ADVANCED ENCRYPTION STANDARD LECTURE 5

Cryptography

Origins

- A replacement for DES was needed
 - have theoretical attacks that can break it
 - have demonstrated exhaustive key search attacks
- Can use Triple-DES but slow, has small blocks
- US NIST issued call for ciphers in 1997
- 15 candidates accepted in Jun 98
- 5 were shortlisted in Aug-99
- Rijndael ("rain-dahl") was selected as the AES in Oct-2000
- Issued as FIPS PUB 197 standard in Nov-2001

The AES Cipher - Rijndael

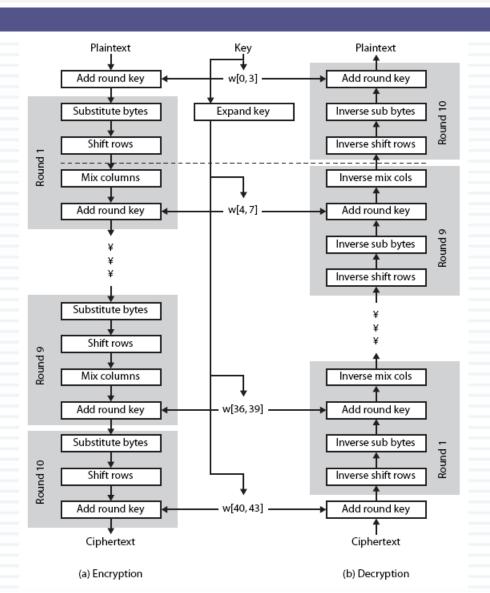
- Designed by Rijmen-Daemen in Belgium
- Has 128/192/256 bit keys, 128 bit data
- An iterative rather than feistel cipher
 - processes data as block of 4 columns of 4 bytes
 - operates on entire data block in every round
- Designed to be:
 - resistant against known attacks
 - speed and code compactness on many CPUs
 - design simplicity

AES Structure

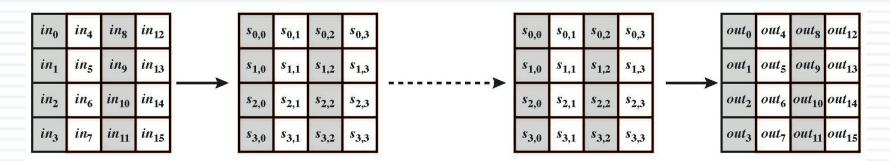
byte substitution (S-box)
shift rows (perm.)
mix columns (subs.)
add round key (XOR)

Implementation:

"XOR + table lookup"



AES Data Structures



(a) Input, state array, and output

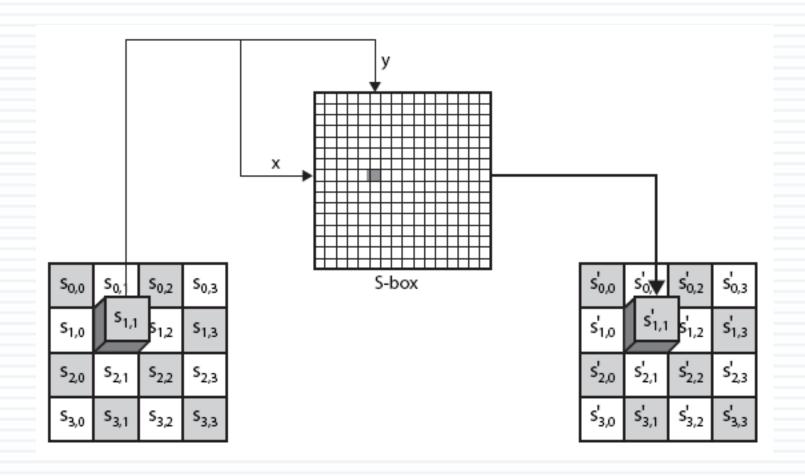


(b) Key and expanded key

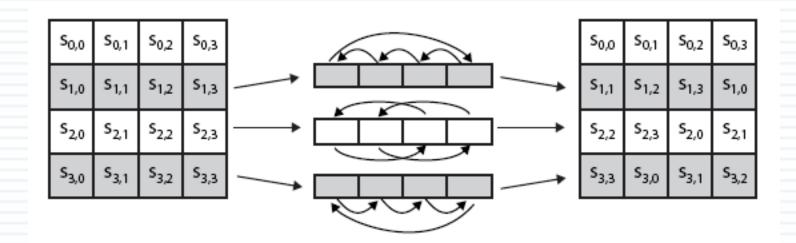
AES S-Box

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		0	1	2	3	4	5	6	7	8	9	A	В	С	D	Е	F
	0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
	1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
	2	В7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
	3	04	C7	23	СЗ	18	96	05	9A	07	12	80	E2	EB	27	В2	75
	4	09	83	2C	1A	1B	6E	5A	A0	52	3B	D6	В3	29	E3	2F	84
	5	53	D1	00	ED	20	FC	B1	5B	6A	СВ	BE	39	4A	4C	58	CF
	6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
$ _{x}$	7	51	A3	40	8F	92	9D	38	F5	ВС	В6	DA	21	10	FF	F3	D2
1	8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
	9	60	81	4F	DC	22	2A	90	88	46	EE	В8	14	DE	5E	0B	DB
	Α	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
	В	E7	C8	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
	С	BA	78	25	2E	1C	A6	В4	C6	E8	DD	74	1F	4B	BD	8B	8A
	D	70	3E	В5	66	48	03	F6	0E	61	35	57	В9	86	C1	1D	9E
	Е	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
	F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	В0	54	BB	16

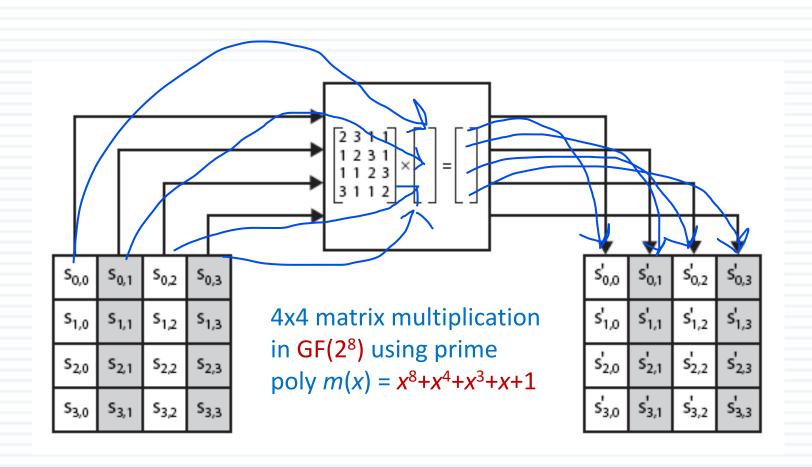
Substitute Bytes



Shift Rows



Mix Columns



Add Round Key

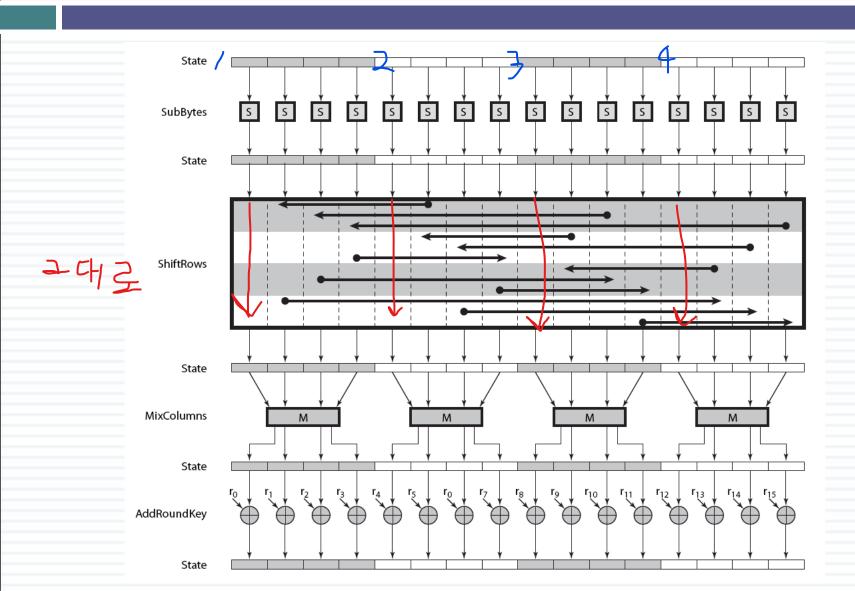
S _{0,0}	S _{0,1}	S _{0,2}	S _{0,3}
S _{1,0}	S _{1,1}	s _{1,2}	S _{1,3}
S _{2,0}	S _{2,1}	S _{2,2}	S _{2,3}
S _{3,0}	S _{3,1}	S _{3,2}	S _{3,3}



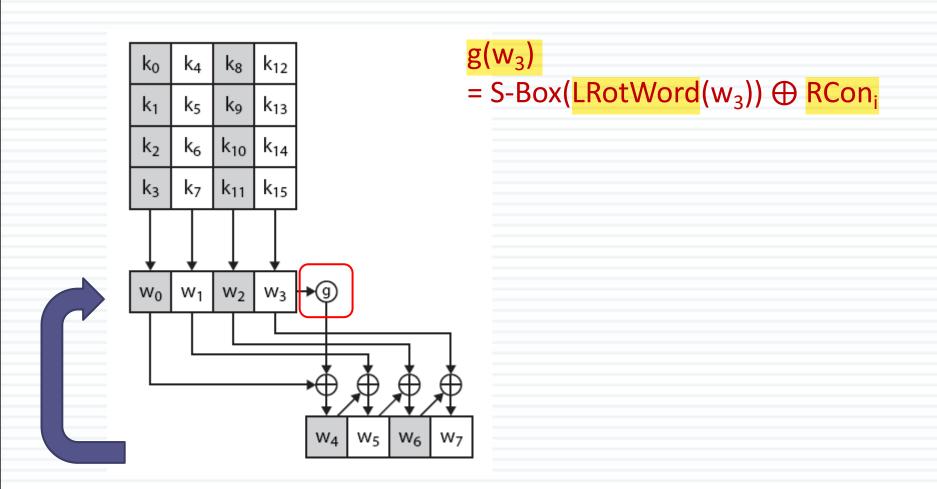
Wi	W _{i+1}	W _{i+2}	W _{i+3}
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s' _{0,0}	s' _{0,1}	s' _{0,2}	s' _{0,3}
s' _{1,0}	s' _{1,1}	s' _{1,2}	s' _{1,3}
s' _{2,0}	s' _{2,1}	s' _{2,2}	s' _{2,3}
s' _{3,0}	s' _{3,1}	s' _{3,2}	s' _{3,3}

AES Round



AES Key Expansion



AES Example Key Expansion

Key Words	Auxiliary Function
w0 = 0f 15 71 c9	RotWord(w3) = 7f 67 98 af = x1
w1 = 47 d9 e8 59	SubWord(x1)= d2 85 46 79 = y1
w2 = 0c b7 ad	Rcon(1)= 01 00 00 00
w3 = af 7f 67 98	y1 ⊕ Rcon(1)= d3 85 46 79 = z1
w4 = w0 ⊕ z1 = dc 90 37 b0	RotWord(w7)= 81 15 a7 38 = x2
w5 = w4 ⊕ w1 = 9b 49 df e9	SubWord(x4) = 0c 59 5c 07 = y2
w6 = w5 ⊕ w2 = 97 fe 72 3f	Rcon(2)= 02 00 00 00
w7 = w6 ⊕ w3 = 38 81 15 a7	y2 ⊕ Rcon(2)= 0e 59 5c 07 = z2
w8 = w4 + z2 = d2 c9 6b b7	RotWord(w11)= ff d3 c6 e6 = x3
w9 = w8 ⊕ w5 = 49 80 b4 5e	SubWord(x2)= 16 66 b4 8e = y3
w10 = w9 ⊕ w6 = de 7e c6 61	Rcon(3) = 04 00 00 00 y3 (4) Rcon(3) = 12 66 b4 8e = z3
w11 = w10 ⊕ w7 = e6 ff d3 c6	y3 ⊕ Rcon(3)= 12 66 b4 8e = z3
w12 = w8 ⊕ z3 = c0 af df 39	RotWord(w15) = ae 7e c0 b1 = x4 SubWord(x3) = e4 f3 ba c8 = y4
w13 = w12 ⊕ w9 = 89 2f 6b 67 w14 = w13 ⊕ w10 = 57 51 ad 06	Rcon(4)= 08 00 00 00
w14 = w13 ⊕ w10 = 57 51 ad 06 w15 = w14 ⊕ w11 = b1 ae 7e c0	y4 ⊕ Rcon(4)= ec f3 ba c8 = 4
w16 = w12 ⊕ z4 = 2c 5c 65 f1	RotWord(w19)= 8c dd 50 43 = x5
w17 = w16 ⊕ w13 = a5 73 0e 96	SubWord(x4)= 64 cl 53 la = y5
	Rcon(5) = 10 00 00 00
w19 = w18 + w15 = 43 8c dd 50	y5 ⊕ Rcon(5)= 74 cl 53 la = z5
w20 = w16 ⊕ z5 = 58 9d 36 eb	RotWord(w23)= 40 46 bd 4c = x6
w21 = w20 ⊕ w17 = fd ee 38 7d	SubWord(x5)= 09 5a 7a 29 = y6
	Rcon(6) = 20 00 00 00
w23 = w22 \oplus w19 = 4c 40 46 bd	y6 ⊕ Rcon(6)= 29 5a 7a 29 = z6
w24 = w20 \oplus z6 = 71 c7 4c c2	RotWord(w27) = a5 a9 ef cf = x7
w25 = w24 @ w21 = 8c 29 74 bf	SubWord(x6)= 06 d3 df 8a = y7
	Rcon(7) = 40 00 00 00
w27 = w26 ⊕ w23 = cf a5 a9 ef	y7 ⊕ Rcon(7)= 46 d3 df 8a = z7
w28 = w24 ⊕ z7 = 37 14 93 48	RotWord(w31) = 7d al 4a f7 = x8
w29 = w28 w25 = bb 3d e7 f7	SubWord(x7)= ff 32 d6 68 = y8
w30 = w29 ⊕ w26 = 38 d8 08 a5 w31 = w30 ⊕ w27 = f7 7d a1 4a	Rcon(8)= 80 00 00 00 y8 ⊕ Rcon(8)= 7f 32 d6 68 = z8
w31 = w30 + w27 = f7 7d a1 4a w32 = w28 + z8 = 48 26 45 20	RotWord(w35)= be 0b 38 3c = x9
w32 = w28 ⊕ 28 = 48 26 45 20 w33 = w32 ⊕ w29 = f3 1b a2 d7	SubWord(x8)= ae 2b 07 eb = y9
	Rcon(9)= 1B 00 00 00
w35 = w34 ⊕ w32 = 3c be 0b 38	y9 ① Rcon(9)= b5 2b 07 eb = z9
w36 = w32 ⊕ z9 = fd 0d 42 cb	RotWord(w39)= 6b 41 56 f9 = x10
w37 = w36 ⊕ w33 = 0e 16 e0 1c	SubWord(x9)= 7f 83 bl 99 = y10
w38 = w37 ⊕ w34 = c5 d5 4a 6e	Rcon(10)= 36 00 00 00
w39 = w38 ⊕ w35 = f9 6b 41 56	y10 + Rcon(10)= 49 83 bl 99 = z10
w40 = w36 ⊕ z10 = b4 8e f3 52	
w41 = w40 ⊕ w37 = ba 98 13 4e	
w42 = w41 \oplus w38 = 7f 4d 59 20	
w43 = w42 \oplus w39 = 86 26 18 76	

AES Example Encryption

Start of round		After	After	After	Round Key		
		SubBytes	ShiftRows	MixColumns			
	01 89 fe 76				0f 47 0c af		
	23 ab dc 54				15 d9 b7 7f		
	45 cd ba 32				71 e8 ad 67		
	67 ef 98 10				c9 59 d6 98		
	0e ce f2 d9	ab 8b 89 35	ab 8b 89 35	ъ9 94 57 75	dc 9b 97 38		
	36 72 6b 2b	05 40 7f f1	40 7f fl 05	e4 8e 16 51	90 49 fe 81		
	34 25 17 55	18 3f f0 fc	f0 fc 18 3f	47 20 9a 3f	37 df 72 15		
	ae b6 4e 88 65 0f c0 4d	e4 4e 2f c4 4d 76 ba e3	c4 e4 4e 2f 4d 76 ba e3	c5 d6 f5 3b 8e 22 db 12	b0 e9 3f a7 d2 49 de e6		
	74 c7 e8 d0	4d 76 ba e3 92 c6 9b 70	4d 76 ba e3 c6 9b 70 92	8e 22 db 12 b2 f2 dc 92	c9 80 7e ff		
	70 ff e8 2a	51 16 9b e5	9b e5 51 16	df 80 f7 cl	6b b4 c6 d3		
	75 3f ca 9c	9d 75 74 de	de 9d 75 74	2d c5 le 52	b7 5e 61 c6		
	5c 6b 05 f4	4a 7f 6b bf	4a 7f 6b bf	bl cl Ob cc	c0 89 57 b1		
	7b 72 a2 6d	21 40 3a 3c	40 3a 3c 21	ba f3 8b 07	af 2f 51 ae		
	b4 34 31 12	8d 18 c7 c9	c7 c9 8d 18	f9 1f 6a c3	df 6b ad 7e		
	9a 9b 7f 94	b8 14 d2 22	22 b8 14 d2	1d 19 24 5c	39 67 06 c0		
	71 48 5c 7d	a3 52 4a ff	a3 52 4a ff	d4 11 fe 0f	2c a5 f2 43		
	15 dc da a9	59 86 57 d3	86 57 d3 59	3b 44 06 73	5c 73 22 8c		
	26 74 c7 bd	f7 92 c6 7a	c6 7a f7 92	cb ab 62 37	65 0e a3 dd		
	24 7e 22 9c	36 f3 93 de	de 36 f3 93	19 b7 07 ec	f1 96 90 50		
	f8 b4 0c 4c	41 8d fe 29	41 8d fe 29	2a 47 c4 48	58 fd 0f 4c		
	67 37 24 ff	85 9a 36 16	9a 36 16 85	83 e8 18 ba	9d ee cc 40		
	ae a5 c1 ea	e4 06 78 87	78 87 e4 06	84 18 27 23	36 38 9b 46		
	e8 21 97 bc	9b fd 88 65	65 9b fd 88	eb 10 0a f3	eb 7d ed bd		
	72 ba cb 04	40 f4 lf f2	40 f4 lf f2	7b 05 42 4a	71 8c 83 cf		
	le 06 d4 fa b2 20 bc 65	72 6f 48 2d 37 b7 65 4d	6f 48 2d 72 65 4d 37 b7	1e d0 20 40 94 83 18 52	c7 29 e5 a5 4c 74 ef a9		
	00 6d e7 4e	37 b7 65 4d 63 3c 94 2f	65 4d 37 b7 2f 63 3c 94	94 c4 43 fb	4c 74 ef a9 c2 bf 52 ef		
	0a 89 cl 85	67 a7 78 97	67 a7 78 97	ec la c0 80	37 bb 38 f7		
	d9 f9 c5 e5	35 99 a6 d9	99 a6 d9 35	0c 50 53 c7	14 3d d8 7d		
	d8 f7 f7 fb	61 68 68 Of	68 Of 61 68	3b d7 00 ef	93 e7 08 al		
	56 7b 11 14	bl 21 82 fa	fa bl 21 82	b7 22 72 e0	48 f7 a5 4a		
	db al f8 77	b9 32 41 f5	b9 32 41 f5	bl la 44 17	48 f3 cb 3c		
	18 6d 8b ba	ad 3c 3d f4	3c 3d f4 ad	3d 2f ec b6	26 1b c3 be		
	a8 30 08 4e	c2 04 30 2f	30 2f c2 04	0a 6b 2f 42	45 a2 aa 0b		
	ff d5 d7 aa	16 03 0e ac	ac 16 03 0e	9f 68 f3 b1	20 d7 72 38		
	f9 e9 8f 2b	99 le 73 fl	99 le 73 fl	31 30 3a c2	fd 0e c5 f9		
	1b 34 2f 08	af 18 15 30	18 15 30 af	ac 71 8c c4	0d 16 d5 6b		
	4f c9 85 49	84 dd 97 3b	97 3b 84 dd	46 65 48 eb	42 e0 4a 41		
	bf bf 81 89	08 08 0c a7	a7 08 08 0c	6a 1c 31 62	cb 1c 6e 56		
	cc 3e ff 3b	4b b2 16 e2	4b b2 16 e2	4b 86 8a 36	b4 8e f3 52		
	al 67 59 af	32 85 cb 79	85 cb 79 32	bl cb 27 5a	ba 98 13 4e		
	04 85 02 aa	f2 97 77 ac	77 ac f2 97	fb f2 f2 af	7f 4d 59 20		
	al 00 5f 34	32 63 cf 18	18 32 63 cf	cc 5a 5b cf	86 26 18 76		
	ff 08 69 64						
	0b 53 34 14						
	84 bf ab 8f 4a 7c 43 b9						
	4d /C 43 D9						

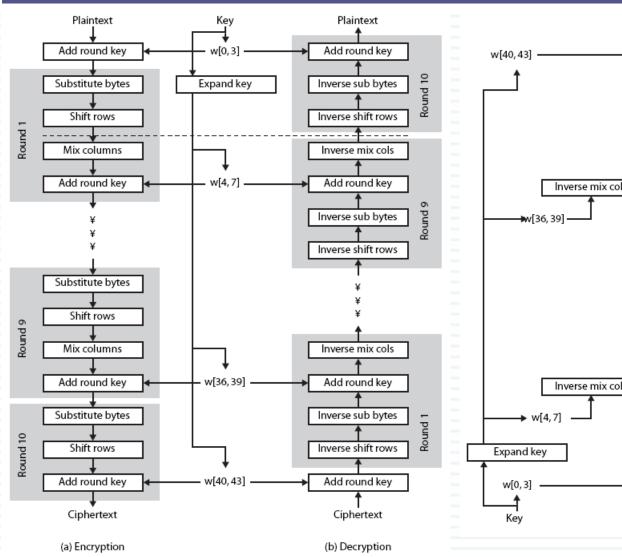
AES Example Avalanche

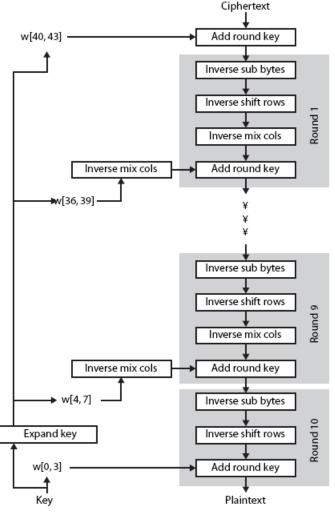
Round		Number of bits that differ
	0123456789abcdeffedcba9876543210	1
	0023456789abcdeffedcba9876543210	1
0	0e3634aece7225b6f26b174ed92b5588	1
U	0f3634aece7225b6f26b174ed92b5588	1
1	657470750fc7ff3fc0e8e8ca4dd02a9c	20
1	c4a9ad090fc7ff3fc0e8e8ca4dd02a9c	20
2	5c7bb49a6b72349b05a2317ff46d1294	58
2	fe2ae569f7ee8bb8c1f5a2bb37ef53d5	36
3	7115262448dc747e5cdac7227da9bd9c	59
,	ec093dfb7c45343d689017507d485e62	39
4	f867aee8b437a5210c24c1974cffeabc	61
7	43efdb697244df808e8d9364ee0ae6f5	01
5	721eb200ba06206dcbd4bce704fa654e	68
	7b28a5d5ed643287e006c099bb375302	08
6	0ad9d85689f9f77bc1c5f71185e5fb14	64
	3bc2d8b6798d8ac4fe36a1d891ac181a	04
7	db18a8ffa16d30d5f88b08d777ba4eaa	67
,	9fb8b5452023c70280e5c4bb9e555a4b	07
8	f91b4fbfe934c9bf8f2f85812b084989	65
	20264e1126b219aef7feb3f9b2d6de40	
9	cca104a13e678500ff59025f3bafaa34	61
,	b56a0341b2290ba7dfdfbddcd8578205	01
10	ff0b844a0853bf7c6934ab4364148fb9	58
10	612b89398d0600cde116227ce72433f0	36

AES Decryption

- We can define an equivalent inverse cipher with steps as for encryption
 - but using inverses of each step
 - with a different key schedule
- Works since result is unchanged when
 - swap byte substitution & shift rows
 - swap mix columns & add round key

AES Decryption





Implementation Aspects

- Can efficiently implement on 8-bit CPU
 - byte substitution works on bytes using a table of 256 entries
 - shift rows is simple byte shift
 - add round key works on byte XOR's
 - mix columns requires matrix multiply in GF(2⁸) which works on byte values, can be simplified to use table lookups & byte XOR's
- Designers believe this very efficient implementation was a key factor in its selection as the AES cipher