinIter() << endl;
// TestCase 8
NAryTree tree8(14);
tree8.addChild(0, 1);
tree8.addChild(0, 2);
tree8.addChild(0, 3);
tree8.addChild(0, 4);
tree8.addChild(0, 5);
tree8.addChild(1, 6);
tree8.addChild(2, 7);
tree8.addChild(3, 8);
tree8.addChild(4, 9);
tree8.addChild(6, 10);
tree8.addChild(7, 11);
tree8.addChild(8, 12);
tree8.addChild(9, 13);
cout << "TestCase 8 - Minimum Iteration: "
         << tree8.getMinIter() << endl;
// TestCase 9
NAryTree tree9(25);
tree9.addChild(0, 1);
tree9.addChild(0, 2);
tree9.addChild(0, 3);
tree9.addChild(0, 4);
tree9.addChild(0, 5);
tree9.addChild(0, 6);
tree9.addChild(1, 7);
tree9.addChild(2, 8);
tree9.addChild(3, 9);
tree9.addChild(4, 10);
tree9.addChild(5, 11);
tree9.addChild(6, 12);
tree9.addChild(7, 13);
tree9.addChild(8, 14);
tree9.addChild(9, 15);
tree9.addChild(10, 16);
tree9.addChild(11, 17);
tree9.addChild(12, 18);
tree9.addChild(13, 19);
tree9.addChild(14, 20);
tree9.addChild(15, 21);
tree9.addChild(16, 22);
tree9.addChild(17, 23);
tree9.addChild(19, 24);
cout << "TestCase 9 - Minimum Iteration: "
         << tree9.getMinIter() << endl;
```

```
return 0;
```

Ans 7-

This question is very hard and I am not able to implement this completely.

The pseudo code is given below-

```
MaxValue(X[0 .. 2n]):
for i \leftarrow n down to 0
Max[i, i] \leftarrow X[2k]
Min[i, i] \leftarrow X[2k]
for k \leftarrow i + 1 to n
localMax ← -∞
localMin ← ∞
for j \leftarrow i to k - 1
if X[2j + 1] = +
localMax \leftarrow max\{localMax, Max[i, j] + Max[j + 1, k]\}
localMin ← min{localMin, Min[i, j] + Min[ j + 1, k]}
else
localMax \leftarrow max\{localMax, Max[i, j] - Min[j + 1, k]\}
localMin ← min{localMin, Min[i, j] - Max[j + 1, k]}
Max[i, k] \leftarrow localMax
Min[i, k] \leftarrow localMin
return Max[0, n]
```

Lab evaluation question asked by sir. So, please try this-

<u>Minimize the maximum difference between the heights</u> - GeeksforGeeks

Length of longest increasing subsequence-

```
#include <bits/stdc++.h>
using namespace std;
int solve(int arr[] ,int sizei){
  int dp[sizei];
  dp[0]=1;
  for(int i=1;i<sizei;i++){
    dp[i]=1;</pre>
```

```
for(int j=0;j<i;j++){
        if(arr[i]>arr[j]&&dp[i]+1)dp[i]=dp[j]+1;
    }
}
int answer=0;
for(int i=0;i<sizei;i++){
    if(answer<dp[i])answer=dp[i];
}
return answer;
}
int main()
{
    int s[]={10, 22, 9, 33, 21, 50, 41, 60};
    cout<<"The length of increasing subsequence is "<<solve(s,8);
    return 0;
}</pre>
```

Q-Find the length of the longest palindromic substring.

Ans-

Using recursion-

Ask why this below given code is giving error-

```
#include <iostream>
```

```
using namespace std;
int f(int i,int j,string s){
    if(i==j)return 1;
    int inner=0;
    int left=0;
    int right=0;
    if(s[i]==s[j]&&(j-i)>1){
        int temp=f(i+1,j-1,s);
        if(temp==j-i-1){
            inner=temp+2;
        }
    }
    if(j!=0)left=f(i,j-1,s);
    if(i!=s.length()-1)right=f(i+1,j,s);
    return max(inner,max(left,right));
}
```

```
int main()
{
    //Let f(i,j,s) means the length of the longest plindromic substring in the string s.
    string s="nigttin";
    cout<<"The length of the longest palindromic substring is:"<<f(0,5,s);
    return 0;
}</pre>
```

Q-Find if divisible by M using + or - between elements of the array.

Using recursion-

1-

```
#include<bits/stdc++.h>
using namespace std;
bool f(int i,int sum,int M,int arr[],int n){
  if(i==n){
     if(sum%M==0)return true;
     else return false;
  }
  //+
  bool plus=f(i+1,sum+arr[i],M,arr,n);
  //-
  bool minus=f(i+1,sum-arr[i],M,arr,n);
  return plus||minus;
int main(){
  int arr[] = \{12,1,1\};
  int M=12;
  int sum=arr[0];
  int n=3:
  if(f(1,sum,M,arr,n))cout<<"Y";
  else cout<<"No":
  return 0;
}
//12 3 1
```

```
#include<bits/stdc++.h>
using namespace std;
bool f(int i,int sum,int M,int arr[]){
  if(i==0)
     int temp1=sum+arr[0];
     int temp2=arr[0]-sum;
     if(temp1%M==0||temp2%M==0)return true;
     else return false;
  }
  //+
  bool plus=f(i-1,sum+arr[i],M,arr);
  bool minus=f(i-1,sum-arr[i],M,arr);
  return plus||minus;
int main(){
  int arr[] = \{12,1,1\};
  vector<
  int M=12;
  int sum=0;
  if(f(2,sum,M,arr))cout<<"Y";</pre>
  else cout<<"No";
  return 0;
//12 3 1
```

Using DP memoization-

```
#include<bits/stdc++.h>
using namespace std;
bool f(int i,int sum,int M,int arr[],vector<bool>&dp){
   if(i==0){
```

```
int temp1=sum+arr[0];
     int temp2=arr[0]-sum;
     if(temp1%M==0||temp2%M==0)return true;
     else return false;
  if(dp[i]!=false)return dp[i];
  //+
  bool plus=f(i-1,sum+arr[i],M,arr,dp);
  bool minus=f(i-1,sum-arr[i],M,arr,dp);
  return dp[i]=plus||minus;
}
int main(){
  vector<bool>dp(3,false);
  int arr[] = \{12,1,1\};
  int M=12;
  int sum=0;
  if(f(2,sum,M,arr,dp))cout<<"Y";
  else cout<<"No";
  return 0;
//12 3 1
```