

$$\begin{array}{c}
\frac{\text{Store}(v, i)}{\text{Heap}(v, i)} \quad (\text{H-1}) \qquad \frac{\frac{\text{Update}(*, p, val)}{\text{CreatedBy}(p, p')} \quad \text{Heap}(p', *)}{\text{Heap}(p', val)} \quad (\text{H-2}) \qquad \frac{\text{LitAssign}(v, *, *)}{\text{CreatedBy}(v, v)} \quad (\text{CBY-1}) \\
\\
\frac{\text{Node}(n, *)}{\text{CreatedBy}(n, n)} \quad (\text{CBY-2}) \qquad \frac{\text{Store}(p, *)}{\text{CreatedBy}(p, p)} \quad (\text{CBY-3}) \qquad \frac{\text{Update}(v, *, *)}{\text{CreatedBy}(v, v)} \quad (\text{CBY-4}) \\
\\
\frac{\text{LitAssign}(v, *, *)}{\text{CreatedBy}(v, v)} \quad (\text{CBY-5}) \qquad \frac{\text{Move}(v, n)}{\frac{\text{CreatedBy}(n, n')}{\text{CreatedBy}(v, n')}} \quad (\text{CBY-6}) \\
\\
\frac{\frac{\text{FunctionParameter}(*, *, p)}{\frac{\text{CreatedBy}(v_1, p)}{\text{CreatedBy}(p, v_2)}}}{\text{CreatedBy}(v_1, v_2)} \quad (\text{CBY-7}) \qquad \frac{\frac{\text{Fetch}(v, p)}{\text{CreatedBy}(p, p')} \quad \text{Heap}(p', n)}{\text{CreatedBy}(n, n')} \quad (\text{CBY-8}) \\
\\
\frac{\frac{\text{CallArgument}(r, i, arg)}{\text{Call}(r, f)} \quad \text{FunctionParameter}(f, i, x)}{\text{CreatedBy}(arg, arg')} \quad (\text{CBY-9}) \qquad \frac{\text{Call}(r, f) \quad \text{ReturnValue}(f, v)}{\frac{\text{CreatedBy}(v, v')}{\text{CreatedBy}(r, v')}} \quad (\text{CBY-10}) \\
\\
\frac{\text{NodePattern}(v, tag, n) \quad \text{NodeParameter}(v, i, u) \quad \text{CreatedBy}(n, n') \quad \text{Node}(n', tag)}{\frac{\text{NodeArgument}(n', i, arg)}{\text{CreatedBy}(arg, arg')}} \quad (\text{CBY-11}) \qquad \frac{\text{NodePattern}(v, *, n)}{\frac{\text{CreatedBy}(n, n')}{\text{CreatedBy}(v, n')}} \quad (\text{CBY-12})
\end{array}$$

$$\frac{\text{Case}(r, \text{scrut}) \quad \text{AltLiteral}(r, \text{alt}, *) \quad \text{CreatedBy}(\text{scrut}, \text{scrut}')}{\text{CreatedBy}(\text{alt}, \text{scrut}')} \quad (\text{CBY-13})$$

$$\frac{\text{Case}(r, \text{scrut}) \quad \text{AltLiteral}(r, \text{alt}, \text{tag}) \quad \text{CreatedBy}(\text{scrut}, \text{scrut}') \quad \text{Node}(\text{scrut}', \text{tag})}{\text{CreatedBy}(\text{alt}, \text{scrut}')} \quad (\text{CBY-14})$$

$$\frac{\text{Case}(r, \text{scrut}) \quad \text{AltDefault}(r, \text{alt}) \quad \text{CreatedBy}(\text{scrut}, \text{scrut}')}{\text{CreatedBy}(\text{alt}, \text{scrut}')} \quad (\text{CBY-15})$$

$$\frac{\text{Case}(r, \text{scrut}) \quad \text{Alt}(r, *, \text{tag}) \quad \text{AltParameter}(r, \text{tag}, i, \text{altParam}) \quad \text{CreatedBy}(\text{scrut}, \text{scrut}') \quad \text{Node}(\text{scrut}', \text{tag}) \quad \text{NodeArgument}(\text{scrut}', i, \text{nodeArg}) \quad \text{CreatedBy}(\text{nodeArg}, \text{nodeArg}')}{\text{CreatedBy}(\text{altParam}, \text{nodeArg}')} \quad (\text{CBY-16})$$

$$\frac{\text{Case}(r, \text{scrut}) \quad \text{Alt}(r, \text{alt}, \text{tag}) \quad \text{CreatedBy}(\text{scrut}, \text{scrut}') \quad \text{Node}(\text{scrut}', \text{tag}) \quad \text{ReturnValue}(\text{alt}, v) \quad \text{CreatedBy}(v, v')}{\text{CreatedBy}(r, v')} \quad (\text{CBY-17})$$

$$\frac{\text{Case}(r, *) \quad \text{AltLiteral}(r, \text{alt}, *) \quad \text{ReturnValue}(\text{alt}, v) \quad \text{CreatedBy}(v, v')}{\text{CreatedBy}(r, v')} \quad (\text{CBY-18})$$

$$\frac{\text{Case}(r, *) \quad \text{AltDefault}(r, \text{alt}) \quad \text{ReturnValue}(\text{alt}, v) \quad \text{CreatedBy}(v, v')}{\text{CreatedBy}(r, v')} \quad (\text{CBY-19})$$

$$\frac{\text{Node}(n', t) \quad \text{CreatedBy}(v, v')}{\text{NodeCreatedBy}(n, t, n')} \quad (\text{NCBY})$$

$$\frac{\text{NodeCreatedBy}(n, t, *)}{\text{PossibleNodeTag}(n, t)} \quad (\text{PNT})$$

$$\frac{\text{AltDefault}(*, \text{alt})}{\text{PossibleAlt}(\text{alt})} \quad (\text{PA-1})$$

$$\frac{\text{AltLiteral}(*, \text{alt}, *)}{\text{PossibleAlt}(\text{alt})} \quad (\text{PA-2})$$

$$\frac{\text{Case}(r, \text{scrut}) \quad \text{Alt}(r, \text{alt}, t) \quad \text{NodeCreatedBy}(\text{scrut}, t, \text{scrut}')}{\text{PossibleAlt}(\text{alt})} \quad (\text{PA-3})$$

$$\frac{\text{Store}(q, *) \quad \text{CreatedBy}(p, q)}{\text{PointerOrigin}(p, q)} \quad (\text{PO})$$

$$\frac{\text{Heap}(p, n) \quad \text{PossibleNodeTag}(n, \text{tag})}{\text{PossibleLocTag}(p, t)} \quad (\text{PLT})$$

$$\begin{array}{c}
\text{EntryPoint}(\text{main}) \\
\text{ReturnValue}(\text{main}, x) \\
\hline
\text{LiveSVal}(x)
\end{array}
\quad (\text{LS-1})
\quad
\begin{array}{c}
\text{Call}(y, f) \\
\text{CallArgument}(y, *, x) \\
\text{External}(f, \text{true}, *) \\
\hline
\text{LiveSVal}(x)
\end{array}
\quad (\text{LS-2})
\quad
\begin{array}{c}
\text{LiveSVal}(y) \\
\text{Move}(y, x) \\
\hline
\text{LiveSVal}(x)
\end{array}
\quad (\text{LS-3})$$

$$\frac{
\begin{array}{c}
\text{LiveSVal}(\text{res}) \quad \text{PossibleAlt}(\text{alt}) \quad \text{ReturnValue}(\text{alt}, \text{ret}) \\
(\text{Alt}(\text{res}, \text{alt}, *) \vee \text{AltLiteral}(\text{res}, \text{alt}, *) \vee \text{AltDefault}(\text{res}, \text{alt}))
\end{array}
}{
\text{LiveSVal}(\text{ret})
}
\quad (\text{LS-4})$$

$$\frac{
\begin{array}{c}
\text{LiveSVal}(\text{alt}) \quad \text{PossibleAlt}(\text{alt}) \quad \text{Case}(\text{res}, \text{scrut}) \\
(\text{Alt}(\text{res}, \text{alt}, *) \vee \text{AltLiteral}(\text{res}, \text{alt}, *) \vee \text{AltDefault}(\text{res}, \text{alt}))
\end{array}
}{
\text{LiveSVal}(\text{scrut})
}
\quad (\text{LS-5})$$

$$\begin{array}{c}
\text{LiveSVal}(y) \\
\text{Call}(y, f) \\
\hline
\text{LiveFunRetSimple}(f)
\end{array}
\quad (\text{LFS-3})
\quad
\begin{array}{c}
\text{LiveFunRetSimple}(f) \\
\text{ReturnValue}(f, \text{ret}) \\
\hline
\text{LiveSVal}(\text{ret})
\end{array}
\quad (\text{LS-6})$$

$$\begin{array}{c}
\text{LiveSVal}(\text{param}) \\
\text{FunctionParameter}(f, i, \text{param}) \\
\text{Call}(y, f) \\
\text{CallArgument}(y, i, x) \\
\hline
\text{LiveSVal}(x)
\end{array}
\quad (\text{LS-7})
\quad
\begin{array}{c}
\text{LiveFunRetSimple}(f_{\text{ext}}) \\
\text{External}(f_{\text{ext}}, *, *) \\
\text{Call}(y, f_{\text{ext}}) \\
\text{CallArgument}(y, *, x) \\
\hline
\text{LiveSVal}(x)
\end{array}
\quad (\text{LS-8})$$

$$\frac{
\begin{array}{c}
\text{LiveNodeArg}(n, t, i) \\
\text{Node}(n, t) \\
\text{NodeArgument}(n, i, x)
\end{array}
}{
\text{LiveSVal}(x)
}
\quad (\text{LS-9})$$

$$\frac{\text{LiveSVal}(x) \quad \text{NodeParameter}(as, i, x) \quad \text{NodePattern}(as, t, n)}{\text{LiveNodeArg}(n, t, i)} \quad (\text{LNA-1}) \qquad \frac{\text{LiveNodeArg}(as, t, i) \quad \text{NodePattern}(as, t, n)}{\text{LiveNodeArg}(n, t, i)} \quad (\text{LNA-2})$$

$$\frac{\text{LiveSVal}(()x) \quad \text{NodePattern}(as, t, n) \quad \text{NodeParameter}(as, i, x)}{\text{LiveNodeArg}(n, t, i)} \quad (\text{LNA-3}) \qquad \frac{\text{LiveNodeArg}(n, t, i) \quad \text{Move}(n, m)}{\text{LiveNodeArg}(m, t, i)} \quad (\text{LNA-4})$$

$$\frac{\text{LiveNodeArg}(alt, t, i) \quad \text{Case}(r, scrut) \quad \text{Alt}(r, alt, t) \quad \text{AltParameter}(r, t, i, *)}{\text{LiveNodeArg}(scrut, t, i)} \quad (\text{LNA-5}) \qquad \frac{\text{LiveSVal}(x) \quad \text{Case}(r, scrut) \quad \text{AltParameter}(r, t, i, x)}{\text{LiveNodeArg}(scrut, t, i)} \quad (\text{LNA-6})$$

$$\frac{\text{LiveNodeArg}(res, t_{res}, i) \quad \text{Case}(res, scrut) \quad \text{Alt}(res, alt, t_{alt}) \quad \text{ReturnValue}(alt, ret) \quad \text{PossibleAlt}(alt) \quad \text{CreatedBy}(ret, ret') \quad \text{Node}(ret', t_{res})}{\text{LiveNodeArg}(ret, t_{res}, i)} \quad (\text{LNA-7})$$

$$\frac{\text{LiveNodeArg}(res, t_{res}, i) \quad \text{Case}(res, *) \quad (\text{AltLiteral}(res, alt, *) \vee \text{AltDefault}(res, alt)) \quad \text{ReturnValue}(alt, ret) \quad \text{CreatedBy}(ret, ret') \quad \text{Node}(ret', t_{res})}{\text{LiveNodeArg}(ret, t_{res}, i)} \quad (\text{LNA-8})$$

$$\frac{\text{LiveNodeArg}(y, t, i) \quad \text{Call}(y, f)}{\text{LiveFunRetNodeArg}(f, t, i)} \quad (\text{LFN}) \qquad \frac{\text{LiveFunRetNodeArg}(f, t, i) \quad \text{ReturnValue}(f, r)}{\text{LiveNodeArg}(r, t, i)} \quad (\text{LNA-9})$$

$$\frac{\text{LiveNodeArg}(param, t, i) \quad \text{FunctionParameter}(f, j, param) \quad \text{Call}(y, f) \quad \text{CallArgument}(y, j, x)}{\text{LiveNodeArg}(x, t, i)} \quad (\text{LNA-10}) \qquad \frac{\text{LiveNodeArg}(n, t, i) \quad \text{Fetch}(n, p) \quad \text{PointerOrigin}(p, q) \quad \text{PossibleLocTag}(q, t)}{\text{LiveHeapNodeArg}(q, t, i)} \quad (\text{LHN})$$

$$\frac{\text{LiveHeapNodeArg}(p, t, i) \quad \text{Store}(q, n) \quad \text{PointerOrigin}(p, q) \quad \text{PossibleNodeTag}(n, t)}{\text{LiveNodeArg}(n, t, i)} \quad (\text{LNA-11}) \qquad \frac{\text{LiveHeapNodeArg}(q, t, i) \quad \text{Update}(*, p, n) \quad \text{PointerOrigin}(p, q) \quad \text{PossibleNodeTag}(n, t)}{\text{LiveNodeArg}(n, t, i)} \quad (\text{LNA-12})$$