

$$\begin{aligned} C[m] &= 1/N \sum_{n=0}^{N-1} x[n] * \exp(-2 * PI * m * n * j/N) C[0] = 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 0 * n * j/5) = 1/5 * 8 * (\cos(-2 * PI * 0 * 0/5) + j * \sin(-2 * PI * 0 * 0/5)) + \\ &1/5 * 8 * (\cos(-2 * PI * 0 * 1/5) + j * \sin(-2 * PI * 0 * 1/5)) + 1/5 * 8 * (\cos(-2 * PI * 0 * 2/5) + j * \sin(-2 * PI * 0 * 2/5)) + \\ &1/5 * 8 * (\cos(-2 * PI * 0 * 3/5) + j * \sin(-2 * PI * 0 * 3/5)) + 1/5 * 8 * (\cos(-2 * PI * 0 * 4/5) + j * \sin(-2 * PI * 0 * 4/5)) = \\ &0.6 + j * 0.0 = 0.6 * e^{0.0} \end{aligned}$$

$$\begin{aligned} A[0] &= \sqrt{REAL(C[0])^2 + IM(C[0])^2} = \sqrt{0.36 + 0.0} = 0.6 \\ PHI[0] &= \arctg IM(C[0]) / REAL(C[0]) = \arctg 0.0 / 0.6 = 0.0 \end{aligned}$$

$$\begin{aligned} C[1] &= 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 1 * n * j/5) = 1/5 * -7 * (\cos(-2 * PI * 1 * 0/5) + j * \sin(-2 * PI * 1 * 0/5)) + \\ &1/5 * -7 * (\cos(-2 * PI * 1 * 1/5) + j * \sin(-2 * PI * 1 * 1/5)) + 1/5 * -7 * (\cos(-2 * PI * 1 * 2/5) + j * \sin(-2 * PI * 1 * 2/5)) + \\ &1/5 * -7 * (\cos(-2 * PI * 1 * 3/5) + j * \sin(-2 * PI * 1 * 3/5)) + 1/5 * -7 * (\cos(-2 * PI * 1 * 4/5) + j * \sin(-2 * PI * 1 * 4/5)) = \\ &2.41 + j * 3.49 = 4.24 * e^{0.97} \end{aligned}$$

$$\begin{aligned} A[1] &= \sqrt{REAL(C[1])^2 + IM(C[1])^2} = \sqrt{5.8081 + 12.1801} = 4.24 \\ PHI[1] &= \arctg IM(C[1]) / REAL(C[1]) = \arctg 3.49 / 2.41 = 0.97 \end{aligned}$$

$$\begin{aligned} C[2] &= 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 2 * n * j/5) = 1/5 * -6 * (\cos(-2 * PI * 2 * 0/5) + j * \sin(-2 * PI * 2 * 0/5)) + \\ &1/5 * -6 * (\cos(-2 * PI * 2 * 1/5) + j * \sin(-2 * PI * 2 * 1/5)) + 1/5 * -6 * (\cos(-2 * PI * 2 * 2/5) + j * \sin(-2 * PI * 2 * 2/5)) + \\ &1/5 * -6 * (\cos(-2 * PI * 2 * 3/5) + j * \sin(-2 * PI * 2 * 3/5)) + 1/5 * -6 * (\cos(-2 * PI * 2 * 4/5) + j * \sin(-2 * PI * 2 * 4/5)) = \\ &1.29 + j * 0.31 = 1.33 * e^{0.24} \end{aligned}$$

$$\begin{aligned} A[2] &= \sqrt{REAL(C[2])^2 + IM(C[2])^2} = \sqrt{1.6641 + 0.0961} = 1.33 \\ PHI[2] &= \arctg IM(C[2]) / REAL(C[2]) = \arctg 0.31 / 1.29 = 0.24 \end{aligned}$$

$$\begin{aligned} C[3] &= 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 3 * n * j/5) = 1/5 * 1 * (\cos(-2 * PI * 3 * 0/5) + j * \sin(-2 * PI * 3 * 0/5)) + 1/5 * 1 * (\cos(-2 * PI * 3 * 1/5) + \\ &j * \sin(-2 * PI * 3 * 1/5)) + 1/5 * 1 * (\cos(-2 * PI * 3 * 2/5) + j * \sin(-2 * PI * 3 * 2/5)) + \\ &1/5 * 1 * (\cos(-2 * PI * 3 * 3/5) + j * \sin(-2 * PI * 3 * 3/5)) + 1/5 * 1 * (\cos(-2 * PI * 3 * 4/5) + j * \sin(-2 * PI * 3 * 4/5)) = \\ &1.29 + j * -0.31 = 1.33 * e^{-0.24} \end{aligned}$$

$$\begin{aligned} A[3] &= \sqrt{REAL(C[3])^2 + IM(C[3])^2} = \sqrt{1.6641 + 0.0961} = 1.33 \\ PHI[3] &= \arctg IM(C[3]) / REAL(C[3]) = \arctg -0.31 / 1.29 = -0.24 \end{aligned}$$

$$\begin{aligned} C[4] &= 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 4 * n * j/5) = 1/5 * 7 * (\cos(-2 * PI * 4 * 0/5) + j * \sin(-2 * PI * 4 * 0/5)) + 1/5 * 7 * (\cos(-2 * PI * 4 * 1/5) + \\ &j * \sin(-2 * PI * 4 * 1/5)) + 1/5 * 7 * (\cos(-2 * PI * 4 * 2/5) + j * \sin(-2 * PI * 4 * 2/5)) + \\ &1/5 * 7 * (\cos(-2 * PI * 4 * 3/5) + j * \sin(-2 * PI * 4 * 3/5)) + 1/5 * 7 * (\cos(-2 * PI * 4 * 4/5) + j * \sin(-2 * PI * 4 * 4/5)) = \end{aligned}$$

$$2.41 + j * -3.49 = 4.24 * e^{-0.97}$$

$$A[4] = \sqrt{REAL(C[4])^2 + IM(C[4])^2} = \sqrt{5.8081 + 12.1801} = 4.24$$

$$PHI[4] = \arctan(IM(C[4])/REAL(C[4])) = \arctan(-3.49/2.41) = -0.97$$

-----2-----

$$\begin{aligned} X[0] &= \sum_{n=0}^4 C[n] * \exp(-2 * PI * 0 * n * j/5) = (0.6 + j * 0.0) * (\cos(-2 * PI * 0 * 0/5) + j * \sin(-2 * PI * 0 * 0/5)) + \\ &(2.41 + j * 3.49) * (\cos(-2 * PI * 0 * 1/5) + j * \sin(-2 * PI * 0 * 1/5)) + (1.29 + j * 0.31) * (\cos(-2 * PI * 0 * 2/5) + j * \sin(-2 * PI * 0 * 2/5)) + \\ &(1.29 + j * -0.31) * (\cos(-2 * PI * 0 * 3/5) + j * \sin(-2 * PI * 0 * 3/5)) + (2.41 + j * -3.49) * (\cos(-2 * PI * 0 * 4/5) + j * \sin(-2 * PI * 0 * 4/5)) = \\ &(0.6 + j * 0.0) * (1.0 + j * 0.0) + (2.41 + j * 3.49) * (1.0 + j * 0.0) + \\ &(1.29 + j * 0.31) * (1.0 + j * 0.0) + (1.29 + j * -0.31) * (1.0 + j * 0.0) + (2.41 + j * -3.49) * (1.0 + j * 0.0) = 8.0 + j * 0.0 \end{aligned}$$

$$\begin{aligned} X[1] &= \sum_{n=0}^4 C[n] * \exp(-2 * PI * 1 * n * j/5) = (0.6 + j * 0.0) * (\cos(-2 * PI * 1 * 0/5) + j * \sin(-2 * PI * 1 * 0/5)) + \\ &(2.41 + j * 3.49) * (\cos(-2 * PI * 1 * 1/5) + j * \sin(-2 * PI * 1 * 1/5)) + (1.29 + j * 0.31) * (\cos(-2 * PI * 1 * 2/5) + j * \sin(-2 * PI * 1 * 2/5)) + \\ &(1.29 + j * -0.31) * (\cos(-2 * PI * 1 * 3/5) + j * \sin(-2 * PI * 1 * 3/5)) + (2.41 + j * -3.49) * (\cos(-2 * PI * 1 * 4/5) + j * \sin(-2 * PI * 1 * 4/5)) = \\ &(0.6 + j * 0.0) * (1.0 + j * 0.0) + (2.41 + j * 3.49) * (0.31 + j * 0.95) + (1.29 + j * 0.31) * (-0.81 + j * 0.59) + (1.29 + j * -0.31) * (-0.81 + j * \\ &-0.59) + (2.41 + j * -3.49) * (0.31 + j * -0.95) = -6.9924 + j * 4.4408920985e - 16 \end{aligned}$$

$$\begin{aligned} X[2] &= \sum_{n=0}^4 C[n] * \exp(-2 * PI * 2 * n * j/5) = (0.6 + j * 0.0) * (\cos(-2 * PI * 2 * 0/5) + j * \sin(-2 * PI * 2 * 0/5)) + \\ &(2.41 + j * 3.49) * (\cos(-2 * PI * 2 * 1/5) + j * \sin(-2 * PI * 2 * 1/5)) + (1.29 + j * 0.31) * (\cos(-2 * PI * 2 * 2/5) + j * \sin(-2 * PI * 2 * \\ &2/5)) + (1.29 + j * -0.31) * (\cos(-2 * PI * 2 * 3/5) + j * \sin(-2 * PI * 2 * 3/5)) + \\ &(2.41 + j * -3.49) * (\cos(-2 * PI * 2 * 4/5) + j * \sin(-2 * PI * 2 * 4/5)) = (0.6 + j * 0.0) * (1.0 + j * 0.0) + \\ &(2.41 + j * 3.49) * (-0.81 + j * 0.59) + (1.29 + j * 0.31) * (0.31 + j * -0.95) + (1.29 + j * -0.31) * (0.31 + j * 0.95) + (2.41 + j * -3.49) * (-0.81 + j * -0.59) = \\ &-6.0336 + j * 0.0 \end{aligned}$$

$$\begin{aligned} X[3] &= \sum_{n=0}^4 C[n] * \exp(-2 * PI * 3 * n * j/5) = (0.6 + j * 0.0) * (\cos(-2 * PI * 3 * 0/5) + j * \sin(-2 * PI * 3 * 0/5)) + \\ &(2.41 + j * 3.49) * (\cos(-2 * PI * 3 * 1/5) + j * \sin(-2 * PI * 3 * 1/5)) + (1.29 + j * 0.31) * (\cos(-2 * PI * 3 * 2/5) + j * \sin(-2 * PI * 3 * \\ &2/5)) + (1.29 + j * -0.31) * (\cos(-2 * PI * 3 * 3/5) + j * \sin(-2 * PI * 3 * 3/5)) + \\ &(2.41 + j * -3.49) * (\cos(-2 * PI * 3 * 4/5) + j * \sin(-2 * PI * 3 * 4/5)) = \\ &(0.6 + j * 0.0) * (1.0 + j * 0.0) + (2.41 + j * 3.49) * (-0.81 + j * -0.59) + (1.29 + j * 0.31) * (0.31 + j * 0.95) + \\ &(1.29 + j * -0.31) * (0.31 + j * -0.95) + (2.41 + j * -3.49) * (-0.81 + j * 0.59) = 1.0248 + j * 0.0 \end{aligned}$$

$$\begin{aligned} X[4] &= \sum_{n=0}^4 C[n] * \exp(-2 * PI * 4 * n * j/5) = (0.6 + j * 0.0) * (\cos(-2 * PI * 4 * 0/5) + j * \sin(-2 * PI * 4 * 0/5)) + \\ &(2.41 + j * 3.49) * (\cos(-2 * PI * 4 * 1/5) + j * \sin(-2 * PI * 4 * 1/5)) + (1.29 + j * 0.31) * (\cos(-2 * PI * 4 * 2/5) + j * \sin(-2 * PI * 4 * \\ &2/5)) + (1.29 + j * -0.31) * (\cos(-2 * PI * 4 * 3/5) + j * \sin(-2 * PI * 4 * 3/5)) + \\ &(2.41 + j * -3.49) * (\cos(-2 * PI * 4 * 4/5) + j * \sin(-2 * PI * 4 * 4/5)) = \end{aligned}$$

$$(0.6 + j * 0.0) * (1.0 + j * 0.0) + (2.41 + j * 3.49) * (0.31 + j * -0.95) + (1.29 + j * 0.31) * (-0.81 + j * -0.59) + (1.29 + j * -0.31) * (-0.81 + j * 0.59) + (2.41 + j * -3.49) * (0.31 + j * 0.95) = 7.0012 + j * 0.0$$

$$\begin{aligned} \text{SIGMA} &= \sqrt{1/N * \sum_{n=0}^{N-1} x[n]^2} = \sqrt{1/5 * \sum_{n=0}^4 x[n]^2} = \\ &= \sqrt{1/5 * ((8 - 8.0)^2 + (-7 - -6.9924)^2 + (-6 - -6.0336)^2 + (1 - 1.0248)^2 + (7 - 7.0012)^2)} = \\ &= \sqrt{1/5 * (0.0^2 + -0.0076^2 + 0.0336^2 + -0.0248^2 + -0.0012^2)} = 0.0189905239528 \end{aligned}$$

—————3—————

$$\begin{aligned} &8+-7+-6+1+7+0+0+0 \\ &8+7+-6+-1+7+0+0+0 \\ &8+-7+6+-1+7+0+0+0 \\ &8+7+6+1+7+0+0+0 \\ &8+-7+-6+1+-7+0+0+0 \\ &8+7+-6+-1+-7+0+0+0 \\ &8+-7+6+-1+-7+0+0+0 \\ &8+7+6+1+-7+0+0+0 \end{aligned}$$

$$[0.375, 1.875, 1.625, 3.625, -1.375, 0.125, -0.125, 1.875]$$

—————4—————

$$\begin{aligned} &0.375+1.875+1.625+3.625+-1.375+0.125+-0.125+1.875 \\ &0.375+-1.875+1.625+-3.625+-1.375+-0.125+-0.125+-1.875 \\ &0.375+1.875+-1.625+-3.625+-1.375+0.125+0.125+-1.875 \\ &0.375+-1.875+-1.625+3.625+-1.375+-0.125+0.125+1.875 \\ &0.375+1.875+1.625+3.625+1.375+-0.125+0.125+-1.875 \\ &0.375+-1.875+1.625+-3.625+1.375+0.125+0.125+1.875 \\ &0.375+1.875+-1.625+-3.625+1.375+-0.125+-0.125+1.875 \\ &0.375+-1.875+-1.625+3.625+1.375+0.125+-0.125+-1.875 \end{aligned}$$

—————5—————

$$\begin{aligned} Z &= 1/N * \sqrt{\sum_{n=0}^{N-1} x_1[n] * \sum_{n=0}^{N-1} x_2[n]} = 1/5 * \sqrt{\sum_{n=0}^4 x_1[n] * \sum_{n=0}^4 x_2[n]} = \\ &= 1/5 * \sqrt{(8^2 + -7^2 + -6^2 + 1^2 + 7^2)^2} = 1/5 * (64 + 49 + 36 + 1 + 49) = 39.8 \end{aligned}$$

$$\begin{aligned} \text{r12}[0] &= 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[0] + x[1] * x[1] + x[2] * x[2] + x[3] * x[3] + x[4] * x[4]) = 1/5 * (8 * 8 + -7 * -7 + -6 * \\ &-6 + 1 * 1 + 7 * 7) = 1/5 * (8 * 8 + -7 * -7 \\ &+ -6 * -6 + 1 * 1 + 7 * 7) = 39.8 \end{aligned}$$

$$\begin{aligned} \text{r12}[1] &= 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[-1] + x[1] * x[0] + x[2] * x[1] + x[3] * x[2] + x[4] * x[3]) = 1/5 * (8 * 0 + -7 * 8 + -6 * \\ &-7 + 1 * -6 + 7 * 1) = 1/5 * (8 * 0 + -7 * 8 \\ &+ -6 * -7 + 1 * -6 + 7 * 1) = -2.6 \end{aligned}$$

$$\begin{aligned} \text{r12}[2] &= 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[-2] + x[1] * x[-1] + x[2] * x[0] + x[3] * x[1] + x[4] * x[2]) = 1/5 * (8 * 0 + -7 * 0 + \\ &-6 * 8 + 1 * -7 + 7 * -6) = 1/5 * (8 * 0 + -7 * \\ &0 + -6 * 8 + 1 * -7 + 7 * -6) = -19.4 \end{aligned}$$

$$\begin{aligned} \text{r12}[3] &= 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[-3] + x[1] * x[-2] + x[2] * x[-1] + x[3] * x[0] + x[4] * x[1]) = 1/5 * (8 * 0 + -7 * 0 + \\ &-6 * 0 + 1 * 8 + 7 * -7) = 1/5 * (8 * 0 + -7 * \\ &0 + -6 * 0 + 1 * 8 + 7 * -7) = -8.2 \end{aligned}$$

$$\begin{aligned} \text{r12}[4] &= 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[-4] + x[1] * x[-3] + x[2] * x[-2] + x[3] * x[-1] + x[4] * x[0]) = 1/5 * (8 * 0 + -7 * \\ &0 + -6 * 0 + 1 * 0 + 7 * 8) = 1/5 * (8 * 0 + -7 * \\ &0 + -6 * 0 + 1 * 0 + 7 * 8) = 11.2 \end{aligned}$$

$$\begin{aligned} \text{B12}[0] &= \text{r12}[0]/Z = 39.8/39.8 = 1.0 \\ \text{B12}[1] &= \text{r12}[1]/Z = -2.6/39.8 = -0.0653266331658 \\ \text{B12}[2] &= \text{r12}[2]/Z = -19.4/39.8 = -0.48743718593 \\ \text{B12}[3] &= \text{r12}[3]/Z = -8.2/39.8 = -0.206030150754 \\ \text{B12}[4] &= \text{r12}[4]/Z = 11.2/39.8 = 0.281407035176 \end{aligned}$$