

1 a

$$G(\omega) = \int_{-\infty}^{\infty} g(t) \cdot e^{-j\omega t} dt$$

$$i = j = \sqrt{-1}$$

$$g_n = 2+t$$

$$g_p = 2-t$$

$$G(\omega) = \int_{-2}^0 (2+t) \cdot e^{-j\omega t} dt + \int_0^2 (2-t) \cdot e^{-j\omega t} dt$$

$$G(\omega) = \frac{2e^{-2i\omega} (-2i\omega + e^{2i\omega} - 1)}{\omega^2}$$

① b

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$$D_n = \frac{1}{T_0} \int_{T_0} g(t) \cdot e^{-j n \omega_0 t} dt$$

$$g_n = 2+t$$

$$g_p = 2-t$$

$$\omega_0 = 2\pi f$$

$$f = \frac{1}{T_0} = \frac{1}{4}$$

$$\omega_0 = \pi/2$$

$$D_n = \frac{1}{T_0} \int_{-2}^0 (2+t) \cdot e^{-j n \omega_0 t} dt + \int_0^2 (2-t) \cdot e^{-j n \omega_0 t} dt$$

$$e^{-j n \frac{\pi}{2} t} = (e^{-j \frac{\pi}{2}})^{nt} = [\cos \frac{\pi}{2} - j \sin \frac{\pi}{2}]^{nt} = -1^j = -j$$

$$D_n = \frac{1}{4} \int_{-2}^0 (2+t) \cdot -j^{nt} dt + \int_0^2 (2-t) \cdot -j^{nt} dt$$

$$D_n = \frac{1}{4} \left(\frac{-j^{n+1} - 4e^{j^{n+1}} + 4}{\pi^2 \cdot n^2} \right) + \frac{1}{4} \left(\frac{-j^{n+1} - 4e^{j^{n+1}} - 4}{\pi^2 \cdot n^2} \right)$$

$$D_n = \frac{-e^{j^{n+1}} - e^{j^{n+1}} + 2}{\pi^2 \cdot n^2}$$

$$D_n = \frac{-2e^{j^{n+1}} + 2}{\pi^2 \cdot n^2} \sim 2e^{j^{n+1}} \cdot 2[\cos \frac{\pi}{2} - j \sin \frac{\pi}{2}] = 2$$

$$D_{[1]} = 0,40528$$

$$D_{[2]} = 0$$

$$D_n = \frac{-2 \cos \pi n + 2}{\pi^2 \cdot n^2} = D_{[3]} = 0,0450316$$

2 a e b

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$$G(\omega) = \int_0^2 t \cdot e^{-j\omega_0 t} dt + \int_2^6 (4-t) \cdot e^{-j\omega_0 t} dt + \int_6^8 (t-8) e^{-j\omega_0 t} dt$$

$$G(\omega) = \frac{16i e^{-4i\omega} \sin^3(\omega) \cdot \cos(\omega)}{\omega^2}$$

$$\omega_0 = \frac{\pi}{4}$$

$$D_n = \frac{G(\omega_n)}{T_0} = \frac{2 \cdot i e^{-4i\omega_0 n} \sin^3(\omega_0 n) \cdot \cos(\omega_0 n)}{(\omega_0 \cdot n)^2} \Rightarrow G\left(\frac{\pi}{4}n\right)$$

$$* D_n[n] = \frac{2 \cdot i \left(e^{-i\pi n} \cdot \sin^3\left(\frac{\pi}{4}n\right) \cdot \cos\left(\frac{\pi}{4}n\right) \right)}{\left(\frac{\pi n}{4}\right)^2}$$