# missingHE: A Package to Handle Missing Data in Health Economic Evaluations

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#### Abstract

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### 1. Introduction

A well-known issue in health economic evaluations based on individual-patient data, especially within a randomised controlled trial (RCT) setting, is the presence of missing data in the outcome variables (Faria, Gomes, Epstein, and White 2014). More specifically, patients may be lost to follow-up, questionnaires may be lost or unreturned and responses to individual questionnaire items may be illegible, nonsensical or nonexistent (The National Academies Press 2010).

Removing the unobserved cases (a method usually referred to as Complete Case Analysis, CCA) or replacing a missing observation with a single predicted value (Single Imputation, SI) generally leads to a loss in efficiency and possible serious biases in the parameter estimates (Rubin 1987; Schafer 1997; Molenberghs and Kenward 2007). Nevertheless, many reviews concluded that most applied within-trial cost effectiveness analyses (CEAs) widely use these approaches or are unclear on the methodology used (Wood, White, and Thompson 2004; Noble, Hollingworth, and Tilling 2012; Gabrio, Mason, and Baio 2017). As a result, it can be difficult to understand the assumptions underpinning these analyses as well as to use their findings in subsequent research or in resource allocation decisions.

A more flexible missing data method is multiple imputation (MI; Rubin 1987), which has become extremely popular in clinical studies (Carpenter and Kenward 2013). In a nutshell, MI proceeds by replacing each missing data point with a value simulated from a suitable model M complete (i.e. without missing data) replicates of the original dataset are thus created, each of which is then analysed separately using standard methods. The individual estimates are pooled together using meta-analytic tools such as *Rubin's rules*, to reflect the inherent uncertainty in imputing the missing values. As a consequence of the separation between the imputation and the analysis steps, MI MI requires the property of *congeniality*, i.e. the imputation model needs to be specified as equally or less restrictive than the analysis model (Van Buuren 2012).

Additionally, in many applications, MI is based upon a missing at random (MAR) mechanism, which implies the assumption that the observed data can explain fully the reason for why some observations are missing. However, this may not be reasonable in practice (e.g. for self-

reported questionnaire data) and it is important to explore whether the resulting inferences are robust to a range of plausible *missing not at random* (MNAR) mechanisms, which cannot be explained fully by observed data only. Neither MAR nor MNAR assumptions can be tested using the available data alone and thus it is crucial to perform *sensitivity analysis* (SA) to explore how variations in assumptions about the missing values impact the results (Carpenter, Kenward, and White 2007).

The problem associated with the missing values in economic evaluations is often coupled with the fact that resource use and health related quality of life data, e.g. quality-adjusted life years (QALYs), are generally affected by different types of idiosyncrasies (e.g. skewness, spikes at the boundary) that may bias estimates from standard regression models (Rascati, Smith, and Neilands 2001; SG. Thompson and Nixon 2005; Basu and Manca 2012). Simplifying assumptions often (implicitly) made in routine analyses are: 1) normality for the underlying cost and effectiveness data, 2) independence between the outcomes and 3) failure to adjust for some potentially relevant baseline variables (O'Hagan and Stevens 2001; Manca, Hawkins, and Sculpher 2005; Vazquez Polo, Hernandez, and Lopez-Valcarcel 2005; Van Asselt, van Mastrigt, Dirksen, Arntz, Severens, and Kessels 2009). Different methods have been proposed to handle each of these issues, such as the use of bootstrapping or alternative parametric models (Rascati et al. 2001). However, when a combination of these affects the data, the building of a more complex model that accounts for all of them simultaneously is desirable.

A full Bayesian modelling framework provides a unified framework that allows to jointly tackle the different types of issues discussed above, which in turns produces several advantages in comparison to a frequentist counterpart, specifically in health care technology assessments (Spiegelhalter, Abrams, and Myles 2004; Baio 2012). Among these, the Bayesian approach naturally allows for the principled incorporation of external evidence (e.g. expert opinions) through the use of prior distributions. This is often crucial for conducting sensitivity analysis to a plausible range of missingness assumptions including MNAR (Daniels and Hogan 2008), particularly when the evidence produced by the current study is limited, as is the case of small pilot trials, whose objective is to aid decision making about larger investments.

The often-quoted objection to Bayesian modelling, i.e. that it is too computationally intensive in comparison to simpler frequentist counterparts, is likely to dissolve in the presence of extremely complex models, which would require tailor-made routines for the optimisation of non-standard multivariate likelihood functions, thus effectively surrendering their computational advantage over intensive but efficient sampling methods such as Markov chain Monte Carlo (MCMC; Brooks, Gelman, Jones, and Meng 2011).

The objective of this work is to develop a suite of functions and tools for the freely available statistical software R, specifically designed to provide a unified full Bayesian framework that allows to explore alternative plausible missingness assumption scenarios, while simultaneously account for different potential bias sources in CEAs.

## 2. The R package of missingHE

missingHE is a package designed to aid in the process of economic evaluations and costeffectiveness analysis in Health Economics in the presence of missing data in the outcome variables. The modelling perspective used is that of the Bayesian approach, exploiting its natural suitability to assess the intrinsic uncertainty of the missing data and the uncertainty underpinning decision-making problems. In fact, missingHE can be considered a wrapper for some other R packages. The first package, R2jags (Su and Yajima 2015), allows to interface R with JAGS (Plummer 2010), a program for simulation from Bayesian hierarchical models using MCMC methods that is based on the BUGS modelling language (Lunn, Jackson, Thomas, and Spiegelhalter 2012). The second, BCEA (Baio, Berardi, and Heath 2016), is used to produce an economic evaluation output from the posterior inference generated via JAGS (Plummer 2010). The package also relies on other packages such as ggplot2 (Wickham and Chang 2016), gridExtra (Auguie and Antonov 2016), ggthemes (Arnold, Daroczi, Werth, Weitzner, Kunst, Auguie, Rudis, and Wickham 2017), mcmcplots (Curtis, Goldin, and Evangelou 2015) and ggmcmc (Marin 2016), mainly for graphics purposes.

## 3. Missing data mechanism

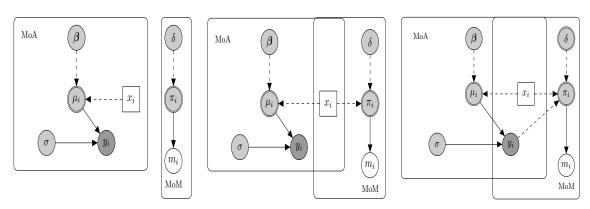
When analysing partially observed data, it is essential to investigate the possible reasons behind missingness. This formally translates into an *assumed* missing data mechanism (Rubin 1987) that is linked to the data generating process, as a key concept to address missingness in a "principled" way. We specifically refer to "principled" methods for missing data as those based on a well-defined statistical model for the complete data, and explicit assumptions about the missing value mechanism.

We consider a sample of i = 1, ..., n individuals and for each the relevant outcome is indicated as  $y_i$ , which is unobserved for some individuals. Typically, trial data also include a set of J covariates  $\mathbf{x}_i = (x_{1i}, ..., x_{iJ})$ , e.g. sex, age or co-morbidities. While in general these may be partially or fully observed, in this section we consider only the latter case. In addition, we define a missingness indicator  $m_i$  taking value 1 if the i-th subject is associated with missing outcome and 0 otherwise.

This setting can be modelled using two sub-models, or "modules". The first module is the missing data mechanism, denoted as Model of Missingness (MoM). It describes a probability distribution for  $m_i$ , as a function of some unobserved parameters  $\pi_i$  and  $\delta$ , defining the probability of missingness in the outcome variable  $y_i$ . The second module is the data generating process of the outcome variable, denoted as Model of Analysis (MoA). This contains the main parameters of interest (e.g. the population average costs and effectiveness) and describes a probability model for the outcome  $y_i$ . As a general example, we can think of a simple regression model where  $y_i \sim \text{Normal}(\mu_i, \sigma)$ , and  $\mu_i = \beta_0 + \beta_1 x_i$ . In this case, the parameters of the MoA are the regression coefficients  $\beta = (\beta_0, \beta_1)$  representing respectively the intercept and the slope, and the individual standard deviation  $\sigma$ .

The most accepted classification of missingness mechanisms is based on three classes (Rubin 1987), which are distinguished according to the way the probability of missingness in the MoM is modelled. A simple graphical representation of the three classes is provided in Figure 1





- (a) Missing completely at random (MCAR)
- (b) Missing at random (MAR)
- (c) Missing not at random (MNAR)

Figure 1: Graphical representation of Rubin's missing data mechanism classes, namely (a) MCAR, (b) MAR and (c) MNAR. Variables and parameters are represented through nodes of different shapes and colours. Parameters are indicated by grey circles with logical parameters defined by double circles, while predictor variables are assumed fixed and drawn as white squares. Fully observed variables are denoted by white circles, partially observed variables by darker grey circles. Nodes are related to each other through dashed and solid arrows which respectively represent logical functions and stochastic dependence. MoA=Model of analysis, MoM=Model of missingness.

The missing data mechanism specifies a probability model for the distribution of  $m_i$  conditional on all other variables, broadly distinguished, according to Rubin's classification, into three classes.

- 1. Figure 1 (a) illustrates the class of Missing completely at random (MCAR), in which the probability of missingness is fully independent of any other partially or fully observed variable. Consequently, the MoA and MoM are not connected and  $\pi_i$  does not depend on any quantity in the MoA. This amounts to assuming that there is no systematic difference between partially and fully observed individuals in terms of the outcome  $y_i$ . In other words, in this case we would be assuming that observed cases are a representative sample of the full sample.
- 2. Figure 1 (b) shows a case of missing at random (MAR), in which the missingness probability may depend on a fully observed variable. As a result, MoA and MoM are connected by means of the predictor variable affecting both the mechanisms generating  $y_i$  and  $m_i$ . Because of this relationship, the partially observed cases are systematically different from the fully observed cases; crucially, however, the difference is fully captured by  $x_i$ .
- 3. Figure 1 (c) provides an example of missing not at random (MNAR). This is characterised by dependence of the probability of missingness on both the partially and fully observed variables. Thus,  $\pi_i$  depends on both the fully observed predictor  $x_i$  and the partially observed outcome  $y_i$ . This means that the difference between fully and partially observed cases still depends on the missing values, even after taking  $x_i$  into account.

Therefore more structured assumptions that go beyond the information contained in the data are required.

Regardless of the setting, it is important to notice that it is never possible to definitively distinguish between MAR and MNAR models. The data alone do not provide all the information necessary to make this choice and, at the same time, different MNAR models can provide identical fits to the observed data. However, they may have quite different implications for the unobserved data, leading to different conclusions (Molenberghs, Fitzmaurice, Kenward, Tsiatis, and Verbeke 2015). Therefore, it becomes crucial to explore the sensitivity of the results with respect to different missing data assumptions and quantify results' uncertainty. What is generally recommended is to set MAR as the reference assumption and then explore different MNAR departures. However, the base-case analysis should be primarily defined according to the available state of knowledge in the given setting.

### 4. Selection models

When informative missingness it thought to be the most realistic scenario, then context-specific MNAR assumptions should be set as the reference case, with suitably-defined departures being explored in sensitivity analysis. For nonignorable/informative models, this is typically implemented through advanced statistical methods, which can explicitly model a MNAR mechanism. In this package we focus on a specific class of these, named selection models (Molenberghs et al. 2015; Daniels and Hogan 2008; Mason, Richardson, Plewis, and Best 2012).

To show how selection models work we consider a simple example. We assume a data set comprising a partially observed response variable y, the corresponding missing data indicator vector m, and a fully-observed covariate x. Under the selection model approach, the joint distribution p(y,m) is factored as the product of the marginal distribution p(y) and the conditional distribution  $p(m \mid y)$ , that is:

$$p(y, m \mid x, \pmb{\theta}^{MoA}, \pmb{\theta}^{MoM}) = p(y \mid x, \pmb{\theta}^{MoA}) p(m \mid y, x, \pmb{\theta}^{MoM})$$

where,  $\boldsymbol{\theta}^{MoA}$ ,  $\boldsymbol{\theta}^{MoM}$  are the set of parameters associated with the MoA and the MoM, respectively. We need to specify the complete data model for the response, so that the probability of nonresponse is modelled conditionally on the possibly unobserved outcomes. The model is identified through the form and priors assumed for the MoM, and the distribution assumed for y in the MoA.

#### 4.1. Model of analysis

In health economic evaluations, the MoA corresponds to a joint model assumed for the effectiveness and cost data. **missingHE** specifies this model within a general Bayesian framework which allows the user to choose among a set of alternative structures for both outcomes.

Assume that some patient-level data are collected from a trial on i = 1, ..., n individuals who are randomly allocated to either a control (t = 1) or intervention (t = 2) group, with sample sizes  $n_1$  and  $n_2$ , respectively. We denote by  $e_{it}$  and  $c_{it}$  the effectiveness and cost outcome variables for the i-th person in group t of the trial. To simplify the notation unless

necessary we suppress the treatment subscript t. In order to account for correlation between the outcomes, in general we can specify the joint distribution p(e,c) using the following factorisation:

$$p(e,c) = p(c)p(e \mid c) = p(e)p(c \mid e)$$

where, for example, p(e) is the marginal distribution of the effectiveness and  $p(c \mid e)$  is the conditional distribution of the costs given the effectiveness. Note that while it is possible to use interchangeably either factorisation, **missingHE** always assumes a marginal for the effectiveness and a conditional for the costs.

Without loss of generality, we can consider for each individual a marginal distribution  $p(e_i \mid \boldsymbol{\theta}_e^{MoA})$ , indexed by a set of parameters  $\boldsymbol{\theta}_e^{MoA}$ , composed by a location  $\phi_{ie}$  and a set of ancillary parameters  $\boldsymbol{\psi}_e$  typically including some measure of marginal variance,  $\sigma_e^2$ . We can model the location parameter using a generalised linear structure, e.g.

$$g_e(\phi_{ie}) = \alpha_0 \ [+\ldots],$$

where  $\alpha_0$  is the intercept and the notation  $[+\ldots]$  indicates that other terms (e.g. quantifying the effect of relevant covariates) may or may not be included in the model. In the absence of covariates or assuming that a centered version  $x_i^* = (x_i - \bar{x})$  is used, the parameter  $\mu_e = g_e^{-1}(\alpha_0)$  represents the population average effectiveness.

As for the costs, we can consider a model  $p(c_i \mid e_i, \boldsymbol{\theta}_c^{MoA})$ , which explicitly depends on the effectiveness variable, as well as on a set of quantities  $\boldsymbol{\theta}_c^{MoA}$ , again comprising of the location and ancillary parameters. Note that in this case  $\psi_c$  includes a *conditional* variance  $\tau_c^2$ , which can be typically expressed as a function of the marginal variance  $\sigma_c^2$  (Nixon and Thompson 2005; Baio 2012). The location can be modelled as a function of the effectiveness variable as:

$$g_c(\phi_{ic}) = \beta_0 \ \beta_f(e_i - \mu_e) \ [+ \ldots],$$

Here,  $(e_i - \mu_e)$  is the centered version of the effectiveness variable, while  $\beta_f$  quantifies the correlation between costs and effectiveness. Assuming other covariates are either also centered or not present at all,  $\mu_c = g_c^{-1}(\beta_0)$  is the population average cost.

Note that missingHE expands any categorical covariates to a set of dummy variables: so if a covariate has four categories, in line with R notation, missingHE considers three binary indicators. Thus the profile (0,0,0) indicates the first (reference) category, while the profiles (1,0,0), (0,1,0) and (0,0,1) indicate the second, third and fourth category, respectively. In missingHE, the total number of covariates depends on this full expansion of the design matrix.

Figure 2 shows a graphical representation of the general modelling framework described above. The effectiveness and cost distributions are represented in terms of combined "modules" — the blue and the red boxes — in which the random quantities are linked trough logical relationships. This ensures the full characterisation of the uncertainty for each variable in the model. Notably, this is general enough as to be extended to any suitable distributional assumption, as well as to handle covariates in either or both the modules.

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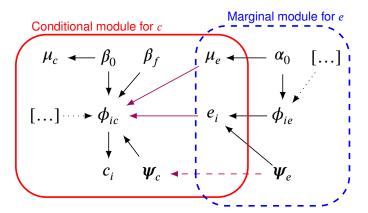


Figure 2: Joint distribution p(e,c), expressed in terms of a marginal distribution for the effectiveness and a conditional distribution for the costs, respectively indicated with a solid red line and a dashed blue line. The parameters indexing the corresponding distributions or "modules" are indicated with different Greek letters, while i denotes the individual index. The solid black and magenta arrows show the dependence relationships between the parameters within and between the two models, respectively. The dashed magenta arrow indicates that the ancillary parameters of the cost model may be expressed as a function of the corresponding effectiveness parameters. The dots enclosed in the square brackets indicate the potential inclusion of other covariates at the mean level for both modules.

Table 1 shows the different types of models for both the effectiveness and costs that are implemented in **missingHE**. In each, by default, minimally informative priors are specified on all the relevant parameters.

MoA	Marginal Mean	Ancillary	Default Priors
Effectiveness			
$e_i \sim \text{Normal}(\phi_{ie}, \sigma_e^2)$	$\mu_e = \alpha_0$	$\sigma_e$	$\alpha \stackrel{iid}{\sim} \text{Normal}(0, 1000)$ $\log \sigma_e \sim \text{Uniform}(-5, 10)$
$e_i \sim \text{Beta}(\phi_{ie}\tau_{ie}, (1 - \phi_{ie})\tau_{ie}))$	$\mu_e = \frac{\exp(\alpha_0)}{1 + \exp(\alpha_0)}$	$\tau_{ie} = \frac{\phi_{ie}(1 - \phi_{ie})}{\sigma_e^2} - 1$	$\boldsymbol{\alpha} \stackrel{iid}{\sim} \text{Normal}(0, 1000)$ $\sigma_e \sim \text{Uniform}(0, \sqrt{\mu_e(1 - \mu_e)})$
Cost			
$c_i \sim \text{Normal}(\phi_{ic}, \sigma_c^2)$	$\mu_c=eta_0$	$\sigma_c$	$oldsymbol{eta} \stackrel{iid}{\sim}  ext{Normal}(0, 1000) \\ \log \sigma_c \sim  ext{Uniform}(-5, 10)$
$c_i \sim \text{Gamma}(\phi_{ic}\tau_{ic}, \tau_{ic})$	$\mu_c = \exp(\beta_0)$	$ au_{ic} = rac{\phi_{ic}}{\sigma_c^2}$	$eta \stackrel{iid}{\sim} \text{Normal}(0, 1000)$ $\sigma_c \sim \text{Uniform}(0, 1000)$
$c_i \sim \text{LogNormal}(\phi_{ic}, \sigma_c^2)$	$\mu_c = \exp(\beta_0 + \frac{\log \sigma_c^2}{2})$	$\sigma_c$	$oldsymbol{eta} \stackrel{iid}{\sim} \operatorname{Normal}(0, 1000) \\ \log \sigma_c \sim \operatorname{Uniform}(-5, 10)$

Table 1: A list of the distributions supported by **missingHE** for the effectiveness  $(e_i)$  and cost  $(c_i)$  variables. The set of logistic regression parameters for  $\phi_{ie}$  and  $\phi_{ic}$  are indicated with  $\alpha = (\alpha_0, \alpha_1, ...)$  and  $\beta = (\beta_0, \beta_1, ...)$ . Notice that JAGS specifies Normal and LogNormal distributions in terms of the precision rather than the variance (precision=1/variance).

For all these distributions, when a joint model for  $e_i$  and  $c_i$  is assumed, the additional parameter  $\beta_f$  indexes the costs model and captures the correlation with the effectiveness. The default prior for this parameter is  $\beta_f \sim \text{Normal}(0, 1000)$ .

### 4.2. Model of missingness

The existence of a bivariate outcome in economic evaluations requires the specification of two different mechanisms when missingness affects both outcomes. Under a selection model, the MoM for the effectiveness  $p(m_{ie} \mid e_i, \boldsymbol{\theta}_e^{MoM})$  and costs  $p(m_{ic} \mid c_i, \boldsymbol{\theta}_c^{MoM})$  are indexed by the two different sets of parameters  $\boldsymbol{\theta}_e^{MoM}$  and  $\boldsymbol{\theta}_c^{MoM}$ . These include the two missingness probabilities  $\pi_{ie}$  and  $\pi_{ic}$ , which inturnare typically expressed as functions of some other parameters.

More specifically, **missingHE** models the two missing value probabilities using logistic regressions:

$$logit(\pi_{ie}) = \gamma_{0e} + \delta_e e_i \ [+ \dots]$$
 and  $logit(\pi_{ic}) = \gamma_{0c} + \delta_c c_i \ [+ \dots]$ 

where  $\gamma_{0e}$  and  $\gamma_{0c}$  are the baseline parameters, while  $\delta_e$  and  $\delta_c$  are the parameters that capture the impact of the unobserved values on the missingness probabilities for the effectiveness and costs on the logit scale, respectively. The possible inclusion of other centered covariates in either or both the MoMs is indicated by the terms  $[+ \dots]$ .

A feature of selection models is that missingness assumptions can be neatly fitted inside the Rubin's categories according to the variables included and form assumed for the MoM. In

particular, the inclusion of the quantities  $\delta_e$  and  $\delta_c$  denotes the existence of a MNAR mechanism for e and c, respectively, as these parameters cannot be identified using the observed data alone; when, instead, they are set to zero, the mechanism becomes MAR (MCAR if no covariate is included in the models).

Table 2 shows how **missingHE** specifies the MoM in the effectiveness and costs under either a MAR or MNAR assumption. By default, minimally informative priors are used on all parameters.

MoM	Mechanism	Marginal Missingness Probability	Default Priors
Effectiveness			
$m_{ie} \sim \text{Bernoullli}(\pi_{ie})$	MAR MNAR	$\bar{\pi}_e = \frac{\exp(\gamma_{0e})}{1 + \exp(\gamma_{0e})}$ $\bar{\pi}_e = \frac{\exp(\gamma_{0e} + \delta_e \bar{e}_i)}{1 + \exp(\gamma_{0e} + \delta_e \bar{e}_i)}$	$\gamma_e \stackrel{iid}{\sim} \text{Normal}(0, 1000)$ $\gamma_e \stackrel{iid}{\sim} \text{Normal}(0, 1000); \ \delta_e \sim \text{Normal}(0, 1)$
Cost			
$m_{ic} \sim \text{Bernoullli}(\pi_{ic})$	MAR	$\bar{\pi_c} = \frac{\exp(\gamma_{0c})}{1 + \exp(\gamma_{0c})}$	$\gamma_c \stackrel{iid}{\sim} \text{Normal}(0, 1000)$
	MNAR	$\bar{\pi_c} = \frac{\exp(\gamma_{0c} + \delta_c \bar{c}_i)}{1 + \exp(\gamma_{0c} + \delta_c \bar{c}_i)}$	$\gamma_c \stackrel{iid}{\sim} \text{Normal}(0, 1000);  \delta_c \sim \text{Normal}(0, 1)$

Table 2: The distributions used by **missingHE** for the missing indicators for the effectiveness  $(m_{ie})$  and cost  $(m_{ic})$  variables. The set of logistic regression parameters for  $\pi_{ie}$  and  $\pi_{ic}$  are indicated with  $\gamma_e = (\delta_e, \gamma_{0e}, \gamma_{1e}, \ldots)$  and  $\gamma_c = (\delta_c, \gamma_{0c}, \gamma_{1c}, \ldots)$ . Notice that JAGS specifies Normal distributions in terms of the precision rather than the variance (precision=1/variance).

Selection models allow to directly model the target distribution of the full data (observed and missing) under MNAR. This has the advantage to straightforwardly formulate assumptions about the nonresponse mechanism. The drawback is how we can translate these assumptions into assumptions on the distribution of the missing data.

Indeed, model identification depends on distributional assumptions in the MoA (often difficult to check) and on the form of the MoM (on which unverifiable assumptions have to be made). SA is an important tool that should always be used in order to handle missingness uncertainty. Specifically, two different types of sensitivity analysis are (Mason *et al.* 2012):

- 1. Assumption sensitivity varies the distribution assumptions in the MoA for  $e_i$  and  $c_i$ .
- 2. Parameter sensitivity varies the prior distributions for  $\delta_e$  and  $\delta_c$  in the MoM. Priors must be chosen according to the available information (e.g. expert opinions) and define a set of plausible missingness assumptions to explore.

After all required SAs have been performed, it is important to examine the results to establish how much the quantities of interest vary. In the event conclusions are not robust we may need to gather more information to better specify the model.

Finally, it is important to stress that any conclusion derived from a nonignorable missing data model must be treated very cautiously. Each model specification makes assumptions about the missing data that can only be formulated using external information, should such information exist. Hence, SA is required to the test the robustness of results to different plausible assumptions.

### 5. Hurdle models

A common type of idiosyncrasy in economic evaluations relates to data showing spikes at one or both of the boundaries of the range for the underlying distribution. For example, some patients in a trial may not accrue any cost at all (i.e.  $c_i = 0$ ), thus invalidating the assumptions for the Gamma distribution, which is defined on the range  $(0, +\infty)$ . Similarly, we may observe individuals who are associated with perfect health, i.e. unit QALY (Basu and Manca 2012), which makes it difficult to use a Beta distribution, defined on the open interval (0, 1).

A simple solution is to add/subtract a small constant  $\epsilon$  to the entire set of observed values for the cost/effectiveness variable, thus artificially re-scaling it in the desired interval (Cooper, Sutton, Mugford, and Abrams 2003). Despite being very easy to implement, this strategy is potentially problematic as the results are likely to be strongly affected by the actual choice of the scaling parameter  $\epsilon$  and no clear guideline exists about the value to use (e.g. 0.1, 0.01, ...). In addition, when the proportion of these values is substantial, they may induce high skewness in the data and the application of simple methods may lead to biased inferences (Mihaylova, Briggs, O'Hagan, and Thompson 2011). A more efficient solution suggested to handle this issue is the application of hurdle models (Ntzoufras 2009; Baio 2014).

These are mixture models defined by two components: the first one is a mass distribution at the spike, while the second is a parametric model applied to the natural range of the relevant variable. Usually, a logistic regression is used to estimate the probability of incurring a *structural* value (e.g. 0 for the costs, or 1 for the QALYs); this is then used to weigh the mean of the *non-structural* values estimated in the second component. Hurdle models have been discussed and applied in CEA mainly for handling structural zero costs (Tooze, Grunwald, and Jones 2002; Harkanen, Maljanen, Lindfors, Virtala, and Knekt 2013; Baio 2014).

Within the **missingHE** framework for the MoA shown in Figure 2, we can extend all the models described in Table 1 to a hurdle version for both outcome variables. Specifically, for each subject in the trial i = 1, ..., n we define two indicator variables  $d_{ie}$  and  $d_{ic}$  taking value 1 if the i-th individual is associated with a structural value in the effectiveness  $(e_i = se)$  and costs  $(c_i = sc)$ , respectively, and 0 otherwise. This is then modelled as

$$d_{ie} := \mathbb{I}(e_i = 1) \sim \text{Bernoulli}(\pi_{ie}) \text{ and } d_{ic} := \mathbb{I}(c_i = 1) \sim \text{Bernoulli}(\pi_{ic})$$
  
$$\log \operatorname{id}(\pi_{ie}) = \gamma_{0e} \ [+ \dots] \text{ and } \log \operatorname{id}(\pi_{ic}) = \gamma_{0c} \ [+ \dots],$$

where  $\pi_{ie}$  and  $\pi_{ic}$  are the individual probabilities of a structural value in the effectiveness and costs, which are estimated on the logit scale as a function of some baseline parameters  $\gamma_{0e}$  and  $\gamma_{0c}$ . Other centered covariates ([+...]) can be additively included in the model of  $d_{ie}$  and  $d_{ic}$ . Within this framework, the quantities

$$\bar{\pi}_e = \frac{\exp(\gamma_{0e})}{1 + \exp(\gamma_{0e})}$$
 and  $\bar{\pi}_c = \frac{\exp(\gamma_{0c})}{1 + \exp(\gamma_{0c})}$ 

represents the estimated marginal probability of structural  $e_i$  and  $c_i$ . The parameters  $\bar{\pi}_e$  and  $\bar{\pi}_c$  in effect represent the weights used to mix the two components.

To make a parallel with the missing data literature, when no covariates are included in the models of  $\pi_{ie}$  and  $\pi_{ic}$ , these probabilities are randomly predicted and describe what we call

a structural completely at random (SCAR) mechanism, in which the chance of observing an individual associated with structural value does not depend on any other variable. When, instead, some relevant covariates are included and they contribute to estimate the probabilities, we have a structural at random (SAR) mechanism.

Table 3 shows how **missingHE** specifies the structural value mechanism in the effectiveness and costs under either a SCAR or SAR assumption. By default, minimally informative priors are used on all parameters.

Model	Mechanism	Marginal Structural Value Probability	Default Priors	
Effectiveness				
$d_{ie} \sim \text{Bernoullli}(\pi_{ie})$	SCAR SAR	$\bar{\pi_e} = \frac{\exp(\gamma_{0e})}{1 + \exp(\gamma_{0e})}$	$\gamma_{0e} \sim \text{Normal}(0, 1000)$ $\gamma_e \stackrel{iid}{\sim} \text{Normal}(0, 1000)$	
Cost				
$d_{ic} \sim \text{Bernoullli}(\pi_{ic})$	SCAR	$ar{\pi}_c = rac{\exp(\gamma_{0c})}{1+\exp(\gamma_{0c})}$	$\gamma_{0c} \sim \text{Normal}(0, 1000)$	
	SAR	$+\exp(\gamma_{0c})$	$\gamma_c \stackrel{iid}{\sim} \text{Normal}(0, 1000)$	

Table 3: The distributions used by **missingHE** for the structural value indicators for the effectiveness  $(d_{ie})$  and cost  $(d_{ic})$  variables. The set of logistic regression parameters for  $\pi_{ie}$  and  $\pi_{ic}$  are indicated with  $\gamma_e = (\gamma_{0e}, \gamma_{1e}, ...)$  and  $\gamma_c = (\gamma_{0c}, \gamma_{1c}, ...)$ . Notice that JAGS specifies Normal distributions in terms of the precision rather than the variance (precision=1/variance).

Depending on the value of  $d_{ie}$  and  $d_{ic}$ , we can effectively partition the observed data into two sets: structural and non-structural.

- 1. The first one is made by the  $n^{se}$  subjects for whom  $d_{ie} = 1$  and the  $n^{sc}$  subjects for whom  $d_{ic} = 1$ . For these individuals we define the variables  $e_i^{se} = se$  and  $e_i^{sc} = sc$ , where se and sc denote the specific structural values.
- 2. The second one is made by the  $n^{-se} = (n n^{se})$  subjects for whom  $d_{ie} = 0$  and the  $n^{-sc} = (n n^{sc})$  subjects for whom  $d_{ic} = 0$ . For these individuals we define the variables  $e_i^{-se}$  and  $c_i^{-sc}$ .

We can model the non-structural component using a distribution characterised by overall means  $\mu_e^{-se}$  and  $\mu_c^{-se}$ . For example, among the distributions available in **missingHE**, when we observe the structural values se=1 and sc=0, we can directly apply the Beta for the effectiveness and the Gamma for the costs. The parameterisation and priors assigned are exactly the same of those in Table 1, except the fact that they now apply to the non-structural components only.

Finally, using the estimated value for  $\bar{\pi}_e$  and  $\bar{\pi}_c$ , we can compute the overall population average effectiveness and cost measures in both treatment groups  $\mu_{et}$  and  $\mu_{ct}$  as the linear combinations

$$\mu_{et} = (1 - \bar{\pi}_{et})\mu_{et}^{-se} + \bar{\pi}_{et}se$$
 and  $\mu_{ct} = (1 - \bar{\pi}_{ct})\mu_{ct}^{-sc} + \bar{\pi}_{ct}sc$ 

## 5.1. Hurdle models and missingness

Hurdle models can be easily framed to handle missingness under different assumptions. More specifically, if outcome data are unobserved then also the structural value indicators  $d_{ie}$  and  $d_{ic}$  cannot be directly computed. In general, these will be typically imputed based on the available information in the model. This information may come either from the observed data or from informative priors and may be associated with different types of MoM structures.

Under MAR, no information other than that contained in the observed data is used to impute the missing values, both in the structural and non-structural components. Under MNAR, Hurdle models offer a convenient framework to explore the robustness of the results to some pluasible scenarios and therefore allow to perform a simple type of sensitivity analysis to the missingness assumptions. More specifically, it is possible to arbitrarily set the unobserved values in  $d_{ie}$  and  $d_{ic}$  to either 1 or 0, using different configurations, i.e. vary the number of structural values potentially observed in a given scenario, and assess the results across them.

This corresponds to assessing the impact on the inferences of alternative missingness assumptions. Since these configurations are based on assumptions that cannot be verified from the data at hand (but are in fact arbitrarily set by the experimenter), they effectively represent a way to assess the robustness of the results to some MNAR departures.

Even though this approach associates the missing data with specific MNAR values (structural values), it has the advantage of being easy to implement and offers a starting point to investigate MNAR more thoroughly. Specifically, if one of these scenarios is thought to be more realistic, then it can be explored by means of methods that explicitly account for variability in the MNAR values, e.g. selection models.

## 6. Example

We use a running example to show how selection models and hurdle models can be specified in **missingHE**. Suppose that the user has a suitable dataset, perhaps obtained from a trial, in which data for each individual are recorded for the effectiveness and cost variables as well as for an arm indicator specifying whether the individual to whom the data refer belongs in the control or the active treatment arm of the trial. Of course, other variables may be observed, e.g. relevant covariates, such as sex, age or co-morbidity. Both outcome variables can have missing values while no unobserved values is allowed for the covariates as **missingHE** can only deal with missingness in the outcomes.

Assume that the data are available in the R workspace as a data-frame (say, data) that can be visualised using, for example, histogram plots

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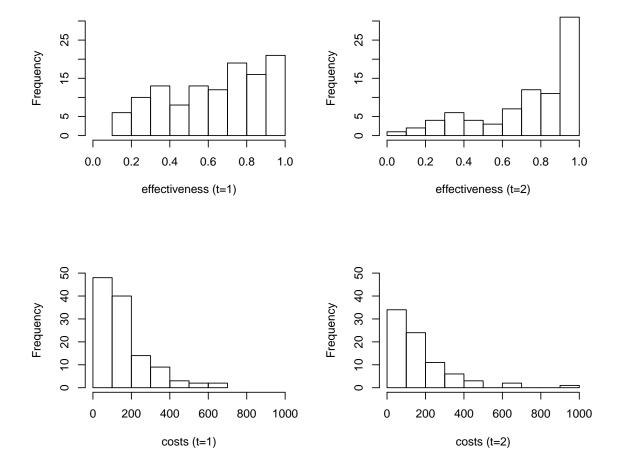


Figure 3: Histograms of the observed data distributions for the effectiveness and costs in the control (t=1) and intervention (t=2) arms

Figure 3 shows the histograms for the observed data distributions. The dataset consists of 250 individuals in total, grouped in two arms (here arm 1 indicates the control and arm 2 indicates the active treatment). 51 individuals have unobserved outcome data (32 in the control and 19 in the intervention), and 24 individuals show structural values in both the effectiveness (1) and costs (0).

### 6.1. Selection models in missingHE

Selection models are implemented in **missingHE** using the Bayesian software program JAGS, which is called from the R package **R2jags**. The program is based on the BUGS language and performs Bayesian inference using the Gibbs sampling as a specific type of MCMC algorithm. To illustrate how **missingHE** interfaces with these programs we first load the package using the command

### R> require(missingHE)

Then we specify a joint bivariate Normal MoA distribution to the effectiveness and cost variables in the dataset data. With respect to the MoM, we assume a MNAR structure for the effectiveness while we keep a MAR assumption for the costs in both treatment arms. In missingHE we can implement the model using the selection function:

where the different arguments of the function have the following interpretations:

- 1. data must contain the data to analyse, specified in a data frame format
- 2. dist\_e and dist\_c indicate the assumed effectiveness and cost MoA distributions, specified as character names among a set of pre-defined choices. Available choices are: Normal ("norm") for both outcomes, Beta ("beta") for the effectiveness and Gamma ("gamma") or LogNormal ("lnorm") for the costs.
- 3. model.eff and model.cost are formulas that specify which variables should be included in the effectiveness and cost models as covariates (among those available in data). A joint bivariate distribution can be assumed by placing e on the right-hand side of the formula for the costs. By default both formulas do not contain any covariate (indicated with 1) and assume independence between the outcomes.
- 4. model.me and model.mc are formulas that specify which variables should be included in the effectiveness and cost missingness models as covariates (among those available in data). It is possible to specify a MNAR mechanism by placing e and c in the formulas for the missing effectiveness and cost models, respectively. By default no covariate is included (indicated with 1), implicitly assuming a MAR mechanism.
- 5. type specifies the type of mechanism to be assumed, either MAR or MNAR, respectively indicated by the character values "MAR" and "MNAR".
- 6. n.iter specifies the number of iterations in each chain of the MCMC algorithm.
- 7. **prior** specifies the prior distribtions to be used for the parameters of the model, by default those shown in Table 1 and Table 2. These priors can be overwritten by the user who may desire to change them. In this case, the new hyperpriors for each parameter in the model can be provided by creating a list object that contains the new values.
- 8. Other additional arguments that may be provided are: the burnin period to be discarded (n.burnin), the number of the chains (n.chains), the thinning interval (n.thin), the initialised values for the parameters in each chain (inits), the upper and lower bounds of the credible intervals for describing the uncertainty around the imputed values (prob) and whether the model text file should be saved in the current working directory (save\_model).

missingHE allows to provide user-specific priors for all parameters in the model. For example, in the model contained in model.sel, the priors for the parameters  $\alpha_0$  and  $\delta_e$  can be defined as follows:

```
R> myprior <- list("alpha0.prior" = c(0, 0.00001), "delta.prior.e" = c(1, 1))
```

The list object myprior can then be supplied to the argument prior in the function selection. It is necessary that specific character names are used to indicate for which parameter the prior should be overwritten. A list of the character names to be used by type of model and parameter can be accessed by typing help(selection).

The results of the model specified are stored in object model.sel. The usual R command

```
R> names(model.sel)
```

returns the names of the elements in the list

The objects data\_set, model\_output and cea are themselves lists that contain different elements related to the data provided, the model results and the economic analysis, respectively. For example, the elements in the first object can be accessed using the standard R notation model.sel\$data\_set[] (i.e. using double square brackets) and can be inspected by typing the command

```
R> names(model.sel$data_set[])
    [1] "effects"
##
                                        "costs"
##
    [3] "N in reference arm"
                                        "N in comparator arm"
##
    [5] "N observed in reference arm"
                                        "N observed in comparator arm"
    [7] "N missing in reference arm"
                                         "N missing in comparator arm"
##
    [9] "covariates_effects"
                                        "covariates_costs"
## [11] "covariates_missing_effects"
                                        "missing_effects"
   [13] "covariates_missing_costs"
                                        "missing_costs"
```

These are merely related to the data provided as inputs to the function selection, such as effectiveness and cost data, total number of individuals in each arm, number of observed and unobserved individuals and covariate data (if included in the model). The other elements in the object model.sel are

- 1. "model\_output" is a list storing the output of the JAGS model. Depending on the type of model, the results shown in this list can vary as they contain the posterior samples of the parameters of interest based on the MoA-MoM structure assumed. In the list a summary of the posterior estimates of the JAGS model is also available, taken directly from the output of the function jags in the package R2jags.
- "cea" is another list that stores the output of the economic evaluation based on the
  posterior samples of the marginal mean effectiveness and cost parameters, obtained using the function bcea in the package BCEA. This object can be analysed using tailored

functions of **BCEA** to visually represent standard CEA outputs such as the cost effectiveness plane (CEP; Black 1990) and the cost effectiveness acceptability curve (CEAC; Van Hout, Al, Gordon, Rutten, and Kuntz 1994).

3. "type" is a character name that reports the type of missingness mechanism assumed by the model.

Model results can be shown using the **print** function which returns the table related to the posterior estimates of the parameters in the model.

```
R> print(x = model.sel, value.mis = FALSE)
##
                              sd
                                     2.5%
                                              97.5% Rhat n.eff
                    mean
## alpha[1]
                  0.633
                          0.028
                                    0.577
                                              0.688
                                                            3800
## alpha[2]
                          0.032
                                              0.800
                  0.737
                                    0.673
                                                        1 10000
## beta[1]
                147.593 12.473
                                  122.784
                                            171.954
                                                        1 10000
## beta[2]
                154.011 18.669
                                  117.305
                                            190.638
                                                        1 10000
## beta_f[1]
                -39.905 26.700
                                  -91.975
                                             13.313
                                                            3300
                                                        1
## beta_f[2]
                 -1.777 28.884
                                  -59.506
                                             54.533
                                                        1 10000
## delta_e[1]
                 -0.338
                          0.964
                                   -2.201
                                               1.619
                                                            1800
## delta_e[2]
                 -0.381
                          0.885
                                   -2.078
                                               1.438
                                                        1
                                                            2800
## deviance
               3089.837
                          6.413 3077.766 3103.375
                                                        1 10000
## gamma_c[1]
                 -1.291
                                   -1.683
                                             -0.912
                                                            1200
                          0.197
                                                        1
   gamma_c[2]
                 -1.434
                          0.250
                                   -1.950
                                             -0.974
                                                            1400
                                                        1
## gamma_e[1]
                 -1.114
                          0.624
                                   -2.489
                                             -0.003
                                                        1
                                                            2300
## gamma_e[2]
                 -1.189
                          0.671
                                   -2.663
                                              0.005
                                                        1
                                                            1600
## mu_c[1]
                147.593 12.473
                                  122.784
                                            171.954
                                                        1 10000
## mu_c[2]
                154.011 18.669
                                  117.305
                                            190.638
                                                        1 10000
## mu_e[1]
                  0.633
                          0.028
                                    0.577
                                              0.688
                                                        1
                                                            3800
## mu_e[2]
                  0.737
                          0.032
                                    0.673
                                              0.800
                                                        1 10000
## p_c[1]
                  0.218
                          0.033
                                    0.157
                                              0.287
                                                        1
                                                            1200
## p_c[2]
                  0.195
                          0.039
                                    0.125
                                              0.274
                                                            1400
## p_e[1]
                  0.214
                                              0.281
                          0.033
                                    0.152
                                                        1 10000
## p_e[2]
                  0.192
                          0.039
                                    0.121
                                              0.275
                                                        1
                                                            4800
## s_c[1]
                134.834
                          8.832
                                  118.963
                                            153.326
                                                            8600
                                                        1
## s_c[2]
                171.385 13.895
                                  146.689
                                            200.962
                                                        1
                                                             480
## s_e[1]
                  0.259
                                               0.296
                          0.017
                                    0.228
                                                        1 10000
## s_e[2]
                  0.265
                          0.021
                                    0.227
                                               0.311
                                                            1600
```

The optional argument value.mis allows to exclude (FALSE) or include (TRUE) the results associated with the imputed values; by default, these values are omitted from the results displayed.

#### 6.2. Hurdle models in missingHE

To illustrate how it is possible to specify a Hurdle model in **missingHE**, we consider the same dataset **data** and now assume a joint bivariate Beta-Gamma distribution for the effectiveness and cost variables. Individuals associated with a unit effectiveness and zero costs are considered structural values and are handled through a Hurdle appraach.

With respect to the structural value mechanism, we assume a SCAR structure for both outcomes. In **missingHE** we can implement the model using the **hurdle** function:

```
R> model.hur <- hurdle(data = data, dist_e = "beta", dist_c = "gamma",
+ model.eff = e ~ 1, model.cost = c ~ e,
+ model.se = se ~ 1, model.sc = sc ~ 1,se = 1,sc = 0,
+ type = "SCAR", n.iter = 10000, prior = "default", d_e = my.d_e)</pre>
```

Some of the arguments have the same interpretation of those in the function **selection**, but there are some exceptions:

- 1. model.se and model.sc are formulas that specify which variables should be included in the effectiveness and cost structural value models as covariates (among those available in data). By default no covariate is included (indicated with 1), implicitly assuming a SCAR mechanism.
- 2. type specifies the type of mechanism to be assumed, either SCAR or SAR, respectively indicated by the character values "SCAR" and "SAR".
- 3. se and sc define which values in the effectiveness and cost data should be treated as structural by the model. If structural values are observed only for one outcome it is possible to set either se = NULL or sc = NULL. In this case, no hurdle model is assumed for that outcome, which is directly modelled using the distribution specified in dist\_e or dist\_c.
- 4. prior specifies the prior distributions to be used for the parameters of the model, by default those shown in Table 1 and Table 3. These priors can be overwritten in a similar way to the selection function. A list of the character names to be used to change the priors on the model parameters can be accessed by typing help(hurdle).
- 5. d\_e and d\_c (optional) specify the vectors of structural value indicators to be used in the model for the effectiveness and costs. If not provided, missingHE internally computes these vectors based on the observed cases (NA if the cases are missing). When provided, the argument of d\_e and d\_c must be vectors of length equal to the number of rows in data, and should take value 1 or 0 to respectively associate each case with the structural or non-structural component in the hurdle model.

For example, we can define a new variable  $my.d_e$  to specify a scenario where all the 51 missing individuals in data are associated with a structural one in  $e_i$ . This variable is obtained by first computing the usual indicator based on the observed data and then by setting all its missing values to 1:

```
R> my.d_e <- ifelse(data$e == 1, 1, 0)
R> my.d_e[is.na(data$e$) == TRUE] <- 1
```

Once the new variable my.d\_e is passed to the argument d\_e in the function hurdle, then missingHE automatically uses it as the new indicator variable in the model.

Similarly to the selection function, it is possible to access the names of the elements in the list model.hur by typing names(model.hur). Each of these elements is itself a list which contains objects with similar interpretations to those of the selection function.

Model results can be shown again using the print function.

R>	print(mode	l.hur, val	lue.mis	= FALSE)			
##		mean	sd	2.5%	97.5%	Rhat	n.eff
##	alpha[1]	0.363	0.093	0.176	0.543	1	10000
##	alpha[2]	0.842	0.138	0.570	1.111	1	10000
##	beta[1]	5.094	0.088	4.925	5.267	1	1000
##	beta[2]	5.233	0.106	5.026	5.445	1	2100
##	beta_f[1]	-0.312	0.232	-0.760	0.154	1	10000
##	beta_f[2]	0.209	0.255	-0.264	0.739	1	10000
##	deviance	7703.194	5.270	7694.839	7715.110	1	10000
##	gamma_c[1]	-1.978	0.283	-2.564	-1.444	1	5000
##	gamma_c[2]	-1.919	0.327	-2.600	-1.309	1	10000
##	gamma_e[1]	-0.814	0.175	-1.165	-0.481	1	10000
##	gamma_e[2]	-0.886	0.220	-1.332	-0.461	1	1200
##	mu_c[1]	143.241	13.643	118.645	172.289	1	1700
##	mu_c[2]	163.483	18.714	129.735	203.254	1	4200
##	mu_e[1]	0.716	0.022	0.672	0.757	1	10000
##	mu_e[2]	0.787	0.025	0.736	0.832	1	2700
##	p_c[1]	0.125	0.030	0.071	0.191	1	4900
##	p_c[2]	0.132	0.037	0.069	0.213	1	10000
##	p_e[1]	0.308	0.037	0.238	0.382	1	10000
##	p_e[2]	0.294	0.045	0.209	0.387	1	1100
##	s_c[1]	139.018	14.261	114.614	171.085	1	2000
##	s_c[2]	167.732	22.138	130.709	217.767	1	4200
##	s_e[1]	0.227	0.011	0.206	0.250	1	1600
##	s_e[2]	0.252	0.017	0.220	0.286	1	10000

## 7. Diagnostic checks

As with any MCMC estimation, it is important to thoroughly assess convergence. The function diagnostic in missingHE allows to visualise the model output and assess convergence for each parameter in the model. Different diagnostic tools and plots are taken from the package ggmcmc and mcmcplots and are displayed using functions from ggplot2 according to the inputs provided by the user. For simplicity, we consider only the model output generated in model.hur for the current example, but similar considerations apply to any model generated through the functions hurdle or selection.

We can visually represent via histograms the posterior samples for the mean effectiveness parameters in the two arms using the command:

which displays the histograms in Figure 4.

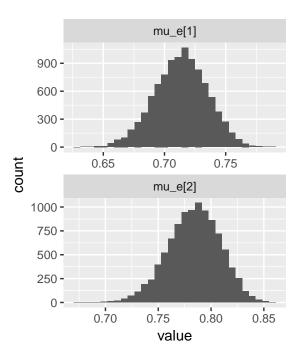


Figure 4: Histograms of the posterior distributions for the mean effectiveness parameters in the two arms

The arguments of the function diagnostic are the followings:

- 1. x is an object of class "missingHE".
- 2. type specifies which type of diagnostic tools to use for assessing convergence. If type = "summary", a summary of some of the most important diagnostic plots for the family of parameters indicated in param is displayed. A variety of plots are available using specific character names, such as histograms ("histogram"), density plots ("denplot"), traceplots ("traceplot"), autocorrelation plots ("acf"), etc. The full list of all available types of diagnostics can be accessed by typing help(diagnostic).
- 3. param specifies for which family of parameters the diagnostic output should be displayed. It must correspond to a character name among a set of pre-defined choices. For example, the mean effectiveness and cost parameters can be accessed via the expressions "mu.e" and "mu.c", respectively. The parameters that are available vary according to the type of model implemented (either Selection or Hurdle models) and the assumptions of the model (MAR/MNAR or SCAR/SAR). The list of all parameters that can be specified with the corresponding character names can be accessed by typing help(diagnostic). By default, all model parameters are selected using the character name "all".

4. theme modifies the pre-defined background theme of the plots generated. Pre-defined themes are taken from the package **ggthemes** and must be indicated with corresponding character names. For a full list of available themes type help(diagnostic).

It is also possible to combine multiple graphs on different parameters generated through the function diagnostic and saved in corresponding R objects. We can then combine these plots into a single one using the function grid.arrange from the gridExtra package (that should be loaded). For example, Figure 7 combines the density and trace plots for the mean effectiveness parameters from model.hur.

```
R> require(gridExtra)
R> dens_eff <- diagnostic(x = model.hur, type = "denplot", param = "mu.e")
R> trace_eff <- diagnostic(x = model.hur, type = "traceplot", param = "mu.e")
R> grid.arrange(dens_eff$plot, trace_eff$plot, ncol = 2)
```

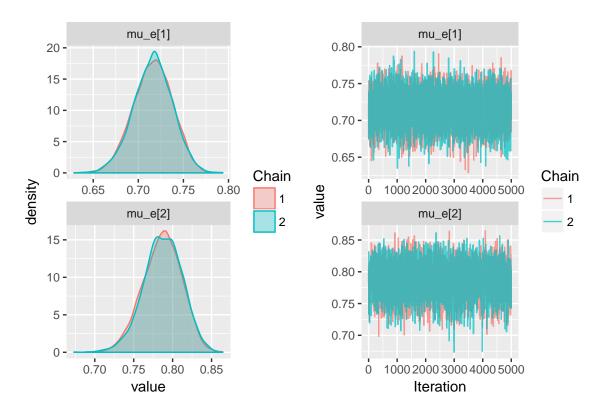


Figure 5: Density and trace plots of the posterior distribution of the mean effectiveness in the two arms

## 8. Missing data plots

Once the model has been estimated, we can visually inspect how missing data in the outcome variables are imputed and compare them to the observed data. **misisngHE** has a specialised function **plot** that can do this, by typing:

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R> plot(x = model.hur, class = "scatter", outcome = "all", theme = "base")

which displays the graphs in Figure 6

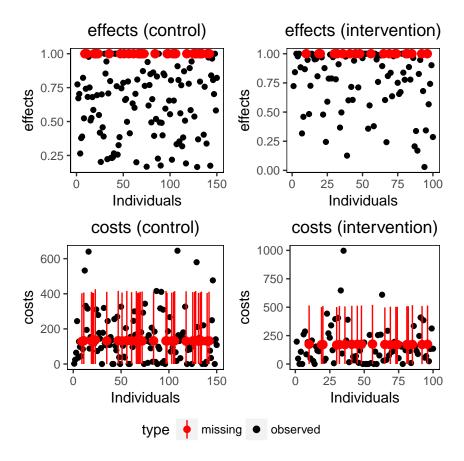


Figure 6: Scatter plots of the observed (black dots) and imputed (red dots and lines) values for both outcomes in the control and intervention groups. Imputations uncertainty is represented in terms of posterior means and 95% credible intervals.

The only compulsory argument to be provided is x, which must be a "missingHE" object. All other arguments are optional and are mainly related to the type of plot to be shown, which outcome and treatment group to consider, and other graphics parameters. These are:

- 1. class specifies the type of plot to be displayed. Two alternative character names are available: "histogram" or "scatter". In the former, the observed and imputed data distributions are compared with a histogram plot and associate them with different colours. In the latter, the observed and imputed values (evaluated at the posterior means) are shown in a scatter plot, with imputed data that are also associated with lines representing their posterior credible intervals. By default these are the 95% CI but they can also be modified by changing the values for the upper and lower bounds using the prob argument in the function selection or hurdle.
- 2. outcome specifies for which variable, either effectiveness, costs or both, and for which

treatment group, either control, intervention or both, results should be visualised. For example, the plots for the effectiveness in both groups can be shown using the character name "effects", while the plots by arm can be accessed using the name "arm1" (control) or "arm2" (intervention). By default all plots are displayed using the character name "all".

3. theme modifies the graphical output according to some pre-specified themes similarly to what shown for the function diagnostic.

### 9. Economic evaluation

Results from the economic evaluation performed using **missingHE** can be summarised in a tabular form using the function **summary** by typing:

```
R> summary <- summary(model.hur)</pre>
```

which returns the following table:

```
##
##
    Cost-effectiveness analysis summary
##
    Comparator intervention: intervention 1
##
    Reference intervention: intervention 2
##
##
##
    Parameter estimates under SCAR assumption
##
##
    Comparator intervention
##
                             sd
                                     LB
                                              UB
                   mean
## mean effects
                  0.716 0.022
                                  0.679
                                           0.751
                143.241 13.643 122.002 166.284
## mean costs
  sd effects
                  0.227 0.011
                                  0.209
##
  sd costs
                139.018 14.261 118.123 164.741
##
##
   Reference intervention
##
                                     LB
                                              UB
                   mean
                             sd
                                  0.745
## mean effects
                  0.787
                          0.025
                                           0.826
## mean costs
                163.483 18.714 134.929 196.108
## sd effects
                  0.252 0.017
                                  0.224
                                           0.281
## sd costs
                167.732 22.138 135.394 208.368
##
##
    Incremental results
                                      LB
                                             UB
##
                    mean
                              sd
## delta effects
                   0.071
                          0.033
                                   0.017 0.124
                  20.242 23.424 -17.026 59.46
## delta costs
## ICER
                 286.192
```

Information is reported only for the main parameters of interest in the model for both outcomes and treatment groups. In addition, the incremental mean results for the effectiveness and costs are provided at the bottom of the table, denoted with delta effects and delta costs respectively. In addition, the value of the incremental cost effectiveness ratio (ICER), which quantifies the cost per incremental unit of effectiveness, is also reported. Results are summarised in terms of posterior mean, standard deviation and 95% credible intervals for each parameter.

A series of useful functions are included in the package **BCEA** that summarises the results of the economic evaluation. As an example, the CEP and CEAC plots from their respective functions <code>ceac.plot</code> and <code>ceplane.plot</code> in **BCEA** can be obtained by applying these functions to the "BCEA" object contained in model.hur, which can be accessed via model.hur\$cea. The R commands used to generate and combine these plots are the following:

```
R> require(ggplot2)
R> require(BCEA)
R> cep <- ceplane.plot(model.hur$cea, graph = "ggplot2") + ggtitle("CEP")
R> ceac <- ceac.plot(model.hur$cea, graph = "ggplot2") + ggtitle("CEAC")
R> grid.arrange(cep, ceac, ncol = 2)
```

and the resulting output is given in Figure 7

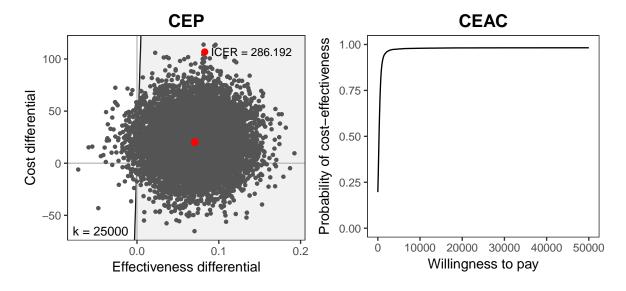


Figure 7: Cost effectiveness plane (CEP) and cost effectiveness acceptability curve (CEAC) obtained using respectively the functions ceplane.plot and ceac.plot in the package **BCEA** and applied to the model results contained in the object model.hur\$cea

### 10. Conclusions

The **missingHE** package presented in this paper performs economic evaluations with missing outcome values for two-arms trial data under a Bayesian framework. In addition, the package

provides a set of models that can be flexibly specified to jointly handle a series of features typically affecting effectiveness and cost data, e.g. skewness and structural values.

Missing data represent a serious threat for the economic evaluation as, when confronted with a partially-observed dataset, each analysis makes assumptions about the missing values that cannot be ultimately verified from the data at hand. This means that any measure of fit or predictive accuracy, such as the Deviance Information Criterion or Posterior Predictive Checks (Gelman, Carlin, Stern, and Rubin 2004; Spiegelhalter, Best, Carlin, and van der Linde 2002), cannot be easily interpreted. This in turns makes the validation of the model more complex. Thus, the use of sensitivity analysis to explore the impact on the results of a set of plausible missingness assumptions, included MNAR, becomes unavoidable. The Bayesian approach naturally allows to perform these assessments through the incorporation in the model of external evidence (e.g. expert opinions) using prior distributions while ensuring consistency and the correct propagation of uncertainty throughout the model.

missingHE handles missingness under alternative mechanism scenarios through the functions selection and hurdle which respectively implement selection and hurdle models for either or both outcome variables. Selection models assume a specific MoA-MoM modelling structure, where either MAR or MNAR mechanisms can be specified directly, while hurdle models are mostly based on MAR but allow the exploration of MNAR through specific assumptions about the structural values.

In conclusion, **missingHE** allows the analyst who wants to perform an economic evaluation to:
a) jointly model costs and effectiveness; b) account for skewness and structural values; and c)
assess the robustness of the results under a set of plausible missingness assumptions. These
are typical issues affecting individual-level data that should be simultaneously addressed to
avoid biased results, which may in turn lead to misleading cost-effectiveness conclusions. The
availability of methodological and practical tools such as the ones used in this package have
the potential to improve the workflow of modellers and regulators alike, thus advancing the
fields of economic evaluation of health care interventions.

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