

DS1QQ88

Lista de Exercícios Sobre Vetores

13. Dado $u = (4, -1)$, $v = (0, 5)$ e $w = (-3, -3)$
Encontre as componentes de:

a) $u + w$ $R = (4, -1) + (-3, -3)$
 $R = (1, -4)$

b) $v - 3u$
 $R = (0, 5) - 3(4, -1)$
 $R = (0, 5) - (12, -3)$
 $R = (-12, 8)$

c) $2(u - 5w)$
 $R = 2[(4, -1) - 5(-3, -3)]$
 $R = 2[(4, -1) - (-15, -15)]$
 $R = 2[(19, 14)]$
 $R = (38, 28)$

d) $3v - 2(u + 2w)$
 $R = 3(0, 5) - 2[(4, -1) + 2(-3, -3)]$
 $R = (0, 15) - 2[(4, -1) + (-6, -6)]$
 $R = (0, 15) - 2(-2, -7)$
 $R = (0, 15) - (-4, -14)$
 $R = (4, 29)$

e) $-3(w - 2u + v) = -3[(-3, -3) - 2(4, -1) + (0, 5)]$
 $R = -3[(-3, -3) - (8, -2) + (0, 5)]$
 $R = -3(-11, 4)$
 $R = (33, -12)$

$$\begin{aligned}
 & 2) (-2u - v) - 5(v + 3u) \\
 & [-2(4, -1) - (0, 5)] - 5[(0, 5) + 3(-3, -3)] \\
 & [(-8, 2) - (0, 5)] - 5[(0, 5) + (-9, -9)] \\
 & (-8, -3) - 5(-9, -4) \\
 & (-8, -3) - (-45, -20) \\
 & (37, 17)
 \end{aligned}$$

15) Sejam $u = (-3, 2, 1, 0)$, $v = (4, 7, -3, 2)$ e $w = (5, -2, 8, 1)$. Encontre as componentes de:

a) $v - w$

$$\begin{aligned}
 & (4, 7, -3, 2) - (5, -2, 8, 1) \\
 & P = (-1, 9, -11, 1)
 \end{aligned}$$

b) $2u + 7v$

$$\begin{aligned}
 & 2(-3, 2, 1, 0) + 7(4, 7, -3, 2) \\
 & (-6, 4, 2, 0) + (28, 49, -21, 14) \\
 & (22, 53, -19, 14)
 \end{aligned}$$

c) $-u + (v - 4w)$

$$\begin{aligned}
 & -(-3, 2, 1, 0) + [(4, 7, -3, 2) - 4(5, -2, 8, 1)] \\
 & (3, -2, -1, 0) + [(4, 7, -3, 2) - (20, -8, 32, 4)] \\
 & (3, -2, -1, 0) + (-16, 15, -35, -2) \\
 & (-13, 13, -36, -2)
 \end{aligned}$$

d) $6(u - 3v)$

$$\begin{aligned}
 & 6[(-3, 2, 1, 0) - 3(4, 7, -3, 2)] \\
 & 6[(-3, 2, 1, 0) - (12, 21, -9, 6)] = 6(-15, -19, 10, -6) \\
 & (-90, -114, 60, -36)
 \end{aligned}$$

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2) $-v - w$

$-(4, 7, -3, 2) - (5, -2, 8, 1)$

$(-4, -7, 3, -2) + (-5, 2, -8, -1)$

$(-9, -5, -5, -3)$

3) $(6v - w) - (4u + v)$

$[6(4, 7, -3, 2) - (5, -2, 8, 1)] - [4(-3, 2, 1, 0) + (4, 7, -1, 2)]$

$[24, 42, -18, 12] - (5, -2, 8, 1) - [(-12, 8, 4, 0) + (4, 7, -3, 2)]$

$(19, 44, -26, 11) - (-8, 15, 1, 2)$

$(27, 29, -27, 9)$

17) Dado $u = (5, -1, 0, 3, -3)$, $v = (-1, -1, 7, 2, 0)$ e

$w = (-4, 2, -3, -5, 2)$. Encontre os componentes de:

a) $w - u$

$(-4, 2, -3, -5, 2) - (5, -1, 0, 3, -3)$

$(-9, 3, -3, -8, 5)$

b) $2v + 3u$

$(-2, -2, 14, 4, 0) + (15, -3, 0, 9, -9)$

$(13, -5, 14, 13, -9)$

c) $-w + 3(v - u)$

$(4, -2, 3, 5, -2) + 3[(-1, -1, 7, 2, 0) - (5, -1, 0, 3, -3)]$

$(4, -2, 3, 5, -2) + 3(-6, 0, 7, -1, 3)$

$(4, -2, 3, 5, -2) + (-18, 0, 21, -3, 9)$

$(-14, -2, 24, 2, 7)$

$$d) 5(-v + 4u - w)$$

$$5[-(-1, -1, 7, 2, 0) + 4(5, -1, 0, 3, -3) - (-4, 2, -3, -5, 2)]$$

$$5[(1, 1, -7, -2, 0) + (20, -4, 0, 12, -12) + (4, -2, 3, 5, -2)]$$

$$5[(21, -3, -7, 10, -12) + (4, -2, 3, 5, -2)]$$

$$5(25, -5, -4, 15, -14)$$

$$(125, -25, -20, 75, -70)$$

$$e) -2(3w + v) + (2u + w)$$

$$-2[3(-4, 2, -3, -5, 2) + (-1, -1, 7, 2, 0)] + [2u + w]$$

$$-2[-12, 6, -9, -15, 6] + [-1, -1, 7, 2, 0] + [2u + w]$$

$$-2(-13, 5, -2, -13, 6) + [2(5, -1, 0, 3, -3) + (-4, 2, -3, -5, 2)]$$

$$(26, -10, 4, 26, -12) + [(10, -2, 0, 6, -6) + (-4, 2, -3, -5, 2)]$$

$$(26, -10, 4, 26, -12) + (6, 0, -3, 1, -4)$$

$$(32, -10, 1, 27, -16)$$

$$f) \frac{1}{2}(w - 5v + 2u) + v$$

$$\frac{1}{2}[(-4, 2, -3, -5, 2) - 5(-1, -1, 7, 2, 0) + 2(5, -1, 0, 3, -3)] + v$$

$$\frac{1}{2}[(-4, 2, -3, -5, 2) - (-5, -5, 35, 10, 0) + (10, -2, 0, 6, -6)] + v$$

$$\frac{1}{2}[(1, 7, -38, -15, 2) + (10, -2, 0, 6, -6)] + v$$

$$\frac{1}{2}(11, 5, -38, -9, -4) + v$$

$$(\frac{11}{2}, \frac{5}{2}, -19, -\frac{9}{2}, -2) + (-1, -1, 7, 2, 0)$$

$$(\frac{9}{2}, \frac{3}{2}, -12, -\frac{5}{2}, -2)$$

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19. Suponha $u = (-3, 1, 2, 4, 4)$, $v = (4, 0, -8, 1, 2)$ e $w = (6, -1, -4, 3, -5)$. Encontre os componentes de

(a) $v - w$

$$(4, 0, -8, 1, 2) - (6, -1, -4, 3, -5) \\ (-2, -1, -12, -2, 7)$$

b) $6u + 2v$

$$6(-3, 1, 2, 4, 4) + 2(4, 0, -8, 1, 2) \\ (-18, 6, 12, 24, 24) + (8, 0, -16, 2, 4) \\ (-10, 6, -4, 26, 28)$$

c) $(2u - 7w) - (8v + u)$

$$[2(-3, 1, 2, 4, 4) - 7(6, -1, -4, 3, -5)] - (8v + u)$$

$$[(-6, 2, 4, 8, 8) - (42, -7, -28, 21, -35)] - (8v + u)$$

$$[(-48, 9, 32, -13, 43)] - [8(4, 0, -8, 1, 2) + (-3, 1, 2, 4, 4)]$$

$$[(-48, 9, 32, -13, 43)] - [(32, 0, -64, 8, 16) + (-3, 1, 2, 4, 4)]$$

$$(-48, 9, 32, -13, 43) - (29, 1, -62, 12, 20)$$

$$(-77, 8, 94, -25, 23)$$