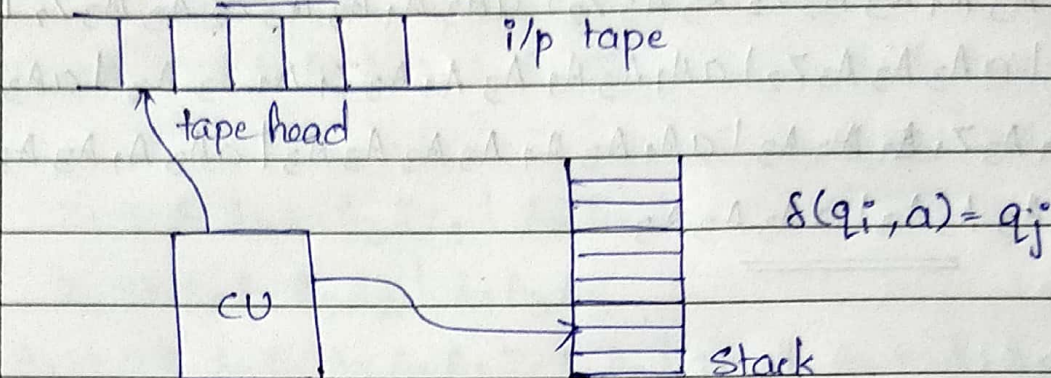


MODULE-4

Push Down Automata (PDA)



If it reaches final state \Rightarrow accepting string

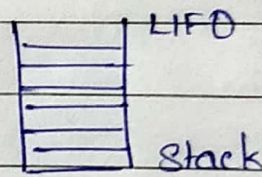
Tape head moves towards right

2-way PDA can move in both directions, but during a particular transition it moves either towards left/right

Memory - Stack

Stack symbol $\rightarrow \Gamma$

Initial stack symbol $\rightarrow Z_0$



Notations

$$M = (Q, \Sigma, \Gamma, \delta, q_0, Z_0, F)$$

$$\delta: Q \times ((\Sigma \cup \{\epsilon\}) \times \Gamma)$$

$$\rightarrow Q \times \Gamma^*$$

$$L = \{a^n b^n \mid n \geq 0\}$$

$$\delta(q_0, \overset{\text{i/p symbol}}{a}, \overset{\text{O/S X}}{Z_0}) = (q_0, \overset{\text{O/S X}}{a} Z_0)$$

$$\delta(q_0, \overset{\text{O/S X}}{a}, \overset{\text{O/S X X}}{a}) = (q_0, \overset{\text{O/S X X}}{aa})$$

$$\delta(q_0, \overset{\text{O/S X}}{b}, \overset{\text{O/S X}}{a}) = (q_0, \overset{\text{O/S X}}{a}) \rightarrow \text{pop}$$

$$\delta(q_1, \epsilon, Z_0) = (q_2, \epsilon)$$

$$M = (\{q_0, q_1, q_2\}, \{a, b\}, \{a\}, \delta, q_0, Z_0, \{q_2\})$$

$$M = (\{q_0, q_1, q_2\}, \{a, b\}, \{x\}, \delta, q_0, Z_0, \{q_2\})$$

$$(q_i, a) \rightarrow \text{pop } a$$

$$(q_i, aa) \rightarrow \text{push } a \text{ to TOS}$$

↓
top of stack

$Z_0 \rightarrow$ default top of stack

$$(q_i, \epsilon) \rightarrow \text{Neither push nor pop}$$

