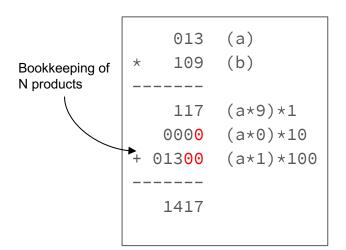
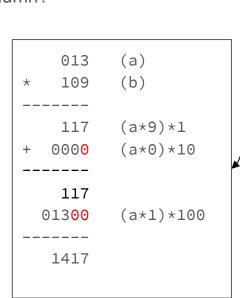
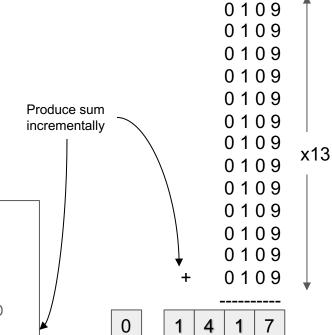
Multiplication

- Consider: 109 x 13 = 1417
- Approach: Successive Additions
 - \circ Consider: 9 + 9 + 9 .. + 9 (13 times) = ?
 - What is carry value for the 10's column?
- Approach: Long Multiplication







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Algorithm for Decimal Multiplication

- Consider a number is an array:
 int[] B = { 9, 0, 1 };
- Base10 Algorithm:

```
sum = 0;

for (d = 0; d < 3; d ++) {

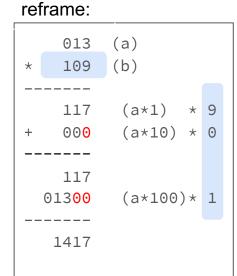
    sum += a * B[d];

    a = a * 10; // Base 10 shift left

}
```

- Complexity: O(#digits)
 - o For 2^32, at most 10 iterations

_



original:

```
013 (a)

* 109 (b)

-----

117 (a*9)*1

+ 000 (a*0)*10

-----

117

01300 (a*1)*100

-----

1417
```

Note: commuta

Algorithm for Binary Multiplication

Base 2 Algorithm:

```
sum = 0;
for (d = 0; d < 3; d ++) {
   if (B[d] == 1) {
      sum += a * B[d];
   }
   a = a * 2; // Base 2 shift left
   a = a << 1;
}</pre>
```

```
0010
             (a = 2)
             (b = 11)
      1011
0000 0010
             (a*2^0)*1
             (a*2^1)*1
   0 0100
0000 0110
  00 0000
             (a*2^2)*0
0000 0110
             (a*2^4)*1
+ 001 0000
0001 0110
             (a*b = 10)
```

Complexity: O(word_size)

For MIPS, at most 32 iterations

original:

```
0010
             (a = 2)
     1011
             (b = 11)
0000 0010
             (a*1)* 2^0
    0 0100
            (a*1)* 2^1
0000 0110
  00 0000
            (a*0)* 2^2
0000 0110
           (a*1)* 2^4
+ 001 0000
0001 0110
           (a*b = 22)
```

Algorithm for Binary Multiplication

- Use the register as an stack
- Base 2 Algorithm:

```
sum = 0;
for (; b != 0; ) {
    bit = pop(b);
    if (bit == 1) {
        sum += a;
    }
    a = a << 1;
}</pre>
```

Complexity: O(word_size)

reframe:

```
0010
             (a = 2)
             (b = 11)
      1011
             (a*2^0)*1
0000 0010
             (a*2^1)*1
   0 0100
0000 0110
             (a*2^4)*0
  00 0000
0000 0110
             (a*2^8)*1
+ 001 0000
0001 0110
             (a*b = 10)
```

original:

```
0010
             (a = 2)
      1011
             (b = 11)
0000 0010
             (a*1)* 2^0
    0 0100
             (a*1)* 2^1
0000 0110
  00 0000
             (a*0)* 2^4
0000 0110
+ 001 0000
             (a*1)* 2^8
0001 0110
            (a*b = 22)
```