

$$\begin{aligned}
C[m] &= 1/N \sum_{n=0}^{N-1} x[n] * \exp(-2 * PI * m * n * j/N) C[0] = 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 0 * n * j/5) = 1/5 * 11 * (\cos(-2 * PI * 0 * 0/5) + \\
&j * \sin(-2 * PI * 0 * 0/5)) + \\
&1/5 * 11 * (\cos(-2 * PI * 0 * 1/5) + j * \sin(-2 * PI * 0 * 1/5)) + 1/5 * 11 * (\cos(-2 * PI * 0 * 2/5) + j * \sin(-2 * PI * 0 * 2/5)) + \\
&1/5 * 11 * (\cos(-2 * PI * 0 * 3/5) + j * \sin(-2 * PI * 0 * 3/5)) + 1/5 * 11 * (\cos(-2 * PI * 0 * 4/5) + j * \sin(-2 * PI * 0 * 4/5)) = 1.6 + j * 0.0 = 1.6 * e^{0.0} \\
A[0] &= \sqrt{REAL(C[0])^2 + IM(C[0])^2} = \sqrt{2.56 + 0.0} = 1.6 \\
PHI[0] &= \arctg IM(C[0]) / REAL(C[0]) = \arctg 0.0 / 1.6 = 0.0 \\
C[1] &= 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 1 * n * j/5) = 1/5 * -8 * (\cos(-2 * PI * 1 * 0/5) + j * \sin(-2 * PI * 1 * 0/5)) + \\
&1/5 * -8 * (\cos(-2 * PI * 1 * 1/5) + j * \sin(-2 * PI * 1 * 1/5)) + 1/5 * -8 * (\cos(-2 * PI * 1 * 2/5) + j * \sin(-2 * PI * 1 * 2/5)) + 1/5 * - \\
&8 * (\cos(-2 * PI * 1 * 3/5) + j * \sin(-2 * PI * 1 * 3/5)) + 1/5 * -8 * (\cos(-2 * PI * 1 * 4/5) + j * \sin(-2 * PI * 1 * 4/5)) = 2.91 + j * 4.4 = 5.28 * e^{0.99} \\
A[1] &= \sqrt{REAL(C[1])^2 + IM(C[1])^2} = \sqrt{8.4681 + 19.36} = 5.28 \\
PHI[1] &= \arctg IM(C[1]) / REAL(C[1]) = \arctg 4.4 / 2.91 = 0.99
\end{aligned}$$

$$\begin{aligned}
C[2] &= 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 2 * n * j/5) = 1/5 * -7 * (\cos(-2 * PI * 2 * 0/5) + j * \sin(-2 * PI * 2 * 0/5)) + \\
&1/5 * -7 * (\cos(-2 * PI * 2 * 1/5) + j * \sin(-2 * PI * 2 * 1/5)) + 1/5 * -7 * (\cos(-2 * PI * 2 * 2/5) + j * \sin(-2 * PI * 2 * 2/5)) + 1/5 * -7 * (\cos(-2 * PI * 2 * 3/5) + \\
&j * \sin(-2 * PI * 2 * 3/5)) + 1/5 * -7 * (\cos(-2 * PI * 2 * 4/5) + j * \sin(-2 * PI * 2 * 4/5)) = 1.79 + j * 0.1 = 1.79 * e^{0.06} \\
A[2] &= \sqrt{REAL(C[2])^2 + IM(C[2])^2} = \sqrt{3.2041 + 0.01} = 1.79 \\
PHI[2] &= \arctg IM(C[2]) / REAL(C[2]) = \arctg 0.1 / 1.79 = 0.06 \\
C[3] &= 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 3 * n * j/5) = 1/5 * 3 * (\cos(-2 * PI * 3 * 0/5) + j * \sin(-2 * PI * 3 * 0/5)) + \\
&1/5 * 3 * (\cos(-2 * PI * 3 * 1/5) + j * \sin(-2 * PI * 3 * 1/5)) + 1/5 * 3 * (\cos(-2 * PI * 3 * 2/5) + j * \sin(-2 * PI * 3 * 2/5)) + 1/5 * 3 * (\cos(-2 * PI * 3 * 3/5) + \\
&j * \sin(-2 * PI * 3 * 3/5)) + 1/5 * 3 * (\cos(-2 * PI * 3 * 4/5) + j * \sin(-2 * PI * 3 * 4/5)) = 1.79 + j * -0.1 = 1.79 * e^{-0.06} \\
A[3] &= \sqrt{REAL(C[3])^2 + IM(C[3])^2} = \sqrt{3.2041 + 0.01} = 1.79 \\
PHI[3] &= \arctg IM(C[3]) / REAL(C[3]) = \arctg -0.1 / 1.79 = -0.06 \\
C[4] &= 1/5 * \sum_{n=0}^4 x[n] * \exp(-2 * PI * 4 * n * j/5) = 1/5 * 9 * (\cos(-2 * PI * 4 * 0/5) + j * \sin(-2 * PI * 4 * 0/5)) + \\
&1/5 * 9 * (\cos(-2 * PI * 4 * 1/5) + j * \sin(-2 * PI * 4 * 1/5)) + 1/5 * 9 * (\cos(-2 * PI * 4 * 2/5) + j * \sin(-2 * PI * 4 * 2/5)) + 1/5 * 9 * (\cos(-2 * PI * 4 * 3/5) + \\
&j * \sin(-2 * PI * 4 * 3/5)) + 1/5 * 9 * (\cos(-2 * PI * 4 * 4/5) + j * \sin(-2 * PI * 4 * 4/5)) = 2.91 + j * -4.4 = 5.28 * e^{-0.99} \\
A[4] &= \sqrt{REAL(C[4])^2 + IM(C[4])^2} = \sqrt{8.4681 + 19.36} = 5.28 \\
PHI[4] &= \arctg IM(C[4]) / REAL(C[4]) = \arctg -4.4 / 2.91 = -0.99
\end{aligned}$$

$$\begin{aligned}
X[0] &= \sum_{n=0}^4 C[n] * \exp(-2 * PI * 0 * n * j/5) = (1.6 + j * 0.0) * (\cos(-2 * PI * 0 * 0/5) + j * \sin(-2 * PI * 0 * 0/5)) + (2.91 + j * 4.4) * \\
&(\cos(-2 * PI * 0 * 1/5) + j * \sin(-2 * PI * 0 * 1/5)) + (1.79 + j * 0.1) * (\cos(-2 * PI * 0 * 2/5) + j * \sin(-2 * PI * 0 * 2/5)) + \\
&(1.79 + j * -0.1) * (\cos(-2 * PI * 0 * 3/5) + j * \sin(-2 * PI * 0 * 3/5)) + (2.91 + j * -4.4) * (\cos(-2 * PI * 0 * 4/5) + j * \sin(-2 * PI * 0 * \\
&4/5)) = (1.6 + j * 0.0) * (1.0 + j * 0.0) + (2.91 + j * 4.4) * (1.0 + j * 0.0) + \\
&(1.79 + j * 0.1) * (1.0 + j * 0.0) + (1.79 + j * -0.1) * (1.0 + j * 0.0) + (2.91 + j * -4.4) * (1.0 + j * 0.0) = 11.0 + j * 0.0 \\
X[1] &= \sum_{n=0}^4 C[n] * \exp(-2 * PI * 1 * n * j/5) = (1.6 + j * 0.0) * (\cos(-2 * PI * 1 * 0/5) + j * \sin(-2 * PI * 1 * 0/5)) + (2.91 + j * 4.4) \\
&(\cos(-2 * PI * 1 * 1/5) + j * \sin(-2 * PI * 1 * 1/5)) + (1.79 + j * 0.1) * (\cos(-2 * PI * 1 * 2/5) + j * \sin(-2 * PI * 1 * 2/5)) + \\
&(1.79 + j * -0.1) * (\cos(-2 * PI * 1 * 3/5) + j * \sin(-2 * PI * 1 * 3/5)) + (2.91 + j * -4.4) \\
&(\cos(-2 * PI * 1 * 4/5) + j * \sin(-2 * PI * 1 *
\end{aligned}$$

$$\begin{aligned} &4/5)) = (1.6+j*0.0)*(1.0+j*0.0)+(2.91+j*4.4)*(0.31+j*0.95)+ \\ &(1.79+j*0.1)*(-0.81+j*0.59)+(1.79+j*-0.1)*(-0.81+j*-0.59) \\ &+(2.91+j*-4.4)*(0.31+j*-0.95) = -7.9736+j*0.0 \end{aligned}$$

$$\begin{aligned} X[2] = \sum_{n=0}^4 C[n] * \exp(-2 * PI * 2 * n * j/5) &= 1.6 + j * 0.0 * (\cos(-2 * PI * 2 * 0/5) + j * \sin(-2 * PI * 2 * 0/5)) + (2.91 + j * 4.4) \\ &(\cos(-2 * PI * 2 * 1/5) + j * \sin(-2 * PI * 2 * 1/5)) + (\end{aligned}$$

$$\begin{aligned} &1.79+j*0.1)*(\cos(-2*PI*2*2/5)+ \\ &j*\sin(-2*PI*2*2/5))+(1.79+j*-0.1)*(\cos(-2*PI*2*3/5)+j*\sin(-2*PI*2*3/5))+(2.91+j*-4.4) \\ &(\cos(-2*PI*2*4/5)+j*\sin(-2*PI*2* \end{aligned}$$

$$\begin{aligned} &4/5)) = (1.6+j*0.0)*(1.0+j*0.0)+ \\ &(2.91+j*4.4)*(-0.81+j*0.59)+(1.79+j*0.1)*(0.31+j*-0.95)+(1.79+j*-0.1)*(0.31+j*0.95)+(2.91+j*-4.4)*(-0.81+j*-0.59) = -7.0064+j*0.0 \end{aligned}$$

$$\begin{aligned} X[3] = \sum_{n=0}^4 C[n] * \exp(-2 * PI * 3 * n * j/5) &= (1.6 + j * 0.0) * (\cos(-2 * PI * 3 * 0/5) + j * \sin(-2 * PI * 3 * 0/5)) \\ &+ (2.91 + j * 4.4) * (\cos(-2 * PI * 3 * 1/5) + j * \sin(-2 * PI * 3 * 1/5)) + (1.79 + j * 0.1) * (\cos(-2 * PI * 3 * 2/5) + j * \sin(-2 * PI * 3 * 2/5)) \\ &+ (1.79 + j * -0.1) * (\cos(-2 * PI * 3 * 3/5) + j * \sin(-2 * PI * 3 * 3/5)) + (2.91 + j * -4.4) * (\cos(-2 * PI * 3 * 4/5) \\ &+ j * \sin(-2 * PI * 3 * 4/5)) = \end{aligned}$$

$$\begin{aligned} &(1.6 + j * 0.0) * (1.0 + j * 0.0) + (2.91 + j * 4.4) * (-0.81 + j * -0.59) + \\ &(1.79 + j * 0.1) * (0.31 + j * 0.95) + (1.79 + j * -0.1) * (0.31 + j * -0.95) + (2.91 + j * -4.4) * (-0.81 + j * 0.59) = 2.9976 + j * 0.0 \end{aligned}$$

$$\begin{aligned} X[4] = \sum_{n=0}^4 C[n] * \exp(-2 * PI * 4 * n * j/5) &= (1.6 + j * 0.0) * (\cos(-2 * PI * 4 * 0/5) + j * \sin(-2 * PI * 4 * 0/5)) \\ &+ (2.91 + j * 4.4) * (\cos(-2 * PI * 4 * 1/5) + j * \sin(-2 * PI * 4 * 1/5)) + (1.79 + j * 0.1) * (\cos(-2 * PI * 4 * 2/5) \\ &+ j * \sin(-2 * PI * 4 * 2/5)) + (1.79 + j * -0.1) * (\cos(-2 * PI * 4 * 3/5) \\ &+ j * \sin(-2 * PI * 4 * 3/5)) + (2.91 + j * -4.4) * (\cos(-2 * PI * 4 * 4/5) + j * \sin(-2 * PI * 4 * 4/5)) \\ &= (1.6 + j * 0.0) * (1.0 + j * 0.0) + (2.91 + j * 4.4) * (0.31 + j * -0.95) + (1.79 + j * 0.1) * (-0.81 + j * -0.59) \\ &+ (1.79 + j * -0.1) * (-0.81 + j * 0.59) + (2.91 + j * -4.4) * (0.31 + j * 0.95) = 8.9824 + j * 0.0 \end{aligned}$$

$$\begin{aligned} \text{SIGMA} &= \sqrt{1/N * \sum_{n=0}^{N-1} x[n] - X[n]^2} = \sqrt{1/5 * \sum_{n=0}^4 x[n] - X[n]^2} \\ &= \sqrt{1/5 * ((11 - 11.0)^2 + (-8 - -7.9736)^2 + (-7 - -7.0064)^2 + (3 - 2.9976)^2 + (9 - 8.9824)^2)} = \sqrt{1/5 * (0.0^2 + -0.0264^2 + 0.0064^2 + 0.0024^2 + 0.0} \\ &0.0145150955905 \end{aligned}$$

11+-8+-7+3+9+0+0+0
11+8+-7+-3+9+0+0+0
11+-8+7+-3+9+0+0+0
11+8+7+3+9+0+0+0
11+-8+-7+3+-9+0+0+0
11+8+-7+-3+-9+0+0+0
11+-8+7+-3+-9+0+0+0
11+8+7+3+-9+0+0+0

[1.0, 2.25, 2.0, 4.75, -1.25, 0.0, -0.25, 2.5]

4

1.0+2.25+2.0+4.75+-1.25+0.0+-0.25+2.5
1.0+-2.25+2.0+-4.75+-1.25+-0.0+-0.25+-2.5
1.0+2.25+-2.0+-4.75+-1.25+0.0+0.25+-2.5
1.0+-2.25+-2.0+4.75+-1.25+-0.0+0.25+2.5
1.0+2.25+2.0+4.75+1.25+-0.0+0.25+-2.5
1.0+-2.25+2.0+-4.75+1.25+0.0+0.25+2.5
1.0+2.25+-2.0+-4.75+1.25+-0.0+-0.25+2.5
1.0+-2.25+-2.0+4.75+1.25+0.0+-0.25+-2.5

5

$$Z = 1/N * \sqrt{\sum_{n=0}^{N-1} x_1[n] * \sum_{n=0}^{N-1} x_2[n]}$$

$$= 1/5 * \sqrt{\sum_{n=0}^4 x_1[n] * \sum_{n=0}^4 x_2[n]} = 1/5 \sqrt{(11^2 + -8^2 + -7^2 + 3^2 + 9^2)^2} = 1/5 * (121 + 64 + 49 + 9 + 81) = 64.8$$

$$r12[0] = 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[0] + x[1] * x[1] + x[2] * x[2] + x[3] * x[3] + x[4] * x[4]) =$$

$$1/5 * (11 * 11 + -8 * -8 + -7 * -7 + 3 * 3 + 9 * 9) = 1/5 * (11 * 11 + -8 * -8 + -7 * -7 + 3 * 3 + 9 * 9) = 64.8$$

$$r12[1] = 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[-1] + x[1] * x[0] + x[2] * x[1] + x[3] * x[2] + x[4] * x[3]) =$$

$$1/5 * (11 * 0 + -8 * 11 + -7 * -8 + 3 * -7 + 9 * 3) = 1/5 * (11 * 0 + -8 * 11 + -7 * -8 + 3 * -7 + 9 * 3) = -5.2$$

$$r12[2] = 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[-2] + x[1] * x[-1] + x[2] * x[0] + x[3] * x[1] + x[4] * x[2]) =$$

$$1/5 * (11 * 0 + -8 * 0 + -7 * 11 + 3 * -8 + 9 * -7) = 1/5 * (11 * 0 + -8 * 0 + -7 * 11 + 3 * -8 + 9 * -7) = -32.8$$

$$r12[3] = 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[-3] + x[1] * x[-2] + x[2] * x[-1] + x[3] * x[0] + x[4] * x[1]) =$$

$$1/5 * (11 * 0 + -8 * 0 + -7 * 0 + 3 * 11 + 9 * -8) = 1/5 * (11 * 0 + -8 * 0 + -7 * 0 + 3 * 11 + 9 * -8) = -7.8$$

$$r12[4] = 1/N * \sum_{n=0}^{N-1} x[n] * x[n-1] = 1/5 * (x[0] * x[-4] + x[1] * x[-3] + x[2] * x[-2] + x[3] * x[-1] + x[4] * x[0]) =$$

$$1/5 * (11 * 0 + -8 * 0 + -7 * 0 + 3 * 0 + 9 * 11) = 1/5 * (11 * 0 + -8 * 0 + -7 * 0 + 3 * 0 + 9 * 11) = 19.8$$

$$B12[0] = r12[0]/Z = 64.8/64.8 = 1.0$$

$$B12[1] = r12[1]/Z = -5.2/64.8 = -0.0802469135802$$

$$B12[2] = r12[2]/Z = -32.8/64.8 = -0.506172839506$$

$$B12[3] = r12[3]/Z = -7.8/64.8 = -0.12037037037$$

$$B12[4] = r12[4]/Z = 19.8/64.8 = 0.30555555555556$$