

# Advanced Data Analytics

## Workshop I

This workshop leverages the power of Python to solve mathematical, statistical, and data analysis problems. Your task is to solve the following problems **without** using any libraries and with the fewest lines of code possible. Academic integrity is imperative. Any form of dishonesty will result in a grade of zero and formal reporting to the university. As a university representative, you are expected to uphold the highest standards of ethical conduct.

### Requirements

- Solutions *must* be submitted **by midnight on the agreed deadline**.
- Solutions *must* be submitted in a Jupyter Notebook `.ipynb` with its outputs.
- Solutions *must* include your name, student ID and be written in English.
- Solutions *must* be clear, concise, and well documented.
- Solutions *must* be submitted first to the submission library provided.

### Exercise 1 (15 points)

This section explores Python concepts with creative and practical tasks.

1. Write a function `char_count(s: str) -> dict[str, int]` that returns a dictionary mapping each character in the string `s` to its frequency. (5 points)
2. Write a function `generate_primes(n: int) -> list[int]` that generates a list of all prime numbers less than or equal to `n`. (5 points)
3. Write a function `is_prime(n: int) -> bool` that checks whether a given number `n` is a prime number. Return `True` if `n` is prime, `False` otherwise. (5 points)

### Exercise 2 (15 points)

This section contains problems to understand and tackle the basics of mathematical operations in Python.

1. Write a function `factorial(n: int) -> int` that calculates the factorial of a given number `n` iteratively. (5 points)
2. Write a function `fibonacci(n: int) -> list[int]` that generates a list containing the first `n` numbers in the Fibonacci sequence. (5 points)
3. Write a function `sum_naturals(n: int) -> int` that calculates the sum of the first `n` natural numbers. (5 points)

### Exercise 3 (15 points)

This section contains problems to understand and tackle the basics of statistical operations in Python.

1. Write a function `calculate_stats(data: list[float]) -> tuple[float, float, float]` that calculates the mean, median, and mode of a given list of numbers. (5 points)
2. Write a function `variance_and_std(data: list[float]) -> tuple[float, float]` that calculates the variance and standard deviation of a dataset. (5 points)
3. Write a function `weighted_mean(data: list[float], weights: list[float]) -> float` that calculates the weighted mean of a dataset *data* given a corresponding list of weights *weights*. Ensure both lists have the same length. (5 points)

### Exercise 4 (15 points)

This section focuses on analytical problems to develop problem-solving and logical reasoning in Python.

1. Write a function `is_palindrome(s: str) -> bool` that checks if a given string *s* is a palindrome. Return `True` if it is, `False` otherwise. (5 points)
2. Write a function `reverse_words(sentence: str) -> str` that reverses the words in a sentence while preserving their order. (5 points)
3. Write a function `find_longest_word(words: list[str]) -> str` that returns the longest word from a list of strings. If there is a tie, return the first one. (5 points)

### Exercise 5 (15 points)

This section contains intermediate-level problems to reinforce Python concepts.

1. Write a function `remove_duplicates(data: list[int]) -> list[int]` that removes duplicates from a list while preserving the order of elements. (5 points)
2. Write a function `group_by_key(data: list[tuple[str, int]]) -> dict[str, list[int]]` that groups values in *data* by their keys. For example, the input `[('a', 1), ('b', 2), ('a', 3)]` results in the dictionary `{'a': [1, 3], 'b': [2]}`. (5 points)
3. Write a function `flatten_list(nested_list: list[list[int]]) -> list[int]` that flattens a nested list of integers into a single list. For example, `[[1, 2], [3, 4]]` becomes `[1, 2, 3, 4]`. (5 points)