Auto-generated report from BCEA

Version: 13 December, 2018

Cost-effectiveness analysis

The cost-effectiveness analysis is based on the maximisation of the expected utility, defined as the *monetary net benefit* $nb_t = ke_t - c_t$. Here t indicates one of the interventions (treatments) being assessed, while (e, c) indicate the relevant measures of *effectiveness* and *cost*. For each intervention, the expected utility is computed as $\mathcal{NB}_t = k\mathrm{E}[e_t] - \mathrm{E}[c_t]$. When comparing two interventions (say, $t = 1$ vs $t = 0$), or using a pairwise comparison, we can determine the "best" alternative by considering the difference in the expected utilities $\mathrm{EIB} = \mathcal{NB}_1 - \mathcal{NB}_0$. This can also be expressed in terms of the *population effectiveness and cost differentials* $\mathrm{EIB} = k\mathrm{E}[\Delta_e] - \mathrm{E}[\Delta_c]$, where $\Delta_e = \mathrm{E}[e \mid \boldsymbol{\theta}_1] - \mathrm{E}[e \mid \boldsymbol{\theta}_0]$ and $\Delta_c = \mathrm{E}[c \mid \boldsymbol{\theta}_1] - \mathrm{E}[c \mid \boldsymbol{\theta}_0]$ are the average effectiveness and cost, as function of the relevant model parameters $\boldsymbol{\theta} = (\boldsymbol{\theta}_0, \boldsymbol{\theta}_1)$.

This sub-section presents a summary table reporting basic economic results as well as the optimal decision, given the selected willingness-to-pay threshold $k = 20100$. The table below presents a summary of the optimal decision, as well as the values of the Expected Incremental Benefit $\mathrm{EIB} = k\mathrm{E}[\Delta_e] - \mathrm{E}[\Delta_c]$, Cost-Effectiveness Acceptability Curve $\mathrm{CEAC} = \mathrm{Pr}(k\Delta_e - \Delta_c)$ and Incremental Cost-Effectiveness Ratio $\mathrm{ICER} = \dfrac{\mathrm{E}[\Delta_c]}{\mathrm{E}[\Delta_e]}$, for the set willingness-to-pay value.

```
summary(m,wtp=wtp)
```

```
Cost-effectiveness analysis summary


Reference intervention:   intervention 2
Comparator intervention: intervention 1


Optimal decision: choose intervention 1 for k<20100 and intervention 2 for k>=20100



Analysis for willingness to pay parameter k = 20100


                Expected utility
intervention 1          -30.880
intervention 2          -30.879


                                    EIB CEAC  ICER
intervention 2 vs intervention 1 0.00060352 0.46 20098

Optimal intervention (max expected utility) for k=20100: intervention 2

EVPI 2.5268
```

Cost-effectiveness plane

The following graph shows the cost-effectiveness plane. This presents the joint distribution of the population average benefit and cost differential, (Δ_e, Δ_c) and can be used to assess the uncertainty underlying the decision-making problem.

Each point in the graph represents a 'potential future' in terms of expected incremental economic outcomes.

The shaded portion of the plane is the '*sustainability area*'. The more points lay in the sustainability area, the more likely that the reference intervention will turn out to be cost-effective, at a given willingness to pay threshold, k (in this case selected at $k = 20100$).

```
n.ints <- m$n.comparators
if (n.ints==2) {graph="base"; pos=c(1,1)} else {graph="ggplot2"; pos=TRUE}
ceplane.plot(m,graph=graph,pos=pos,wtp=wtp)
```

Cost effectiveness plane
## intervention 2 vs intervention 1
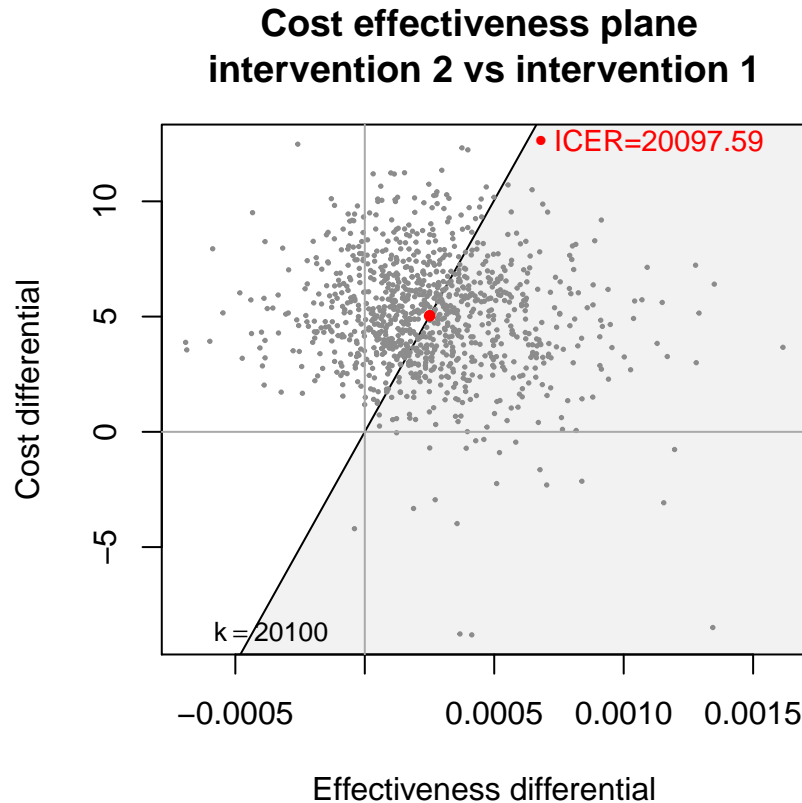
Expected Incremental Benefit

The following graph shows the Expected Incremental Benefit (EIB), as a function of a grid of values for the willingness to pay k (in this case in the interval 0 - 50000).

The EIB can be directly linked with the decision rule applied to the ICER. If a willingness to pay value k^* exists in correspondence of which EIB $= 0$ this value of k is called the *break-even point*. It corresponds to the maximum uncertainty associated with the decision between the two comparators, with equal expected utilities for the two interventions. In other terms, for two willingness to pay values, one greater and one less than k^*, there will be two different optimal decisions. The graph also reports the 95% credible limits around the EIB.

```
n.ints <- m$n.comparators
if (n.ints==2) {graph="base"; pos=c(1,1)} else {graph="ggplot2"; pos=TRUE}
eib.plot(m,graph=graph,pos=pos)
```

**Expected Incremental Benefit
and 95% credible intervals**


k* = 20100

EIB
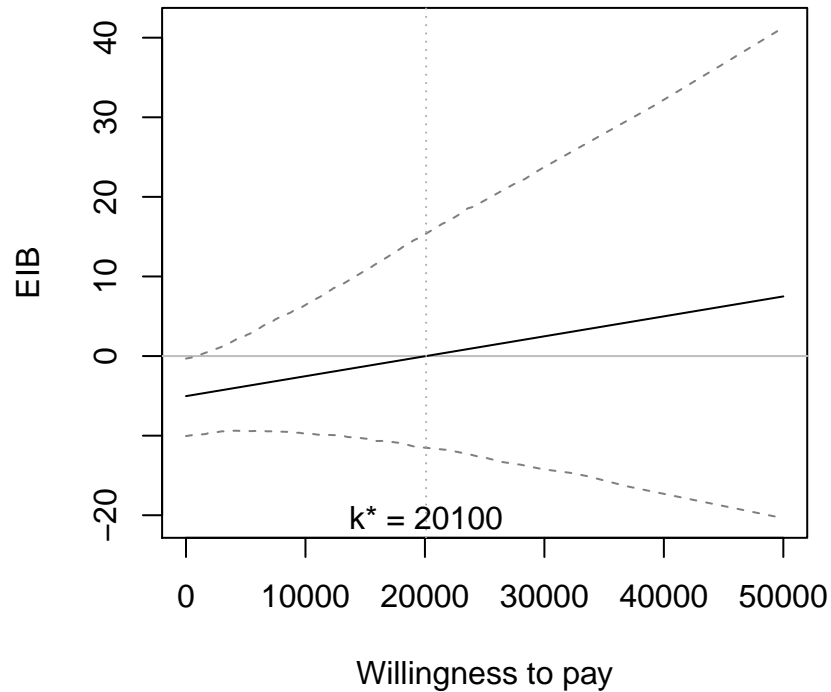
Willingness to pay

Cost-effectiveness acceptability curve

The Cost-Effectiveness Acceptability Curve estimates the probability of cost-effectiveness, for different willingness to pay thresholds. The CEAC is used to evaluate the uncertainty associated with the decision-making process, since it quantifies the degree to which a treatment is preferred. This is measured in terms of the difference in utilities, normally the incremental benefit. Effectively, the CEAC represents the proportion of simulations in which $t = 1$ is associated with a higher utility than $t = 0$.

The following graph shows the cost-effectiveness acceptability curve (CEAC). The CEAC represents the proportion of 'potential futures' in which the reference intervention is estimated to be more cost-effective than the comparator. Thus, it can be interpreted as the 'probability of cost-effectiveness'.

```
ceac.plot(m)
```

Cost Effectiveness Acceptability Curve
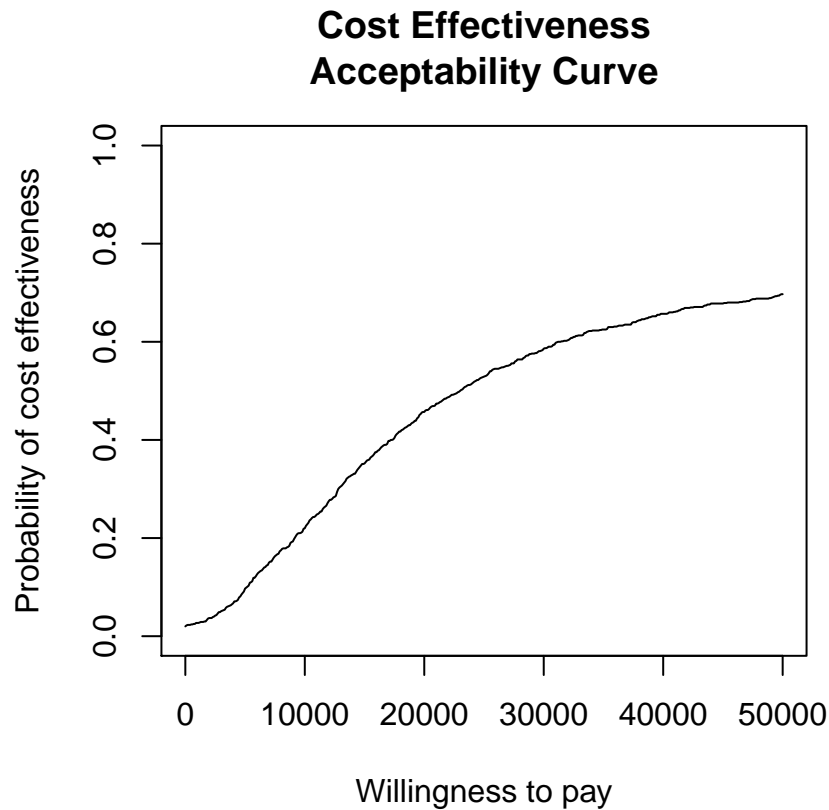
Cost-effectiveness acceptability frontier

In addition to the CEAC, we can also visualise the uncertainty in the decision-making process using the Cost-Effectiveness Acceptability Frontier. The frontier is defined as the maximum value of the probability of cost-effectiveness among all comparators. It is an indication of the uncertainty associated with choosing the cost effective intervention. In other terms, higher frontier values correspond to lower decision uncertainty.

```
n.ints <- m$n.comparators
if (n.ints==2) {graph="base"; pos=c(1,1)} else {graph="ggplot2"; pos=TRUE}
ceaf.plot(multi.ce(m),graph=graph)
```

Cost–effectiveness acceptability frontier
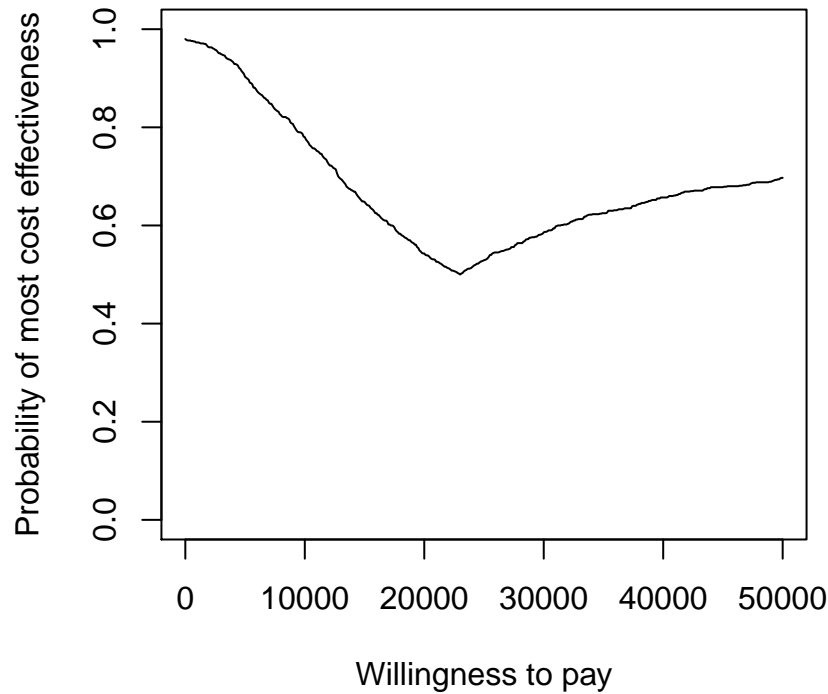
Cost-effectiveness efficiency frontier

The Cost-Effectiveness Efficiency Frontier (CEEF) compares the net costs and benefits of different interventions in a given therapeutic area. It is different from the comon differential approach (e.g. based on the Cost-Effectiveness plane), beacuse it is based on the *net* measures. The predicted costs and effectiveness for the interventions under consideration are compared directly to the costs and effectiveness for the treatments that are currently available. The frontier in itself defines the set of interventions for which cost is at an acceptable level for the benefits given by the treatment. A new intervention is *efficient* if its average effectiveness is greater than any of the currently available alternatives, or its cost are lower than that associated with other interventions of the same effectiveness.

In the following plot, the circles indicate the mean for the cost and effectiveness distributions for each treatment option. The number in each circle corresponds to the order of the treatments in the legend. If the number is black then the intervention is on the efficiency frontier. Grey numbers indicate dominated treatments.

```
n.ints <- m$n.comparators
if (n.ints==2) {graph="base"; pos=c(1,1)} else {graph="ggplot2"; pos=TRUE}
ceef.plot(m,graph=graph)
```

```
Cost-effectiveness efficiency frontier summary

Interventions on the efficiency frontier:
               Effectiveness   Costs Increase slope Increase angle
intervention 1   -0.00105595  9.6555             NA             NA
intervention 2   -0.00080537 14.6914          20098         1.5707
```

Cost–effectiveness efficiency frontier
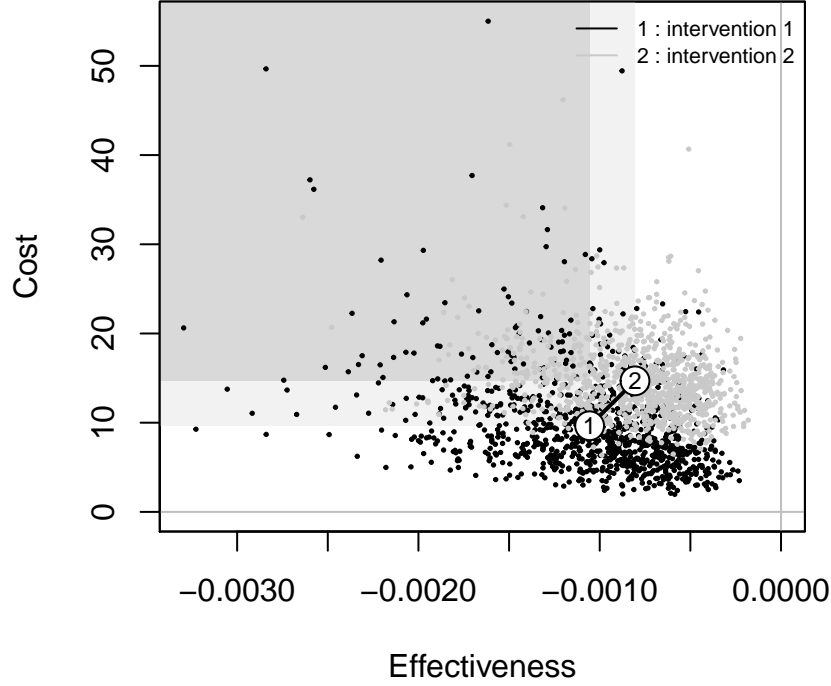
The summary is composed of two tables, reporting information for the comparators included on the frontier. It also details the average health effects and costs for the comparators not on the frontier, if any. For the interventions included on the frontier, the slope of the frontier segment connecting the intervention to the previous efficient one and the angle inclination of the segment (with respect to the $x-$axis), measured in radians, are also reported. In particular, the slope can be interpreted as the increase in costs for an additional unit in effectiveness, i.e. the ICER for the comparison against the previous treatment.

The dominance type for comparators not on the efficiency frontier is reported in the output table. This can be of two types: absolute or extended dominance. An intervention is absolutely dominated if another comparator has both lower costs and greater health benefits, i.e. the ICER for at least one pairwise comparison is negative. Comparators in a situation of extended dominance are not wholly inefficient, but are dominated because a combination of two other interventions will provide more benefits for lower costs.

Expected value of perfect information

One measure to quantify the value of additional information is known as the *Expected Value of Perfect Information* (EVPI). This measure translates the uncertainty associated with the cost-effectiveness evaluation in the model into an economic quantity. This quantification is based on the *Opportunity Loss* (OL), which is a measure of the potential losses caused by choosing the most cost-effective intervention *on average* when it does not result in the intervention with the highest utility in a 'possible future'. A future can be thought of as obtaining enough data to know the exact value of the utilities for the different interventions. This would allow the decision makers to known the optimal treatment with certainty. The opportunity loss occurs when the optimal treatment on average is non-optimal for a specific point in the distribution for the utilities.

To calculate the EVPI practically, possible futures for the different utilities are represented by the simulations. The utility values in each simulation are assumed to be known, corresponding to a possible future, which could happen with a probability based on the current available knowledge included in and represented by the model. The opportunity loss is the difference between the maximum value of the simulation-specific (known-distribution) utility $\text{NB}^*(\boldsymbol{\theta}) = k\Delta_e - \Delta_c$ and the utility for the intervention resulting in the overall

maximum expected utility $\text{NB}(\boldsymbol{\theta}^\tau)$, where $\tau = \arg\max_t \mathcal{NB}^t$.

Usually, for a large number simulations the OL will be 0 as the optimal treatment on average will also be the optimal treatment for the majority of simulations. This means that the opportunity loss is always positive as either we choose the current optimal treatment or the treatment with a higher utility value for that specific simulation. The EVPI is then defined as the average of the opportunity loss. This measures the average potential losses in utility caused by the simulation specific optimal decision being non-optimal in reality.

If the probability of cost-effectiveness is low then more simulations will give a non-zero opportunity loss and consequently the EVPI will be higher. This means that if the probability of cost-effectiveness is very high, it is unlikely that more information would be worthwhile, as the most cost-effective treatment is already evident. However, the EVPI gives additional information over the EVPI as it takes into account the opportunity lost as well as simply the probability of cost-effectiveness.

For example, there may be a setting where the probability of cost-effectiveness is low, so the decision maker believes that decision uncertainty is important. However, this is simply because the two treatments are very similar in both costs and effectiveness. In this case the OL will be low as the utilities will be similar for both treatments for all simulations. Therefore, the cost of making the incorrect decision is very low. This will be reflected in the EVPI but not in the CEAC and implies that the optimal treatment can be chosen with little financial risk, even with a low probability of cost-effectiveness.

```
evi.plot(m)
```

Expected Value of Information
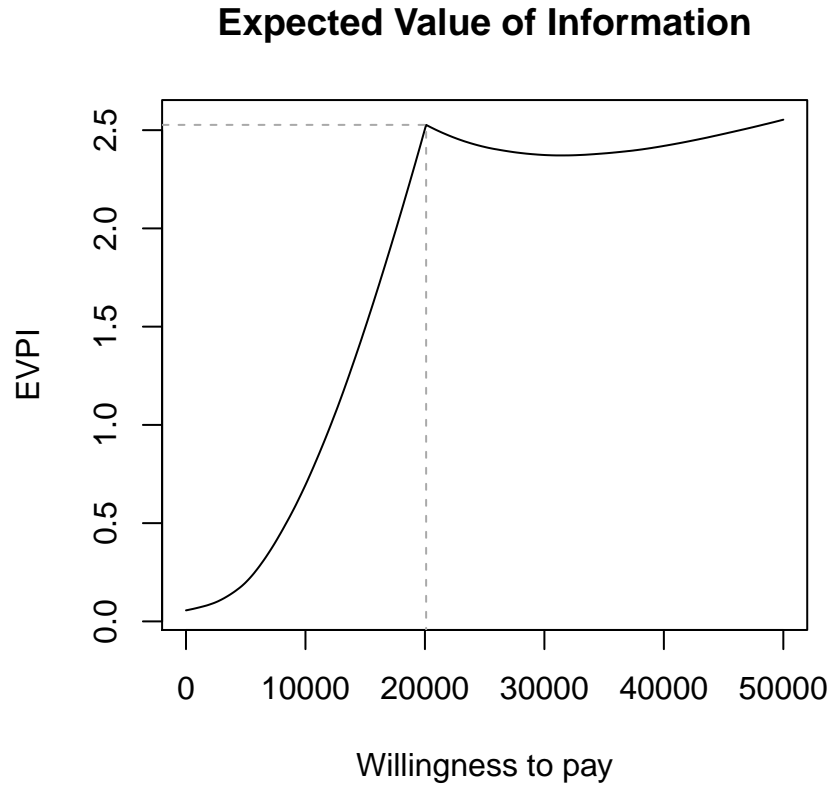
Info-rank plot

Another way in which the analysis of the value of information (specifically based on the Expected Value of Perfect *Partial* Information, EVPPI) can be used is to provide an 'overall' assessment of the impact of each single parameter on the decision uncertainty. To this aim, BCEA has a specialised function that produces a plot of the univariate EVPPI for all the parameters of interest (as specified by the user). While this is not ideal, since correlation among parameters and model structure does have an impact on the joint value of the

EVPPI (which is not a linear combination of the individual EVPPIs!), the Info-rank plot with all the model parameters ranked can be used as a sort of *Tornado diagram*, a tool often used in deterministic sensitivity analysis.

For each parameter and value of the willingness-to-pay threshold k, a barchart is plotted to describe the ratio of EVPPI (specific to that parameter) to EVPI. This represents the relative 'importance' of each parameter in terms of the expected value of information.

```r
# Uses the BCEA function 'CreateInputs' to pre-process the PSA runs and obtain a suitable format
mat=CreateInputs(psa_sims)
```

```
 [1] 14 15 16 17 18 19 20 21 22 29 44 45 46 47
[1] "Linear dependence: removing column pi[2,2]"
 [1] 14 15 16 17 18 19 20 21 22 29 44 45
[1] "Linear dependence: removing column pi[2,1]"
 [1] 14 15 16 17 18 19 20 21 22 29 44
[1] "Linear dependence: removing column pi[1,1]"
[1] 14 15 16 17 18 19 20 21 22
[1] "Linear dependence: removing column Repeat.GP[2,2]"
[1] 14 15 17 18 20 21
[1] "Linear dependence: removing column Repeat.GP[2,1]"
[1] 14 17 20
[1] "Linear dependence: removing column Repeat.GP[1,1]"
```

```r
IR=info.rank(1:ncol(mat$mat),mat$mat,he=m,wtp=wtp)
```

Info−rank plot for willingness to pay=20100
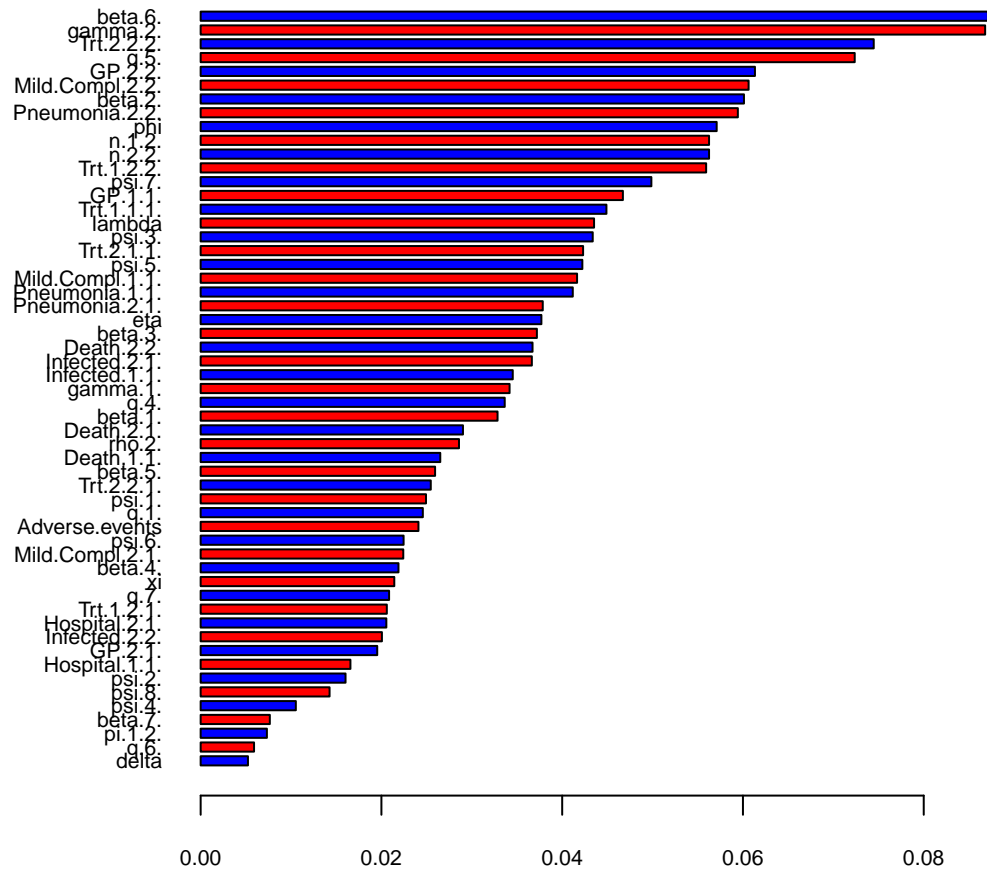
Proportion of total EVPI

```
if(show.tab){IR$rank}
```

```
        parameter          info
1          beta.6.  0.087099250
2          gamma.2.  0.086793906
3        Trt.2.2.2.  0.074466654
4              q.5.  0.072364451
5           GP.2.2.  0.061326394
6   Mild.Compl.2.2.  0.060624120
7           beta.2.  0.060111463
8     Pneumonia.2.2.  0.059435327
9               phi  0.057091505
10            n.1.2.  0.056248723
11            n.2.2.  0.056248723
12        Trt.1.2.2.  0.055926540
13            psi.7.  0.049868025
14           GP.1.1.  0.046715089
15        Trt.1.1.1.  0.044894257
16            lambda  0.043525017
17            psi.3.  0.043378661
```

```
18       Trt.2.1.1. 0.042313521
19          psi.5. 0.042229569
20 Mild.Compl.1.1. 0.041647637
21  Pneumonia.1.1. 0.041172165
22  Pneumonia.2.1. 0.037848812
23             eta 0.037698226
24          beta.3. 0.037201514
25       Death.2.2. 0.036719833
26   Infected.2.1. 0.036643162
27   Infected.1.1. 0.034530407
28         gamma.1. 0.034177981
29             q.4. 0.033641336
30          beta.1. 0.032849489
31       Death.2.1. 0.029021706
32           rho.2. 0.028580813
33       Death.1.1. 0.026510651
34          beta.5. 0.025937290
35       Trt.2.2.1. 0.025459364
36           psi.1. 0.024932309
37             q.1. 0.024582008
38  Adverse.events 0.024097477
39           psi.6. 0.022452561
40 Mild.Compl.2.1. 0.022417051
41          beta.4. 0.021887814
42              xi 0.021424577
43             q.7. 0.020849552
44       Trt.1.2.1. 0.020598011
45    Hospital.2.1. 0.020543716
46   Infected.2.2. 0.020054423
47          GP.2.1. 0.019535538
48    Hospital.1.1. 0.016571473
49           psi.2. 0.016030287
50           psi.8. 0.014262464
51           psi.4. 0.010530648
52          beta.7. 0.007654661
53           pi.1.2. 0.007327684
54             q.6. 0.005907220
55           delta 0.005235527
```

The graph shows a set of bars quantifying the proportion of the total EVPI associated with each parameter. The larger the bar, the higher the impact of a given parameter on decision uncertainty. As mentioned above, care is needed in giving this graph an 'absolute' interpretation — just because a parameter shows a relatively low position in the Info-rank plot, does not mean that there will be no value in investigating it in conjunction with other parameters.

However, it can be shown that the EVPPI of a set of parameters must be at least as big as the individual EVPPI values. Therefore, parameters with high individual EVPPI will always result in joint parameter subset with high value. But, *nothing* can be said about parameters with small individual EVPPI values especially in decision tree models which are typically multiplicative in the parameters. This means that learning the value of one of these parameters has little value as the other elements remain uncertain. However, learning all the parameters can greatly decrease decision uncertainty and therefore has large value to the decision maker. Nonetheless, the Info-rank plot gives an overview, which is perhaps useful (in conjunction with expert knowledge about the model parameters) to drive the selection of the subset ϕ to be included in the full analysis of the EVPPI.

References

Baio, G, A Berardi, and A Heath. 2017. *Bayesian Cost-Effectiveness Analysis with the R package BCEA*. New York, NY: Springer. https://doi.org/10.1007/978-3-319-55718-2.